

Supporting Information

First-Principles Anharmonic Quantum Calculations for Peptide Spectroscopy: VSCF Calculations and Comparison with Experiments

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Pair-wise coupling and VSCF-PT2 approximation

VSCF potential can be written as a sum of one-mode (diagonal approximation) and pair-wise coupling in terms of normal coordinate (Q),

$$V(Q_1, \dots, Q_N) = \sum_{i=1}^N V^{diag}_i(Q_i) + \sum_j \sum_{i>j} V^{2coup}_{ij}(Q_i, Q_j) . \quad (1)$$

This type of potential needs multi-dimensional grid point calculations and the number of grid points increases rapidly with the dimensionality of the potential and the vibrational modes. If NG is the number of grid points along a normal mode and NV is the number of vibrational modes then the number of total grid points (NP) is

$$NP = [NV \times NG] + \frac{[NV(NV - 1) \times NG^2]}{2} . \quad (2)$$

The PT2 correction on to of VSCF is described by the following equation:

$$E_n^{PT2} = E_n^{VSCF} + \sum_{m \neq n} \frac{\left| \left\langle \prod_{j=1}^N \psi_j^{(n)}(Q_j) \right| \Delta V \left| \prod_{j=1}^N \psi_j^{(m)}(Q_j) \right\rangle \right|^2}{E_n^{(0)} - E_m^{(0)}}, \quad (3)$$

where E_n^{PT2} is the correlation corrected energy of the state n .

Table S1. Comparisons of frequencies and intensities of experimental and computed vibrational frequencies and intensities of C5 conformer of NATA (local minima). % error is calculated for VSCF-PT2 against experimental frequencies.

| Mode description | Exp. Freq. | Exp. intensity | HO (HF) | VSCF-PT2 | Intensity | % error |
|---------------------|------------|----------------|---------|----------|-----------|-------------|
| NH ₂ str | 3538 | 1.0 | 3942 | 3537 | 0.80 | 0.03 |
| Indole NH str | 3523 | 0.85 | 3911 | 3568 | 1.0 | 1.28 |
| φ-amide NH str. | 3430 | 0.80 | 3869 | 3424 | 0.83 | 0.17 |
| NH ₂ str | 3417 | 0.53 | 3802 | 3428 | 0.50 | 0.32 |
| Pyrole CH str | -- | -- | 3407 | 3127 | 0.02 | -- |
| Phenyl CH str. | 3074 | 0.97 | 3367 | 3071 | 0.25 | 0.10 |
| Phenyl CH str. | 3059 | 0.57 | 3356 | 3054 | 0.14 | 0.16 |
| Phenyl CH str. | -- | -- | 3344 | 3050 | 0.13 | -- |
| Phenyl CH str. | -- | -- | 3334 | 3041 | 0.01 | -- |
| Alkyl CH str. | 3004 | 0.35 | 3293 | 3002 | 0.19 | 0.07 |
| Alkyl CH str. | -- | -- | 3287 | 2993 | 0.08 | -- |
| Alkyl CH str. | -- | -- | 3269 | 2902 | 0.12 | -- |
| Alkyl CH str. | 2956 | 0.24 | 3255 | 2966 | 0.11 | 0.51 |
| Alkyl CH str. | | -- | 3202 | 2917 | 0.12 | -- |
| Alkyl CH str. | 2933 | 0.43 | 3201 | 2889 | 0.24 | 1.5 |
| Avg. % error | | | | | | 0.46 |

Table S2: Comparisons frequencies and intensities of experimental and computed vibrational frequencies of C7 conformer of NATA (global minima).). % error is calculated for VSCF-PT2 against experimental frequencies.

| Mode description | Exp. freq | Exp. Intensity | HO | VSCF- PT2 | Intensity | % error |
|---------------------|-----------|----------------|------|-----------|-----------|-------------|
| NH ₂ str | 3516 | 0.63 | 3921 | 3521 | 1.0 | 0.14 |
| Indole NH str. | 3521 | 0.74 | 3911 | 3573 | 0.94 | 1.47 |
| φ-amide NH str. | 3429 | 0.85 | 3861 | 3461 | 0.86 | 0.93 |
| NH ₂ str | 3334 | 1.00 | 3773 | 3406 | 0.66 | 2.16 |
| Pyrole CH str | -- | -- | 3441 | 3064 | 0.02 | -- |
| Phenyl CH str. | 3092 | 0.18 | 3366 | 3076 | 0.23 | 0.52 |
| Phenyl CH str. | 3072 | 0.36 | 3353 | 3082 | 0.35 | 0.33 |
| Phenyl CH str. | 3048 | 0.18 | 3341 | 3067 | 0.05 | 0.62 |
| Phenyl CH str. | -- | -- | 3332 | 3072 | 0.01 | - |
| Alkyl CH str. | 2999 | 0.19 | 3281 | 2975 | 0.12 | 0.80 |
| Alkyl CH str. | 2979 | 0.14 | 3310 | 2961 | 0.11 | 0.60 |
| Alkyl CH str. | -- | | 3278 | 2949 | 0.11 | -- |
| Alkyl CH str. | 2938 | 0.51 | 3211 | 2915 | 0.22 | 0.78 |
| Alkyl CH str. | 2919 | 0.15 | 3237 | 2895 | 0.16 | 0.82 |
| Alkyl CH str. | -- | -- | 3199 | 2962 | 0.05 | -- |
| Avg. % error | | | | | | 0.83 |

Table S3: Comparisons of experimental and computed vibrational frequencies of global minima of AVPO. % error is calculated for VSCF-PT2 against experimental frequencies.

| Mode description | Experiments | HO | PES except | % error |
|-----------------------|-------------|------|------------|-------------|
| Phe NH str. | 3451 | 3866 | 3423 | 0.81 |
| Val NH str. | 3441 | 3842 | 3411 | 0.87 |
| Phenyl CH str. | 3096 | 3370 | 3064 | 1.03 |
| Phenyl CH str. | 3076 | 3350 | 3048 | 0.91 |
| Phenyl CH str. | 3038 | 3359 | 3071 | 1.09 |
| Phenyl CH str. | 3006 | 3331 | 3040 | 1.13 |
| Methyl CH str. of Val | 2974 | 3256 | 2997 | 0.77 |
| Methyl CH str. of Val | 2965 | 3268 | 2974 | 0.30 |
| Methyl CH str. of Val | 2941 | 3259 | 2942 | 0.03 |
| Phenyl CO str. | 1765 | 1998 | 1789 | 1.36 |
| Acetyl CO str. | 1711 | 1950 | 1753 | 2.00 |
| Val CO str. | 1696 | 1913 | 1730 | 2.45 |
| Avg. % error | | | | 1.06 |

Fig. S1. Spectra of AVPO (Black: experiment; Magenta: VSCF-PT2)

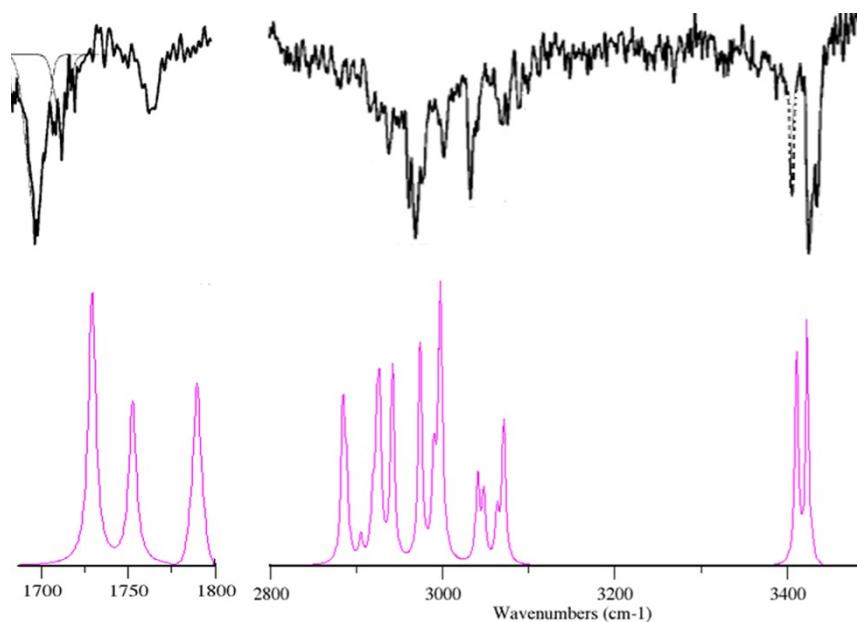


Table S4: Comparisons of computed vibrational harmonic frequencies by HF and MP2 of C7 conformer of NATA (using cc-pVDZ basis)

| | MP2 (Harmonic) | HF (Harmonic) |
|----|----------------|---------------|
| 1 | 3720 | 3921 |
| 2 | 3619 | 3911 |
| 3 | 3610 | 3861 |
| 4 | 3520 | 3773 |
| 5 | 3309 | 3441 |
| 6 | 3239 | 3366 |
| 7 | 3226 | 3353 |
| 8 | 3214 | 3341 |
| 9 | 3212 | 3310 |
| 10 | 3207 | 3332 |
| 11 | 3196 | 3278 |
| 12 | 3174 | 3281 |
| 13 | 3101 | 3199 |
| 14 | 3095 | 3237 |
| 15 | 3084 | 3211 |

Table S5: Comparisons of computed vibrational harmonic frequencies by HF and MP2 of C5 conformer of NATA (using cc-pVDZ basis)

| | MP2 (Harmonic) | HF (Harmonic) |
|----|-----------------------|----------------------|
| 1 | 3726 | 3942 |
| 2 | 3680 | 3911 |
| 3 | 3612 | 3868 |
| 4 | 3573 | 3802 |
| 5 | 3278 | 3407 |
| 6 | 3239 | 3367 |
| 7 | 3227 | 3355 |
| 8 | 3215 | 3344 |
| 9 | 3209 | 3334 |
| 10 | 3217 | 3392 |
| 11 | 3194 | 3287 |
| 12 | 3099 | 3269 |
| 13 | 3149 | 3255 |
| 14 | 3096 | 3202 |
| 15 | 3080 | 3201 |

Table S6: Comparisons of computed vibrational harmonic frequencies by HF and MP2 of AVPO (using cc-pVDZ basis)

| S. No. | MP2 (Harmonic) | HF (Harmonic) |
|--------|----------------|---------------|
| 1 | 3609 | 3866 |
| 2 | 3590 | 3842 |
| 3 | 3246 | 3370 |
| 4 | 3243 | 3350 |
| 5 | 3234 | 3337 |
| 6 | 3222 | 3332 |
| 7 | 3221 | 3359 |
| 8 | 3212 | 3317 |
| 9 | 3206 | 3340 |
| 10 | 3201 | 3318 |
| 11 | 3189 | 3268 |
| 12 | 3181 | 3268 |
| 13 | 3181 | 3278 |
| 14 | 3179 | 3226 |
| 15 | 3177 | 3262 |
| 16 | 3172 | 3259 |
| 17 | 3118 | 3256 |
| 18 | 3110 | 3249 |
| 19 | 3107 | 3245 |
| 20 | 3104 | 3224 |
| 21 | 3093 | 3194 |
| 22 | 3078 | 3186 |
| 23 | 3076 | 3179 |
| 24 | 3071 | 3172 |
| 25 | 1819 | 1998 |
| 26 | 1781 | 1950 |
| 27 | 1763 | 1913 |

**RESULTS OF VIBRATIONAL SCF CALCULATION: (FREQUENCIES IN CM-1) for
NATA-C7 (using HF/MP2 potential with cc-pVDZ basis)**

| HARMONIC | DIAGONAL | VSCF | PT2-VSCF |
|----------|----------|---------|----------|
| 3920.57 | 3743.99 | 3533.98 | 3520.89 |
| 3910.98 | 3535.65 | 3562.47 | 3572.71 |
| 3861.17 | 3469.52 | 3452.83 | 3460.62 |
| 3772.64 | 3436.06 | 3426.71 | 3406.27 |
| 3440.59 | 3177.92 | 3157.81 | 3163.96 |
| 3366.02 | 3173.31 | 3109.76 | 3075.98 |
| 3353.46 | 3220.59 | 3094.68 | 3082.20 |
| 3341.02 | 3181.23 | 3078.51 | 3066.89 |
| 3332.14 | 3202.53 | 3081.40 | 3071.71 |
| 3310.27 | 3191.36 | 2988.99 | 2961.47 |
| 3280.62 | 3099.21 | 2986.22 | 2974.79 |
| 3277.59 | 3206.86 | 2988.11 | 2949.42 |
| 3236.96 | 2977.76 | 2909.16 | 2895.06 |
| 3211.36 | 3029.53 | 2939.89 | 2914.51 |
| 3198.93 | 3023.92 | 3003.48 | 2961.66 |
| 1943.15 | 1781.79 | 1775.32 | 1774.47 |
| 1908.03 | 1741.98 | 1738.23 | 1737.97 |
| 1813.63 | 1672.86 | 1654.08 | 1652.39 |
| 1767.98 | 1615.68 | 1598.02 | 1596.43 |
| 1763.40 | 1612.35 | 1581.31 | 1576.91 |
| 1729.27 | 1599.30 | 1580.90 | 1578.60 |
| 1695.21 | 1559.84 | 1527.24 | 1523.22 |
| 1645.08 | 1516.74 | 1499.62 | 1498.34 |
| 1605.10 | 1462.11 | 1445.77 | 1444.31 |
| 1587.36 | 1474.33 | 1510.58 | 1509.76 |
| 1584.90 | 1456.19 | 1440.69 | 1439.19 |
| 1573.28 | 1448.94 | 1434.91 | 1432.95 |
| 1567.10 | 1458.44 | 1502.50 | 1502.39 |
| 1545.73 | 1416.40 | 1390.47 | 1387.35 |
| 1517.18 | 1392.35 | 1414.62 | 1413.09 |
| 1497.32 | 1380.82 | 1403.46 | 1404.89 |
| 1477.68 | 1356.03 | 1340.56 | 1339.40 |
| 1453.64 | 1342.45 | 1325.94 | 1324.07 |
| 1415.25 | 1320.83 | 1305.85 | 1304.23 |
| 1398.21 | 1292.16 | 1274.03 | 1271.97 |
| 1385.93 | 1364.86 | 1351.91 | 1349.65 |
| 1379.79 | 1259.81 | 1251.04 | 1248.71 |
| 1371.93 | 1265.64 | 1256.25 | 1254.97 |
| 1332.35 | 1250.86 | 1237.87 | 1236.46 |
| 1327.72 | 1227.25 | 1256.08 | 1258.04 |
| 1229.52 | 1144.93 | 1132.11 | 1130.87 |
| 1228.87 | 1159.55 | 1194.57 | 1196.36 |
| 1226.43 | 1141.45 | 1132.58 | 1128.08 |
| 1217.06 | 1194.66 | 1190.41 | 1188.98 |
| 1183.89 | 1104.13 | 1097.21 | 1095.81 |
| 1171.85 | 1092.38 | 1127.89 | 1129.75 |
| 1150.83 | 1051.18 | 1088.85 | 1087.36 |
| 1106.29 | 1026.22 | 1047.09 | 1045.29 |
| 1104.84 | 1026.69 | 1022.74 | 1020.86 |
| 1083.90 | 969.22 | 964.24 | 960.29 |
| 1080.57 | 994.51 | 1010.28 | 1008.95 |
| 1071.75 | 995.54 | 988.29 | 986.44 |
| 1049.02 | 909.26 | 905.69 | 901.72 |
| 1028.34 | 953.23 | 952.62 | 950.49 |
| 981.66 | 832.33 | 817.24 | 811.30 |

| | | | |
|--------|--------|---------|---------|
| 948.08 | 834.29 | 833.33 | 829.64 |
| 946.36 | 881.41 | 879.36 | 878.33 |
| 908.26 | 842.17 | 844.69 | 842.80 |
| 855.17 | 838.70 | 838.48 | 837.68 |
| 830.14 | 755.44 | 756.61 | 751.22 |
| 819.22 | 761.29 | 759.92 | 758.45 |
| 802.24 | 749.55 | 752.51 | 750.28 |
| 784.53 | 734.73 | 739.76 | 738.62 |
| 740.84 | 690.82 | 691.74 | 690.99 |
| 697.08 | 650.85 | 695.85 | 693.36 |
| 684.33 | 702.58 | 725.19 | 711.79 |
| 679.03 | 636.79 | 663.97 | 655.72 |
| 640.67 | 580.99 | 598.95 | 596.88 |
| 631.74 | 542.20 | 548.79 | 548.08 |
| 602.65 | 555.03 | 560.26 | 559.71 |
| 596.52 | 547.19 | 564.02 | 562.96 |
| 564.57 | 523.71 | 536.87 | 533.33 |
| 533.78 | 648.90 | 658.74 | 633.58 |
| 499.10 | 459.38 | 462.29 | 461.22 |
| 484.45 | 513.84 | 541.92 | 523.05 |
| 472.66 | 413.53 | 427.02 | 425.38 |
| 441.91 | 462.47 | 481.97 | 467.26 |
| 418.47 | 536.39 | 538.19 | 525.84 |
| 374.82 | 388.94 | 378.72 | 371.10 |
| 372.03 | 353.81 | 385.12 | 382.83 |
| 324.61 | 322.02 | 319.96 | 316.48 |
| 308.91 | 289.63 | 305.00 | 304.33 |
| 243.62 | 224.55 | 249.04 | 247.15 |
| 218.65 | 208.63 | 232.88 | 232.27 |
| 167.36 | 151.77 | 160.86 | 160.64 |
| 162.17 | 157.89 | 176.68 | 175.82 |
| 124.76 | 129.03 | 133.77 | 132.41 |
| 97.11 | 107.96 | 90.69 | 88.93 |
| 88.49 | 103.75 | 73.54 | 65.18 |
| 58.77 | 82.09 | 125.67 | 116.55 |
| 54.78 | 91.19 | 100.24 | 98.35 |
| 45.27 | 51.25 | -122.60 | -135.58 |
| 30.69 | 38.61 | 40.09 | 39.53 |

**RESULTS OF VIBRATIONAL SCF CALCULATION: (FREQUENCIES IN CM-1) for
NATA-C5 (using HF/MP2 potential with cc-pVDZ basis)**

| HARMONIC | DIAGONAL | VSCF | PT2-VSCF |
|----------|----------|---------|----------|
| 3941.78 | 3762.10 | 3550.71 | 3536.74 |
| 3911.47 | 3536.68 | 3551.43 | 3568.11 |
| 3868.48 | 3473.78 | 3420.39 | 3423.97 |
| 3802.40 | 3488.06 | 3454.97 | 3428.24 |
| 3407.14 | 3143.73 | 3120.24 | 3126.79 |
| 3366.98 | 3172.93 | 3104.73 | 3070.74 |
| 3355.25 | 3225.88 | 3078.46 | 3054.10 |
| 3344.40 | 3203.50 | 3073.71 | 3050.35 |
| 3333.51 | 3211.81 | 3058.73 | 3040.73 |
| 3292.39 | 3223.41 | 3030.38 | 3002.27 |
| 3286.91 | 3194.13 | 3021.18 | 2993.44 |
| 3269.23 | 3031.36 | 2922.98 | 2901.97 |
| 3255.35 | 3141.34 | 2990.60 | 2966.30 |
| 3201.60 | 3029.28 | 2965.05 | 2916.87 |

| | | | |
|---------|---------|---------|---------|
| 3200.79 | 2990.60 | 2911.54 | 2888.88 |
| 1949.17 | 1786.90 | 1780.52 | 1778.43 |
| 1913.98 | 1752.20 | 1740.75 | 1739.02 |
| 1815.06 | 1672.38 | 1653.64 | 1652.20 |
| 1775.68 | 1617.84 | 1600.36 | 1598.79 |
| 1763.28 | 1615.18 | 1584.45 | 1579.66 |
| 1742.40 | 1597.43 | 1579.93 | 1577.92 |
| 1689.66 | 1543.30 | 1515.99 | 1511.86 |
| 1646.34 | 1515.74 | 1497.43 | 1495.97 |
| 1608.32 | 1466.28 | 1450.61 | 1449.18 |
| 1589.48 | 1474.18 | 1480.03 | 1478.71 |
| 1586.52 | 1456.38 | 1450.10 | 1448.73 |
| 1570.89 | 1458.02 | 1474.07 | 1472.94 |
| 1566.41 | 1448.28 | 1428.59 | 1425.50 |
| 1551.45 | 1429.18 | 1421.08 | 1419.24 |
| 1509.97 | 1382.72 | 1374.65 | 1372.15 |
| 1502.43 | 1372.30 | 1352.00 | 1349.26 |
| 1482.19 | 1373.61 | 1358.74 | 1357.51 |
| 1441.72 | 1336.63 | 1320.53 | 1318.60 |
| 1414.20 | 1388.11 | 1375.56 | 1373.79 |
| 1408.17 | 1296.71 | 1282.84 | 1281.31 |
| 1383.98 | 1363.24 | 1349.74 | 1347.26 |
| 1363.06 | 1338.22 | 1332.17 | 1330.27 |
| 1354.99 | 1230.26 | 1225.08 | 1223.07 |
| 1334.76 | 1226.99 | 1214.09 | 1212.63 |
| 1280.16 | 1179.05 | 1165.86 | 1163.72 |
| 1258.83 | 1190.23 | 1182.94 | 1180.32 |
| 1229.76 | 1142.71 | 1134.39 | 1132.81 |
| 1222.58 | 1156.83 | 1150.79 | 1148.80 |
| 1206.16 | 1123.98 | 1121.73 | 1117.30 |
| 1177.14 | 1104.79 | 1095.67 | 1093.65 |
| 1161.89 | 1076.41 | 1071.22 | 1069.85 |
| 1150.40 | 1048.96 | 1052.78 | 1050.26 |
| 1125.10 | 1050.54 | 1036.44 | 1034.31 |
| 1114.37 | 1019.01 | 1022.35 | 1020.68 |
| 1105.75 | 979.64 | 972.80 | 968.62 |
| 1103.94 | 1029.32 | 1027.02 | 1025.00 |
| 1081.88 | 993.38 | 1011.28 | 1008.27 |
| 1068.30 | 933.04 | 923.20 | 918.02 |
| 1038.27 | 957.91 | 952.97 | 951.31 |
| 959.02 | 869.07 | 862.28 | 856.46 |
| 948.72 | 881.13 | 874.85 | 874.12 |
| 938.98 | 795.12 | 785.42 | 780.41 |
| 874.32 | 814.38 | 819.13 | 816.76 |
| 856.62 | 839.21 | 839.02 | 838.35 |
| 837.36 | 822.16 | 831.92 | 830.27 |
| 837.08 | 842.03 | 842.86 | 834.05 |
| 820.35 | 803.90 | 802.90 | 802.20 |
| 809.31 | 793.37 | 795.95 | 794.72 |
| 710.31 | 696.74 | 704.78 | 703.39 |
| 702.39 | 694.60 | 718.15 | 713.23 |
| 687.64 | 628.20 | 637.53 | 636.43 |
| 677.80 | 609.83 | 620.30 | 619.60 |
| 635.04 | 580.27 | 588.43 | 588.09 |
| 630.67 | 548.29 | 550.20 | 549.83 |
| 603.14 | 662.08 | 667.99 | 642.72 |
| 582.92 | 539.15 | 554.66 | 552.57 |
| 535.90 | 497.22 | 522.30 | 521.05 |
| 521.12 | 687.52 | 678.20 | 653.72 |
| 502.16 | 459.78 | 470.24 | 469.43 |

| | | | |
|--------|--------|--------|--------|
| 479.00 | 420.86 | 424.53 | 423.41 |
| 444.97 | 439.13 | 451.03 | 444.56 |
| 388.28 | 541.99 | 549.23 | 534.80 |
| 373.99 | 399.93 | 425.97 | 412.74 |
| 349.30 | 384.83 | 390.35 | 376.18 |
| 335.82 | 342.20 | 340.13 | 334.14 |
| 313.47 | 382.64 | 388.34 | 373.11 |
| 276.44 | 266.32 | 289.43 | 286.19 |
| 251.06 | 232.33 | 247.75 | 247.03 |
| 235.51 | 233.43 | 248.33 | 244.54 |
| 163.15 | 162.96 | 184.48 | 183.33 |
| 157.76 | 143.52 | 160.32 | 159.86 |
| 103.75 | 121.55 | 154.75 | 149.23 |
| 78.68 | 91.76 | 102.39 | 99.97 |
| 69.37 | 85.54 | 141.42 | 141.28 |
| 62.09 | 66.05 | 83.59 | 82.22 |
| 41.56 | 55.58 | 69.31 | 69.70 |
| 25.17 | 25.17 | 25.17 | 25.17 |
| 20.59 | 19.07 | 6.36 | 2.26 |

RESULTS OF VIBRATIONAL SCF CALCULATION: (FREQUENCIES IN CM-1) for AVPO (using HF/MP2 potential with cc-pVDZ basis)

| HARMONIC | DIAGONAL | VSCF | PT2-VSCF |
|----------|----------|---------|----------|
| 3865.84 | 3471.22 | 3423.25 | 3422.50 |
| 3841.81 | 3451.85 | 3406.30 | 3411.46 |
| 3369.50 | 3183.88 | 3111.07 | 3063.64 |
| 3358.79 | 3226.21 | 3095.30 | 3071.16 |
| 3350.27 | 3210.64 | 3073.91 | 3047.91 |
| 3339.78 | 3199.41 | 3072.00 | 3057.68 |
| 3337.17 | 3199.35 | 3065.14 | 3041.17 |
| 3331.90 | 3196.97 | 3062.34 | 3039.73 |
| 3318.43 | 3157.53 | 3022.82 | 3000.77 |
| 3317.13 | 3230.71 | 3013.23 | 2990.34 |
| 3277.75 | 3202.99 | 3018.51 | 2997.62 |
| 3268.32 | 3176.20 | 3008.19 | 2974.07 |
| 3267.62 | 3200.37 | 2966.83 | 2941.13 |
| 3262.20 | 3029.88 | 2933.26 | 2921.84 |
| 3259.06 | 3184.02 | 2975.38 | 2942.06 |
| 3255.69 | 3151.16 | 3031.39 | 2997.36 |
| 3249.38 | 3155.53 | 3016.26 | 2988.13 |
| 3244.58 | 3015.37 | 2937.85 | 2918.87 |
| 3225.60 | 3060.32 | 2982.59 | 2942.11 |
| 3223.88 | 3035.56 | 2972.75 | 2927.04 |
| 3193.96 | 3019.15 | 2957.18 | 2905.20 |
| 3186.00 | 3027.37 | 2945.25 | 2888.69 |
| 3178.71 | 3055.77 | 2950.48 | 2924.08 |
| 3171.50 | 2986.07 | 2900.26 | 2884.33 |
| 1998.19 | 1800.40 | 1790.17 | 1789.47 |
| 1949.79 | 1765.65 | 1754.63 | 1752.92 |
| 1912.57 | 1745.67 | 1731.28 | 1729.62 |
| 1803.93 | 1648.22 | 1628.54 | 1626.23 |
| 1775.30 | 1627.68 | 1605.30 | 1603.60 |
| 1710.25 | 1555.66 | 1528.97 | 1526.16 |
| 1680.52 | 1527.10 | 1499.72 | 1496.38 |
| 1650.12 | 1515.41 | 1497.30 | 1496.21 |
| 1609.86 | 1495.81 | 1491.07 | 1490.47 |

| | | | |
|---------|---------|---------|---------|
| 1604.94 | 1491.71 | 1480.69 | 1479.07 |
| 1601.33 | 1486.58 | 1481.01 | 1480.53 |
| 1598.72 | 1567.22 | 1559.54 | 1558.51 |
| 1597.74 | 1475.11 | 1464.68 | 1463.72 |
| 1593.74 | 1480.00 | 1474.59 | 1474.30 |
| 1592.35 | 1561.67 | 1549.89 | 1548.32 |
| 1589.88 | 1477.74 | 1472.53 | 1471.27 |
| 1583.06 | 1474.21 | 1484.48 | 1482.75 |
| 1581.00 | 1466.53 | 1466.42 | 1466.20 |
| 1565.81 | 1454.18 | 1464.02 | 1461.97 |
| 1539.94 | 1410.78 | 1404.95 | 1403.50 |
| 1529.84 | 1399.85 | 1391.55 | 1390.31 |
| 1523.81 | 1395.83 | 1387.84 | 1386.24 |
| 1513.97 | 1384.62 | 1364.53 | 1362.89 |
| 1499.97 | 1363.17 | 1345.56 | 1343.75 |
| 1489.76 | 1367.08 | 1353.24 | 1351.83 |
| 1478.84 | 1350.30 | 1446.23 | 1447.03 |
| 1461.68 | 1335.70 | 1324.26 | 1323.20 |
| 1457.23 | 1332.17 | 1318.93 | 1317.93 |
| 1424.46 | 1305.47 | 1290.70 | 1289.20 |
| 1418.67 | 1263.36 | 1245.56 | 1243.33 |
| 1382.86 | 1271.39 | 1258.43 | 1256.10 |
| 1371.52 | 1346.16 | 1335.52 | 1333.84 |
| 1359.63 | 1334.61 | 1325.91 | 1324.63 |
| 1335.90 | 1312.07 | 1301.38 | 1299.46 |
| 1316.18 | 1293.25 | 1287.69 | 1285.74 |
| 1312.69 | 1287.03 | 1280.02 | 1278.84 |
| 1307.18 | 1282.49 | 1386.86 | 1387.77 |
| 1301.63 | 1276.54 | 1272.94 | 1272.08 |
| 1282.90 | 1193.34 | 1184.75 | 1182.95 |
| 1278.84 | 1254.08 | 1248.12 | 1247.12 |
| 1273.20 | 1186.69 | 1177.03 | 1172.76 |
| 1237.63 | 1151.32 | 1142.73 | 1141.58 |
| 1219.01 | 1133.44 | 1126.18 | 1125.33 |
| 1204.01 | 1184.48 | 1176.89 | 1175.17 |
| 1173.17 | 1097.50 | 1090.36 | 1088.44 |
| 1168.51 | 1078.80 | 1083.86 | 1082.56 |
| 1148.04 | 1046.75 | 1050.44 | 1047.49 |
| 1131.39 | 1048.92 | 1155.37 | 1155.83 |
| 1122.79 | 1042.96 | 1035.97 | 1034.39 |
| 1108.93 | 1096.97 | 1096.96 | 1092.80 |
| 1107.87 | 1033.45 | 1028.11 | 1026.44 |
| 1091.39 | 1083.21 | 1083.91 | 1078.90 |
| 1083.41 | 1001.67 | 993.54 | 992.22 |
| 1079.71 | 1011.77 | 1027.69 | 1024.39 |
| 1072.24 | 992.87 | 987.02 | 985.37 |
| 1048.16 | 1027.70 | 1027.52 | 1026.17 |
| 1040.06 | 1020.82 | 1029.78 | 1028.73 |
| 1036.97 | 1021.79 | 1027.04 | 1024.67 |
| 1024.14 | 921.22 | 926.94 | 924.49 |
| 1006.36 | 944.06 | 953.65 | 952.48 |
| 994.32 | 928.67 | 945.43 | 942.82 |
| 962.18 | 888.41 | 889.90 | 888.28 |
| 946.40 | 878.12 | 876.93 | 871.19 |
| 915.49 | 858.75 | 857.28 | 856.38 |
| 901.95 | 828.57 | 830.16 | 829.05 |
| 855.58 | 798.02 | 799.31 | 798.61 |
| 830.42 | 772.54 | 774.61 | 773.81 |
| 823.53 | 746.71 | 754.05 | 751.45 |
| 774.98 | 764.78 | 773.68 | 770.89 |

| | | | |
|--------|--------|--------|--------|
| 767.50 | 708.64 | 715.08 | 714.09 |
| 697.19 | 643.88 | 651.24 | 650.09 |
| 692.74 | 680.25 | 689.43 | 686.83 |
| 676.66 | 630.37 | 654.20 | 651.49 |
| 676.54 | 617.60 | 615.34 | 615.16 |
| 660.15 | 594.97 | 603.08 | 602.56 |
| 633.19 | 593.34 | 620.78 | 616.39 |
| 596.44 | 721.15 | 721.65 | 691.43 |
| 562.90 | 513.95 | 534.90 | 531.84 |
| 531.60 | 494.71 | 499.85 | 499.06 |
| 518.59 | 666.36 | 663.92 | 648.08 |
| 490.59 | 465.10 | 579.97 | 575.84 |
| 459.84 | 414.97 | 431.49 | 430.71 |
| 454.55 | 412.31 | 418.26 | 417.35 |
| 432.57 | 400.90 | 426.29 | 423.92 |
| 408.21 | 403.41 | 414.42 | 409.55 |
| 387.54 | 361.91 | 375.88 | 375.47 |
| 376.20 | 351.68 | 367.35 | 366.42 |
| 333.83 | 311.71 | 327.38 | 327.14 |
| 307.00 | 273.08 | 280.89 | 280.70 |
| 286.30 | 274.90 | 292.07 | 291.60 |
| 277.17 | 285.19 | 314.47 | 308.02 |
| 260.68 | 304.09 | 315.53 | 304.26 |
| 236.03 | 234.30 | 269.54 | 268.12 |
| 234.63 | 325.72 | 328.53 | 315.87 |
| 202.99 | 205.09 | 221.69 | 219.62 |
| 181.79 | 181.42 | 203.38 | 202.22 |
| 167.88 | 236.82 | 242.43 | 239.19 |
| 164.86 | 199.81 | 228.86 | 224.55 |
| 143.15 | 183.74 | 193.04 | 189.63 |
| 121.00 | 114.37 | 137.37 | 136.29 |
| 90.79 | 114.38 | 135.02 | 133.46 |
| 81.34 | 90.06 | 112.79 | 112.12 |
| 67.35 | 90.52 | 97.58 | 96.57 |
| 65.67 | 82.95 | 95.64 | 95.22 |
| 63.24 | 94.75 | 107.71 | 107.61 |
| 55.89 | 86.56 | 302.47 | 301.74 |
| 53.01 | 73.96 | 175.40 | 172.81 |
| 43.30 | 66.43 | 75.24 | 73.71 |
| 27.34 | 40.18 | 47.18 | 47.78 |
| 19.74 | 26.95 | 37.47 | 38.35 |
| 14.26 | 19.72 | 22.07 | 22.08 |

Optimized coordinates of NATA-C5 at MP2/cc-pVDZ

| | | | | |
|---|-----|---------------|---------------|---------------|
| N | 7.0 | 2.0944038867 | -2.2504652013 | 3.6105076247 |
| C | 6.0 | 2.5134311507 | -0.9949902008 | 4.0078138436 |
| C | 6.0 | 2.0360174903 | -0.0622560009 | 3.0338134415 |
| C | 6.0 | 1.3119281064 | -0.8136073440 | 2.0369663171 |
| C | 6.0 | 1.3714860608 | -2.1472324565 | 2.4364928397 |
| C | 6.0 | 3.2626637376 | -0.5901811374 | 5.1307670890 |
| C | 6.0 | 3.5217433408 | 0.7776977592 | 5.2666142721 |
| C | 6.0 | 3.0461903739 | 1.7195208342 | 4.3138004294 |
| C | 6.0 | 2.3046005695 | 1.3206984297 | 3.1983299148 |
| C | 6.0 | 0.6386478012 | -0.2297576254 | 0.8308445564 |
| C | 6.0 | 1.6354392429 | 0.3977652576 | -0.1832312793 |
| N | 7.0 | 0.9597086888 | 1.2913972485 | -1.0957683970 |
| C | 6.0 | 0.6626571412 | 2.5699481661 | -0.7172241618 |
| C | 6.0 | 0.1204022423 | 3.4579901837 | -1.8238837066 |
| C | 6.0 | 2.3290793858 | -0.6725286288 | -1.0313581696 |
| N | 7.0 | 3.2142719278 | -1.4515881362 | -0.3422787065 |
| O | 8.0 | 2.1112455517 | -0.7909685992 | -2.2365661194 |
| O | 8.0 | 0.8300247200 | 2.9729186581 | 0.4367523206 |
| H | 1.0 | 3.6241740276 | -1.3121519004 | 5.8714620343 |
| H | 1.0 | 4.0996040023 | 1.1294567036 | 6.1278901866 |
| H | 1.0 | 3.2639322299 | 2.7823849392 | 4.4627882324 |
| H | 1.0 | 1.9268968298 | 2.0494084834 | 2.4711815300 |
| H | 1.0 | 0.9379273609 | -3.0319882731 | 1.9670700155 |
| H | 1.0 | 2.2543457047 | -3.1104316642 | 4.1222314634 |
| H | 1.0 | 0.0197144806 | -0.9834998930 | 0.3111213179 |
| H | 1.0 | -0.0278504484 | 0.5894140767 | 1.1501689537 |
| H | 1.0 | 2.3936741168 | 0.9620249599 | 0.3897830120 |
| H | 1.0 | 3.5470694585 | -2.2837976817 | -0.8203839033 |
| H | 1.0 | 0.9633288124 | 1.0019385763 | -2.0721225681 |
| H | 1.0 | -0.6473120613 | 4.1215883133 | -1.4005794503 |
| H | 1.0 | 0.9382139972 | 4.0895721193 | -2.2087687038 |
| H | 1.0 | -0.3051946965 | 2.8801580557 | -2.6586574637 |
| H | 1.0 | 3.1471947674 | -1.4789350217 | 0.6717302348 |

Optimized coordinates at NATA-C7 at MP2/cc-pVDZ

| | | | | |
|---|-----|---------------|---------------|---------------|
| C | 6.0 | -1.6885016730 | -0.1662461258 | 0.4609377502 |
| C | 6.0 | -2.6010527744 | -0.7247055354 | -0.4940284842 |
| C | 6.0 | -3.7470009596 | -0.0333646634 | -0.9358179566 |
| C | 6.0 | -3.9736677867 | 1.2420543542 | -0.4084643953 |
| C | 6.0 | -3.0836946295 | 1.8172942615 | 0.5389971943 |
| C | 6.0 | -1.9491131210 | 1.1295297741 | 0.9793591140 |
| C | 6.0 | -0.6416568579 | -1.1359599058 | 0.6737590785 |
| C | 6.0 | -0.9439079889 | -2.2190092989 | -0.1464439450 |
| H | 1.0 | -4.4352637821 | -0.4745554070 | -1.6653929516 |
| H | 1.0 | -4.8539044115 | 1.8075654765 | -0.7316968082 |
| H | 1.0 | -3.2965848756 | 2.8169915122 | 0.9326552850 |
| H | 1.0 | -1.2719849161 | 1.5831016033 | 1.7124035894 |
| H | 1.0 | -0.3815698230 | -3.1399986223 | -0.2940188042 |
| H | 1.0 | -2.5467402312 | -2.6043350727 | -1.4943360653 |
| N | 7.0 | -2.1169047822 | -1.9691779402 | -0.8317262352 |
| C | 6.0 | 0.5571351559 | -0.9754539734 | 1.5680953347 |
| H | 1.0 | 0.2946971996 | -0.3246634768 | 2.4200422691 |
| H | 1.0 | 0.8709993948 | -1.9509053155 | 1.9695872350 |
| C | 6.0 | 1.7572096040 | -0.3569382019 | 0.8340693712 |
| H | 1.0 | 2.5233332394 | -0.0274957648 | 1.5614251119 |
| C | 6.0 | 2.4420452905 | -1.3957861926 | -0.0827155390 |
| O | 8.0 | 2.0932019083 | -2.5747991883 | -0.1284973386 |
| N | 7.0 | 3.4681532158 | -0.8736689554 | -0.8096333363 |
| H | 1.0 | 4.0401465020 | -1.5227721395 | -1.3389088018 |
| H | 1.0 | 3.8176103677 | 0.0569449859 | -0.5793205163 |
| N | 7.0 | 1.3261359967 | 0.8376415562 | 0.1184489740 |
| H | 1.0 | 0.3702030348 | 0.8461169522 | -0.2308054973 |
| C | 6.0 | 2.1582170683 | 1.8768640631 | -0.1664433133 |
| O | 8.0 | 3.3654036124 | 1.8605421601 | 0.1081103017 |
| C | 6.0 | 1.4998127266 | 3.0569643152 | -0.8574086864 |
| H | 1.0 | 1.8563239346 | 3.9816339499 | -0.3795056842 |
| H | 1.0 | 1.8244858046 | 3.0795240282 | -1.9106366217 |
| H | 1.0 | 0.4003355567 | 3.0184047872 | -0.8167276283 |

Optimized coordinates of AVPO at MP2/cc-pVDZ

| | | | | |
|---|-----|---------------|---------------|---------------|
| C | 6.0 | 1.4074560215 | -1.4677471893 | -1.0084177288 |
| C | 6.0 | 1.7870512199 | -0.1464511168 | -1.7415692846 |
| H | 1.0 | 2.7480019524 | -0.3079507824 | -2.2575071858 |
| H | 1.0 | 1.0110256366 | 0.0406448853 | -2.4996821193 |
| C | 6.0 | 1.8675181474 | 1.0002496084 | -0.7634099487 |
| C | 6.0 | 0.7145211076 | 1.7549065239 | -0.4568146268 |
| C | 6.0 | 3.0606663688 | 1.2777904011 | -0.0639073379 |
| H | 1.0 | -0.2114459794 | 1.5662445718 | -1.0123847031 |
| C | 6.0 | 0.7392498044 | 2.7443716120 | 0.5407069217 |
| C | 6.0 | 3.0982207770 | 2.2798788625 | 0.9205550135 |
| H | 1.0 | 3.9684040632 | 0.7096489877 | -0.3021944429 |
| H | 1.0 | -0.1797866216 | 3.2882854476 | 0.7821689330 |
| C | 6.0 | 1.9351342889 | 3.0064098922 | 1.2321532290 |
| H | 1.0 | 4.0340514514 | 2.4890777422 | 1.4500806324 |
| H | 1.0 | 1.9616625425 | 3.7771032389 | 2.0097475628 |
| H | 1.0 | 1.2508232041 | -2.2564667038 | -1.7647276923 |
| C | 6.0 | 2.5347867536 | -1.8927239910 | -0.0793335846 |
| O | 8.0 | 2.4555207604 | -1.9382883767 | 1.1341797154 |
| O | 8.0 | 3.6491864644 | -2.1804702387 | -0.7823178647 |
| C | 6.0 | 4.7738124498 | -2.5469173077 | 0.0407805751 |
| H | 1.0 | 5.5970527848 | -2.7390513763 | -0.6581444897 |
| H | 1.0 | 5.0293255199 | -1.7271515702 | 0.7292950079 |
| H | 1.0 | 4.5444928802 | -3.4481361941 | 0.6288489100 |
| N | 7.0 | 0.2251403268 | -1.3225835466 | -0.1805073196 |
| H | 1.0 | 0.4175536817 | -1.1368850781 | 0.8026706886 |
| C | 6.0 | -0.9548015256 | -0.8902976534 | -0.7061020556 |
| O | 8.0 | -1.1966176196 | -0.8893018826 | -1.9175658496 |
| C | 6.0 | -1.9765948333 | -0.4158299649 | 0.3296044475 |
| H | 1.0 | -1.4663162686 | 0.2068644867 | 1.0857103464 |
| C | 6.0 | -2.6615997519 | -1.6027031602 | 1.0444282258 |
| H | 1.0 | -1.8527160994 | -2.1947089189 | 1.5163762880 |
| C | 6.0 | -3.5963380718 | -1.0822051119 | 2.1397887075 |
| H | 1.0 | -4.0439546511 | -1.9208980939 | 2.6995416342 |
| H | 1.0 | -3.0606743692 | -0.4304918744 | 2.8497613209 |
| H | 1.0 | -4.4131824304 | -0.4918590224 | 1.6912966539 |
| C | 6.0 | -3.4109374617 | -2.4969151754 | 0.0520668954 |
| H | 1.0 | -4.2114402233 | -1.9219131595 | -0.4451974125 |
| H | 1.0 | -2.7436344433 | -2.8993577908 | -0.7282555311 |
| H | 1.0 | -3.8809452449 | -3.3464238951 | 0.5757826475 |
| N | 7.0 | -2.9257364615 | 0.4467885665 | -0.3525518460 |
| H | 1.0 | -3.0259277869 | 0.2370027521 | -1.3459775954 |
| C | 6.0 | -3.0557590669 | 1.7664543292 | 0.0305638529 |
| O | 8.0 | -2.6250843641 | 2.1990138170 | 1.0985623921 |
| C | 6.0 | -3.7827647263 | 2.6387896065 | -0.9786568762 |
| H | 1.0 | -3.0435111906 | 3.0864161938 | -1.6647560674 |
| H | 1.0 | -4.5104317121 | 2.0650022122 | -1.5731731081 |
| H | 1.0 | -4.2926623040 | 3.4529244374 | -0.4450889308 |