

25/09/2015

Benay and Wipff

**Liquid-Liquid Extraction of Alkali Cations by 18-Crown-6: Complexation
and Interface Crossing Studied by MD and PMF Simulations**

by Gael Benay and Georges Wipff *

Laboratoire MSM, UMR 7177, Institut de Chimie, 1 rue B. Pascal, 67000 Strasbourg,
France. wipff@unistra.fr

Electronic Supplementary Information

Table S1: Force field parameters: alkali ion parameters and atomic polarizabilities of Pic⁻, Cl⁻ ions, 18C6 and solvents used for the "POL" model. Sets of 18C6 charges.

Alkali ion parameters

Ion	R* (Å)	ε (kcal / mol)	α (Å ³)	Ref.
Na ⁺	1.4502	0.1		L. X. Dang, <i>J. Am. Chem. Soc.</i> , 117 (1995) 6954
Na ⁺ POL	1.3350	0.1	0.240	L. X. Dang, <i>J. Phys. Chem. A</i> , 108 (2004) 9014
K ⁺	1.8700	0.1		L. X. Dang, <i>J. Am. Chem. Soc.</i> , 117 (1995) 6954
K ⁺ POL	1.7701	0.1	0.830	T.-M. Chang, L. X. Dang, <i>J. Phys. Chem. B</i> , 101 (1997) 10518
Cs ⁺	2.1798	0.1		L. X. Dang, <i>J. Am. Chem. Soc.</i> , 117 (1995) 6954
Cs ⁺ POL	2.1501	0.1	2.440	T.-M. Chang, L. X. Dang, <i>J. Phys. Chem. B</i> , 101 (1997) 10518

Atomic polarizabilities of Pic⁻, Cl⁻ ions, 18C6 and solvents used for the "POL" model.

Atom type	α (Å ³)	q (e)
C (18C6; CHCl ₃)	0.878 ^a	
H _C (18C6; CHCl ₃)	0.135 ^a	
N (Pic ⁻)	0.530 ^a	
O (18C6; Pic ⁻)	0.465 ^a	
C _{Pic} (Pic ⁻)	0.360 ^b	
H _{Pic} (Pic ⁻)	0.167 ^b	
Cl (CHCl ₃ ; Cl ⁻)	1.910 ^c	
O (H ₂ O POL3)	0.528 ^a	-0.730
H (H ₂ O POL3)	0.170 ^a	0.365

a: Caldwell J.W. and Kollman P.A., *J. Phys. Chem.*, **1995**, 99, 6208

b: Wang, J.; Cieplak, P.; Kollman, P. A., *J. Comput. Chem.*, **2000**, 21, 1049

c: Chang, T.-M.; Dang, L. X.; Peterson, K. A., *J. Phys. Chem. B*, **1997**, 101, 3413

d: Dang, L. X., Chang, T.-M., *J. Chem. Phys.* **119** (2003) 9851-9857

Atomic charges of 18C6 and corresponding dipole moment of dimethyl ether (in D).

Model	q _C	q _H	q _O	q _M	μ _{MeOMe} ^a
18C6(-0.4)	0.244	-0.021	-0.406	+1.000	1.45
18C6(-0.5)	0.300	-0.025	-0.500	+1.000	1.79
18C6(-0.6)	0.360	-0.030	-0.600	+1.000	2.15
18C6(-0.34) ^b	0.086	0.042	-0.340	+1.000	1.43
18C6(-0.30) ^c	0.089	0.032	-0.305	+1.000	1.26
18C6(+0.4)/M(+0.6) ^d	-0.055	0.093	-0.198	+0.618	

a: Experimental value: 1.31 D ; QM value (HF/6-31G(d,p)) : 1.52 D;

b: ESP HF/6-31G(d,p) charges on 18C6.

c: ESP DFT/6-31G(d,p) charges on 18C6.

d: ESP DFT/6-31G(d,p) charges on the whole complex.

Table S2: Complexation of M^+ by 18C6 (" D_{3d} "^a) in the gas phase: complexation energy E_c , enthalpy ΔH , and free energy ΔG (kcal/mol). Average M-O distances. QM (Gaussian 09 software) and AMBER results.

M^+	Na^+	$Na^+ Pic^-$	K^+	$K^+ Pic^-$	$Cs^+{}^b$	$Cs^+ Pic^-{}^b$
QM HF/6-31G(d,p)						
E_c	-87.3		-69.0		-43.6	
ΔG	-77.7		-56.5		-32.7	
ΔH	-85.7		-68.8		-42.9	
q_M (Mulliken)	0.71		0.80		0.89	
q_O (Mulliken)	-0.67		-0.68		-0.70	
$\langle d_{M-O} \rangle$ (Å)	2.700		2.814		3.131	
QM HF/6-311++G(d,p)						
E_c	-84.5		-70.2		-48.3	
ΔG	-74.8		-57.7		-37.2	
ΔH	-82.8		-69.9		-47.5	
QM DFT/6-31G(d,p)						
E_c	-83.3	-33.2	-70.5	-31.5	-34.6	-13.6
ΔG	-74.4		-59.6		-23.7	
ΔH	-81.4		-69.0		-33.4	
q_M (ESP)	0.66	0.41	0.62	0.43	0.78	0.53
q_O (ESP)	-0.25	-0.20	-0.20	-0.18	-0.20	-0.20
$\langle d_{M-O} \rangle$ (Å)	2.769		2.807		3.149	
QM DFT/6-311++G(d,p)						
E_c	-82.4		-70.3		-47.9	
ΔG	-73.5		-59.4		-37.4	
ΔH	-80.6		-68.7		-50.3	
AMBER q_O -0.4						
E_c	-56.5		-49.5		-39.8	
	31.4% ^c		29.6% ^c		16.9% ^c	
AMBER q_O -0.4 + POL						
E_c	-66.5		-59.2		-48.3	
	19.3% ^c		15.8% ^c		0.8% ^c	
AMBER q_O -0.5						
E_c	-68.2		-61.1		-49.7	
	17.2% ^c		13.1% ^c		3.7% ^c	
AMBER q_O -0.6						
E_c	-79.3		-72.4		-59.8	
	3.8% ^c		3.0% ^c		24.8% ^c	
			-75.8 ^d			
			7.8% ^c			
AMBER q_O -0.34^e						
E_c	-63.7		-56.7		-46.1	
	22.7% ^c		19.3% ^c		3.7% ^c	
AMBER q_O -0.34 + POL^e						
E_c	-73.3		-66.1		-54.5	
	11.0% ^c		6.0% ^c		13.8% ^c	
AMBER q_O -0.30^f						
E_c	-56.1		-49.2		-39.8	
	31.9% ^c		30.0% ^c		16.9% ^c	

a: Conformation of 18C6 complexed and uncomplexed.

b: Cs^+ sits in "perched" position over the ring and is described by a SDD basis set with the Stuttgart/Dresden ECPs.

c: % difference relative to E_c at the QM DFT/6-311++G(d,p) level.

d: Cheatham's M^+ parameters: Joung, I. S., Cheatham III, T. E., *J. Phys. Chem. B*, **2008**, *112*, 9020.

e: ESP HF/6-31G(d,p) charges on 18C6.

f: ESP DFT/6-31G(d,p) charges on 18C6.

Table S3: Dissociation PMF_{0.01+t} of 18C6/M⁺ X⁻ complexes (sampling time *t* in ns). Free energy difference ΔA_{CD} (in kcal / mol) between complexed and decomplexed states in water and at interface. Corresponding "selectivities" $\Delta\Delta A_{CD}$

M ⁺	q_0	<i>t</i>	Na ⁺	K ⁺	Cs ⁺	Selectivity $\Delta\Delta A_{CD}$			Order
						K/Na	Cs/K	Na/Cs	
In water M⁺ Cl⁻									
(SPC/E)	-0.4	0.16	6.2	6.0	5.1	+0.2	+0.9	-1.1	Na > K > Cs
		0.5	4.6	4.0	2.8	+0.6	+1.2	-1.8	
	-0.5	0.16	5.0	8.1	3.5	-3.1	+4.6	-1.5	K > Na > Cs
		0.5	6.0	8.8	4.3	-2.8	+4.5	-1.7	
	-0.6	0.16	8.4	9.1	5.0	-0.7	+4.1	-3.4	K > Na > Cs
		0.5	6.6	8.3	4.4	-1.7	+3.9	-2.2	
	-0.34 ^a	0.5	6.4	7.9	3.3	-1.5	+4.6	-3.1	K > Na > Cs
		3.0	6.0	7.4	3.4	-1.4	+4.0	-2.6	
	-0.4+POL	0.5	3.3	8.5	4.2	-2.8	+1.4	+1.4	K > Cs > Na
	(TIP3P)	-0.6	0.5	7.0	11.0	5.2	-4.0	+5.8	-1.8
-0.6 Ch. ^b		0.5	5.2	10.7	8.3	-5.5	+2.4	+3.1	
	Exp. ^c		1.1	2.8	1.3	-1.7	+1.5	+0.2	K > Cs > Na
At the interface M⁺ Pic⁻									
CHCl ₃ / SPC/E	-0.34 ^c	0.5	5.1	7.3	6.2	-2.2	+1.1	+1.1	K > Cs > Na

a: ESP HF 6-31G(d,p) charges on 18C6.

b: Cheatham's parameters.

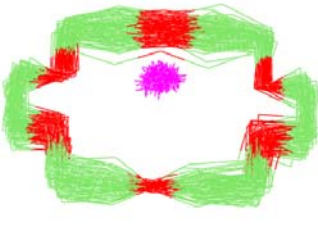
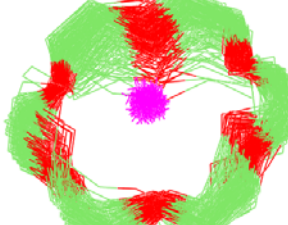
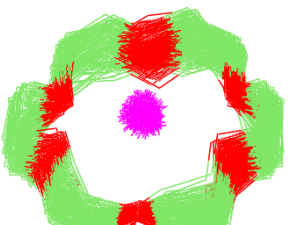

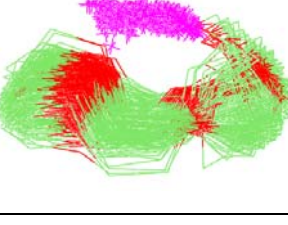
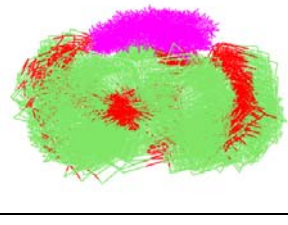

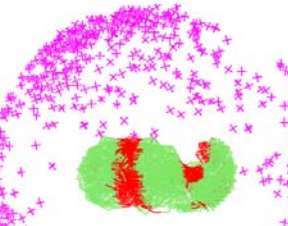
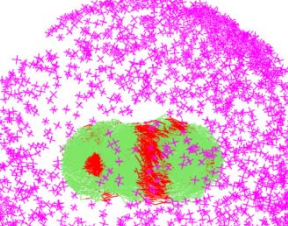
c: Experimental $-\Delta G_c$ decomplexation energy.

Table S4: Analysis of 18C6/ M^+ complexes in water and at interface: $M^+ \dots O(18C6)$ and $M^+ \dots X^-$ distances (in Å), hydration number of M^+ , $n_{+/-}$ number of $g^+ \leftrightarrow g^-$ interconversions of OC-CO dihedrals, and interaction energies (in kcal/mol) between 18C6, M^+ and Water. Averages during 2 ns except when otherwise noted. ^a See also Figures S7 to S9.

		Na ⁺	K ⁺	Cs ⁺
<i>In Water</i>				
18C6(-0.6)	$d_{M-O(18C6)}$	2.6 (x4), 3.2 (x2)	3.0 (x6)	3.2 (x6)
	d_{M-Cl}	14.5 ± 3.9	14.6 ± 3.5	13.0 ± 4.5
	$N_{Water}(M^+)$	2.1 ± 0.3	2.6 ± 0.7	3.5 ± 1.1
	$n_{+/-}$	70	28	9
	$E_{18C6/M}$	-86 ± 6	-70 ± 5	-62 ± 6
	$E_{18C6/Wat}$	-30 ± 7	-33 ± 7	-41 ± 9
	$E_{M/Wat}$	-62 ± 10	-48 ± 10	-36 ± 18
18C6(-0.4) POL	$d_{M-O(18C6)}$	2.9 (x6)	2.9 (x6)	3.3 (x6) ^a
	d_{M-Cl}	14.7 ± 3.4	13.8 ± 4.2	14.0 ± 3.3 ^a
	$N_{Water}(M^+)$	2.0 ± 0.1	2.1 ± 0.5	3.5 ± 0.9 ^a
	$n_{+/-}$	18	4	6 ^a
18C6(-0.34)	$d_{M-O(18C6)}$	2.8 (x6)	3.0 (x6)	3.2 (x6)
	d_{M-Cl}	16 ± 3	15 ± 3	15 ± 3
	$N_{Water}(M^+)$	2.0 ± 0.1	2.7 ± 0.5	3.5 ± 0.7
	$n_{+/-}$ conversions	61	9	0
	$E_{18C6/M}$	-67 ± 3	-53 ± 3	-47 ± 3
	$E_{18C6/Wat}$	-16 ± 5	-21 ± 5	-27 ± 6
	$E_{M/Wat}$	-74 ± 10	-63 ± 9	-53 ± 9
<i>At the interface</i>				
18C6(-0.34)	$d_{M-O(18C6)}$	2.8 (x6)	3.0 (x6)	3.2 (x6)
	d_{M-Pic}	6.9 ± 1.0	20 ± 11	13.3 ± 4.7
	$N_{Water}(M^+)$	2.1 ± 0.3	2.1 ± 0.7	3.0 ± 0.8
	$n_{+/-}$	26	0	0
	$E_{18C6/M}$	-67 ± 4	-57 ± 3	-47 ± 3
	$E_{18C6/Wat}$	0 ± 5	-2 ± 4	-2 ± 3
	$E_{M/Pic}$	-44 ± 4	-23 ± 17	-30 ± 11
	$E_{M/Wat}$	-60 ± 10	-61 ± 20	-54 ± 14

^a: Average over 1 ns since M^+ decomplexes afterwards.

Figure S1: Complexation of $K^+ Cl^-$ by 18C6(-0.6) in SPC/E water: cumulated view of the complex (C in green, O in red, K in purple; recentered on the mean plane of O_1 , O_7 and O_{13} oxygens) at different steps of $PMF_{0.01+0.16}$, $PMF_{0.01+0.5}$ and $PMF_{0.01+3.0}$.

$d_{K-CM(18C6)}$	$PMF_{0.01+0.16}$	$PMF_{0.01+0.5}$	$PMF_{0.01+3.0}$
0.9 Å			
2.5 Å			
8.3 Å			

☞ Note that along a "rapid" PMF (for instance $PMF_{0.01+0.08}$ or $PMF_{0.01+0.16}$) M^+ always sits on top of a single face of the crown. Along a "long" PMF ($PMF_{0.01+3}$) it explores the two faces of the crown at long distances ($d > 8 \text{ \AA}$), while being restrained at a single face at shorter distances, thereby causing some entropy penalty.

Figure S2: Complexation PMF of $K^+ Cl^-$ by 18C6(-0.4) in SPC/E water: association (in blue) and dissociation (in red) pathways. Free energy curves (ΔA in kcal / mol, as a function of the d distance in Å) for different sampling times.

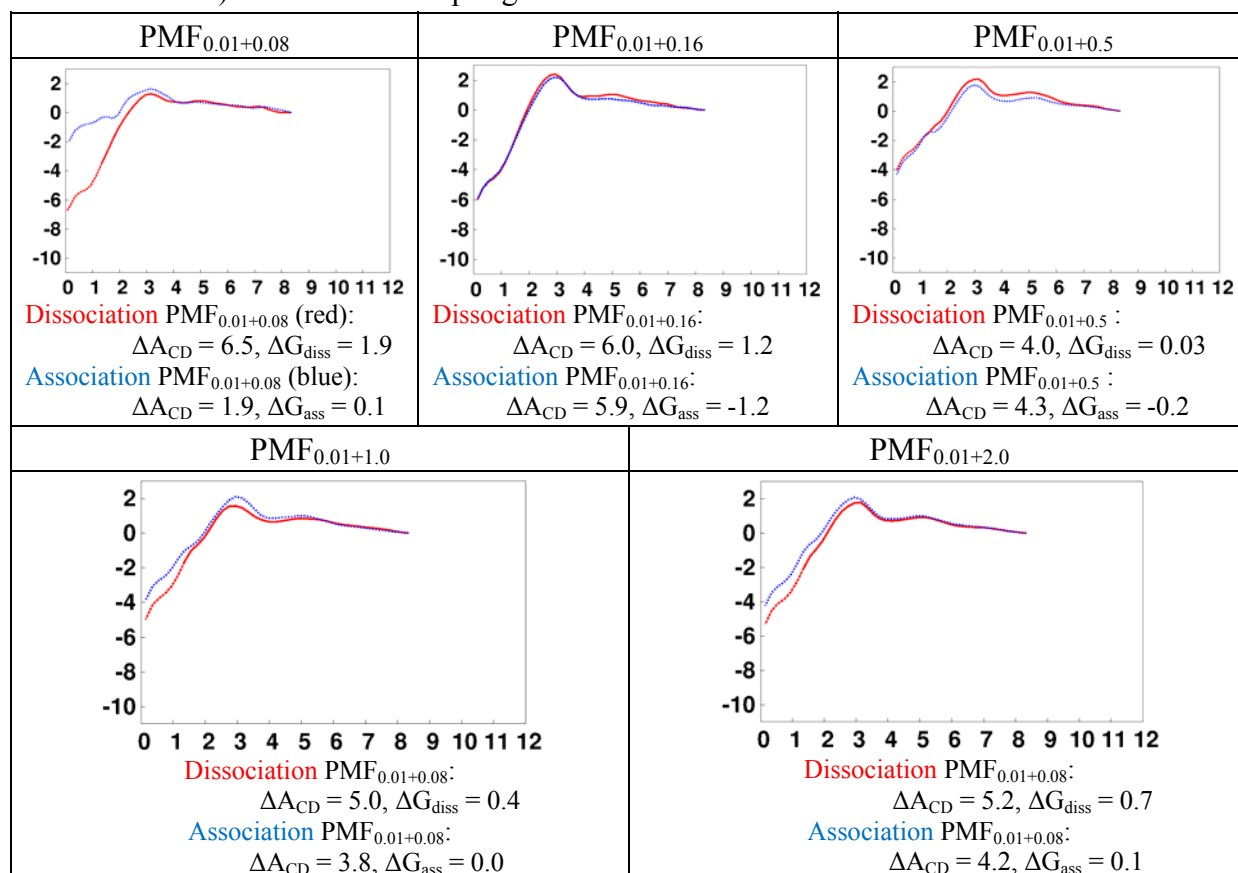


Figure S3: Complexation of $K^+ Cl^-$ by 18C6 in SPC/E water: association or dissociation PMF_{0.01+0.5} with different charges. From top to bottom: (i) Free energy curves (ΔA in kcal / mol, as a function of the d distance in Å) and binding energies ΔG_{ass} and ΔG_{diss} . (ii) Average energy components as a function of the d distance. Energies for the C (complexed) and D (decomplexed) states from the "diss" and "ass" pathways. (iii) Typical structures along the Association and Dissociation PMFs (at K-CM(18C6) distances of 0.7, 1.3 and 1.7 Å, respectively). PMFs results with the three cations and PMF_{0.01+0.016} sampling are shown in Figure S4.

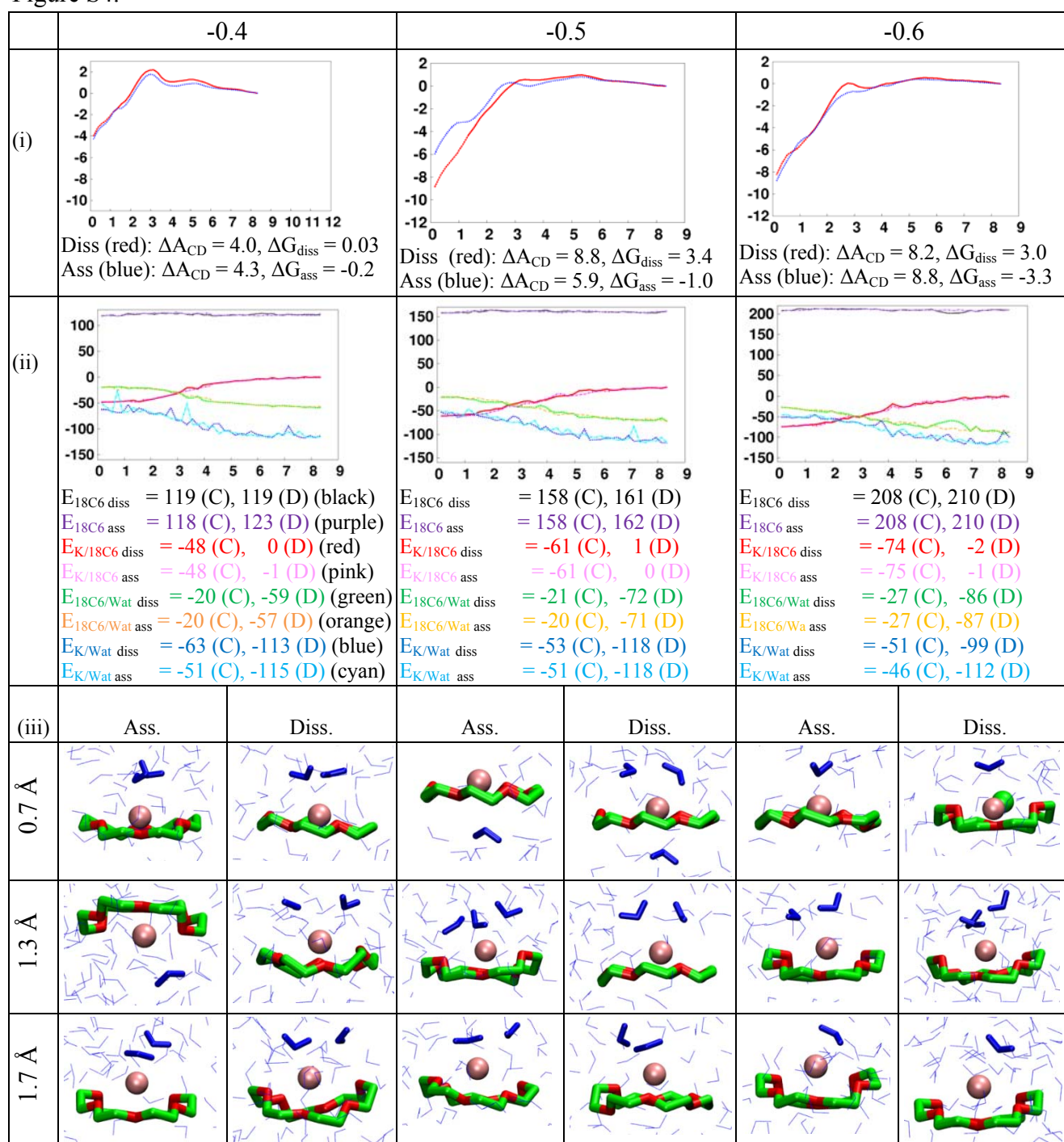


Figure S4: Complexation of $M^+ Cl^-$ by 18C6 in SPC/E water: dissociation PMF_{0.01+0.16} with different charges. Free energy curves (ΔA in kcal / mol, as a function of the d distance in Å) for Na^+ to Cs^+ cations.

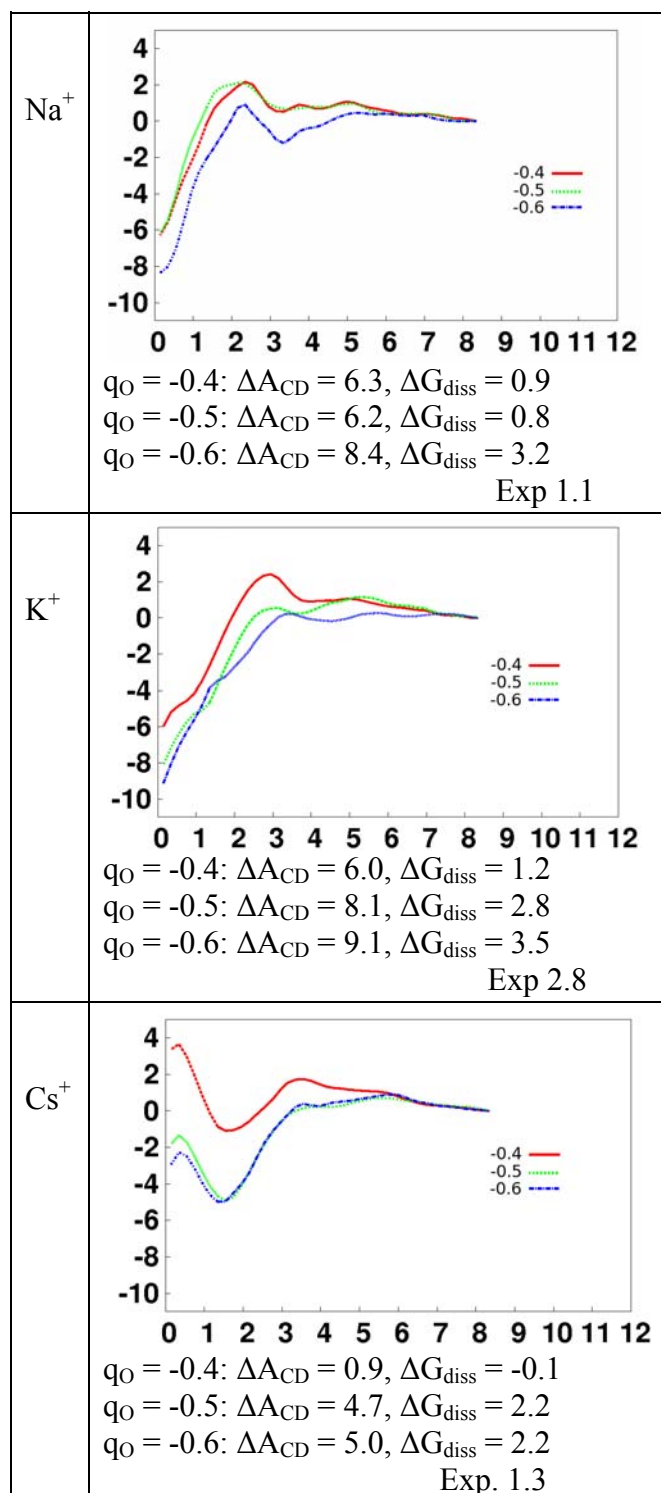


Figure S5: Complexation PMF_{0.01+0.5} of Na⁺ to Cs⁺ chlorides by 18C6(-0.6) in SPC/E water. From top to bottom: (i) Free energy curves (ΔA in kcal / mol, as a function of the d distance in Å). (ii) Snapshots of the complexed and decomplexed states.

(iii to v): Analysis as a function of the d distance: (iii) Curves of energy components, and average energies for Complexed and Decomplexed states. (iv) Number of H₂O molecules coordinated to M⁺. (v) The six OC-CO dihedrals of 18C6 along the PMF. Results with other models are shown in Figure S6.

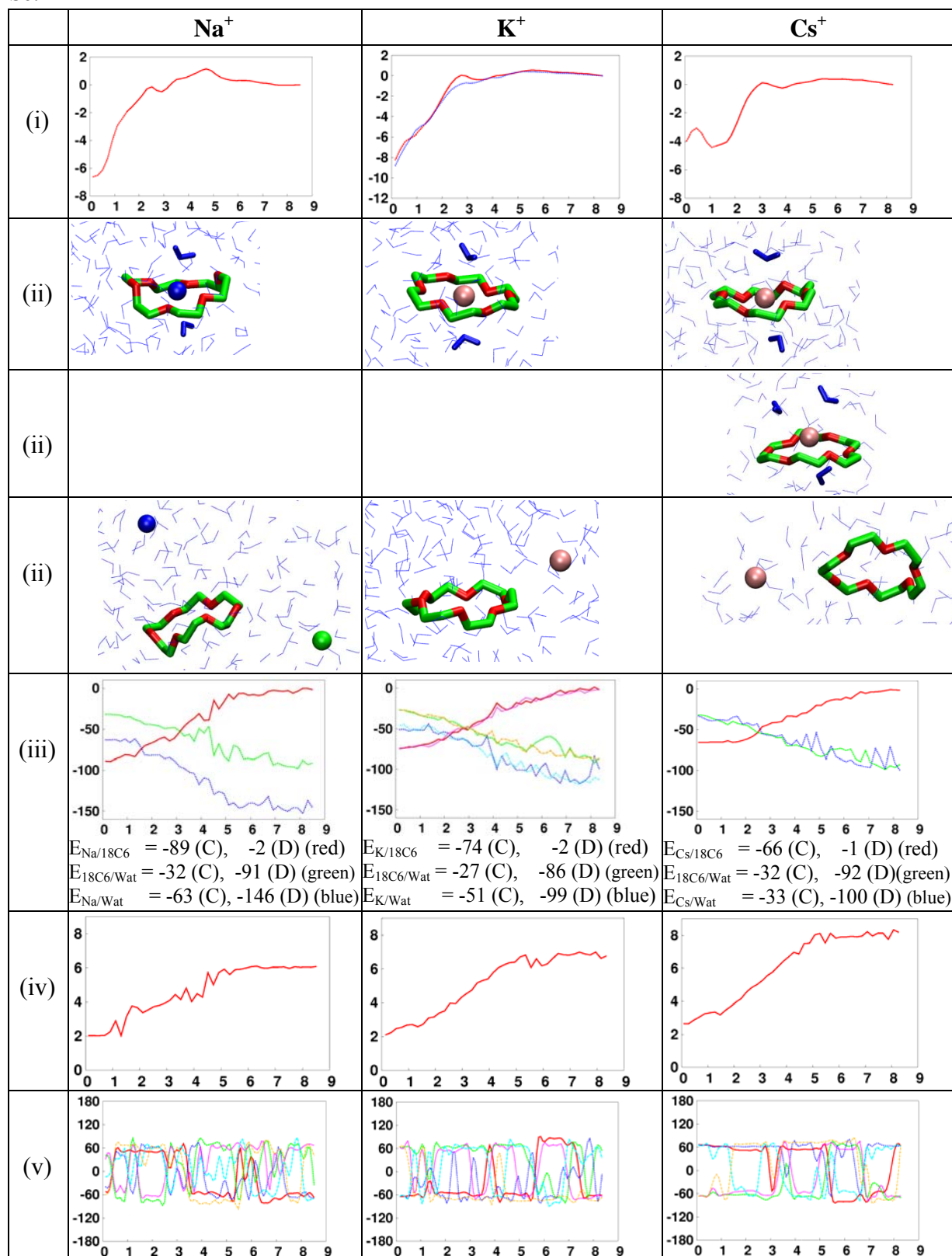


Figure S6: Dissociation PMF_{0.01+0.5} of 18C6/ M⁺ X⁻ complexes in water. (i) Free energy curves (ΔA in kcal / mol, as a function of the d distance in Å) with three models: 18C6(-0.6) (red), 18C6(-0.34) (blue) and POL (green). Snapshots along the PMF ("POL" model) at several d distances : (ii) $d \approx 0$ Å (complexed state); (iii) $d \approx 2$ Å ; (iv) $d \approx 8$ Å (decomplexed state).

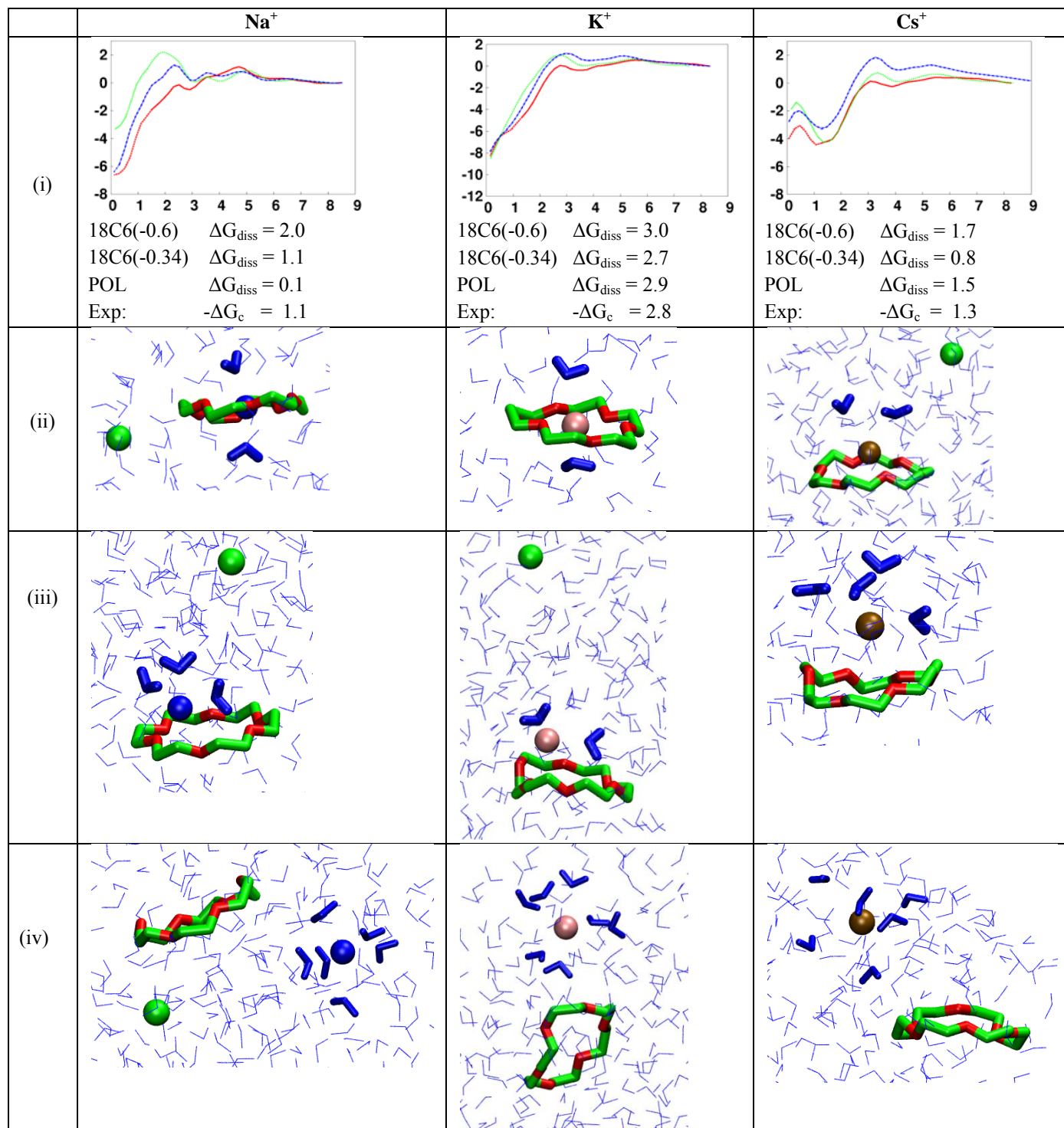


Figure S7: Dynamics of 18C6(-0.6)/M⁺ Cl⁻ complexes in SPC/E water. From top to bottom: (i) Snapshots after 2 ns. Time evolution of distances (in Å) (ii) M-O(18C6), (iii) M-Cl. (iv) Time evolution of: number of water molecules coordinated to M, (v) of OC-CO dihedrals. (vi) Energy components analysis (in kcal / mol, averages over the last 1.5 ns).

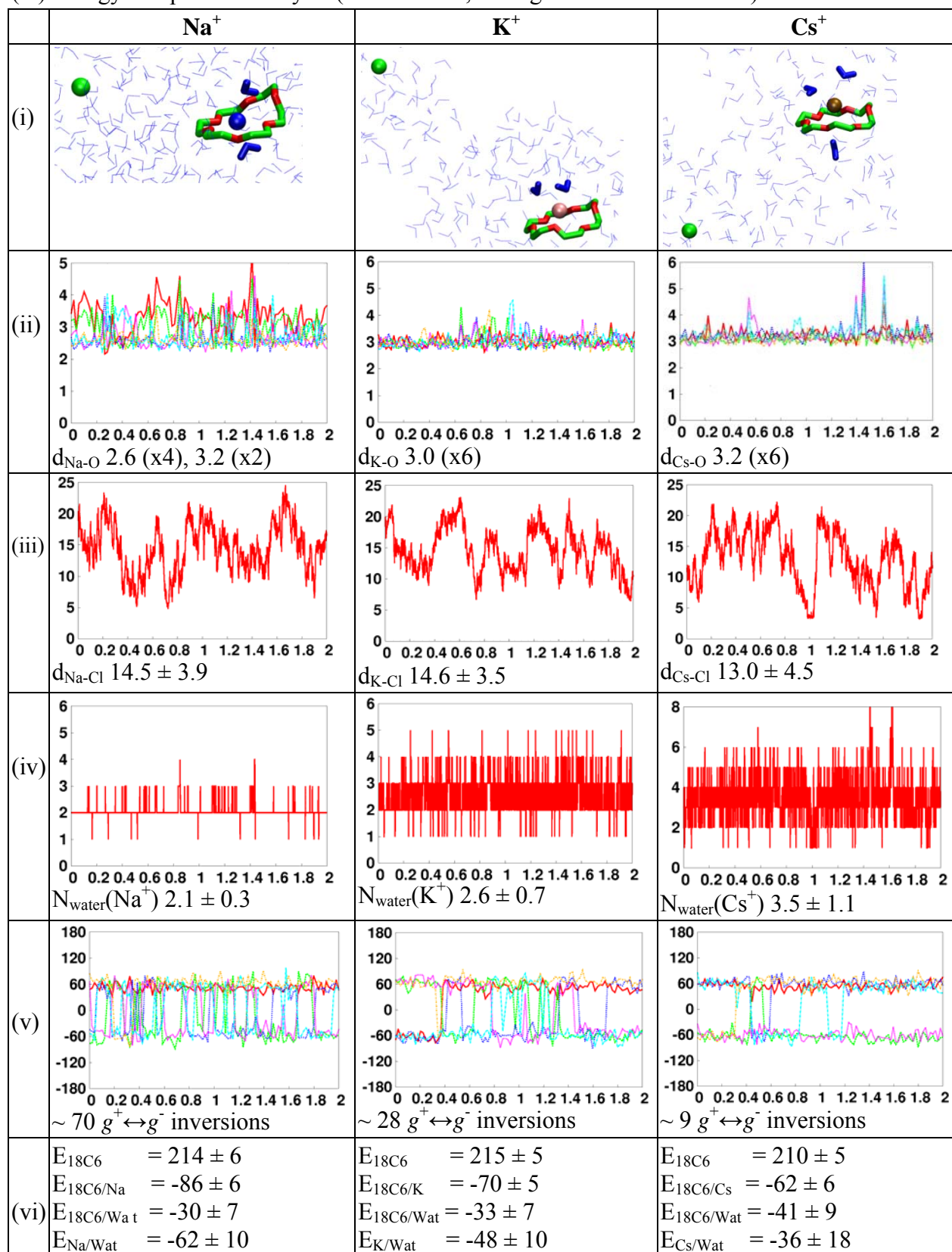


Figure S8: Dynamics of 18C6(-0.34)/M⁺ Cl⁻ complexes in SPC/E water. From top to bottom: (i) snapshots. Time evolution of distances (in Å) (ii) M-O(18C6), (iii) M-Cl. Time evolution of (iv) number of water molecules coordinated to M, (v) OC-CO dihedrals. (vi) Energy components analysis (in kcal / mol; averages over the last 1.5 ns).

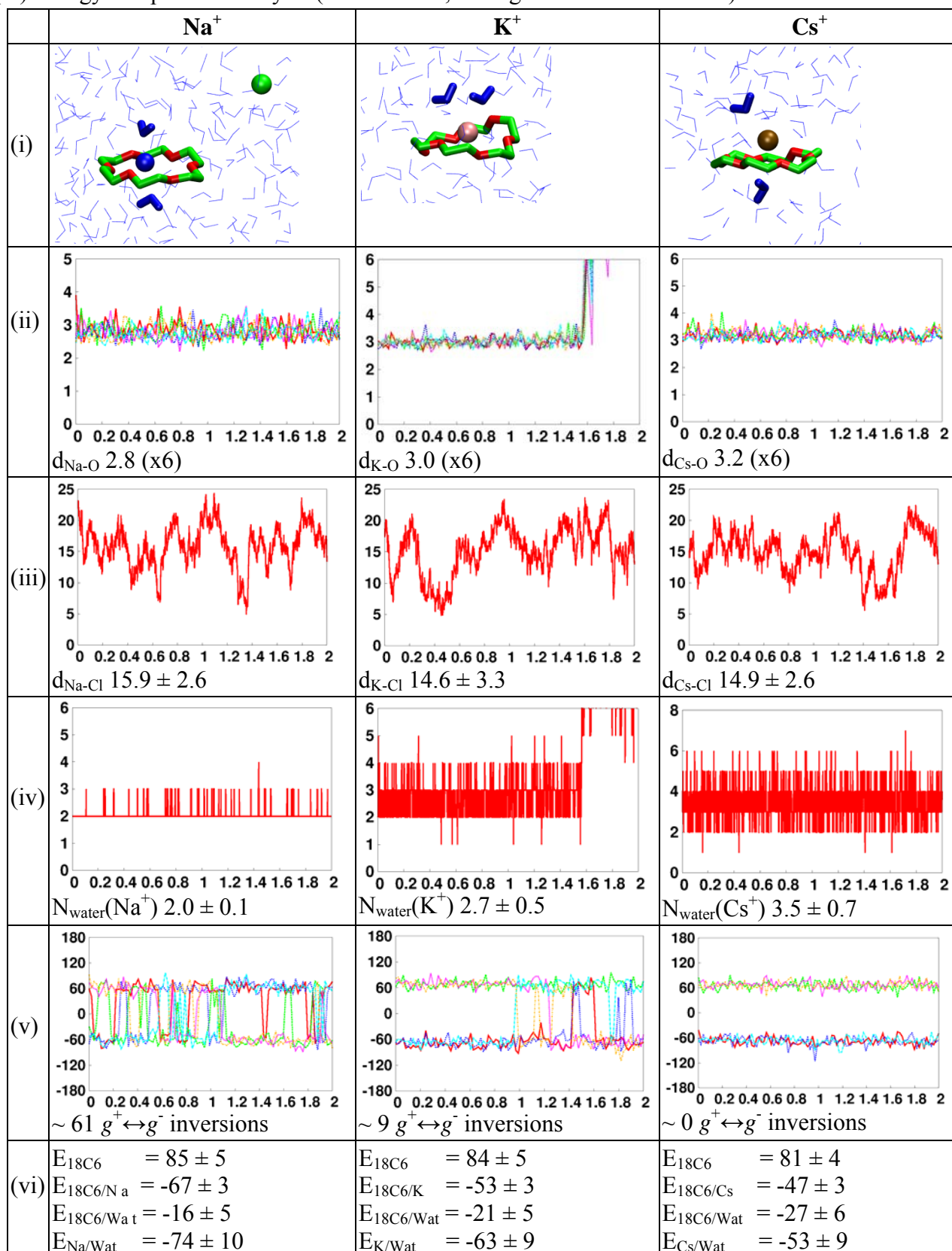


Figure S9: Dynamics of 18C6(-0.4)/M⁺ Cl⁻ complexes in POL3 water ("POL model"). From top to bottom: (i) snapshots of the complexes. Time evolution of distances (in Å) of (ii) M-O(18C6), (iii) M-Cl. Time evolution of (iv) number of water molecules coordinated to M, (v) of OC-CO dihedrals.

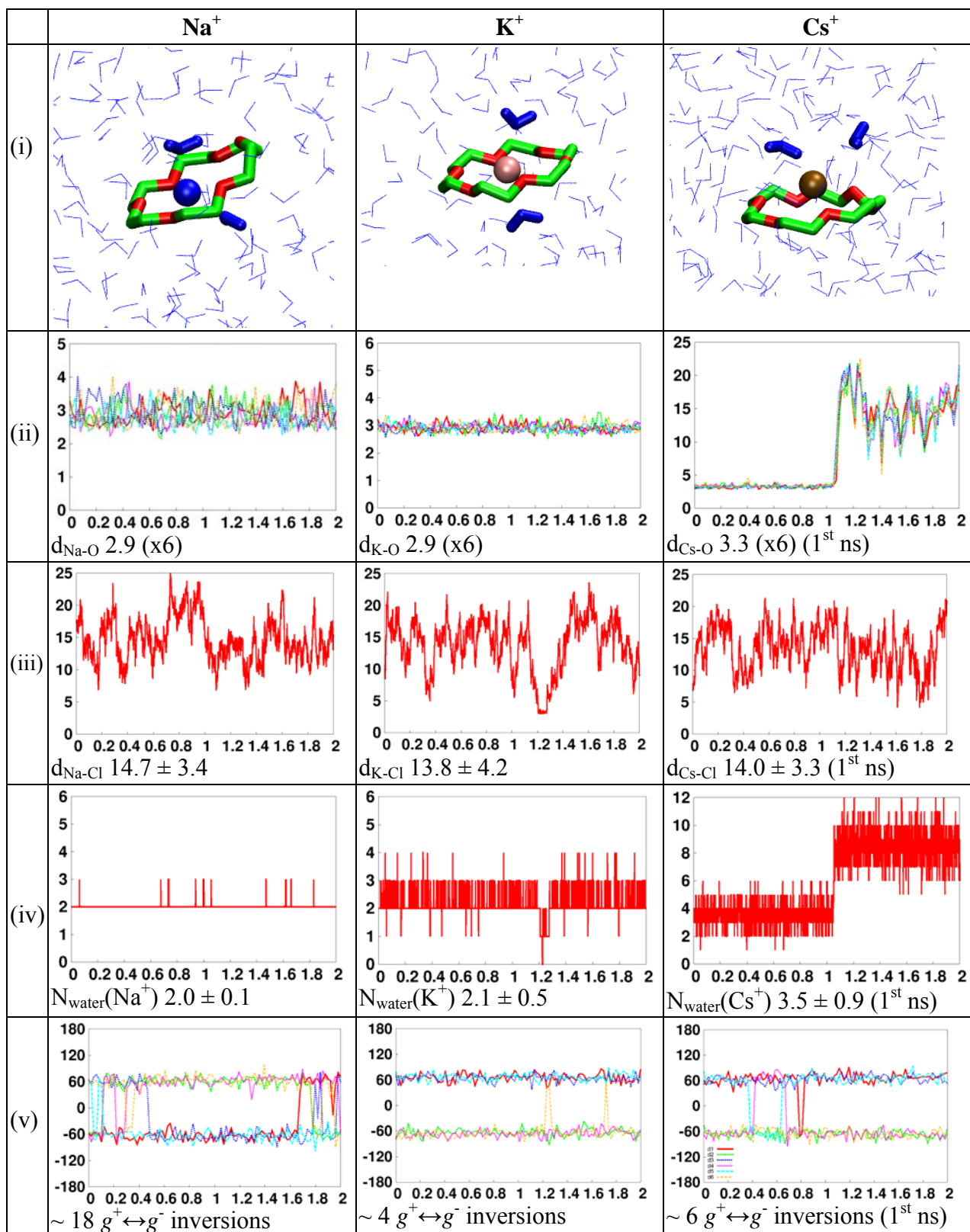


Figure S10: Dynamics of $18C6(-0.34)/M^+ Pic^-$ complexes at the chloroform / water (SPC/E) interface. From top to bottom: (i) snapshots. Time evolution of (ii) distances (in Å) M-O(18C6), (iii) of M-Pic; (iv) of the number of H_2O molecules coordinated to M^+ , (v) of OC-CO dihedral angles.

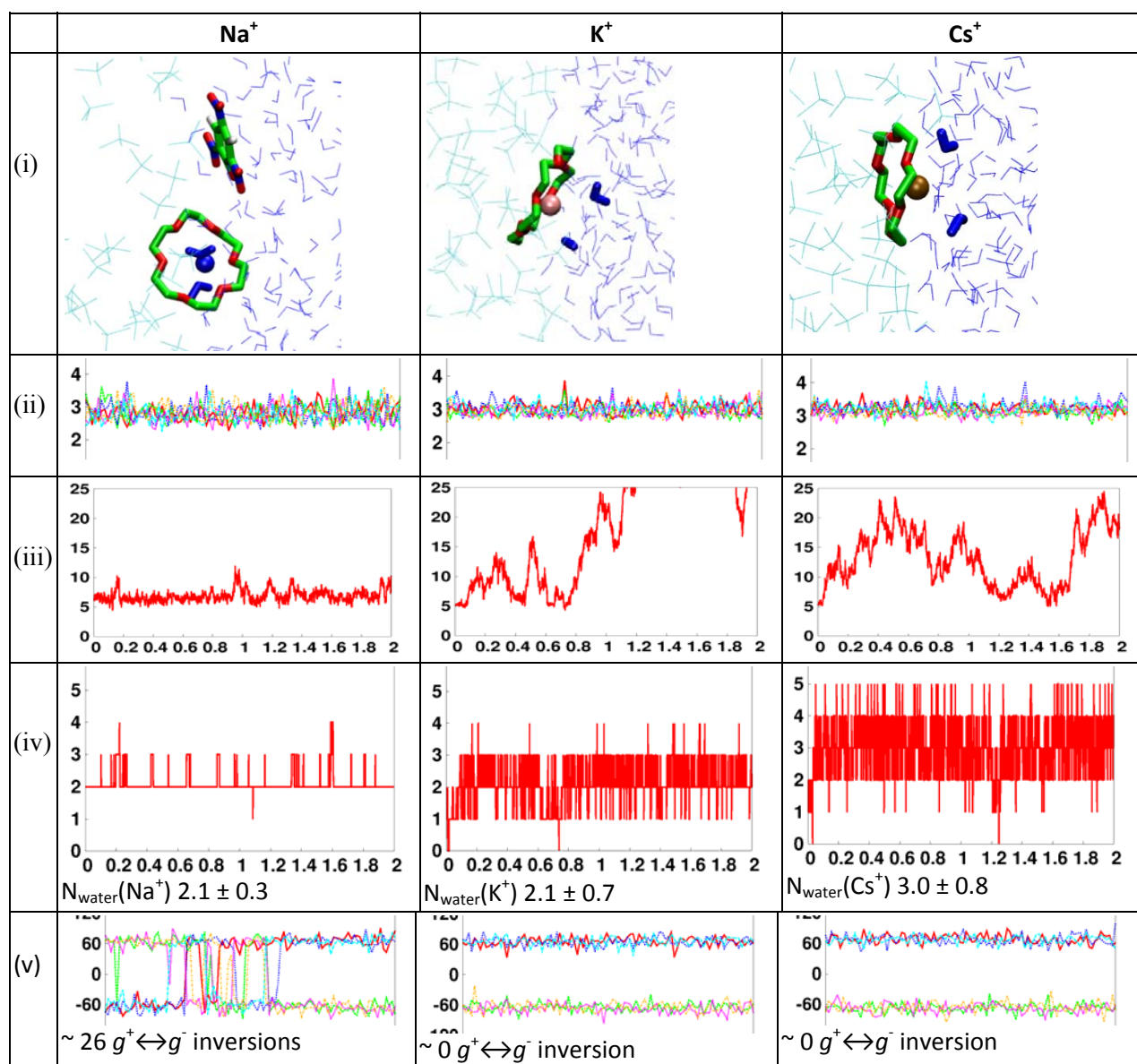


Figure S11 . "Transfer" PMF_{0.5+1.0} of K⁺ Pic⁻ across the interface. From top to bottom: free energy curve (ΔA in kcal / mol, as a function of the z distance in Å) and snapshots at the O, I and W positions.

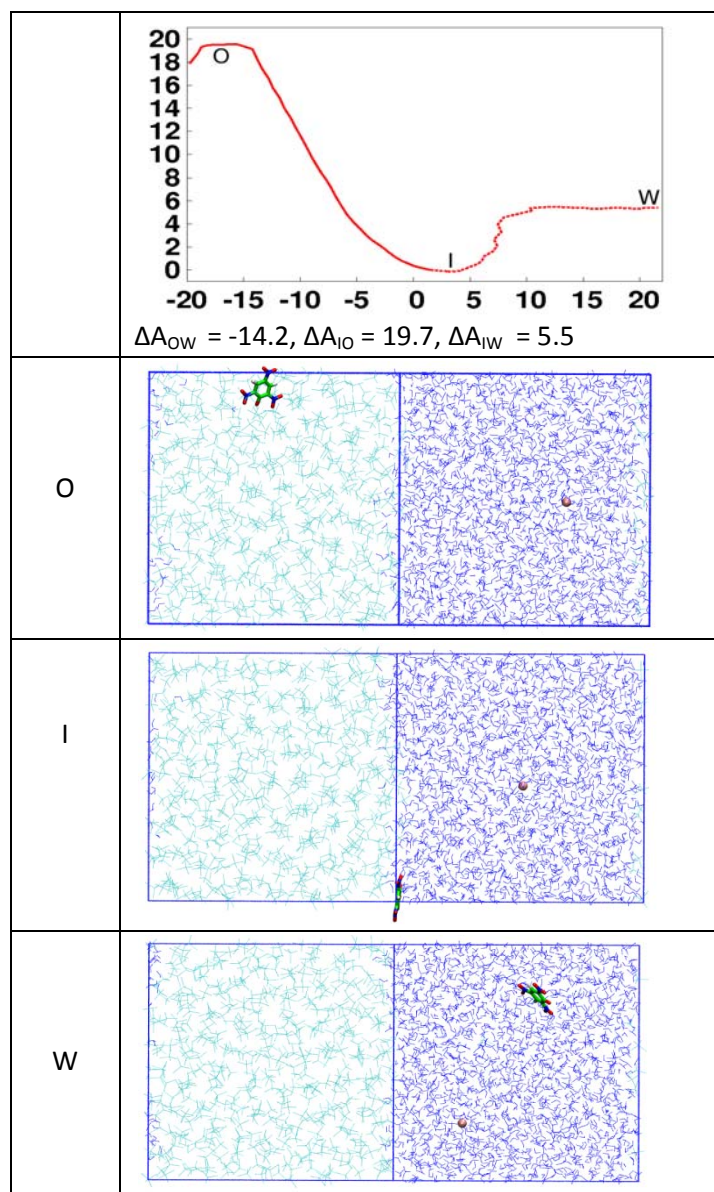
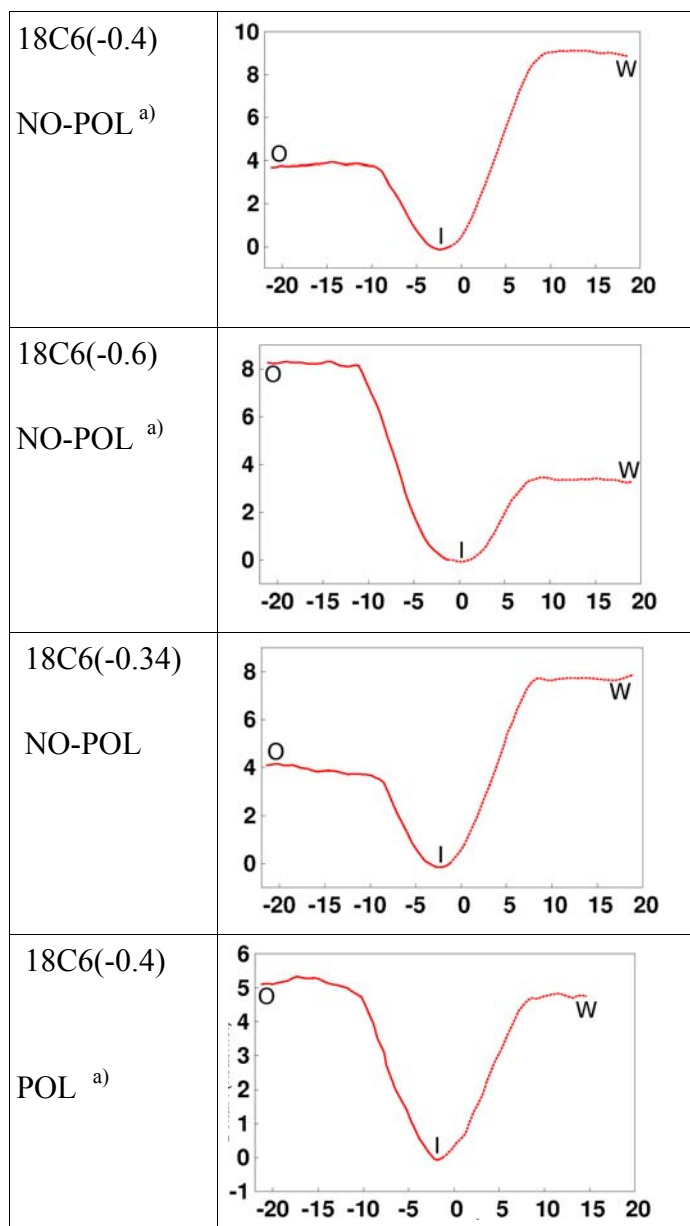


Figure S12: Transfer PMF_{0.5+1.0} of 18C6 across the chloroform / water interface. Free energy curves (ΔA in kcal / mol, as a function of the z distance in Å) with different charge models.



a) G. Benay and G. Wipff *J. Phys. Chem. B* **2014**, 118, 13913.

Figure S13. Transfer PMF_{0.5+1.0} of the 18C6(0.6)/M⁺ Pic⁻ complex across the chloroform / water interface. Free energy curves (ΔA in kcal / mol, as a function of the z distance in Å) and snapshots at the O, I and W positions.

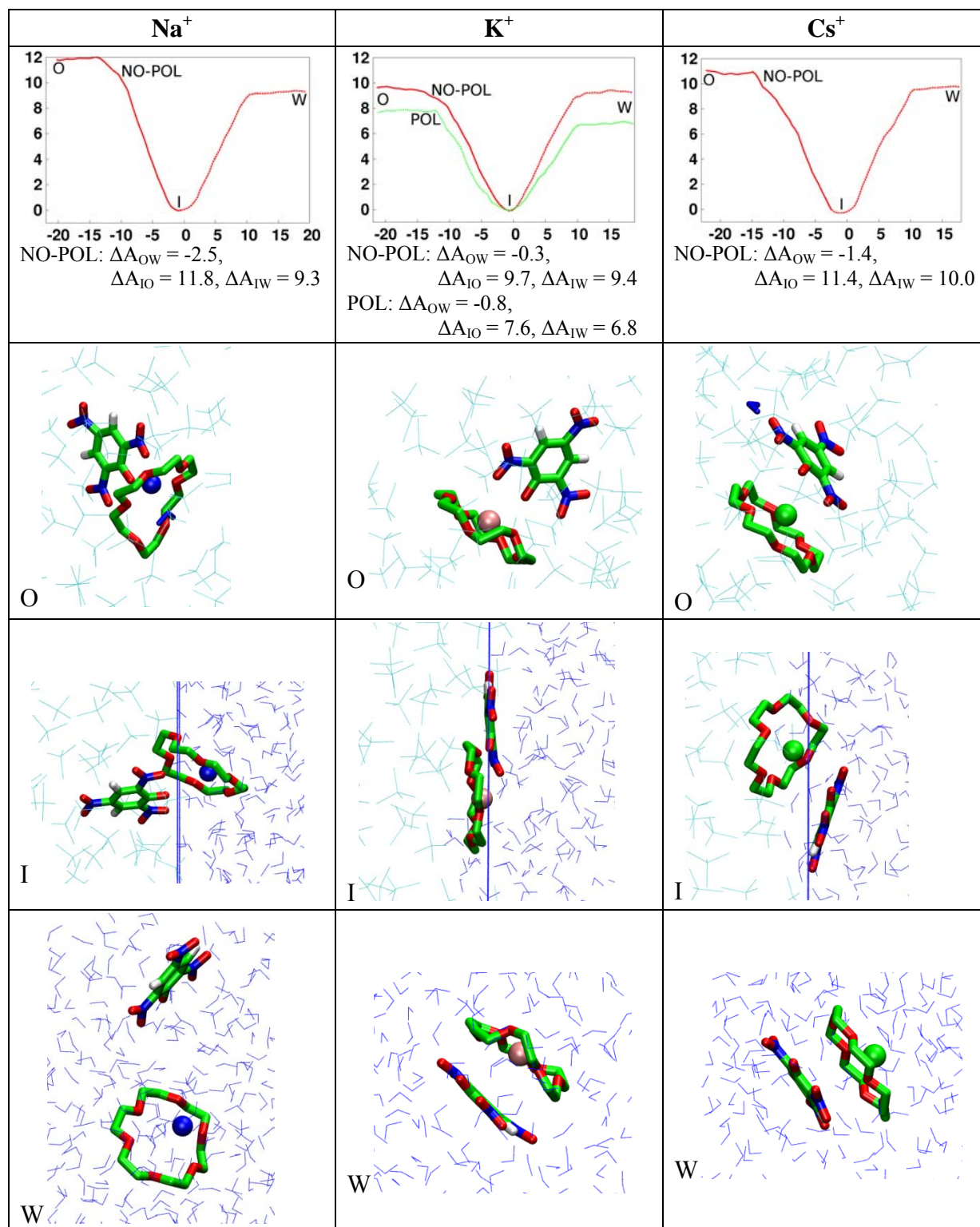
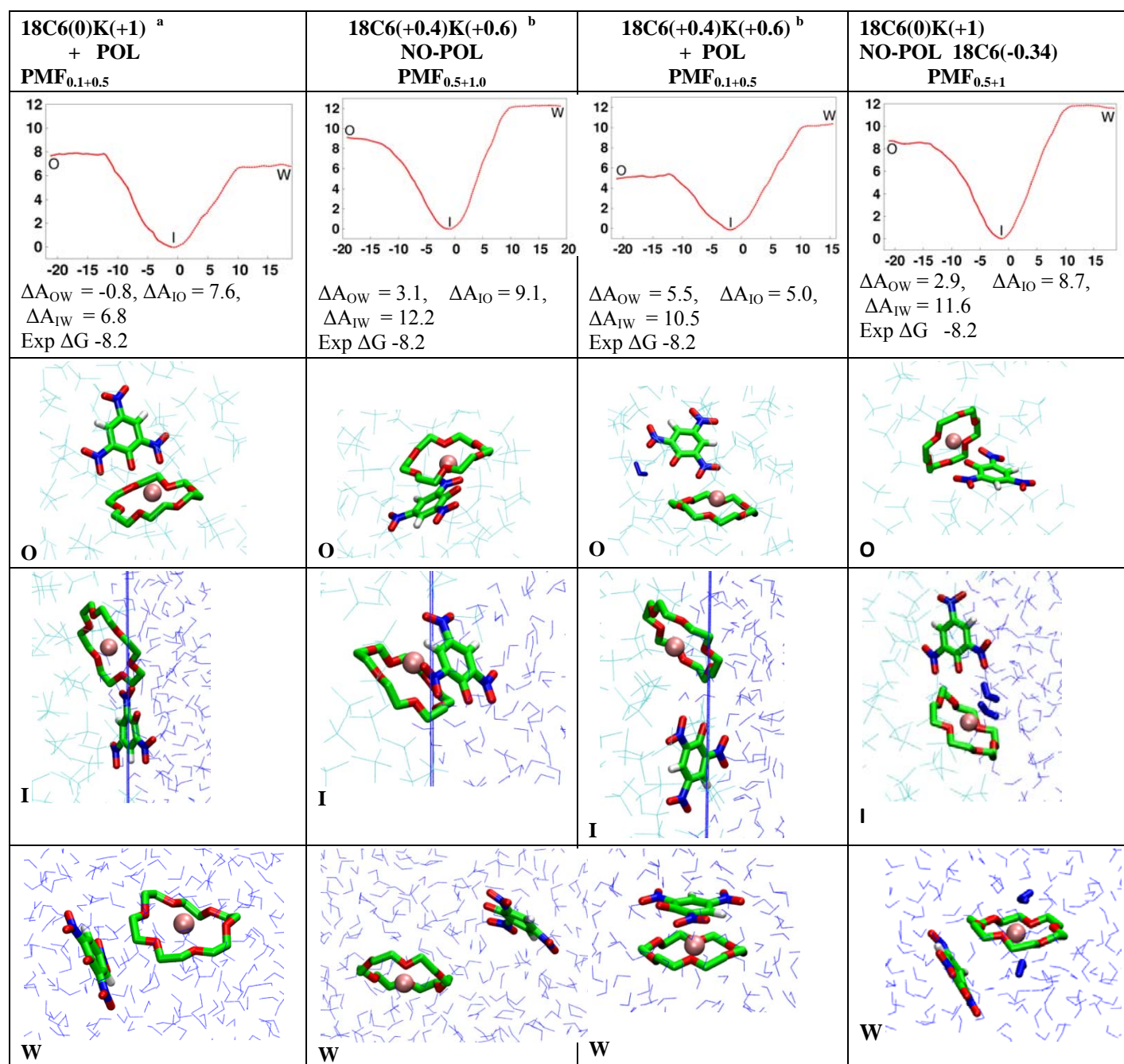


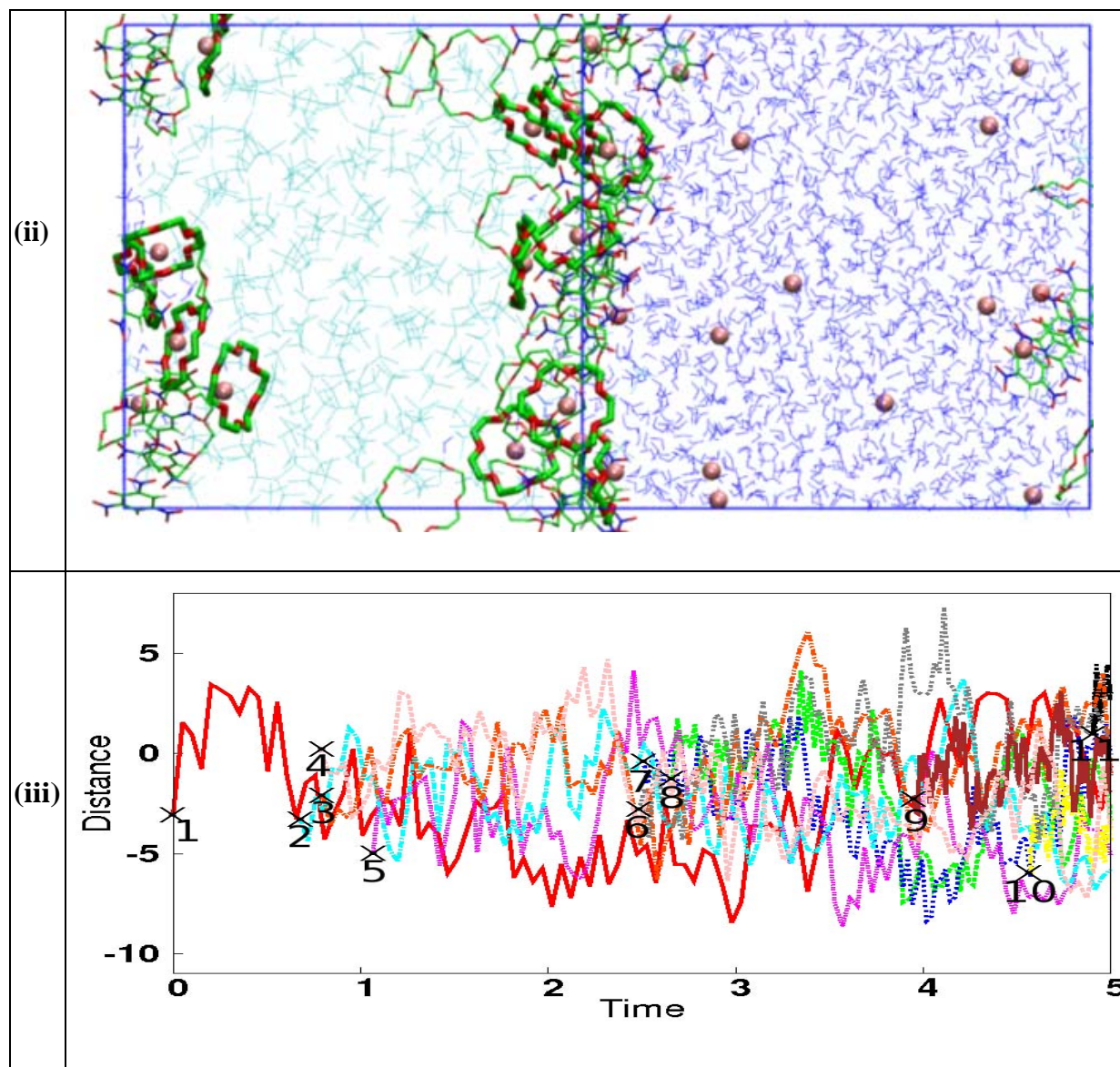
Figure S14: Transfer PMF of 18C6/ K^+ Pic $^-$ across the chloroform / water interface. Free energy curves (ΔA in kcal / mol, as a function of the z distance in Å) and snapshots at the O, I and W positions. Comparison of four models.



^a 18C6(-0.6) charge set, and +1 charged K^+

^b ESP charges on the whole 18C6/ K^+ complex.

Figure S15: 30 K^+ 18C6 Pic^- species at the interface (18C6(-0.4) POL model). Zooms from Figure 8. (ii) Snapshot of the solvent box after 5 ns of dynamics; (iii) K^+ –Interface distance (in Å) for the eleven complexes (color coded and labelled from 1 to 11) as a function of time (in ns), starting from the time of their formation along the dynamics (excluding the complex preformed at 0 ns)



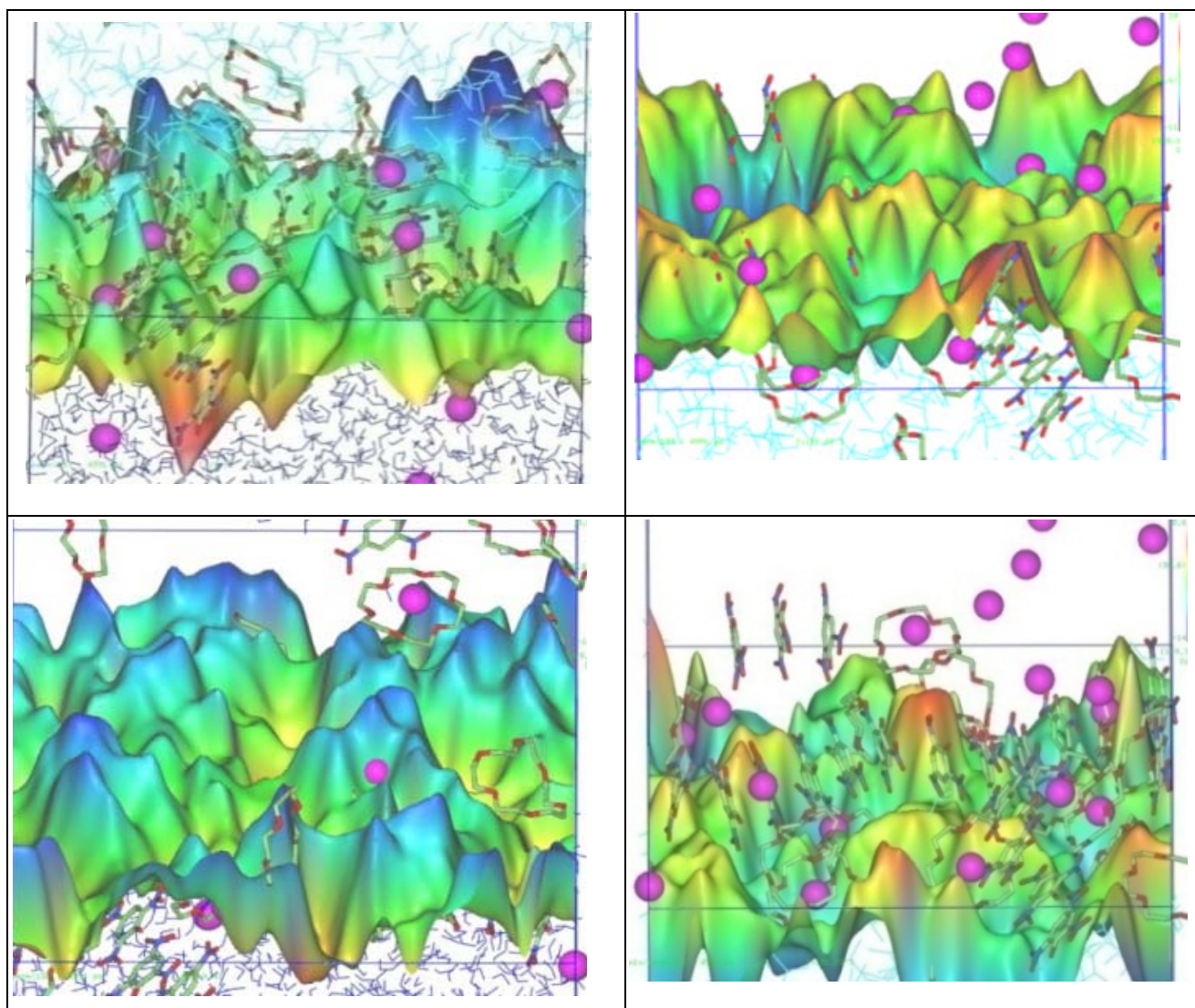


Figure S16: Views of the interfacial surface with 30 K^+ 18C6 Pic^- species (POL force field). The interface is shown "horizontally" with the water phase either below (left side) or on top (right side). Line 1: water surface; line 2: chloroform surface. The surface of a given liquid L is defined by the z_{max} positions of the L molecules that are not "isolated", but connected to the bulk L via other L molecules.