

# Tuning Phase Structures of a Symmetrical Diblock Copolymer with a Patterned Electric Field

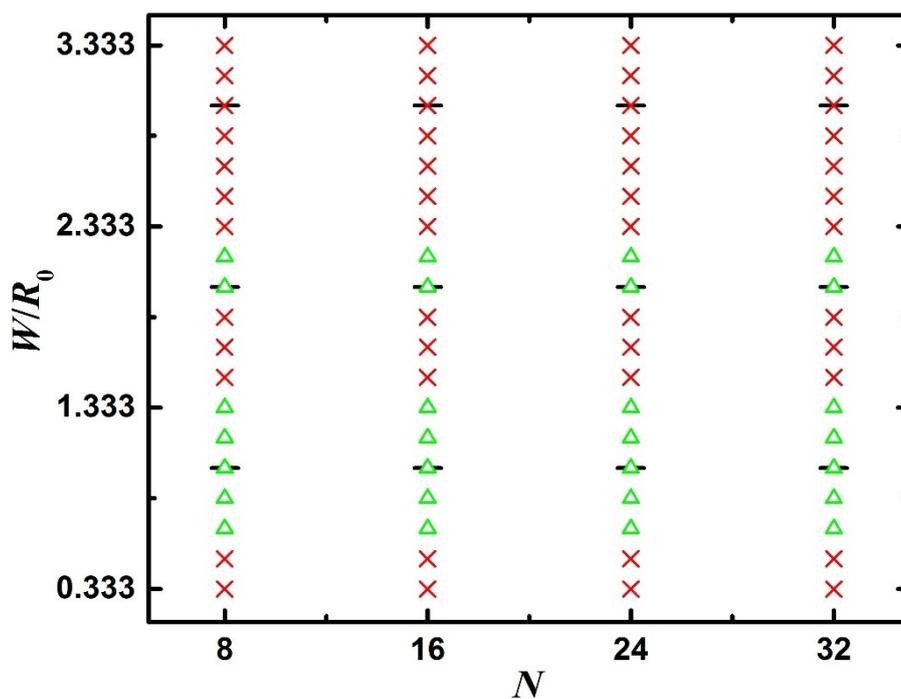
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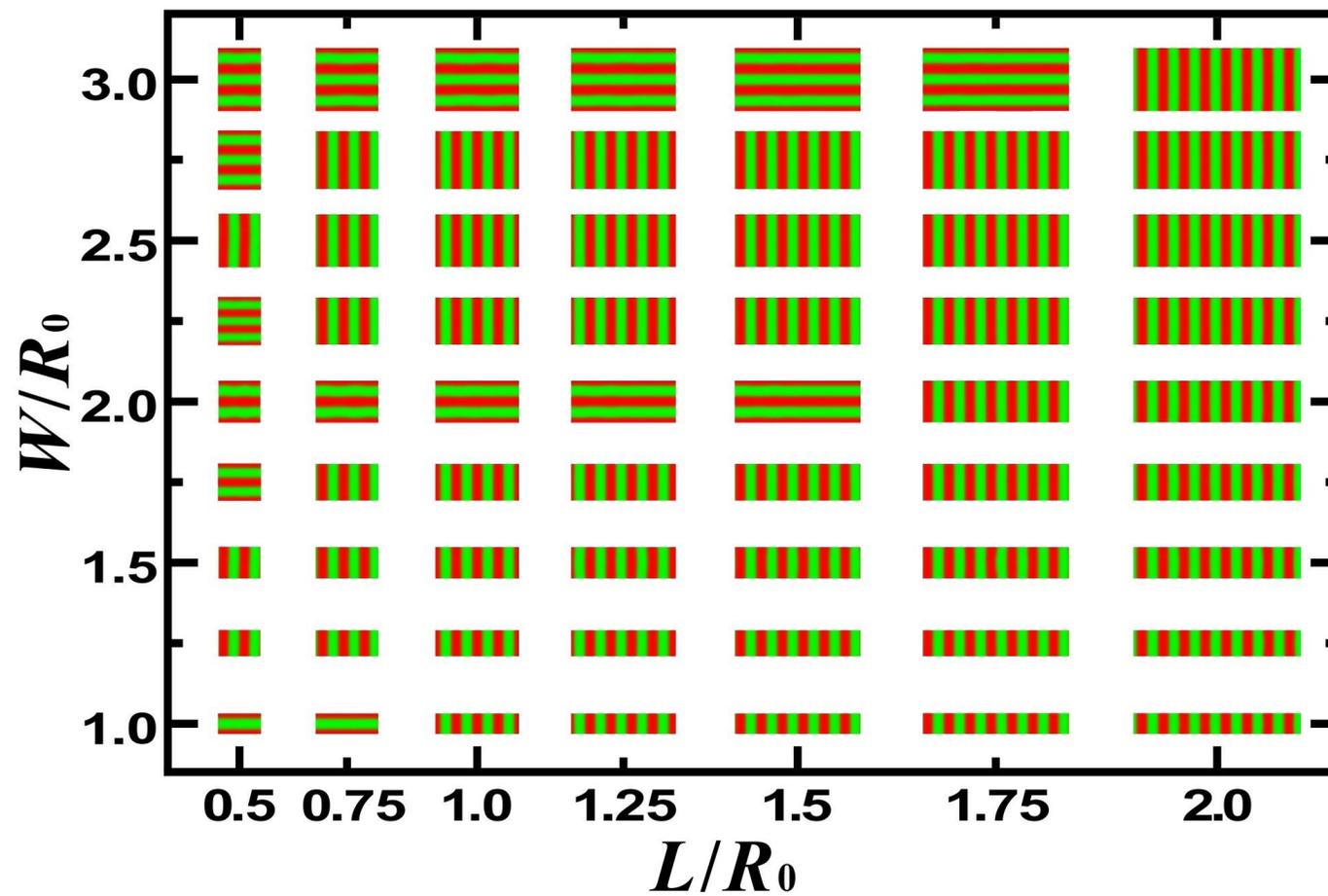
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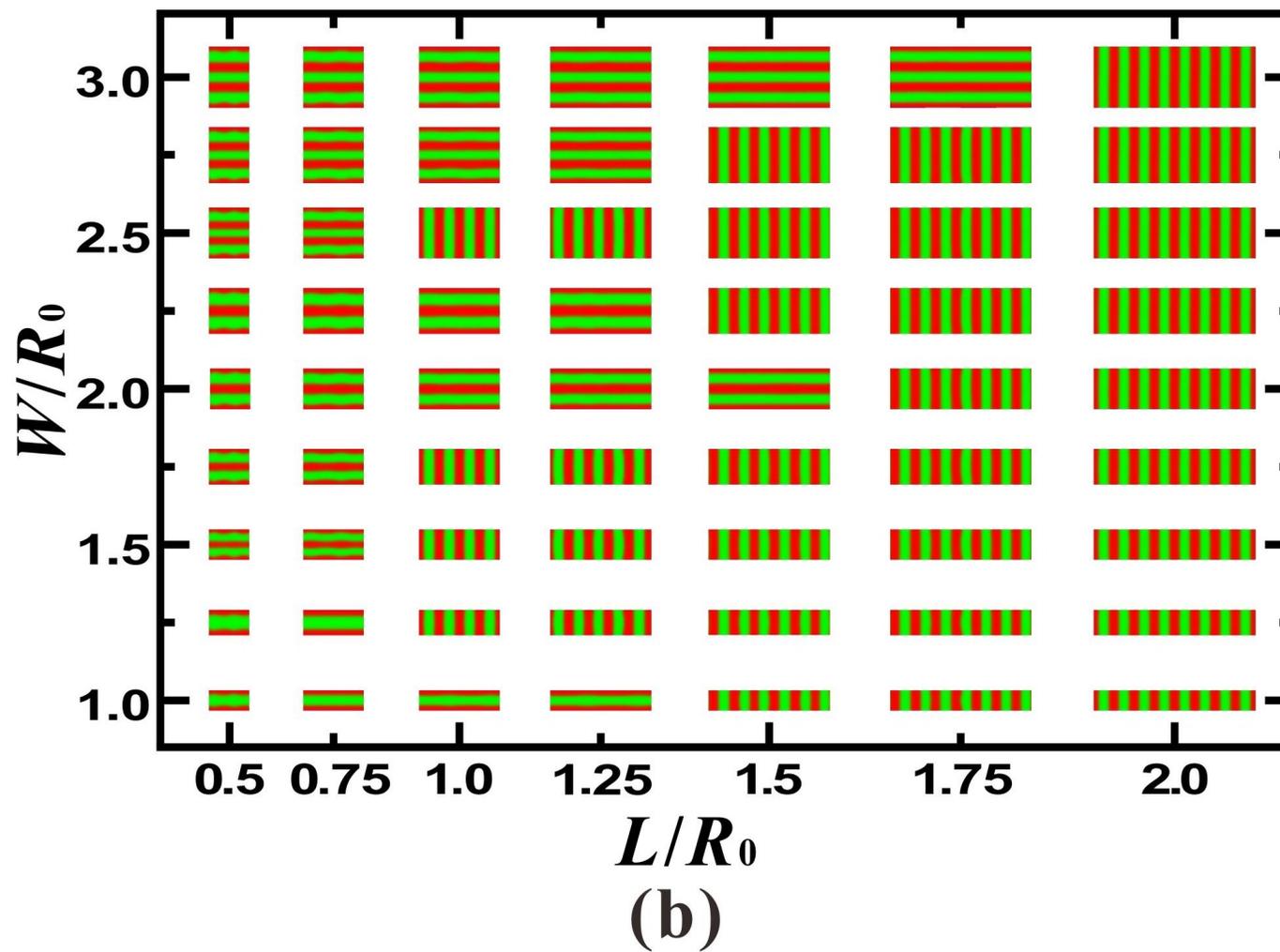
## Supporting information



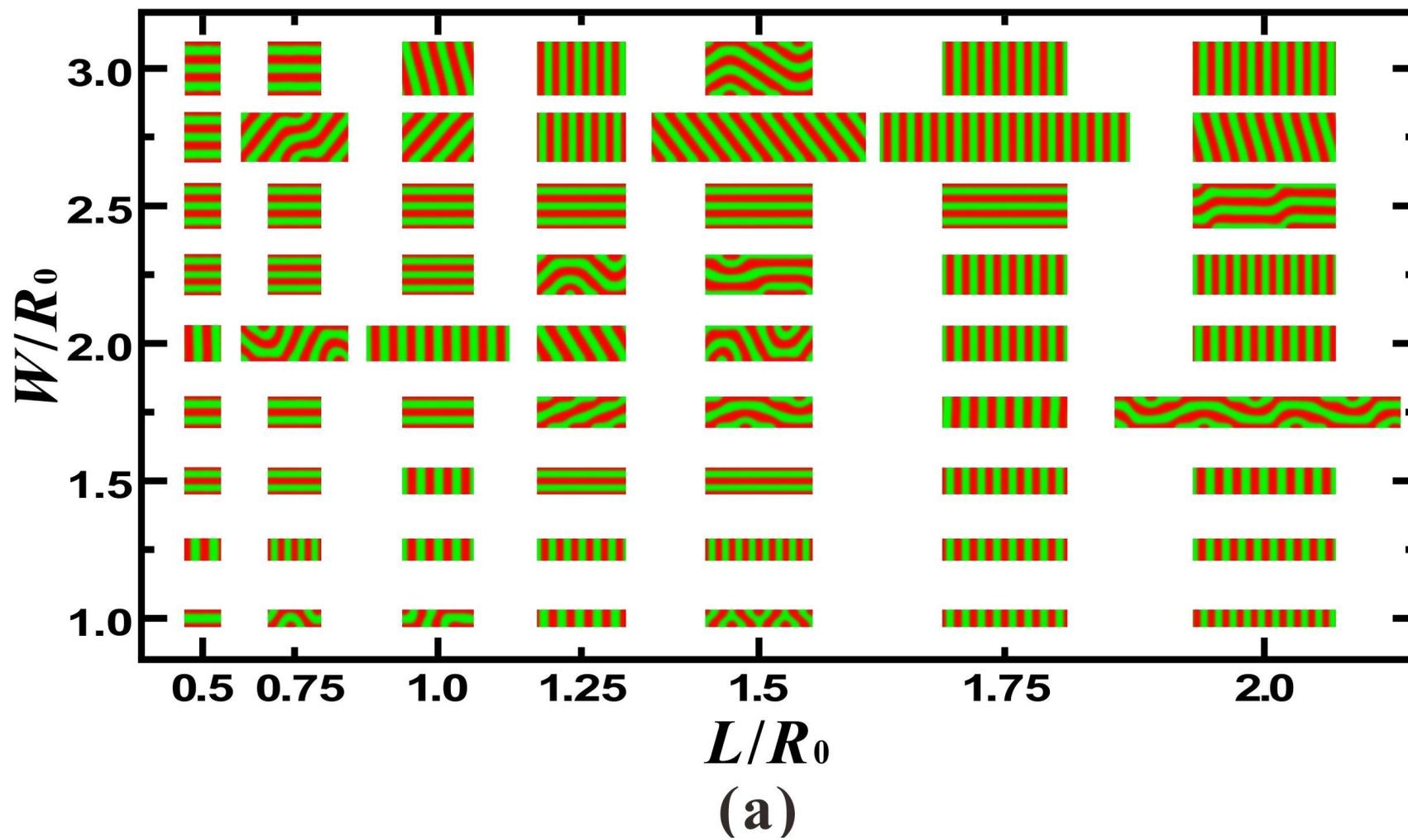
S1 Morphology diagram of a diblock copolymer thin film with  $f = 0.5$ ,  $\chi_{AB}N = 29.1$  and Kuhn length  $b_B = 1.4b_A$ . The diagram shows the equilibrium configuration in the confined space without electric field as a function of a diblock copolymer length  $N$  and film thickness  $W$ . Integer multiples of equilibrium phase period  $R_0$  are indicated with horizontal black bars ( $R_0 \approx 5.25R_g$  for  $N = 8, 16, 24, 32$ ). Red crosses and green triangles indicate perpendicular phase structures and parallel configurations, respectively.

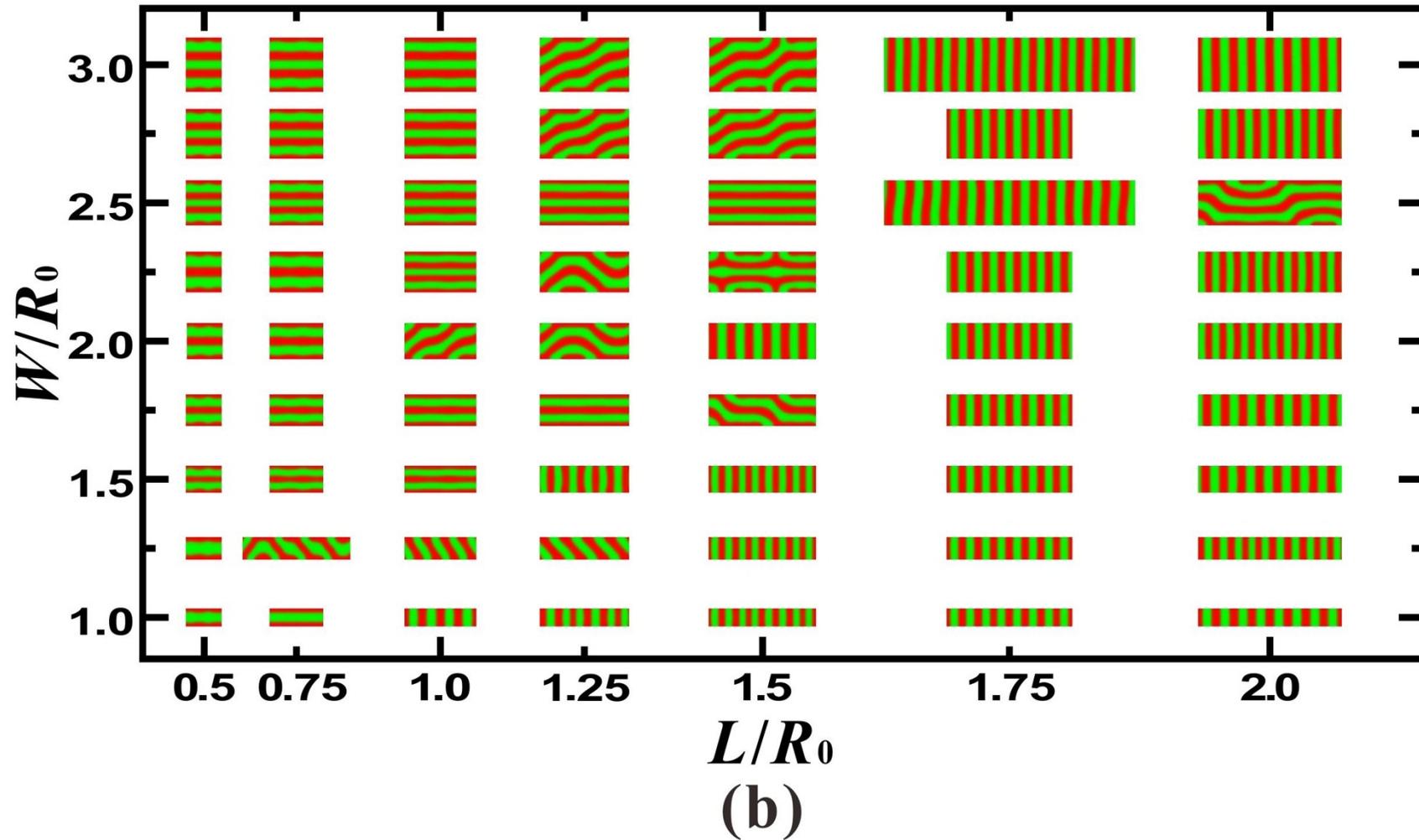


(a)



S2 Phase diagram of AB diblock copolymer melts depending on the film thickness ( $W$ ) and the size of electrode ( $L$ ) under alternatively distributed electric field. (a)  $U_{\text{high}} = 20.0$  V, (b)  $U_{\text{high}} = 40.0$  V. Here,  $U_{\text{low}} = 10.0$  V,  $\kappa_A = 6.0$  and  $\kappa_B = 2.5$ .





S3 The phase structures are achieved using annealing algorithm when varying the film thickness ( $W$ ) and the size of electrode ( $L$ ) under the alternatively distributed electric field. (a)  $U_{\text{high}} = 20.0$  V, (b)  $U_{\text{high}} = 40.0$  V. Here,  $U_{\text{low}} = 10.0$  V,  $\kappa_{\text{A}} = 6.0$  and  $\kappa_{\text{B}} = 2.5$ . Some of these phase structures in the  $X$ -direction with two periods are also examined.

TABLE I . The free energy of phase structures under alternatively distributed electric field ( $U_{\text{high}} = 20.0$  V).

$L/R_0$	$W/R_0$	A	P	V	S	$L/R_0$	$W/R_0$	A	P	V	S
0.50	1.00	0.408915	<b>0.408886</b>	0.413614	P	1.50	1.00	0.431580	0.423068	<b>0.422690</b>	V
	1.25	0.382348	0.383140	<b>0.382193</b>	V		1.25	0.400457	0.396400	<b>0.390142</b>	V
	1.50	0.368323	0.368298	<b>0.360656</b>	V		1.50	0.378436	0.378418	<b>0.367874</b>	V
	1.75	0.344561	<b>0.344548</b>	0.345021	P		1.75	0.355226	0.354172	<b>0.351540</b>	V
	2.00	0.333181	<b>0.330088</b>	0.333181	P		2.00	0.342868	<b>0.339121</b>	0.339158	P
	2.25	0.332216	<b>0.322299</b>	0.323885	P		2.25	0.332945	0.330836	<b>0.329425</b>	V
	2.50	0.318820	0.318823	<b>0.316442</b>	V		2.50	0.326041	0.326219	<b>0.321571</b>	V
	2.75	<b>0.309376</b>	0.309416	0.310330	A		2.75	0.316267	0.316258	<b>0.315101</b>	V
3.00	0.303140	<b>0.303135</b>	0.305222	P	3.00	0.312313	<b>0.309589</b>	0.309684	P		
0.75	1.00	0.425382	<b>0.416951</b>	0.419237	P	1.75	1.00	0.425420	0.423681	<b>0.423094</b>	V
	1.25	0.396586	0.390507	<b>0.386727</b>	V		1.25	0.392927	0.397017	<b>0.390524</b>	V
	1.50	0.374029	0.374002	<b>0.364531</b>	V		1.50	0.370613	0.378865	<b>0.368201</b>	V
	1.75	0.349878	0.349900	<b>0.348407</b>	V		1.75	0.355205	0.354617	<b>0.351866</b>	V
	2.00	0.339402	<b>0.335048</b>	0.336184	P		2.00	0.342113	0.339555	<b>0.339480</b>	V
	2.25	0.336330	0.326859	<b>0.326609</b>	V		2.25	0.332353	0.331266	<b>0.329725</b>	V
	2.50	0.322666	0.322673	<b>0.318916</b>	V		2.50	0.323540	0.326594	<b>0.321862</b>	V
	2.75	0.314226	0.313019	<b>0.312598</b>	V		2.75	0.317585	0.316624	<b>0.315397</b>	V
3.00	0.317191	<b>0.306518</b>	0.307322	P	3.00	0.312561	<b>0.309952</b>	0.309963	P		
1.00	1.00	0.423529	0.420365	<b>0.420233</b>	V	2.00	1.00	0.429859	0.424086	<b>0.423557</b>	V
	1.25	0.389320	0.393734	<b>0.388013</b>	V		1.25	0.392801	0.397415	<b>0.390896</b>	V
	1.50	0.366821	0.376455	<b>0.365891</b>	V		1.50	0.368526	0.379162	<b>0.368511</b>	V
	1.75	0.352233	0.352226	<b>0.349756</b>	V		1.75	0.355793	0.354911	<b>0.352178</b>	V
	2.00	0.338178	<b>0.337262</b>	0.337491	P		2.00	0.341741	0.339868	<b>0.339758</b>	V
	2.25	0.338228	0.329000	<b>0.327870</b>	V		2.25	0.333436	0.331536	<b>0.329990</b>	V
	2.50	0.324471	0.324483	<b>0.320096</b>	V		2.50	0.323571	0.326684	<b>0.322115</b>	V
	2.75	0.314822	0.314704	<b>0.313713</b>	V		2.75	0.316655	0.316877	<b>0.315633</b>	V
3.00	0.308980	<b>0.308153</b>	0.308379	P	3.00	0.312205	0.310204	<b>0.310178</b>	V		
1.25	1.00	0.422192	0.422162	<b>0.422102</b>	V	2.00	1.00	0.429859	0.424086	<b>0.423557</b>	V
	1.25	0.394154	0.395428	<b>0.389608</b>	V		1.25	0.392801	0.397415	<b>0.390896</b>	V
	1.50	0.377721	0.377701	<b>0.367288</b>	V		1.50	0.368526	0.379162	<b>0.368511</b>	V
	1.75	0.354867	0.353462	<b>0.351000</b>	V		1.75	0.355793	0.354911	<b>0.352178</b>	V
	2.00	0.341313	<b>0.338434</b>	0.338626	P		2.00	0.341741	0.339868	<b>0.339758</b>	V
	2.25	0.331753	0.330143	<b>0.328906</b>	V		2.25	0.333436	0.331536	<b>0.329990</b>	V
	2.50	0.325452	0.325637	<b>0.321075</b>	V		2.50	0.323571	0.326684	<b>0.322115</b>	V
	2.75	0.319134	0.315691	<b>0.314630</b>	V		2.75	0.316655	0.316877	<b>0.315633</b>	V
3.00	0.313769	<b>0.309048</b>	0.309223	P	3.00	0.312205	0.310204	<b>0.310178</b>	V		

A represents the annealing result, P represents the parallel lamellar phase structure, V represents the vertical layered phase structure, and S represents the phase structure with the lowest free energy (red).

TABLE II. The free energy of phase structures under alternatively distributed electric field ( $U_{\text{high}} = 40.0$  V).

$L/R_0$	$W/R_0$	A	P	V	S	$L/R_0$	$W/R_0$	A	P	V	S
0.50	1.00	0.172391	<b>0.172386</b>	0.198704	P	1.50	1.00	0.292201	0.284346	<b>0.282561</b>	V
	1.25	<b>0.196451</b>	0.196452	0.222225	A		1.25	0.304789	0.300659	<b>0.295150</b>	V
	1.50	<b>0.228062</b>	0.228197	0.233666	A		1.50	0.307678	0.309819	<b>0.298014</b>	V
	1.75	<b>0.224076</b>	0.224090	0.239387	A		1.75	0.301554	0.300233	<b>0.297227</b>	V
	2.00	0.223644	<b>0.223629</b>	0.242376	P		2.00	0.295084	<b>0.294762</b>	0.295067	P
	2.25	<b>0.226654</b>	0.226663	0.244105	A		2.25	0.296892	0.293064	<b>0.292457</b>	V
	2.50	<b>0.236765</b>	0.236779	0.245203	A		2.50	0.293929	0.293943	<b>0.289790</b>	V
	2.75	<b>0.234094</b>	0.234122	0.245943	A		2.75	0.289311	0.287803	<b>0.287222</b>	V
	3.00	<b>0.233436</b>	0.233574	0.246474	A	3.00	0.287784	<b>0.283961</b>	0.284841	P	
0.75	1.00	0.232599	<b>0.232590</b>	0.249900	P	1.75	1.00	0.287587	0.289903	<b>0.286628</b>	V
	1.25	0.259606	<b>0.250691</b>	0.264514	P		1.25	0.300115	0.306148	<b>0.298639</b>	V
	1.50	0.271623	<b>0.271618</b>	0.269194	P		1.50	0.302941	0.313889	<b>0.301196</b>	V
	1.75	0.263780	<b>0.263735</b>	0.270061	P		1.75	0.302129	0.304072	<b>0.300211</b>	V
	2.00	0.259898	<b>0.259893</b>	0.269440	P		2.00	0.301143	0.298655	<b>0.297902</b>	V
	2.25	0.259753	<b>0.259751</b>	0.268284	P		2.25	0.298316	0.296977	<b>0.295169</b>	V
	2.50	0.265263	<b>0.265261</b>	0.267014	P		2.50	0.293789	0.297300	<b>0.292386</b>	V
	2.75	<b>0.260471</b>	0.260511	0.265781	A		2.75	0.291957	0.291036	<b>0.289737</b>	V
	3.00	<b>0.257953</b>	0.257987	0.264632	A	3.00	0.290756	<b>0.287179</b>	0.287252	P	
1.00	1.00	0.261072	<b>0.260689</b>	0.261067	P	2.00	1.00	0.287214	0.293595	<b>0.287197</b>	V
	1.25	0.285426	0.277487	<b>0.276503</b>	V		1.25	0.307410	0.309887	<b>0.299667</b>	V
	1.50	0.292331	0.292301	<b>0.281211</b>	V		1.50	0.304366	0.316599	<b>0.302459</b>	V
	1.75	0.283399	0.283399	<b>0.281756</b>	V		1.75	0.303151	0.306924	<b>0.301609</b>	V
	2.00	0.283363	<b>0.278584</b>	0.280651	P		2.00	0.306382	0.301310	<b>0.299380</b>	V
	2.25	0.288617	<b>0.277346</b>	0.278935	P		2.25	0.303585	0.299462	<b>0.296687</b>	V
	2.50	0.280270	0.280291	<b>0.277055</b>	V		2.50	0.297208	0.299600	<b>0.293925</b>	V
	2.75	<b>0.274642</b>	<b>0.274642</b>	0.275210	A/P		2.75	0.293626	0.293332	<b>0.291266</b>	V
	3.00	<b>0.271358</b>	<b>0.271358</b>	0.273479	A/P	3.00	<b>0.288786</b>	0.289383	<b>0.288786</b>	A/V	
1.25	1.00	0.281406	<b>0.275646</b>	0.277064	P						
	1.25	0.293392	0.292000	<b>0.290074</b>	V						
	1.50	0.297003	0.303370	<b>0.293036</b>	V						
	1.75	0.293987	0.293987	<b>0.292386</b>	V						
	2.00	0.291289	<b>0.288779</b>	0.290377	P						
	2.25	0.288001	<b>0.287227</b>	0.287909	P						
	2.50	0.288754	0.288754	<b>0.285414</b>	V						
	2.75	0.284296	<b>0.282790</b>	0.283022	P						
	3.00	0.281580	<b>0.279162</b>	0.280809	P						

A represents the annealing result, P represents the parallel lamellar phase structure, V represents the vertical layered phase structure, and S represents the phase structure with the lowest free energy (red).