Supplementary Information

Structural phase transitions of $(Bi_{1-x}Sb_x)_2(Te_{1-y}Se_y)_3$ compounds under high pressure and the influence of the atomic radius on the compression processes of tetradymites[†]

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†Electronic Supplementary Information (ESI): Schematic views of the crystal structures of A_2B_3 type tellurides and selenides (Fig. S1), experimental lattice parameters and atomic coordinates of phase IV of Bi₂Te₂Se (Table S1), calculated lattice parameters and atomic coordinates of Bi₂Te₂Se (Table S2), XRD patterns of BiSbTeSe₂ and Sb₂Te₂Se under high pressure (Fig. S2), fitted results of equation of state for A_2B_3 -type tellurides and selenides (Table S3), schematic views of the crystal structures of (a) tetradymite and rock salt and (b) CsCl-like structure units in the BCT and CN9M models (Fig. S3), and progression of one quintuple layer in the tetradymite series (Fig. S4).

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Fig. S1 Schematic views of the crystal structures of A_2B_3 -type compounds (A = Bi, Sb; B = Te, Se) at ambient and high pressures. The black bold lines denote the unit cells. For Bi₂Te₃, Sb₂Te₃, and Bi₂Se₃, phase α adopts a hexagonal unit cell and phase β adopts the unit cell from Ref. 5.

Table S1. Lattice parameters and atomic coordinates of phase IV of Bi_2Te_2Se at 30.9 GPa, which are simulated by using the body-centered tetragonal (BCT), 9/10-fold monoclinic (CN9M), and disordered body-centered cubic (BCC) structures

Atom	Site	x	у	ζ				
Phase IV (BCT) Space group: <i>I</i> 4/ <i>mmm</i> ; $a = 3.5319(2)$ Å, $c = 17.4573(17)$ Å; $R_p = 1.41\%$, $R_{wp} = 1.69\%$.								
Bi	4e	0	0	0.4003(2)				
Те	4e	0	0	0.2030(2)				
Se	2a	0	0	0				
Phase IV (CN9M) Space group: $C2/m$; $a = 15.036(2)$ Å, $b = 4.9914(3)$ Å, $c = 6.0788(4)$ Å, $\beta = 105.30(1)^{\circ}$; $R_{\rm p} = 2.02\%$, $R_{\rm wp} = 2.96\%$.								
Bi(1)	4i	0.3992(4)	0	0.6083(8)				
Bi(2)	4i	0.1979(6)	0	0.8004(9)				
Te(1)	4i	0.8001(6)	0	0.6983(10)				
Te(2)	2c	0	0	0.5				
Te(3)	2a	0	0	0				
Se	4i	0.3992(5)	0	0.0952(11)				
Phase IV (disordered BCC) Space group: <i>Im</i> -3 <i>m</i> ; $a = 3.5192(2)$ Å; $R_p = 3.21\%$, $R_{wp} = 4.80\%$.								
Bi/Te/Se	2a	0	0	0				

Atom	Site	x	у	z				
Phase I @ 5 GPa (CN6R) * Space group: $R-3m$; $a = 4.2318$ Å, $c = 29.092$ Å.								
Bi	6c	0	0	0.3956				
Те	6c	0	0.2097					
Se	3a	0	0	0				
Phase II @ 15 GPa (CN7M) ** Space group: $C2/m$; $a = 14.476$ Å, $b = 3.9375$ Å, $c = 8.9271$ Å, $\beta = 90.55^{\circ}$.								
Bi(1)	4i	0.9749	0	0.1828				
Bi(2)	4i	0.2201	0	0.2045				
Te(1)	4i	0.8249	0	0.3927				
Te(2)	4i	0.4283	0	0.6242				
Se	4i	0.3655	0	0.0033				
Phase III @ Space group	Phase III @ 15 GPa (CN8M) Space group: $C2/c$; $a = 9.7931$ Å, $b = 7.0632$ Å, $c = 10.241$ Å, $\beta = 135.53^{\circ}$.							
Bi	8f	0.2875	0.1080	0.3525				
Те	8f	0.5997	0.3654	0.4625				
Se	4e	0	0.3649	0.25				
Phase IV @ 30 GPa (BCT) Space group: $I4/mmm$; $a = 3.5345$ Å, $c = 17.1355$ Å.								
Те	4e	0	0	0.1984				
Se	2a	0	0	0				
Phase IV @ Space group	30 GPa (): <i>C</i> 2/ <i>m</i> ; a	CN9M) 2 = 14.845 Å,	<i>b</i> = 4.9757 Å, <i>c</i> = 6.03	$β$ 76 Å, $β = 105.85^{\circ}$.				
Bi(1)	4i	0.4084	0	0.6429				
Bi(2)	4i	0.1939	0	0.8125				
Te(1)	4i	0.7934	0	0.6880				
Te(2)	2c	0	0	0.5				
Te(3)	2a	0	0	0				
Se	4i	0.3957	0	0.1115				

Table S2. Calculated lattice parameters and atomic coordinates of Bi₂Te₂Se

*Phase I adopts a hexagonal unit cell.

**This structure of phase II in Table S2 is equivalent to that in Ref. 5 with same *a*- and *b*-axis and different *c*-axis and β angle.



Fig. S2 Selected angle-dispersive X-ray diffraction (AD-XRD) patterns of (a) BiSbTeSe₂ and (b) Sb₂Te₂Se at room temperature up to 38.5 and 37.5 GPa, respectively.

		Phase I		Phase II		Phase III			Phase IV				
		B ₀ (GPa)	B_0	<i>V</i> ₀ /f.u. (Å ³)	B ₀ (GPa)	B_0	V_0 /f.u. (Å ³)	B ₀ (GPa)	B_0	<i>V</i> ₀ /f.u. (Å ³)	B ₀ (GPa)	B_0	<i>V</i> ₀ / f.u. (Å ³)
Bi ₂ Te ₂ Se	This work	49(2)	4	157.2(4)	62(2)	4	149.1(5)	NA	NA	NA	104(4)	4	133.2(7)
	Ref. 41	38.3(17)	5.0	160.6(2)	68(7)	4	129.6(8)	NA	NA	NA	137(5)	4.0	114.9(1)
Bi ₂ Te _{1.75} Se _{1.19}	Ref. 41	34.5(10)	6.2	158.92(18)	77(3)	4	127.3(2)	NA	NA	NA	146(3)	4.0	111.42(6)
BiSbTe ₂ Se	This work	46.5(7)	4	146.2(2)	55(1)	4	140.0(6)	NA	NA	NA	63(5)	4	130.6(1.8)
Sb ₂ Te ₂ Se	This work	44(2)	4	151.0(6)	60(4)	4	143.1(1.2)	NA	NA	NA	73(4)	4	133.1(1.1)
	Ref. 7	21.85(20)	17.13	(<2.0 GPa)			_	_					
		38.19(42)	4.61 (>	>2.0 GPa)	_	_	_	_	—		_		
	Ref. 8	41.92 (Calc.)	4.89	—	41.25 (Calc.)	4.06	—	45.28 (Calc.)	3.57	—	—		—
Bi ₂ Te ₃		41.61 (Calc.)	4.68	—	—		—	—		—	—		
	Ref. 9	28.1(1.0)	13.8 (<	<3.2 GPa)	—		—	—		—	—		
		36.3(1.0)	5.5 (>2	3.2 GPa)	—		_	_	—		_	—	_
	Ref. 10	56.2(12)	2.1	169.16(7)	112(6)	6	148.3(7)			<u> </u>			
BiSbTe ₃	Ref. 10	56(2)	5.27	164.7(2)	97.5(27)	6.15	147.2(3)			<u> </u>			
	Ref. 11	54.7(2)	4	157.5(1)	77.1(5)	4	148.5(8)	80.5(6)	4	140.0(6)	109.4(4)	4	127.5(5)
	Ref. 12	45(2)	4	158.4(5)	62(3)	4	148.7(8)	69(4)	4	143(1)	72(2)	4	136.5(7)
Sb ₂ Te ₃	Ref. 13	41.0 (Calc.)	5.2	158.1	34.74 (Calc.)	5	—	38.91 (Calc.)	5	_		—	
	Ref. 14	36.1(9)	6.2	_	—	—	—	_	—	_		—	
	Ref. 15	40	4.0	158.3	-		—	—		—	-	—	—
	Ref. 10	30.2(14)	9.4	159.7(2)	60.8(26)	3.4	146.8(5)						
	Ref. 16	53.1(7)	4	141.2(2)	66(2)	4	133.4(6)	NA	NA	NA	97(3)	4	123.3(6)
	Ref. 19	53(8) (Exp.)	2.9	—	66(3) (Exp.)	4.5	—	—		—	_		
Bi ₂ Se ₃		47.8 (Calc.)	3.9		60.4 (Calc.)	4.8	_	77.1 (Calc.)	2.6		_		
		48.0 (Calc.)	4.6	_			_	—	—	_		—	_
	Ref. 20	32.9(8)	5.1	_	_	_	—	_		_	—		—
Sb ₂ Se ₃	Ref. 28	30(1)	6.1	136.4	NA	NA	NA	NA	NA	NA	217(11)	4	87.25(10)

Table S3. Bulk modulus (B_0), first-order pressure derivative (B_0), and fitted ambient unit cell volume (V_0 /f.u.) of phases I–IV for A₂B₃-type compounds (A = Bi, Sb; B = Te, Se) in this work and references,^{7–16,19,20,28,41} in which "NA" and "—" represent no phase and no data, respectively



Fig. S3 Schematic views of (a) the crystal structures of tetradymite and rock salt along the body diagonal direction and (b) the CsCl-like structure units in the BCT and CN9M models. The black bold lines denote the unit cells.



Fig. S4 Progressions of one quintuple layer in the tetradymite series, including As_2Te_3 , $AsSbTe_3$, Sb_2Te_3 , Bi_2Te_2Se , Bi_2Te_2Se , Bi_2TeSe_2 , and Bi_2Se_3 . We have used Cava's work for reference to draw this figure.⁷⁹