

Supporting information

High stability of the He atom confined in a U@C₆₀ fullerene

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Part 1. The calculated energies of UHe@C₆₀

Table S1. The calculated total energies of UHe@C₆₀ with different configurations and various spin multiplicities. The results with ZPE corrections are also included in brackets. All the final geometries have no imaginary frequency and their energies are given in Hartree.

Multiplicity	final structure	E _{bond}	E _{R6}	E _{atom}	E _{R5}
Singlet	UHe@C ₆₀ (R ₆)	-2763.41286 (-2763.04810)	-2763.41284 (-2763.04809)	-2763.41278 (-2763.04807)	-2763.41280 (-2763.04810)
Triplet	UHe@C₆₀ (R₆)	-2763.42516 (-2763.06080)	-2763.42516 (-2763.06079)	-2763.42513 (-2763.06069)	-2763.42516 (-2763.06069)
Quintet	UHe@C ₆₀ (B)	-2763.40560 (-2763.04264)	-2763.40560 (-2763.04264)	-2763.40560 (-2763.04263)	-2763.405602 (-2763.04265)
Septet	UHe@C ₆₀ (A)	-2763.38207 (-2763.01899)	-2763.38208 (-2763.01896)	-2763.38210 (-2763.01898)	-2763.38209 (-2763.01892)

Part 2. The related information for U₂@C₆₀ and U₂@C₆₁.

We used the benchmark calculations on U₂@C₆₀ and U₂@C₆₁ at PBE/SEG_ECP60MWB~6-31G (d) level to show the results are reliable. For the U₂@C₆₀ and U₂@C₆₁, we calculated the data on bond length, IR and Raman spectra, respectively. These results are all listed in the following, which are consistent with the previous theoretical research.^[24,48] For example, both U₂@C₆₀ and U₂@C₆₁ have two types of stretching modes, i.e., symmetric and asymmetric modes. The symmetric U-U stretching mode is IR-inactive, but while the asymmetric U-U stretching is Raman-inactive. Thus, these comparisons confirm the reliability of our current method.

Table S2. Calculated information of U₂@C₆₀ and U₂@C₆₁.

Property	U ₂ @C ₆₀ ^[a]	U ₂ @C ₆₀ ^[c]	U ₂ @C ₆₁ ^[b]	U ₂ @C ₆₁ ^[c]
U-U bond length (Å)	2.72	2.74	2.80	2.84
stretching modes (cm ⁻¹)				
symmetric	168.7	148.6	127.4	116.2
Asymmetric	147.4	156.1	142.0	141.3

^[a] Ref [24]

^[b] Ref [48]

^[c] Our calculations.

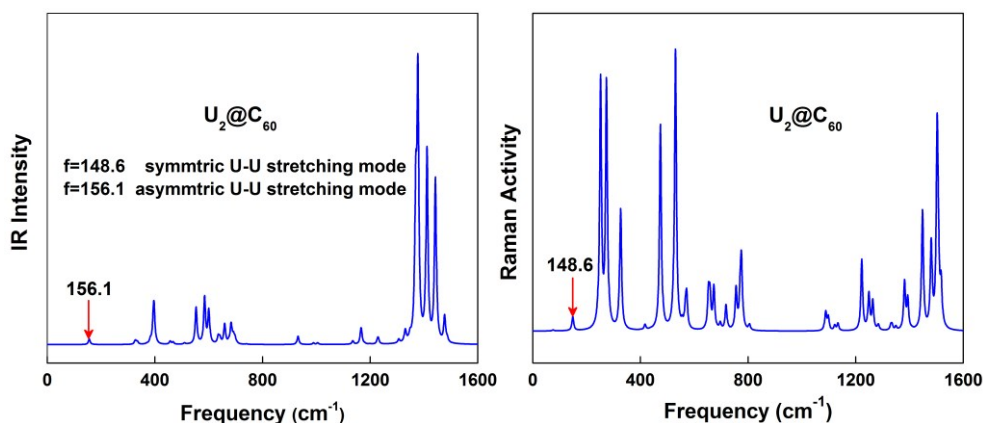


Figure S1. IR and Raman spectra of $U_2@C_{60}$ at PBE/SEG_ECP60MWB~6-31G (d) level.

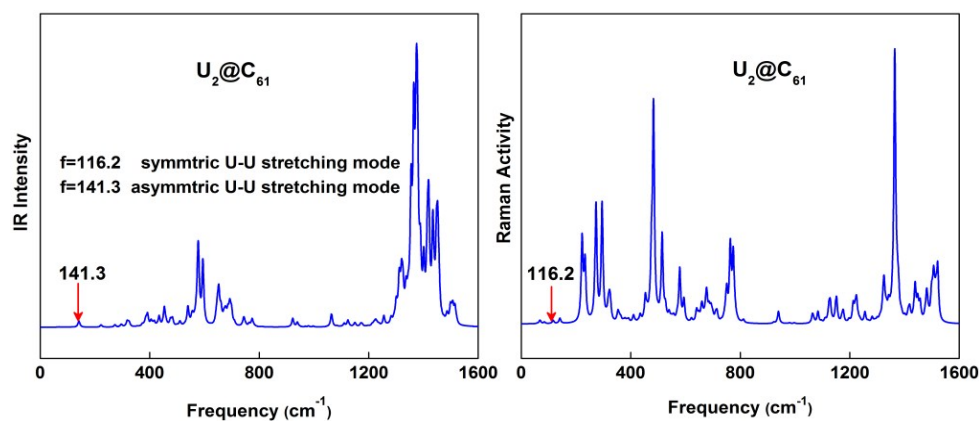


Figure S2. IR and Raman spectra of $U_2@C_{61}$ at PBE/SEG_ECP60MWB~6-31G (d) level.

Part 3. Relative energy calculations for $UHe@C_{60}$ using ZORA approach.

Table S3. Relative energy calculations for $UHe@C_{60}$ using ZORA approach.

Method	ΔE (eV)			
	Singlet	Triplet	Quintet	Septet
SR	0.29	0	0.72	1.28
SOC	2.83	0	0.03	9.70

Combined with the Table S1, we found that RECP and ZORA approach have the consistent results, namely, the ground state is triplet. It is showed that the spin-orbit coupling has no qualitatively influence on the results in this system, which further verifies the reliability of our calculated results.

Part 4. Molecular dynamics simulations of $UHe@C_{60}$

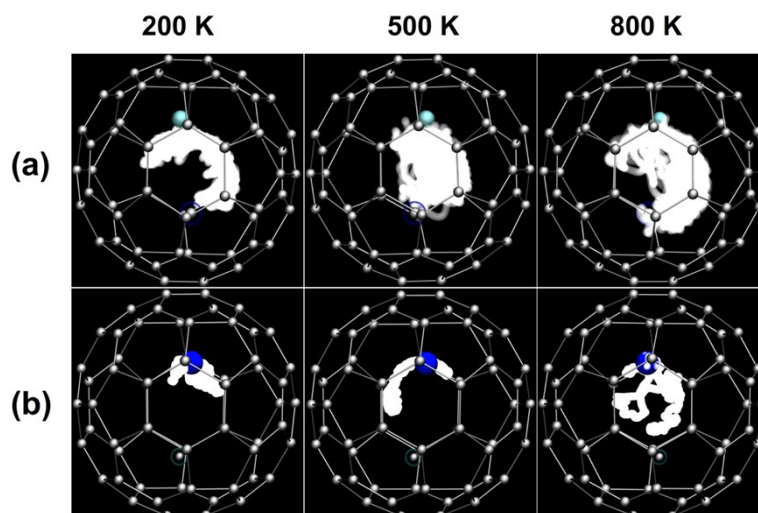


Figure S3. The MD trajectories of He and U atoms inside the C_{60} fullerene at different temperatures (200 K, 500 K and 800 K). The diagrams (a) and (b) demonstrate the trajectories of He and U atoms, respectively. Atom color are shown: U (blue), C (gray), He (cyan). In order to highlight target atom, so corresponding U and He atoms in (a) and (b) are represented in transparent, respectively.

We performed an annealing MD simulation at DFT-PBE level. At high temperature, the carbon cage is vibrating, but the structure is not broken, He and U are rotating in the cage. At low temperature, the location of U and He are both around the hexagonal centers which is in line with the geometry optimization results. It can be seen that the U atom in cage only move slightly, while the He has remarkably larger movement amplitude. Thus, we display the two curves both energy vs. time and Root-Mean-Square-Deviation (RMSD) vs. time for $UHe@C_{60}$ at low temperature. Since these information are more important and can further help us for understanding the $UHe@C_{60}$ system.

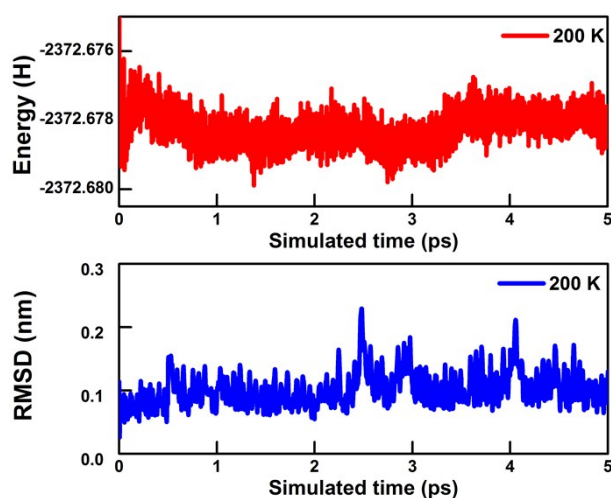


Figure S4. Energy vs. time and RMSD vs. time for $UHe@C_{60}$ system in 200 K.

Part 5. Charge distribution and spin population of UHe@C₆₀ and U@C₆₀.

Table S4. Charge distribution (e) and spin population (e) of UHe@C₆₀ and U@C₆₀.

UHe@C ₆₀ (U@C ₆₀) ^a					
	Charge (e)			Net spin (e)	
	NPA	Hirshfeld	Milliken	Mulliken	Hirshfeld
U	0.52(0.76)	0.47(0.52)	0.41(0.48)	2.21(2.25)	2.03(2.09)
C	-0.66(-0.76)	-0.58(-0.52)	-0.49(-0.48)	-0.21(-0.25)	-0.04(-0.09)
He	0.15	0.11	0.08	0	0
Total	/	/	/	2.00(2.00)	2.00(2.00)

^aThe results for U@C₆₀ are also included in brackets.

Part 6. Contour maps of electron density difference of UHe@C₆₀

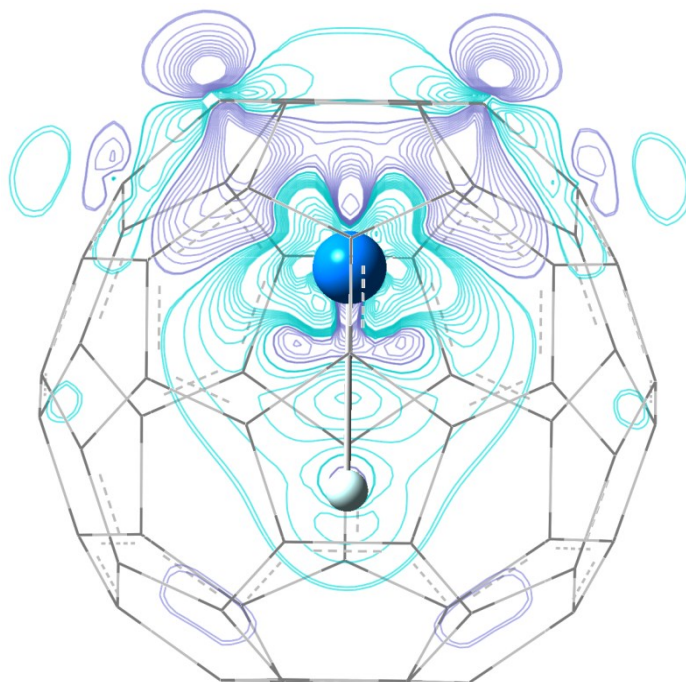


Figure S5. Contour maps of electron density difference. The density differences is obtained by subtracting electron density of isolated U, He and C₆₀ from that of UHe@C₆₀. The purple lines and green lines show the charge accumulation and depletion, respectively.

In order to further investigate the interaction between He and U@C₆₀, we observe the electron gains and losses using electron density difference. As seen in Figure S5,

U and He are surrounded by blue lines, and cage is surrounded by purple lines, which demonstrates the electron depletion and accumulation, respectively. We can see that there is no electrons accumulation either between He and U/fullerene cage. On the other hand, the purple area between U and C atoms indicates U transfer electron to carbon cage. It also demonstrates the presence of covalent interaction between them.

Part 7. Detailed data of energy decomposition analysis for UHe@C₆₀ system.

Table S5. Energy decomposition analysis of UHe@C₆₀ system (energy in eV).

System	$\Delta E_{\text{int}}^{\text{a}}$	$\Delta E_{\text{pauli}}^{\text{b}}$	$\Delta E_{\text{elestat}}^{\text{c}}$	$\Delta E_{\text{orb}}^{\text{d}}$
UHe@C ₆₀	0.10	0.65	-0.21	-0.34

^aInteraction energy, $\Delta E_{\text{int}} = \Delta E_{\text{pauli}} + \Delta E_{\text{elestat}} + \Delta E_{\text{orb}}$; ^bPauli repulsion energy; ^cElectrostatic interaction energy; ^dOrbital interaction energy. Within this energy decomposition scheme the attractive and repulsive terms are negative and positive, respectively.

Part 8. Detailed data of TD-DFT calculations for UHe@C₆₀.

Table S6. TD-DFT excitation energies (E in eV), excitation wavelengths (λ in nm), oscillator strengths (f, only energies with $f > 0.01$ are shown) and weights of UHe@C₆₀ (only contribution > 10% are shown).

E / λ	f	Transitions
1.600\774.88	0.012	75% HOMO α -1[C 2s 1.07%, 2p 29.49%;U 5f 66.38%] \rightarrow LUMO+6[C 2p 86.06%;U 5f 9.62%] 16% HOMO α [C 2p 22.12%;U 5f 73.34%] \rightarrow LUMO α +6
1.603\773.65	0.012	75% HOMO α -1 \rightarrow LUMO α +7 [C 2p 86%;U 5f 9.71%] 16% HOMO α \rightarrow LUMO α +7
1.612\768.95	0.015	12% HOMO α -3[C 2s 1.63%, 2p 61.65%;U 5f 35.28%] \rightarrow LUMO α +1[C 2p 31.27%;U 5f 61.99%] 16% HOMO α -3 \rightarrow LUMO α +3 [C 2p 39.73%;U 6d 2.24%, 5f 52.45%] 11% HOMO α -2[C 2s 1.62%, 2p 61.57%;U 5f 35.35%] \rightarrow LUMO α [C 2p 30.96%;U 5f 62.24%] 17% HOMO α -2 \rightarrow LUMO α +4 [C 2p 39.20%;U 6d 2.13%, 5f 52.08%]
2.034\609.58	0.005	55% HOMO α -8[C 2p 95.43%;U 5f 3.39%] \rightarrow LUMO α

		20% HOMO α -7[C 2p 95.43%;U 5f 3.40%] \rightarrow LUMO α +1
2.160\574.25	0.004	26% HOMO α -8 \rightarrow LUMO α +4 24% HOMO α -7 \rightarrow LUMO α +3 45% HOMO α -4[C 2p 96.30%;U 5f 2.83%] \rightarrow LUMO α +4
3.234\383.41	0.019	14% HOMO α -15[C 2s 1.04%, 2p 94.63%; U 5f 2.89%] \rightarrow LUMO α +2[C 2p 56.07%; U 5f 37.77] 13% HOMO α -11[C 2p 95.21%; U 5f 2.93%] \rightarrow LUMO α +3 13% HOMO α -9[C 2p 98.86%;U 5f 0.1%] \rightarrow LUMO α +5
3.234\383.36	0.020	16% HOMO α -14[C 2s 1.04%, 2p 94.64%;U 5f 2.89%] \rightarrow LUMO α +2 22% HOMO α -12[C 2s 1.05%,2p 90.31%;U 5f 8.15%;] \rightarrow LUMO α +1 17% HOMO α -11 \rightarrow LUMO α +4 12% HOMO α -10[C 2p 98.87%] \rightarrow LUMO α +5[C 2p 35.70%;U 5f 58.89%] 12% HOMO α -2 \rightarrow LUMO α +14[C 2s 6.14.%, 2p 94.49%]
3.244\382.24	0.035	36% HOMO α -13[C 2s 1.05%, 2p 94.86%; U 5f 2.32%] \rightarrow LUMO α +2 14% HOMO α -11 \rightarrow LUMO α +2
3.272\378.90	0.012	12% HOMO α -13 \rightarrow LUMO α 60% HOMO α -12 \rightarrow LUMO α +1
3.272\378.88	0.013	13% HOMO α -13 \rightarrow LUMO α +1 35% HOMO α -12 \rightarrow LUMO α 21% HOMO α -13 \rightarrow LUMO α +1 12% HOMO α -9 [C 2p 98.86%] \rightarrow LUMO α +5
3.285\377.49	0.025	24% HOMO α -12 \rightarrow LUMO α +5 41% HOMO α -1 \rightarrow LUMO+17[He 1s 1.10%; C 2s 1.75%, 2p 4.57%;U 7s 64.59%;]

3.437\360.69	0.014	17% HOMO α -15 \rightarrow LUMO α +1 25% HOMO α -15 \rightarrow LUMO α +3 11% HOMO α -14 \rightarrow LUMO α 20% HOMO α -14 \rightarrow LUMO α +4 23% HOMO α -13 \rightarrow LUMO α +2
3.560\348.25	0.027	20% HOMO α -15 \rightarrow LUMO α +3 42% HOMO α -14 \rightarrow LUMO α +4 18% HOMO α -12 \rightarrow LUMO α +5

Part 9. Infrared and Raman spectra of UHe@C₆₀ and U@C₆₀

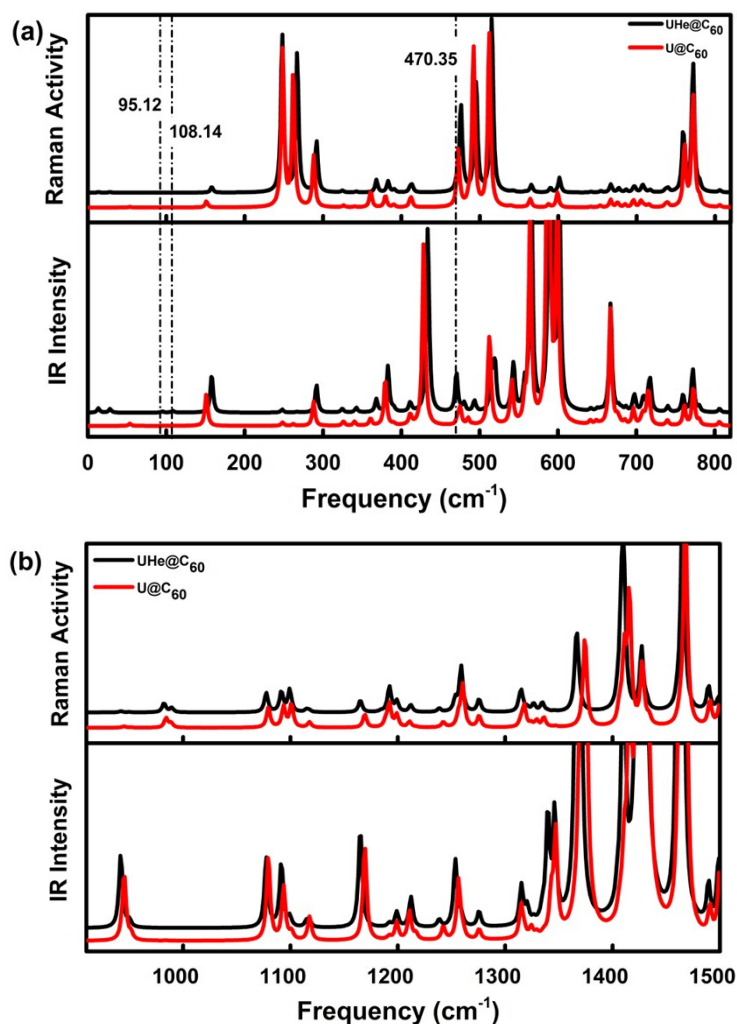


Figure S6. Infrared and Raman Spectra of UHe@C₆₀ and U@C₆₀, which are shown in black and red lines, respectively. Compared UHe@C₆₀ with U@C₆₀, three new characteristic peak positions have been pointed out by dotted lines.