## Supplementary Information

# Vertical $\mathbf{A l}_{2} \mathbf{S e}_{3} / \mathbf{M o S e} \mathbf{2}_{2}$ Heterojunction on Sapphire <br> Synthesized by Using Ion Beam 

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## Calculations

In Fig. S2a, the length of the dashed line, which contains a quadruple reciprocal vector, is equal to $8.933 \mathrm{~nm}^{-1}$, so that the length of the reciprocal vector is $2.233 \mathrm{~nm}^{-1}$. The inverse of $2.233 \mathrm{~nm}^{-1}$ is equal to 0.4478 nm that corresponds to the (011) interplanar distance $(0.4587 \mathrm{~nm})$ of $\mathrm{Al}_{2} \mathrm{Se}_{3}$. On the other hand, the length ( $16.591 \mathrm{~nm}^{-}$ ${ }^{1}$ ) of the dashed line as shown in Fig. S2b contains a quadruple reciprocal vector. Hence, the length of the reciprocal vector is $4.148 \mathrm{~nm}^{-1}$. The inverse of $4.148 \mathrm{~nm}^{-1}$ is equal to 0.241 nm that corresponds to the (400) interplanar distance $(0.25 \mathrm{~nm})$ of $\mathrm{Al}_{2} \mathrm{Se}_{3}$. These calculations, which derived from the experimental results, are in agreement with the theory and the error rate is less than $5 \%$, indicating that the results are believable.


Fig. S1 (a) STEM dark-field image of the $\mathrm{MoSe}_{2} / \mathrm{Al}_{2} \mathrm{Se}_{3} /$ sapphire layer structure. (b) Depth concentration distribution of $\mathrm{Mo}, \mathrm{Se}$, and Al .


Fig. S2 (a) The distance between (011) reciprocal points of $\mathrm{Al}_{2} \mathrm{Se}_{3}$. (b) The distance between (400) reciprocal points of $\mathrm{Al}_{2} \mathrm{Se}_{3}$.


Fig. S3 (a) The top-view SEM image of pristine sapphire. (b) The top-view SEM image of Mo film on sapphire. (c) The tilt-view SEM image of the patterned $\mathrm{MoSe} 2 / \mathrm{Al}_{2} \mathrm{Se}_{3}$ on sapphire. (d) The EDS spectrum of the area corresponding to the rectangle in (c).

