

Supporting Information for

**Effects of the locality of a potential derived from hybrid density functionals  
on Kohn-Sham orbitals and excited states**

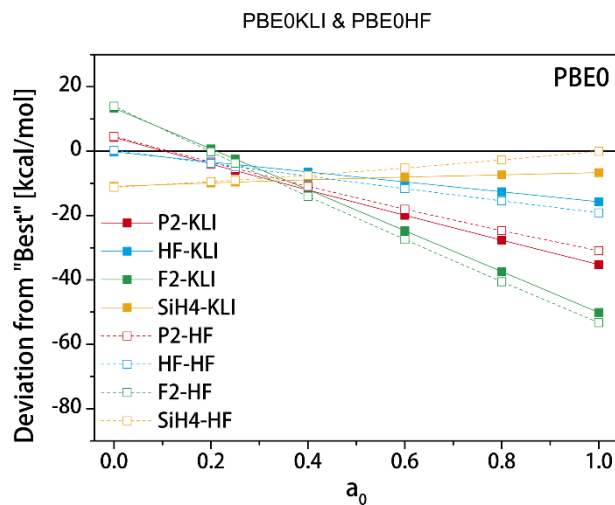
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## 1. Atomization energies



**Figure S1.** Atomization energies of  $P_2$ , HF,  $F_2$ , and  $SiH_4$  as a function of the exact exchange ratio ( $a_0$ ) with respect to the ab initio calculations [R. Haunschuld, W. Klopper, *J. Chem. Phys.* **2012**, *136*, 164102] which are denoted as “Best”.

## 2. Caricato set - Orbital energy gaps from PBE0HF- $a_0$

**Table S1.** The orbital energy gaps from PBE0HF- $a_0$  with various  $a_0$  as an approximation to each excitation energy for the Caricato set. The third column indicates the type of excitations: V and R for valence and Rydberg excitations, respectively. The experimental values were obtained from [M. Caricato, G. W. Trucks, M. J. Frisch, K. B. Wiberg, *J. Chem. Theory Comput.* **2010**, 6 (2), 370–383]. Unit: eV

Molecule	State	Type	PBE0HF- $a_0$ (Orbital energy gap)					Expt.	
			0.0	0.2	0.4	0.6	0.8		1.0
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.52	5.81	8.08	10.27	11.84	13.24	4.00
	1 <sup>1</sup> B <sub>2</sub>	R	5.78	7.35	8.83	10.26	11.66	13.07	7.08
	2 <sup>1</sup> B <sub>2</sub>	R	6.36	7.69	9.07	10.47	11.87	13.27	7.97
	2 <sup>1</sup> A <sub>1</sub>	R	6.34	7.68	9.02	10.38	11.76	13.16	8.14
	2 <sup>1</sup> A <sub>2</sub>	R	6.43	7.75	9.10	10.49	12.31	13.84	8.37
	3 <sup>1</sup> B <sub>2</sub>	R	6.41	7.76	9.12	10.50	11.91	13.33	8.88
	1 <sup>1</sup> B <sub>1</sub>	V	8.27	10.78	13.25	15.63	17.39	18.96	9.00
	3 <sup>1</sup> A <sub>2</sub>	R	6.88	14.49	9.65	11.05	12.50	14.06	9.22
	4 <sup>1</sup> B <sub>2</sub>	R	6.71	8.10	9.50	10.94	12.38	13.81	9.26
	4 <sup>1</sup> A <sub>1</sub>	R	6.81	8.18	9.57	10.97	12.37	13.79	9.58
5 <sup>1</sup> B <sub>2</sub>	R	6.76	13.79	9.61	11.01	12.41	13.83	9.63	
acetaldehyde	1 <sup>1</sup> A''	V	3.87	6.12	8.37	10.58	12.52	15.14	4.28
	2 <sup>1</sup> A'	R	5.38	6.95	8.45	9.87	11.25	12.63	6.82
	3 <sup>1</sup> A'	R	5.89	7.31	8.65	10.00	11.35	12.72	7.46
	4 <sup>1</sup> A'	R	6.04	7.35	8.70	10.05	11.41	12.77	7.75
	6 <sup>1</sup> A'	R	6.13	7.49	8.87	10.21	11.57	12.93	8.43
	7 <sup>1</sup> A'	R	6.23	7.55	8.87	10.22	11.57	12.94	8.69
acetone	1 <sup>1</sup> A <sub>2</sub>	V	3.97	6.18	8.31	10.39	12.53	14.99	4.43
	1 <sup>1</sup> B <sub>2</sub>	R	4.94	2.99	8.11	9.55	10.93	12.29	6.36
	2 <sup>1</sup> A <sub>2</sub>	R	5.73	7.06	8.42	9.70	11.04	12.38	7.36
	2 <sup>1</sup> A <sub>1</sub>	R	5.63	7.02	8.36	9.69	11.03	12.38	7.41
	2 <sup>1</sup> B <sub>2</sub>	R	5.75	7.06	8.40	9.73	11.07	12.42	7.49
	3 <sup>1</sup> A <sub>1</sub>	R	5.85	7.19	8.50	9.82	11.16	12.50	7.80
	3 <sup>1</sup> B <sub>2</sub>	R	5.78	7.09	8.41	9.78	11.17	12.55	8.09
	1 <sup>1</sup> B <sub>1</sub>	R	5.89	7.18	8.49	9.81	11.14	12.48	8.17
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	6.39	7.51	8.53	9.48	10.41	11.33	7.11
	1 <sup>1</sup> B <sub>1u</sub>	V	5.63	7.33	8.87	9.80	10.71	11.63	7.65
	1 <sup>1</sup> B <sub>1g</sub>	R	6.80	7.74	8.65	9.56	10.47	11.38	7.80
	1 <sup>1</sup> B <sub>2g</sub>	R	6.78	7.73	8.65	9.56	10.47	11.38	7.90
	2 <sup>1</sup> A <sub>g</sub>	R	6.92	7.83	8.76	9.68	10.60	11.52	8.28
	2 <sup>1</sup> B <sub>3u</sub>	R	6.86	7.80	8.76	9.74	10.69	11.62	8.62
	3 <sup>1</sup> B <sub>3u</sub>	R	7.08	7.99	8.89	9.80	10.72	11.65	8.90
	4 <sup>1</sup> B <sub>3u</sub>	R	7.30	8.27	9.25	10.24	11.22	12.20	9.08
	3 <sup>1</sup> B <sub>1g</sub>	R	6.97	7.97	8.92	9.86	10.79	11.72	9.20
	2 <sup>1</sup> B <sub>1u</sub>	R	7.09	8.00	9.00	10.46	11.63	12.64	9.33
	5 <sup>1</sup> B <sub>3u</sub>	R	7.81	8.81	9.80	10.77	11.73	12.68	9.51
isobutene	<sup>1</sup> B <sub>1</sub>	R	5.34	6.53	7.62	8.59	9.52	10.44	6.17
	<sup>1</sup> A <sub>1</sub>	R	5.23	6.75	7.80	8.70	9.60	10.51	6.7

trans-butadiene	$1^1B_u$	V	3.91	5.42	6.93	8.36	9.22	10.05	5.91
	$1^1B_g$	R	5.48	6.47	7.37	8.21	9.04	9.87	6.22
	$2^1A_u$	R	5.74	6.65	7.48	8.29	9.10	9.93	6.66
	$2^1B_u$	R	5.99	6.80	7.60	8.49	9.49	10.32	7.07
	$2^1B_g$	R	5.95	6.74	7.57	8.37	9.18	10.00	7.36
	$3^1A_g$	R	6.18	6.95	7.74	8.54	9.36	10.18	7.62
	$3^1B_u$	R	6.30	7.08	7.88	8.68	9.85	10.92	8.00
pyridine	$1^1B_1$	V	3.83	6.05	8.05	10.04	12.02	13.76	4.59
	$1^1B_2$	V	4.80	6.31	7.80	9.27	10.71	11.90	4.99
	$1^1A_2$	V	4.19	6.42	8.44	10.45	12.38	14.09	5.43
	$1^1A_1$	V	5.16	6.69	8.20	9.68	11.07	12.23	6.38
pyrazine	$1^1B_{3u}$	V	3.25	5.23	7.22	9.21	11.15	13.16	3.83
	$1^1B_{2u}$	V	4.44	5.96	7.46	8.93	10.33	11.76	4.81
	$1^1B_{2g}$	V	4.75	6.92	9.10	11.28	13.41	15.58	5.46
	$1^1B_{1g}$	V	5.52	7.72	9.93	12.15	14.35	16.28	6.10
	$1^1B_{1u}$	V	5.76	7.43	9.09	10.72	12.28	13.85	6.51
pyridazine	$1^1B_1$	V	2.79	4.84	6.90	8.97	11.03	13.00	3.60
	$1^1A_1$	V	4.89	6.45	8.00	9.53	11.02	12.41	5.00
	$1^1A_2$	V	4.78	6.84	8.90	10.96	13.00	14.95	5.30
	$1^1B_1$	V	5.34	7.44	9.53	11.61	13.66	15.41	6.00
	$1^1B_2$	V	5.45	7.05	8.63	10.17	11.68	12.88	6.50
pyrimidine	$1^1B_1$	V	3.58	5.59	7.60	9.62	11.75	13.55	3.85
	$1^1A_2$	V	3.92	5.95	7.99	10.03	12.05	13.74	4.62
	$1^1B_2$	V	5.01	6.58	8.13	9.66	11.30	12.60	5.12
	$1^1A_2$	V	4.83	6.92	9.01	11.09	13.28	15.14	5.52
	$1^1B_1$	V	5.17	7.28	9.39	11.50	13.58	15.33	5.90
	$1^1A_1$	V	5.35	6.94	8.51	10.07	11.60	12.79	6.70
s-tetrazine	$1^1B_{3u}$	V	1.53	3.60	5.68	7.78	9.89	12.02	2.25
	$1^1A_u$	V	2.70	4.84	6.99	9.15	11.29	13.47	3.40
	$1^1A_u$	V	4.35	6.44	8.53	10.63	12.73	14.84	5.00
	$1^1B_{3u}$	V	5.52	7.68	9.84	12.00	14.13	16.29	6.34
Mean absolute error (total)			1.30	1.05	1.74	3.20	4.66	6.07	
Mean absolute error (valence)			0.75	1.27	3.14	5.04	6.85	8.55	
Mean absolute error (Rydberg)			1.73	0.89	0.67	1.80	2.98	4.15	

### 3. Caricato set – Orbital energy gaps from PBE0KLI- $a_0$

**Table S2.** The orbital energy gaps from PBE0KLI- $a_0$  with various  $a_0$  as an approximation to each excitation energy for the Caricato set. The third column indicates the type of excitations: V and R for valence and Rydberg excitations, respectively. See **Table S1** for the experimental values. Unit: eV

Molecule	State	Type	PBE0KLI- $a_0$ (Orbital energy gap)						
			0.0	0.2	0.4	0.5	0.6	0.8	1.0
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.46	3.59	3.76	3.77	3.83	3.95	4.28
	1 <sup>1</sup> B <sub>2</sub>	R	5.83	6.41	6.95	7.22	7.48	7.98	8.49
	2 <sup>1</sup> B <sub>2</sub>	R	6.67	7.23	7.76	8.00	8.24	8.69	9.17
	2 <sup>1</sup> A <sub>1</sub>	R	6.61	7.28	7.90	8.22	8.52	9.10	9.75
	2 <sup>1</sup> A <sub>2</sub>	R	6.92	7.53	8.12	8.42	8.70	9.27	10.00
	3 <sup>1</sup> B <sub>2</sub>	R	7.46	8.13	8.74	9.05	9.34	9.88	10.55
	1 <sup>1</sup> B <sub>1</sub>	V	8.07	8.24	8.47	8.48	8.56	8.71	9.00
	3 <sup>1</sup> A <sub>2</sub>	R	7.73	8.44	9.14	9.50	9.84	10.54	11.52
	4 <sup>1</sup> B <sub>2</sub>	R	7.66	8.36	9.04	9.39	9.73	10.39	11.27
	4 <sup>1</sup> A <sub>1</sub>	R	8.23	8.94	9.64	10.02	10.38	11.10	12.20
	5 <sup>1</sup> B <sub>2</sub>	R	7.71	8.46	9.20	9.59	9.97	10.73	11.86
acetaldehyde	1 <sup>1</sup> A''	V	3.84	3.99	4.14	4.21	4.28	4.42	4.75
	2 <sup>1</sup> A'	R	5.38	5.92	6.42	6.66	6.90	7.34	7.78
	3 <sup>1</sup> A'	R	5.94	6.55	7.12	7.39	7.66	8.16	8.66
	4 <sup>1</sup> A'	R	6.33	6.96	7.55	7.82	8.09	8.60	9.10
	6 <sup>1</sup> A'	R	6.90	7.56	8.19	8.50	8.79	9.35	9.98
7 <sup>1</sup> A'	R	7.07	7.78	8.47	8.80	9.13	9.76	10.51	
acetone	1 <sup>1</sup> A <sub>2</sub>	V	3.93	4.11	4.32	4.35	4.44	4.59	4.91
	1 <sup>1</sup> B <sub>2</sub>	R	4.96	5.49	5.97	6.21	6.44	6.87	7.27
	2 <sup>1</sup> A <sub>2</sub>	R	5.93	6.56	7.14	7.44	7.72	8.24	8.77
	2 <sup>1</sup> A <sub>1</sub>	R	5.72	6.37	6.96	7.26	7.53	8.06	8.57
	2 <sup>1</sup> B <sub>2</sub>	R	6.04	6.69	7.31	7.62	7.91	8.50	9.09
	3 <sup>1</sup> A <sub>1</sub>	R	6.53	7.22	7.85	8.16	8.46	9.00	9.55
	3 <sup>1</sup> B <sub>2</sub>	R	6.28	6.90	7.45	7.74	7.99	8.41	8.86
	1 <sup>1</sup> B <sub>1</sub>	R	6.58	7.29	7.96	8.29	8.60	9.18	9.74
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	6.46	6.85	7.21	7.40	7.58	7.91	8.04
	1 <sup>1</sup> B <sub>1u</sub>	V	5.65	5.73	5.79	5.84	5.88	5.95	5.98
	1 <sup>1</sup> B <sub>1g</sub>	R	7.01	7.47	7.89	8.12	8.32	8.70	8.91
	1 <sup>1</sup> B <sub>2g</sub>	R	6.95	7.43	7.86	8.09	8.31	8.72	8.95
	2 <sup>1</sup> A <sub>g</sub>	R	7.33	7.73	8.10	8.31	8.49	8.86	9.14
	2 <sup>1</sup> B <sub>3u</sub>	R	7.79	8.28	8.68	8.89	9.07	9.39	9.59
	3 <sup>1</sup> B <sub>3u</sub>	R	7.99	8.42	8.86	9.12	9.36	9.82	10.23
	4 <sup>1</sup> B <sub>3u</sub>	R	8.26	8.75	9.23	9.50	9.74	10.23	10.78
	3 <sup>1</sup> B <sub>1g</sub>	R	8.55	9.01	9.44	9.67	9.88	10.28	10.70
	2 <sup>1</sup> B <sub>1u</sub>	R	8.12	8.60	9.06	9.31	9.55	10.01	10.54
	5 <sup>1</sup> B <sub>3u</sub>	R	9.30	9.74	10.12	10.34	10.53	10.91	11.37
isobutene	<sup>1</sup> B <sub>1</sub>	R	5.37	5.74	6.08	6.24	6.40	6.70	6.84
	<sup>1</sup> A <sub>1</sub>	R	5.23	5.34	5.43	5.47	5.51	5.58	5.65
	1 <sup>1</sup> B <sub>u</sub>	V	3.93	3.98	4.02	4.06	4.09	4.14	4.18

trans-butadiene	$1^1B_g$	R	5.55	5.93	6.26	6.45	6.62	6.93	7.03
	$2^1A_u$	R	5.84	6.24	6.60	6.78	7.00	7.34	7.49
	$2^1B_u$	R	6.35	6.71	7.04	7.23	7.40	7.74	7.96
	$2^1B_g$	R	6.53	6.99	7.40	7.63	7.84	8.21	8.36
	$3^1A_g$	R	6.86	7.23	7.58	7.78	7.96	8.32	9.29
	$3^1B_u$	R	7.52	7.96	8.36	8.59	8.80	9.21	9.62
pyridine	$1^1B_1$	V	3.99	4.08	4.18	4.22	4.27	4.35	4.62
	$1^1B_2$	V	4.82	4.83	4.83	4.85	4.86	4.87	4.85
	$1^1A_2$	V	4.36	4.48	4.58	4.65	4.71	4.81	5.11
	$1^1A_1$	V	5.19	5.23	5.23	5.28	5.30	5.33	5.34
pyrazine	$1^1B_{3u}$	V	3.19	3.25	3.32	3.33	3.36	3.41	3.66
	$1^1B_{2u}$	V	4.46	4.45	4.43	4.44	4.43	4.42	4.38
	$1^1B_{2g}$	V	4.67	4.76	4.89	4.89	4.93	5.01	5.22
	$1^1B_{1g}$	V	5.45	5.59	5.74	5.79	5.85	5.98	6.25
	$1^1B_{1u}$	V	5.71	5.75	5.82	5.81	5.83	5.87	5.86
pyridazine	$1^1B_1$	V	2.69	2.80	2.87	2.94	2.99	3.08	3.37
	$1^1A_1$	V	4.87	4.89	4.90	4.91	4.91	4.93	4.91
	$1^1A_2$	V	4.68	4.76	4.88	4.88	4.92	4.98	5.22
	$1^1B_1$	V	5.27	5.38	5.49	5.53	5.58	5.67	5.94
	$1^1B_2$	V	5.46	5.50	5.52	5.56	5.58	5.61	5.63
pyrimidine	$1^1B_1$	V	3.48	3.58	3.67	3.72	3.76	3.85	4.13
	$1^1A_2$	V	3.84	3.96	4.06	4.13	4.18	4.29	4.60
	$1^1B_2$	V	5.00	5.02	5.03	5.04	5.05	5.07	5.07
	$1^1A_2$	V	4.73	4.82	4.91	4.95	5.00	5.08	5.34
	$1^1B_1$	V	5.08	5.20	5.30	5.36	5.42	5.52	5.80
	$1^1A_1$	V	5.36	5.40	5.42	5.45	5.47	5.51	5.53
s-tetrazine	$1^1B_{3u}$	V	1.42	1.49	1.55	1.58	1.61	1.67	1.94
	$1^1A_u$	V	2.64	2.76	2.83	2.93	2.98	3.09	3.43
	$1^1A_u$	V	4.25	4.29	4.38	4.34	4.36	4.39	4.59
	$1^1B_{3u}$	V	5.47	5.56	5.65	5.69	5.73	5.81	6.08
Mean absolute error (total)			1.01	0.67	0.40	0.38	0.48	0.72	0.95
Mean absolute error (valence)			0.78	0.70	0.62	0.58	0.54	0.49	0.40
Mean absolute error (Rydberg)			1.18	0.65	0.23	0.23	0.43	0.89	1.38

#### 4. Caricato set – TDDFT results from PBE0HF- $a_0$

**Table S3.** The excitation energies of the Caricato set from TDDFT calculations performed on PBE0HF- $a_0$  orbitals with various  $a_0$ . The third column indicates the type of excitations: V and R for valence and Rydberg excitations, respectively. See **Table S1** for the experimental values. Unit: eV

Molecule	State	Type	PBE0HF- $a_0$ (TDDFT)					
			0.0	0.2	0.4	0.6	0.8	1.0
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.78	3.88	3.98	4.10	4.22	4.37
	1 <sup>1</sup> B <sub>2</sub>	R	5.76	6.51	7.25	7.98	8.68	9.35
	2 <sup>1</sup> B <sub>2</sub>	R	6.36	7.24	7.99	8.72	9.41	10.08
	2 <sup>1</sup> A <sub>1</sub>	R	6.33	7.22	8.04	8.83	9.44	9.44
	2 <sup>1</sup> A <sub>2</sub>	R	6.42	7.35	8.22	9.04	9.83	10.61
	3 <sup>1</sup> B <sub>2</sub>	R	6.40	7.41	8.45	9.46	10.42	11.30
	1 <sup>1</sup> B <sub>1</sub>	V	8.83	9.01	9.17	9.33	9.48	9.62
	3 <sup>1</sup> A <sub>2</sub>	R	6.86	7.75	8.72	9.74	10.81	11.24
	4 <sup>1</sup> B <sub>2</sub>	R	6.71	7.64	8.64	9.64	10.59	11.49
	4 <sup>1</sup> A <sub>1</sub>	R	6.81	7.78	8.75	9.68	10.64	11.56
	5 <sup>1</sup> B <sub>2</sub>	R	6.76	7.75	8.78	9.75	10.67	11.57
acetaldehyde	1 <sup>1</sup> A''	V	4.11	4.22	4.33	4.46	4.60	4.75
	2 <sup>1</sup> A'	R	5.43	6.25	7.04	7.80	8.53	9.22
	3 <sup>1</sup> A'	R	5.88	6.73	7.58	8.41	9.19	9.44
	4 <sup>1</sup> A'	R	6.05	6.96	7.79	8.59	9.27	9.99
	6 <sup>1</sup> A'	R	6.12	7.18	8.23	9.15	10.04	10.89
	7 <sup>1</sup> A'	R	6.22	7.23	8.26	9.23	10.11	10.97
acetone	1 <sup>1</sup> A <sub>2</sub>	V	4.20	4.35	4.50	4.66	4.82	5.00
	1 <sup>1</sup> B <sub>2</sub>	R	4.94	5.83	6.68	7.51	8.30	9.05
	2 <sup>1</sup> A <sub>2</sub>	R	5.72	6.63	7.50	8.35	9.17	9.95
	2 <sup>1</sup> A <sub>1</sub>	R	5.65	6.57	7.48	8.36	9.15	9.43
	2 <sup>1</sup> B <sub>2</sub>	R	5.75	6.68	7.55	8.40	9.23	10.05
	3 <sup>1</sup> A <sub>1</sub>	R	5.86	6.92	7.96	8.91	9.50	10.18
	3 <sup>1</sup> B <sub>2</sub>	R	5.78	6.79	7.79	8.73	9.61	10.46
	1 <sup>1</sup> B <sub>1</sub>	R	5.89	6.94	7.98	8.96	9.53	9.74
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	6.38	6.72	7.04	7.35	7.65	7.93
	1 <sup>1</sup> B <sub>1u</sub>	V	7.07	7.43	7.53	7.57	7.60	7.60
	1 <sup>1</sup> B <sub>1g</sub>	R	6.79	7.23	7.59	7.93	8.26	8.56
	1 <sup>1</sup> B <sub>2g</sub>	R	6.77	7.22	7.63	8.02	8.39	8.76
	2 <sup>1</sup> A <sub>g</sub>	R	6.92	7.42	7.87	8.28	8.65	9.00
	2 <sup>1</sup> B <sub>3u</sub>	R	6.86	7.50	8.10	8.64	9.10	9.50
	3 <sup>1</sup> B <sub>3u</sub>	R	7.08	7.68	8.26	8.80	9.32	9.76
	4 <sup>1</sup> B <sub>3u</sub>	R	7.29	7.85	8.40	8.93	9.40	9.86
	3 <sup>1</sup> B <sub>1g</sub>	R	7.41	7.96	8.30	8.84	9.42	9.96
	2 <sup>1</sup> B <sub>1u</sub>	R	7.33	7.73	8.32	8.89	9.43	9.92
	5 <sup>1</sup> B <sub>3u</sub>	R	7.78	8.23	8.71	9.21	9.75	10.33
isobutene	<sup>1</sup> B <sub>1</sub>	R	5.33	5.79	6.22	6.63	7.01	7.37
	<sup>1</sup> A <sub>1</sub>	R	5.90	6.33	6.68	6.95	7.14	7.26
	1 <sup>1</sup> B <sub>u</sub>	V	5.41	5.60	5.77	5.90	6.00	6.07

trans-butadiene	$1^1B_g$	R	5.46	5.79	6.10	6.41	6.71	7.00
	$2^1A_u$	R	5.73	6.11	6.37	6.82	7.17	7.50
	$2^1B_u$	R	6.03	6.44	6.82	7.17	7.49	7.81
	$2^1B_g$	R	5.95	6.47	6.97	7.40	7.79	8.16
	$3^1A_g$	R	6.17	6.65	7.12	7.57	8.00	8.40
	$3^1B_u$	R	6.31	6.79	7.28	7.76	8.25	8.74
pyridine	$1^1B_1$	V	4.34	4.76	5.11	5.42	5.70	5.97
	$1^1B_2$	V	5.31	5.49	5.64	5.76	5.86	5.94
	$1^1A_2$	V	4.44	5.06	5.67	6.25	6.79	7.31
	$1^1A_1$	V	6.17	6.28	6.38	6.39	6.34	6.25
pyrazine	$1^1B_{3u}$	V	3.54	3.91	4.21	4.47	4.70	4.90
	$1^1B_{2u}$	V	5.21	5.35	5.46	5.54	5.59	5.62
	$1^1B_{2g}$	V	5.11	5.58	5.92	6.18	6.39	6.57
	$1^1B_{1g}$	V	5.57	6.40	7.23	8.07	8.92	9.76
	$1^1B_{1u}$	V	6.37	6.50	6.57	6.56	6.49	6.37
pyridazine	$1^1B_1$	V	3.11	3.53	3.89	4.19	4.45	4.67
	$1^1A_1$	V	5.44	5.62	5.78	5.90	6.00	6.07
	$1^1A_2$	V	5.01	5.45	5.86	6.26	6.68	7.12
	$1^1B_1$	V	5.43	6.07	6.66	7.24	7.79	8.33
	$1^1B_2$	V	6.30	6.36	6.51	6.51	6.43	6.29
pyrimidine	$1^1B_1$	V	3.77	4.22	4.63	5.01	5.36	5.70
	$1^1A_2$	V	3.99	4.56	5.08	5.57	6.00	6.41
	$1^1B_2$	V	5.57	5.75	5.91	6.05	6.17	6.27
	$1^1A_2$	V	5.08	5.64	6.12	6.55	6.96	7.35
	$1^1B_1$	V	5.31	5.94	6.53	7.10	7.65	8.17
	$1^1A_1$	V	6.41	6.58	6.68	6.71	6.70	6.65
s-tetrazine	$1^1B_{3u}$	V	1.82	2.19	2.51	2.78	3.01	3.22
	$1^1A_u$	V	2.80	3.43	4.03	4.58	5.07	5.48
	$1^1A_u$	V	4.61	5.07	5.45	5.80	6.12	6.44
	$1^1B_{3u}$	V	5.63	6.28	6.90	7.49	8.05	8.60
Mean absolute error (total)			1.13	0.63	0.38	0.56	0.98	1.39
Mean absolute error (valence)			0.40	0.19	0.41	0.67	0.93	1.19
Mean absolute error (Rydberg)			1.70	0.98	0.35	0.48	1.01	1.55



**Table S4.** The excitation energies of the Caricato set from TDDFT calculations performed on PBE0HF- $a_0$  orbitals with various  $a_0$ . An LDA kernel was used. The third column indicates the type of excitations: V and R for valence and Rydberg excitations, respectively. See **Table S12** for the experimental values. Unit: eV

Molecule	State	Type	PBE0HF- $a_0$ (TDDFT w/ LDA ker.)					
			0.0	0.2	0.4	0.6	0.8	1.0
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.64	5.93	8.18	10.32	11.83	13.24
	1 <sup>1</sup> B <sub>2</sub>	R	5.64	7.23	8.76	10.22	11.64	13.05
	2 <sup>1</sup> B <sub>2</sub>	R	6.35	7.68	9.04	10.44	11.85	13.26
	2 <sup>1</sup> A <sub>1</sub>	R	6.30	7.66	9.01	10.38	11.76	13.15
	2 <sup>1</sup> A <sub>2</sub>	R	6.42	7.75	9.10	10.51	12.32	13.83
	3 <sup>1</sup> B <sub>2</sub>	R	6.38	7.75	9.11	10.49	11.89	13.31
	1 <sup>1</sup> B <sub>1</sub>	V	8.64	11.12	13.56	15.79	17.92	20.96
	3 <sup>1</sup> A <sub>2</sub>	R	6.85	8.24	9.64	11.05	12.50	14.04
	4 <sup>1</sup> B <sub>2</sub>	R	6.67	8.07	9.47	10.89	12.34	13.79
	4 <sup>1</sup> A <sub>1</sub>	R	6.78	8.14	9.53	10.93	12.34	13.76
	5 <sup>1</sup> B <sub>2</sub>	R	6.73	8.14	9.59	11.00	12.40	13.81
acetaldehyde	1 <sup>1</sup> A''	V	3.99	6.24	8.48	10.60	12.51	15.21
	2 <sup>1</sup> A'	R	5.36	6.93	8.43	9.86	11.24	12.63
	3 <sup>1</sup> A'	R	5.80	7.27	8.64	9.99	11.35	12.71
	4 <sup>1</sup> A'	R	6.04	7.35	8.70	10.05	11.41	12.77
	6 <sup>1</sup> A'	R	6.11	7.45	8.84	10.21	11.56	12.93
	7 <sup>1</sup> A'	R	6.21	7.54	8.87	10.21	11.57	12.93
acetone	1 <sup>1</sup> A <sub>2</sub>	V	4.09	6.30	8.34	10.41	12.53	15.06
	1 <sup>1</sup> B <sub>2</sub>	R	4.90	6.53	8.08	9.54	10.93	12.29
	2 <sup>1</sup> A <sub>2</sub>	R	5.71	7.06	8.47	9.70	11.04	12.38
	2 <sup>1</sup> A <sub>1</sub>	R	5.62	7.02	8.36	9.69	11.03	12.37
	2 <sup>1</sup> B <sub>2</sub>	R	5.74	7.05	8.39	9.73	11.07	12.41
	3 <sup>1</sup> A <sub>1</sub>	R	5.85	7.19	8.50	9.82	11.15	12.50
	3 <sup>1</sup> B <sub>2</sub>	R	5.77	7.08	8.40	9.77	11.16	12.55
	1 <sup>1</sup> B <sub>1</sub>	R	5.89	7.17	8.48	9.81	11.14	12.48
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	6.28	7.43	8.48	9.46	10.39	11.32
	1 <sup>1</sup> B <sub>1u</sub>	V	7.00	7.98	8.89	9.80	10.71	11.62
	1 <sup>1</sup> B <sub>1g</sub>	R	6.77	7.73	8.65	9.56	10.47	11.38
	1 <sup>1</sup> B <sub>2g</sub>	R	6.94	7.94	8.90	9.85	10.78	11.71
	2 <sup>1</sup> A <sub>g</sub>	R	11.50	7.83	8.75	9.67	10.59	11.50
	2 <sup>1</sup> B <sub>3u</sub>	R	6.86	7.78	8.73	9.70	10.66	11.61
	3 <sup>1</sup> B <sub>3u</sub>	R	7.08	7.99	8.89	9.80	10.71	11.63
	4 <sup>1</sup> B <sub>3u</sub>	R	7.28	8.25	9.23	10.21	11.20	12.17
	3 <sup>1</sup> B <sub>1g</sub>	R	7.39	8.39	9.39	10.38	11.35	12.30
	2 <sup>1</sup> B <sub>1u</sub>	R	7.15	8.48	9.63	10.66	11.64	12.61
	5 <sup>1</sup> B <sub>3u</sub>	R	7.75	8.77	9.76	10.73	11.70	12.66
isobutene	<sup>1</sup> B <sub>1</sub>	R	5.27	6.47	7.58	8.57	9.51	10.44
	<sup>1</sup> A <sub>1</sub>	R	5.83	6.87	7.79	8.69	9.60	10.51
trans-butadiene	1 <sup>1</sup> B <sub>u</sub>	V	5.25	6.59	8.68	10.02	9.97	12.77
	1 <sup>1</sup> B <sub>g</sub>	R	5.40	6.41	7.34	8.20	9.03	9.86

	$2^1A_u$	R	5.69	6.63	7.48	8.29	9.10	9.92
	$2^1B_u$	R	6.02	6.88	7.56	8.39	9.21	10.04
	$2^1B_g$	R	5.94	6.73	7.55	8.37	9.18	10.00
	$3^1A_g$	R	6.21	7.42	7.74	8.54	9.35	10.18
	$3^1B_u$	R	6.30	7.09	7.85	8.67	9.49	10.31
pyridine	$^1B_1$	V	4.25	6.24	8.23	10.20	12.16	13.77
	$^1B_2$	V	5.24	6.79	8.29	9.80	11.05	11.90
	$^1A_2$	V	4.41	6.42	8.44	10.45	12.38	14.08
	$^1A_1$	V	5.99	7.53	9.02	10.41	11.08	12.88
pyrazine	$^1B_{3u}$	V	3.45	5.43	7.41	9.40	11.16	13.35
	$^1B_{2u}$	V	5.13	6.70	8.22	9.71	10.34	12.22
	$^1B_{2g}$	V	5.01	7.17	9.35	11.52	13.43	15.85
	$^1B_{1g}$	V	5.55	7.75	9.98	12.16	14.36	16.36
	$^1B_{1u}$	V	6.19	7.75	9.30	10.74	11.78	13.82
pyridazine	$^1B_1$	V	3.03	5.07	7.12	9.18	11.06	13.01
	$^1A_1$	V	5.38	6.97	8.55	10.09	11.05	12.42
	$^1A_2$	V	4.92	6.98	9.03	11.08	13.03	15.15
	$^1B_1$	V	5.39	7.48	9.57	11.65	13.70	15.94
	$^1B_2$	V	6.11	7.73	9.29	10.81	11.59	13.00
pyrimidine	$^1B_1$	V	3.70	5.71	7.72	9.73	11.72	13.61
	$^1A_2$	V	3.95	5.98	8.02	10.05	12.08	13.89
	$^1B_2$	V	5.50	7.11	8.69	10.25	11.72	12.78
	$^1A_2$	V	5.01	7.09	9.17	11.24	13.29	15.21
	$^1B_1$	V	5.26	7.37	9.47	11.57	13.64	15.48
	$^1A_1$	V	6.23	7.82	9.40	10.90	12.23	13.99
s-tetrazine	$^1B_{3u}$	V	1.74	3.81	5.89	7.99	10.10	12.22
	$^1A_u$	V	2.76	4.90	7.05	9.20	11.33	13.24
	$^1A_u$	V	4.53	6.61	8.70	10.79	12.89	13.51
	$^1B_{3u}$	V	5.58	7.74	9.90	12.06	14.17	16.34
Mean absolute error (total)			1.21	1.00	1.87	3.33	4.70	6.17
Mean absolute error (valence)			0.47	1.53	3.45	5.31	6.95	8.81
Mean absolute error (Rydberg)			1.77	0.59	0.66	1.81	2.98	4.14

## 5. Caricato set – TDDFT results from PBE0KLI- $a_0$

**Table S5.** The excitation energies of the Caricato set from TDDFT calculations performed on PBE0KLI- $a_0$  orbitals with various  $a_0$ . An LDA kernel was used. The third column indicates the type of excitations: V and R for valence and Rydberg excitations, respectively. See **Table S12** for the experimental values. Unit: eV

Molecule	State	Type	PBE0KLI- $a_0$ (TDDFT w/ LDA ker.)						
			0.0	0.2	0.4	0.5	0.6	0.8	1.0
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.78	3.91	4.07	4.09	4.15	4.26	4.59
	1 <sup>1</sup> B <sub>2</sub>	R	5.81	6.40	6.95	7.23	7.50	8.01	8.54
	2 <sup>1</sup> B <sub>2</sub>	R	6.66	7.25	7.79	8.05	8.31	8.78	9.31
	2 <sup>1</sup> A <sub>1</sub>	R	6.59	7.27	7.90	8.23	8.54	9.13	9.81
	2 <sup>1</sup> A <sub>2</sub>	R	6.88	7.50	8.08	8.38	8.67	9.23	9.96
	3 <sup>1</sup> B <sub>2</sub>	R	7.48	8.17	8.80	9.12	9.42	9.99	10.68
	1 <sup>1</sup> B <sub>1</sub>	V	8.76	8.92	8.96	9.14	9.22	9.36	9.63
	3 <sup>1</sup> A <sub>2</sub>	R	7.70	8.41	9.11	9.47	9.81	9.89	10.13
	4 <sup>1</sup> B <sub>2</sub>	R	7.63	8.33	9.01	9.36	9.70	10.36	11.24
	4 <sup>1</sup> A <sub>1</sub>	R	8.27	8.98	9.68	10.03	10.36	10.92	11.78
	5 <sup>1</sup> B <sub>2</sub>	R	7.72	8.45	9.20	9.59	9.97	10.72	11.85
acetaldehyde	1 <sup>1</sup> A''	V	4.14	4.29	4.44	4.51	4.58	4.72	5.04
	2 <sup>1</sup> A'	R	5.46	6.00	6.50	6.74	6.97	7.42	7.86
	3 <sup>1</sup> A'	R	5.94	6.56	7.15	7.43	7.71	8.23	8.76
	4 <sup>1</sup> A'	R	6.31	6.95	7.55	7.84	8.11	8.63	9.09
	6 <sup>1</sup> A'	R	6.89	7.55	8.18	8.48	8.78	9.11	9.53
acetone	7 <sup>1</sup> A'	R	7.04	7.75	8.44	8.78	9.03	9.37	10.01
	1 <sup>1</sup> A <sub>2</sub>	V	4.23	4.40	4.61	4.64	4.72	4.87	5.19
	1 <sup>1</sup> B <sub>2</sub>	R	4.96	5.50	5.99	6.24	6.47	6.91	7.31
	2 <sup>1</sup> A <sub>2</sub>	R	5.92	6.55	7.14	7.44	7.62	7.66	7.89
	2 <sup>1</sup> A <sub>1</sub>	R	5.78	6.43	7.02	7.31	7.59	8.10	8.59
	2 <sup>1</sup> B <sub>2</sub>	R	6.03	6.69	7.31	7.62	7.91	8.43	8.90
	3 <sup>1</sup> A <sub>1</sub>	R	6.51	7.20	7.85	8.17	8.46	9.01	9.47
	3 <sup>1</sup> B <sub>2</sub>	R	6.27	6.91	7.48	7.77	8.03	8.55	8.97
1 <sup>1</sup> B <sub>1</sub>	R	6.56	7.27	7.95	8.26	8.33	8.40	8.63	
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	6.44	6.84	7.20	7.40	7.57	7.91	8.05
	1 <sup>1</sup> B <sub>1u</sub>	V	7.64	7.96	8.18	8.31	8.40	8.53	8.53
	1 <sup>1</sup> B <sub>1g</sub>	R	6.98	7.44	7.78	7.81	7.84	7.89	8.17
	1 <sup>1</sup> B <sub>2g</sub>	R	6.95	7.43	7.87	8.11	8.32	8.74	8.99
	2 <sup>1</sup> A <sub>g</sub>	R	7.39	7.79	8.16	8.37	8.56	8.93	9.24
	2 <sup>1</sup> B <sub>3u</sub>	R	7.77	8.27	8.68	8.90	9.09	9.43	9.67
	3 <sup>1</sup> B <sub>3u</sub>	R	7.96	8.40	8.85	9.10	9.34	9.81	10.21
	4 <sup>1</sup> B <sub>3u</sub>	R	8.26	8.75	9.23	9.50	9.75	10.24	10.80
	3 <sup>1</sup> B <sub>1g</sub>	R	8.55	9.02	9.45	9.68	9.89	10.30	10.72
	2 <sup>1</sup> B <sub>1u</sub>	R	8.64	9.00	9.36	9.58	9.78	10.19	10.71
	5 <sup>1</sup> B <sub>3u</sub>	R	9.28	9.74	10.15	10.38	10.59	10.99	11.45
isobutene	<sup>1</sup> B <sub>1</sub>	R	5.36	5.73	6.08	6.25	6.40	6.71	6.85
	<sup>1</sup> A <sub>1</sub>	R	6.07	6.47	6.82	6.98	7.12	7.37	7.53
	1 <sup>1</sup> B <sub>u</sub>	V	5.74	5.87	5.96	6.02	6.06	6.13	6.12

trans-butadiene	$1^1B_g$	R	5.52	5.90	6.23	6.42	6.59	6.91	7.01
	$2^1A_u$	R	5.83	6.24	6.61	6.77	6.96	7.30	7.44
	$2^1B_u$	R	6.67	6.95	7.23	7.41	7.57	7.88	8.13
	$2^1B_g$	R	6.51	6.97	7.38	7.61	7.72	7.76	8.02
	$3^1A_g$	R	6.85	7.23	7.57	7.78	7.96	8.30	8.49
	$3^1B_u$	R	7.50	7.93	8.33	8.56	8.77	9.17	9.57
pyridine	$1^1B_1$	V	4.34	4.43	4.52	4.57	4.61	4.69	4.96
	$1^1B_2$	V	5.46	5.49	5.51	5.55	5.56	5.59	5.58
	$1^1A_2$	V	4.40	4.52	4.63	4.70	4.75	4.86	5.15
	$1^1A_1$	V	6.72	6.73	6.69	6.73	6.74	6.76	6.73
pyrazine	$1^1B_{3u}$	V	3.55	3.61	3.68	3.69	3.71	3.76	4.01
	$1^1B_{2u}$	V	5.43	5.45	5.46	5.47	5.48	5.48	5.45
	$1^1B_{2g}$	V	5.09	5.18	5.31	5.31	5.35	5.43	5.64
	$1^1B_{1g}$	V	5.53	5.66	5.81	5.86	5.93	6.05	6.32
	$1^1B_{1u}$	V	6.96	6.98	6.95	6.98	7.00	7.02	7.00
pyridazine	$1^1B_1$	V	3.09	3.19	3.26	3.33	3.38	3.47	3.76
	$1^1A_1$	V	5.56	5.60	5.63	5.65	5.67	5.70	5.69
	$1^1A_2$	V	4.97	5.05	5.16	5.16	5.20	5.26	5.50
	$1^1B_1$	V	5.37	5.48	5.59	5.63	5.69	5.78	6.05
	$1^1B_2$	V	6.77	6.75	6.83	6.73	6.78	6.80	6.73
pyrimidine	$1^1B_1$	V	3.71	3.80	3.89	3.94	3.98	4.07	4.35
	$1^1A_2$	V	3.93	4.05	4.15	4.22	4.28	4.38	4.69
	$1^1B_2$	V	5.69	5.74	5.77	5.80	5.81	5.85	5.86
	$1^1A_2$	V	5.05	5.14	5.22	5.26	5.30	5.38	5.63
	$1^1B_1$	V	5.28	5.39	5.49	5.55	5.60	5.70	5.98
	$1^1A_1$	V	6.96	6.95	6.94	6.99	7.01	7.03	7.01
s-tetrazine	$1^1B_{3u}$	V	1.77	1.84	1.90	1.93	1.96	2.02	2.29
	$1^1A_u$	V	2.77	2.89	2.95	3.06	3.11	3.21	3.55
	$1^1A_u$	V	4.58	4.61	4.70	4.66	4.67	4.70	4.90
	$1^1B_{3u}$	V	5.60	5.69	5.79	5.82	5.87	5.95	6.22
Mean absolute error (total)			0.83	0.50	0.25	0.26	0.37	0.60	0.85
Mean absolute error (valence)			0.42	0.36	0.33	0.33	0.33	0.33	0.36
Mean absolute error (Rydberg)			1.14	0.61	0.19	0.21	0.40	0.80	1.23

## 6. Caricato set – TDDFT results from PBE0KLI-0.4 and PBE0HF-0.4

**Table S6.** The excitation energies of the Caricato set calculated using PBE0KLI-0.4. The third column indicates excitation types: V and R for vertical and Rydberg excitations, respectively. Experimental values were obtained from [M. Caricato, G. W. Trucks, M. J. Frisch, K. B. Wiberg, *J. Chem. Theory Comput.* **2010**, 6 (2), 370–383]. Unit: eV

Molecule	State	Type	PBE0KLI-0.4 (Orbital energy gaps)	PBE0KLI-0.4 w/ LDA kernel (TDDFT)	the portion of the major configuration in TDDFT calculation ( $ c ^2$ )	Expt.
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.76	4.07	1.00	4.00
	1 <sup>1</sup> B <sub>2</sub>	R	6.95	6.95	1.00	7.08
	2 <sup>1</sup> B <sub>2</sub>	R	7.76	7.79	0.99	7.97
	2 <sup>1</sup> A <sub>1</sub>	R	7.90	7.90	0.99	8.14
	2 <sup>1</sup> A <sub>2</sub>	R	8.12	8.08	1.00	8.37
	3 <sup>1</sup> B <sub>2</sub>	R	8.74	8.80	0.97	8.88
	1 <sup>1</sup> B <sub>1</sub>	V	8.47	8.96	0.94	9.00
	3 <sup>1</sup> A <sub>2</sub>	R	9.14	9.11	1.00	9.22
	4 <sup>1</sup> B <sub>2</sub>	R	9.04	9.01	1.00	9.26
	4 <sup>1</sup> A <sub>1</sub>	R	9.64	9.68	0.96	9.58
5 <sup>1</sup> B <sub>2</sub>	R	9.20	9.20	0.98	9.63	
acetaldehyde	1 <sup>1</sup> A''	V	4.14	4.44	1.00	4.28
	2 <sup>1</sup> A'	R	6.42	6.50	0.99	6.82
	3 <sup>1</sup> A'	R	7.12	7.15	0.99	7.46
	4 <sup>1</sup> A'	R	7.55	7.55	0.98	7.75
	6 <sup>1</sup> A'	R	8.19	8.18	0.98	8.43
	7 <sup>1</sup> A'	R	8.47	8.44	0.99	8.69
acetone	1 <sup>1</sup> A <sub>2</sub>	V	4.32	4.61	1.00	4.43
	1 <sup>1</sup> B <sub>2</sub>	R	5.97	5.99	1.00	6.36
	2 <sup>1</sup> A <sub>2</sub>	R	7.14	7.14	1.00	7.36
	2 <sup>1</sup> A <sub>1</sub>	R	6.96	7.02	0.98	7.41
	2 <sup>1</sup> B <sub>2</sub>	R	7.31	7.31	1.00	7.49
	3 <sup>1</sup> A <sub>1</sub>	R	7.85	7.85	1.00	7.80
	3 <sup>1</sup> B <sub>2</sub>	R	7.45	7.48	0.99	8.09
	1 <sup>1</sup> B <sub>1</sub>	R	7.96	7.95	0.99	8.17
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	7.21	7.20	1.00	7.11
	1 <sup>1</sup> B <sub>1u</sub>	V	5.79	8.18	0.69	7.65
	1 <sup>1</sup> B <sub>1g</sub>	R	7.89	7.78	0.74	7.80
	1 <sup>1</sup> B <sub>2g</sub>	R	7.86	7.87	1.00	7.90
	2 <sup>1</sup> A <sub>g</sub>	R	8.10	8.16	0.99	8.28
	2 <sup>1</sup> B <sub>3u</sub>	R	8.68	8.68	0.99	8.62
	3 <sup>1</sup> B <sub>3u</sub>	R	8.86	8.85	0.99	8.90
	4 <sup>1</sup> B <sub>3u</sub>	R	9.23	9.23	1.00	9.08
	3 <sup>1</sup> B <sub>1g</sub>	R	9.44	9.45	1.00	9.20
	2 <sup>1</sup> B <sub>1u</sub>	R	9.06	9.36	0.69	9.33
5 <sup>1</sup> B <sub>3u</sub>	R	10.12	10.15	0.92	9.51	

isobutene	<sup>1</sup> B <sub>1</sub>	R	6.08	6.08	1.00	6.17
	<sup>1</sup> A <sub>1</sub>	R	5.43	6.82	0.52	6.70
trans-butadiene	<sup>1</sup> B <sub>u</sub>	V	4.02	5.96	0.82	5.91
	<sup>1</sup> B <sub>g</sub>	R	6.26	6.23	1.00	6.22
	<sup>2</sup> A <sub>u</sub>	R	6.60	6.61	0.99	6.66
	<sup>2</sup> B <sub>u</sub>	R	7.04	7.23	0.87	7.07
	<sup>2</sup> B <sub>g</sub>	R	7.40	7.38	0.99	7.36
	<sup>3</sup> A <sub>g</sub>	R	7.58	7.57	0.96	7.62
	<sup>3</sup> B <sub>u</sub>	R	8.36	8.33	0.99	8.00
pyridine	<sup>1</sup> B <sub>1</sub>	V	4.18	4.52	0.99	4.59
	<sup>1</sup> B <sub>2</sub>	V	4.83	5.51	0.67	4.99
	<sup>1</sup> A <sub>2</sub>	V	4.58	4.63	1.00	5.43
	<sup>1</sup> A <sub>1</sub>	V	5.23	6.69	0.55	6.38
pyrazine	<sup>1</sup> B <sub>3u</sub>	V	3.32	3.68	1.00	3.83
	<sup>1</sup> B <sub>2u</sub>	V	4.43	5.46	0.80	4.81
	<sup>1</sup> B <sub>2g</sub>	V	4.89	5.31	0.98	5.46
	<sup>1</sup> B <sub>1g</sub>	V	5.74	5.81	1.00	6.10
	<sup>1</sup> B <sub>1u</sub>	V	5.82	6.95	0.61	6.51
pyridazine	<sup>1</sup> B <sub>1</sub>	V	2.87	3.26	0.99	3.60
	<sup>1</sup> A <sub>1</sub>	V	4.90	5.63	0.64	5.00
	<sup>1</sup> A <sub>2</sub>	V	4.88	5.16	0.99	5.30
	<sup>1</sup> B <sub>1</sub>	V	5.49	5.59	0.99	6.00
	<sup>1</sup> B <sub>2</sub>	V	5.52	6.83	0.37	6.50
pyrimidine	<sup>1</sup> B <sub>1</sub>	V	3.67	3.89	0.99	3.85
	<sup>1</sup> A <sub>2</sub>	V	4.06	4.15	0.98	4.62
	<sup>1</sup> B <sub>2</sub>	V	5.03	5.77	0.66	5.12
	<sup>1</sup> A <sub>2</sub>	V	4.91	5.22	0.97	5.52
	<sup>1</sup> B <sub>1</sub>	V	5.30	5.49	0.99	5.90
	<sup>1</sup> A <sub>1</sub>	V	5.42	6.94	0.54	6.70
s-tetrazine	<sup>1</sup> B <sub>3u</sub>	V	1.55	1.90	1.00	2.25
	<sup>1</sup> A <sub>u</sub>	V	2.83	2.95	0.99	3.40
	<sup>1</sup> A <sub>u</sub>	V	4.38	4.70	0.99	5.00
	<sup>1</sup> B <sub>3u</sub>	V	5.65	5.79	0.99	6.34
Mean absolute error (total)			0.399	0.253	Average of  c  <sup>2</sup> : 0.92	
Mean absolute error (valence)			0.617	0.334		
Mean absolute error (Rydberg)			0.231	0.191		

**Table S7.** The excitation energies of the Caricato set calculated using PBE0HF-0.4. The third column indicates excitation types: V and R for vertical and Rydberg excitations, respectively. Experimental values were obtained from [M. Caricato, G. W. Trucks, M. J. Frisch, K. B. Wiberg, *J. Chem. Theory Comput.* **2010**, 6 (2), 370–383]. Unit: eV

Molecule	State	Type	PBE0HF-0.4 (Orbital energy gaps)	PBE0HF-0.4 (TDDFT)	the portion of the major configuration in TDDFT calculation ( $ c ^2$ )	Expt.
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	8.08	3.98	0.96	4.00
	1 <sup>1</sup> B <sub>2</sub>	R	8.83	7.25	0.61	7.08
	2 <sup>1</sup> B <sub>2</sub>	R	9.07	7.99	0.34	7.97
	2 <sup>1</sup> A <sub>1</sub>	R	9.02	8.04	0.39	8.14
	2 <sup>1</sup> A <sub>2</sub>	R	9.10	8.22	0.53	8.37
	3 <sup>1</sup> B <sub>2</sub>	R	9.12	8.45	0.38	8.88
	1 <sup>1</sup> B <sub>1</sub>	V	13.25	9.17	0.96	9.00
	3 <sup>1</sup> A <sub>2</sub>	R	9.65	8.72	0.46	9.22
	4 <sup>1</sup> B <sub>2</sub>	R	9.50	8.64	0.67	9.26
	4 <sup>1</sup> A <sub>1</sub>	R	9.57	8.75	0.62	9.58
	5 <sup>1</sup> B <sub>2</sub>	R	9.61	8.78	0.41	9.63
acetaldehyde	1 <sup>1</sup> A''	V	8.37	4.33	0.97	4.28
	2 <sup>1</sup> A'	R	8.45	7.04	0.63	6.82
	3 <sup>1</sup> A'	R	8.65	7.58	0.23	7.46
	4 <sup>1</sup> A'	R	8.70	7.79	0.20	7.75
	6 <sup>1</sup> A'	R	8.87	8.23	0.41	8.43
	7 <sup>1</sup> A'	R	8.87	8.26	0.29	8.69
acetone	1 <sup>1</sup> A <sub>2</sub>	V	8.31	4.50	0.49	4.43
	1 <sup>1</sup> B <sub>2</sub>	R	8.11	6.68	0.73	6.36
	2 <sup>1</sup> A <sub>2</sub>	R	8.42	7.50	0.35	7.36
	2 <sup>1</sup> A <sub>1</sub>	R	8.36	7.48	0.44	7.41
	2 <sup>1</sup> B <sub>2</sub>	R	8.40	7.55	0.34	7.49
	3 <sup>1</sup> A <sub>1</sub>	R	8.50	7.96	0.54	7.80
	3 <sup>1</sup> B <sub>2</sub>	R	8.41	7.79	0.25	8.09
	1 <sup>1</sup> B <sub>1</sub>	R	8.49	7.98	0.67	8.17
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	8.53	7.04	0.49	7.11
	1 <sup>1</sup> B <sub>1u</sub>	V	8.87	7.53	0.70	7.65
	1 <sup>1</sup> B <sub>1g</sub>	R	8.65	7.59	0.44	7.80
	1 <sup>1</sup> B <sub>2g</sub>	R	8.65	7.63	0.47	7.90
	2 <sup>1</sup> A <sub>g</sub>	R	8.76	7.87	0.67	8.28
	2 <sup>1</sup> B <sub>3u</sub>	R	8.76	8.10	0.50	8.62
	3 <sup>1</sup> B <sub>3u</sub>	R	8.89	8.26	0.78	8.90
	4 <sup>1</sup> B <sub>3u</sub>	R	9.25	8.40	0.46	9.08
	3 <sup>1</sup> B <sub>1g</sub>	R	8.92	8.30	0.66	9.20
	2 <sup>1</sup> B <sub>1u</sub>	R	9.00	8.32	0.69	9.33
	5 <sup>1</sup> B <sub>3u</sub>	R	9.80	8.71	0.72	9.51
isobutene	<sup>1</sup> B <sub>1</sub>	R	7.62	6.22	0.63	6.17
	<sup>1</sup> A <sub>1</sub>	R	7.80	6.68	0.29	6.70

trans-butadiene	$1^1B_u$	V	6.93	5.77	0.98	5.91
	$1^1B_g$	R	7.37	6.10	0.54	6.22
	$2^1A_u$	R	7.48	6.37	0.42	6.66
	$2^1B_u$	R	7.60	6.82	0.71	7.07
	$2^1B_g$	R	7.57	6.97	0.33	7.36
	$3^1A_g$	R	7.74	7.12	0.75	7.62
	$3^1B_u$	R	7.88	7.28	0.44	8.00
pyridine	$1^1B_1$	V	8.05	5.11	0.97	4.59
	$1^1B_2$	V	7.80	5.64	0.77	4.99
	$1^1A_2$	V	8.44	5.67	0.99	5.43
	$1^1A_1$	V	8.20	6.38	0.64	6.38
pyrazine	$1^1B_{3u}$	V	7.22	4.21	0.99	3.83
	$1^1B_{2u}$	V	7.46	5.46	0.90	4.81
	$1^1B_{2g}$	V	9.10	5.92	0.95	5.46
	$1^1B_{1g}$	V	9.93	7.23	0.96	6.10
	$1^1B_{1u}$	V	9.09	6.57	0.77	6.51
pyridazine	$1^1B_1$	V	6.90	3.89	0.98	3.60
	$1^1A_1$	V	8.00	5.78	0.74	5.00
	$1^1A_2$	V	8.90	5.86	0.97	5.30
	$1^1B_1$	V	9.53	6.66	0.97	6.00
	$1^1B_2$	V	8.63	6.51	0.54	6.50
pyrimidine	$1^1B_1$	V	7.60	4.63	0.99	3.85
	$1^1A_2$	V	7.99	5.08	0.98	4.62
	$1^1B_2$	V	8.13	5.91	0.76	5.12
	$1^1A_2$	V	9.01	6.12	0.97	5.52
	$1^1B_1$	V	9.39	6.53	0.98	5.90
	$1^1A_1$	V	8.51	6.68	0.73	6.70
s-tetrazine	$1^1B_{3u}$	V	5.68	2.51	1.00	2.25
	$1^1A_u$	V	6.99	4.03	0.99	3.40
	$1^1A_u$	V	8.53	5.45	0.99	5.00
	$1^1B_{3u}$	V	9.84	6.90	0.99	6.34
Mean absolute error (total)			1.743	0.376	Average of $ c ^2$ : 0.67	
Mean absolute error (valence)			3.142	0.405		
Mean absolute error (Rydberg)			0.667	0.353		



## 7. Caricato set – Orbital energy gaps and TDDFT results from BH&H (KLI)

**Table S8.** The excitation energies of the Caricato set calculated using BH&H (KLI). The third column indicates excitation types: V and R for vertical and Rydberg excitations, respectively. Experimental values were obtained from [M. Caricato, G. W. Trucks, M. J. Frisch, K. B. Wiberg, *J. Chem. Theory Comput.* **2010**, 6 (2), 370–383]. Unit: eV

Molecule	State	Type	BH&H (KLI) (Orbital energy gaps)	BH&H (KLI) w/ LDA kernel (TDDFT)	Expt.
formaldehyde	1 <sup>1</sup> A <sub>2</sub>	V	3.73	4.05	4.00
	1 <sup>1</sup> B <sub>2</sub>	R	6.89	6.90	7.08
	2 <sup>1</sup> B <sub>2</sub>	R	7.66	7.71	7.97
	2 <sup>1</sup> A <sub>1</sub>	R	7.91	7.92	8.14
	2 <sup>1</sup> A <sub>2</sub>	R	8.13	8.09	8.37
	3 <sup>1</sup> B <sub>2</sub>	R	8.74	8.82	8.88
	1 <sup>1</sup> B <sub>1</sub>	V	8.49	9.00	9.00
	3 <sup>1</sup> A <sub>2</sub>	R	9.22	9.19	9.22
	4 <sup>1</sup> B <sub>2</sub>	R	9.09	9.06	9.26
	4 <sup>1</sup> A <sub>1</sub>	R	9.71	9.75	9.58
	5 <sup>1</sup> B <sub>2</sub>	R	9.29	9.28	9.63
acetaldehyde	1 <sup>1</sup> A''	V	4.18	4.47	4.28
	2 <sup>1</sup> A'	R	6.34	6.43	6.82
	3 <sup>1</sup> A'	R	7.10	7.14	7.46
	4 <sup>1</sup> A'	R	7.51	7.53	7.75
	6 <sup>1</sup> A'	R	8.20	8.19	8.43
	7 <sup>1</sup> A'	R	8.53	8.51	8.69
acetone	1 <sup>1</sup> A <sub>2</sub>	V	4.39	4.67	4.43
	1 <sup>1</sup> B <sub>2</sub>	R	5.85	5.88	6.36
	2 <sup>1</sup> A <sub>2</sub>	R	7.15	7.15	7.36
	2 <sup>1</sup> A <sub>1</sub>	R	6.96	7.04	7.41
	2 <sup>1</sup> B <sub>2</sub>	R	7.30	7.31	7.49
	3 <sup>1</sup> A <sub>1</sub>	R	7.89	7.90	7.80
	3 <sup>1</sup> B <sub>2</sub>	R	7.45	7.48	8.09
	1 <sup>1</sup> B <sub>1</sub>	R	8.03	8.02	8.17
ethylene	1 <sup>1</sup> B <sub>3u</sub>	R	7.08	7.08	7.11
	1 <sup>1</sup> B <sub>1u</sub>	V	5.75	8.05	7.65
	1 <sup>1</sup> B <sub>1g</sub>	R	7.84	7.66	7.80
	1 <sup>1</sup> B <sub>2g</sub>	R	7.80	7.81	7.90
	2 <sup>1</sup> A <sub>g</sub>	R	8.04	8.12	8.28
	2 <sup>1</sup> B <sub>3u</sub>	R	8.60	8.60	8.62
	3 <sup>1</sup> B <sub>3u</sub>	R	8.84	8.83	8.90
	4 <sup>1</sup> B <sub>3u</sub>	R	9.22	9.23	9.08
	3 <sup>1</sup> B <sub>1g</sub>	R	9.42	9.43	9.20
	2 <sup>1</sup> B <sub>1u</sub>	R	9.07	9.33	9.33
	5 <sup>1</sup> B <sub>3u</sub>	R	10.04	10.07	9.51
isobutene	<sup>1</sup> B <sub>1</sub>	R	5.88	5.89	6.17
	<sup>1</sup> A <sub>1</sub>	R	5.39	6.71	6.70

trans-butadiene	$1^1B_u$	V	4.01	5.87	5.91
	$1^1B_g$	R	6.12	6.09	6.22
	$2^1A_u$	R	6.49	6.50	6.66
	$2^1B_u$	R	6.95	7.17	7.07
	$2^1B_g$	R	7.32	7.31	7.36
	$3^1A_g$	R	7.50	7.51	7.62
	$3^1B_u$	R	8.30	8.27	8.00
pyridine	$1^1B_1$	V	4.19	4.53	4.59
	$1^1B_2$	V	4.81	5.49	4.99
	$1^1A_2$	V	4.60	4.65	5.43
	$1^1A_1$	V	5.22	6.63	6.38
pyrazine	$1^1B_{3u}$	V	3.31	3.66	3.83
	$1^1B_{2u}$	V	4.41	5.43	4.81
	$1^1B_{2g}$	V	4.91	5.33	5.46
	$1^1B_{1g}$	V	5.78	5.85	6.10
	$1^1B_{1u}$	V	5.83	6.89	6.51
pyridazine	$1^1B_1$	V	2.91	3.29	3.60
	$1^1A_1$	V	4.90	5.63	5.00
	$1^1A_2$	V	4.90	5.18	5.30
	$1^1B_1$	V	5.51	5.62	6.00
	$1^1B_2$	V	5.51	6.79	6.50
pyrimidine	$1^1B_1$	V	3.71	3.93	3.85
	$1^1A_2$	V	4.10	4.19	4.62
	$1^1B_2$	V	5.02	5.77	5.12
	$1^1A_2$	V	4.92	5.22	5.52
	$1^1B_1$	V	5.31	5.50	5.90
	$1^1A_1$	V	5.41	6.89	6.70
s-tetrazine	$1^1B_{3u}$	V	1.59	1.93	2.25
	$1^1A_u$	V	2.86	2.98	3.40
	$1^1A_u$	V	4.37	4.68	5.00
	$1^1B_{3u}$	V	5.64	5.78	6.34
Mean absolute error (total)			0.402	0.250	
Mean absolute error (valence)			0.607	0.316	
Mean absolute error (Rydberg)			0.244	0.199	