Supplementary Information

Unusual renormalization group (RG) flow and temperature-dependent phase transition in strongly-insulating monolayer epitaxial graphene

Lung-I Huang^{a,b}, Yanfei Yang^{a,c}, Chieh-Wen Liu^{d,a}, Randolph E. Elmquist^a, Shun-Tsung Lo^{d*}, Fan-Hung Liu^d, and Chi-Te Liang^{b,c,d*}

^aNational Institute of Standards and Technology (NIST), Gaithersburg, MD 20899, USA

^bDepartment of Physics, National Taiwan University, Taipei 106, Taiwan ^cDepartment of Physics, Georgetown University, Washington, DC 20057, USA ^dGraduate Institute of Applied Physics, National Taiwan University, Taipei 106, Taiwan ^eDepartment of Physics, Stanford University, Stanford, CA 94305, USA

* ctliang@phys.ntu.edu.tw and shuntsunglo@mail.ncku.edu.tw



Figure S1 Schematic diagram showing a monolayer epitaxial graphene (EG) sample. S and D correspond to source and drain contacts. 1, 2, 3, 1^{*}, 2^{*} and 3^{*} are voltage probes. Channel dimensions, which are the same for all devices studied, are L = 0.6mm, W = 0.1 mm, with voltage contacts spaced 0.1 mm apart along both sides of the device.



Figure 2 (a) $\rho_{xx}(B)$ and $\rho_{xy}(B)$ of a disordered GaAs-based electron system at various temperatures *T* [Ref. 1]. The device is always in the insulating phase in the sense that $\rho_{xx}(B)$ decreases with increasing *T*.



Figure 2 (b) The corresponding RG flow derived from the data in Fig. 2(a). No cusplike RG flow is observed. The arrows indicate the flows from high temperature-data (1.11 K) to low-temperature data (0.31 K). The solid curve corresponds to the data taken at T=0.31 K. The dotted curve represents the theoretical expected semi-circle.

References

1 T.-Y. Huang, C. F. Huang, G. H. Kim, C. P. Huang, C.-T. Liang, and D. A. Ritchie, *Chin. J. Phys.*, 2009, 47, 401-407

2 S. H. Song, D. Shahar, D. C. Tsui, Y. H. Xie, and D. Monroe, *Phys. Rev. Lett.*, 1997, 78, 2200-2203