

Electronic Supporting Information  
for

Quasiparticle Energies, Exciton Level Structure and Optical Absorption Spectra of  
Ultra-narrow ZSiCNRs

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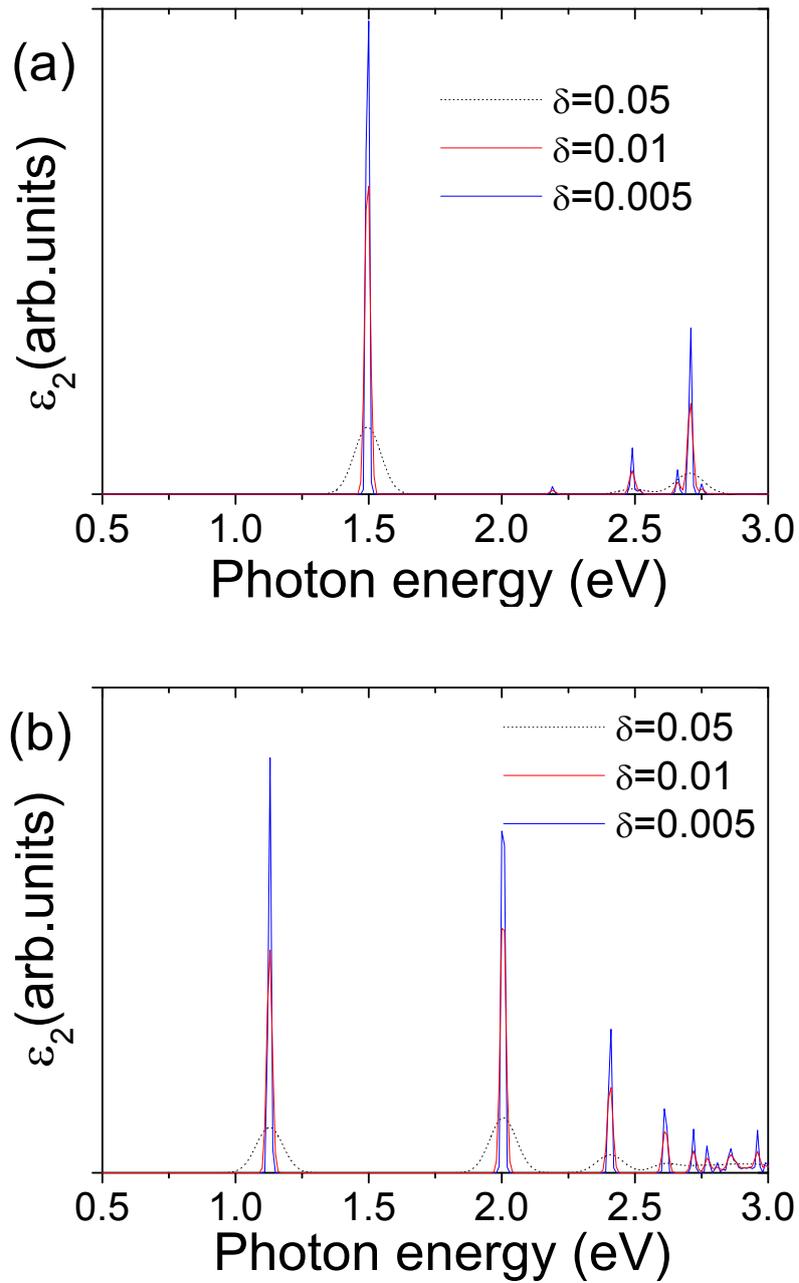


FIG. S1: (color online) (a) the longitudinal optical absorption spectra of 2-ZSiCNR including the effect of the electron-hole (e-h) interaction, (b) the transverse optical absorption spectra of 2-ZSiCNR including the effect of the electron-hole (e-h) interaction. Where different Gaussian broadening  $\delta$  have been used.

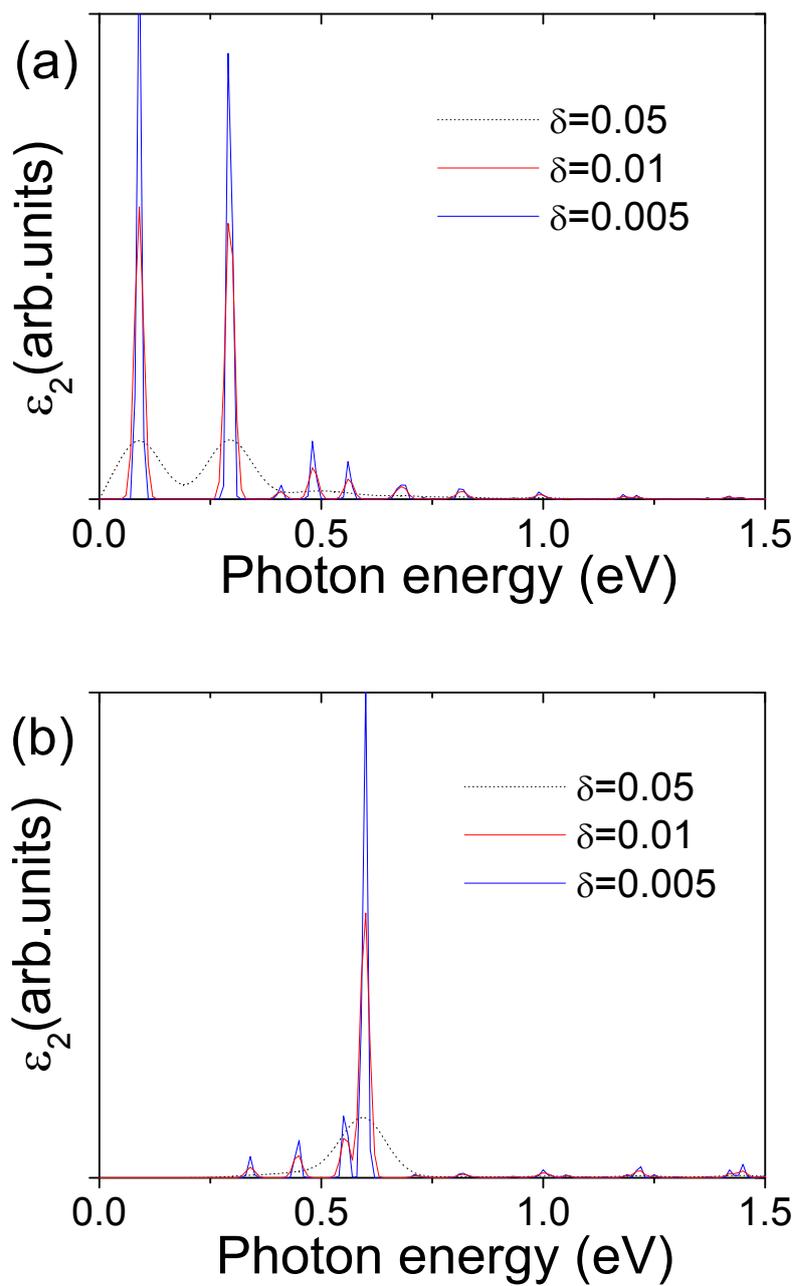


FIG. S2: (color online) (a) the longitudinal optical absorption spectra of 3-ZSiCNR including the effect of the electron-hole (e-h) interaction, (b) the transverse optical absorption spectra of 3-ZSiCNR including the effect of the electron-hole (e-h) interaction. Where different Gaussian broadening  $\delta$  have been used.

TABLE I: Special analysis for exciton wave functions of the degeneracy energy levels of 2-ZSiCNR associated with the interband transitions  $E^{ij}$ .

$E^{ij}$	$n$ -exciton	Energy (eV)	Weight	Transition point
$E^{11}$	6	2.489	0.42837	$Z$
$E^{21}$	1	2.489	0.53292	$Z$
$E^{11}$	10	2.708	0.21162	$Z$
$E^{12}$	1	2.708	0.69132	$Z$

TABLE II: Special analysis for exciton wave functions of the degeneracy energy levels of 3-ZSiCNR associated with the interband transitions  $E^{ij}$ .

$E^{ij}$	$n$ -exciton	Energy (eV)	Weight	Transition point
$E^{11}$	75	1.814	0.62481	non- $Z$
$E^{21}$	1	1.814	0.34912	$Z$
$E^{11}$	82	1.936	0.12358	non- $Z$
$E^{21}$	2	1.936	0.81733	$Z$
$E^{11}$	88	2.054	0.13026	non- $Z$
$E^{21}$	3	2.054	0.86282	$Z$
$E^{11}$	90	2.107	0.38683	non- $Z$
$E^{21}$	4	2.107	0.567292	$Z$
$E^{11}$	96	2.176	0.02024	non- $Z$
$E^{21}$	5	2.176	0.97640	$Z$
$E^{11}$	100	2.220	0.01141	non- $Z$
$E^{21}$	6	2.220	0.97691	$Z$
$E^{11}$	102	2.258	0.00156	non- $Z$
$E^{21}$	7	2.258	0.99704	$Z$
$E^{11}$	107	2.312	0.01603	non- $Z$
$E^{21}$	8	2.312	0.97002	$Z$

TABLE III: Convergence of band gap energies  $E_g$  calculated by  $GW$  of  $N$ -SiCNRs with respect to the  $k$ -grid.

$k$	2-SiCNR	3-SiCNR
16	2.818 eV	0.949 eV
32	2.909 eV	0.869 eV
64	2.911 eV	0.804 eV

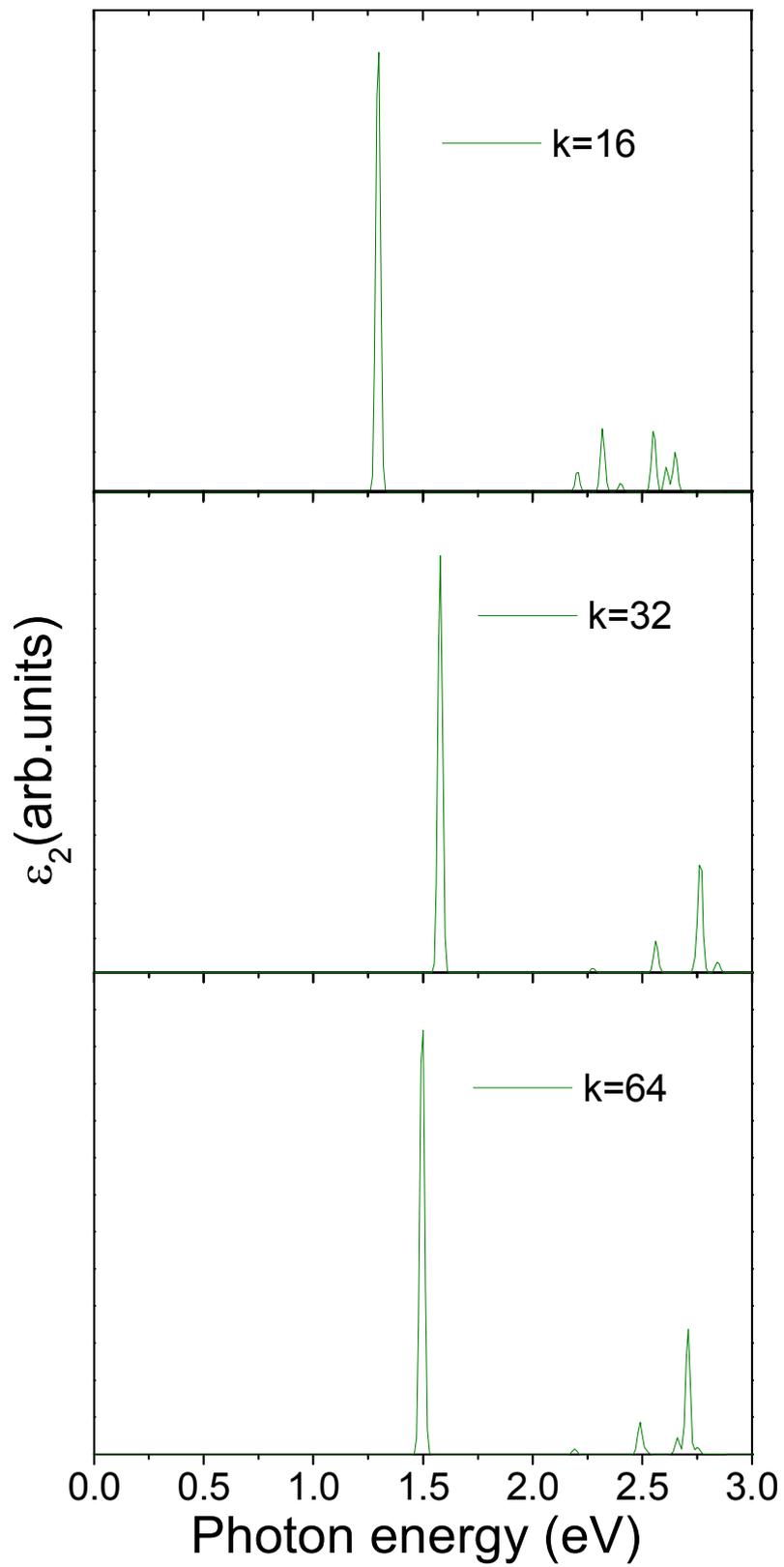


FIG. S3: (color online) Convergence of the optical absorption spectrum with respect to the k-grid. The longitudinal optical absorption spectra of 2-ZSiCNR including the effect of the electron-hole (e-h) interaction. A Gaussian broadening of 0.01 eV has been used.

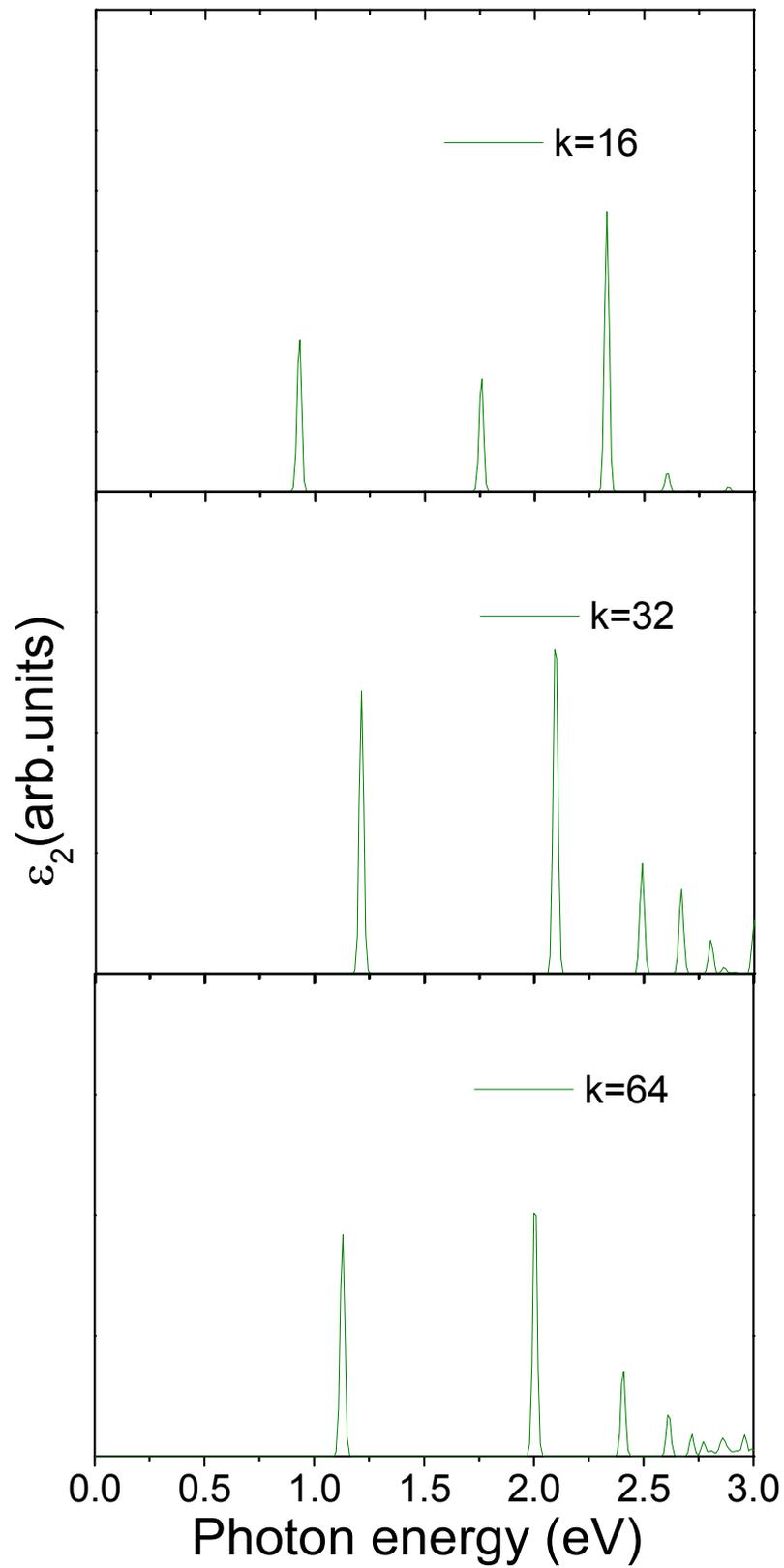


FIG. S4: (color online) Convergence of the optical absorption spectrum with respect to the k-grid. The transverse optical absorption spectra of 2-ZSiCNR including the effect of the electron-hole (e-h) interaction. A Gaussian broadening of 0.01 eV has been used.

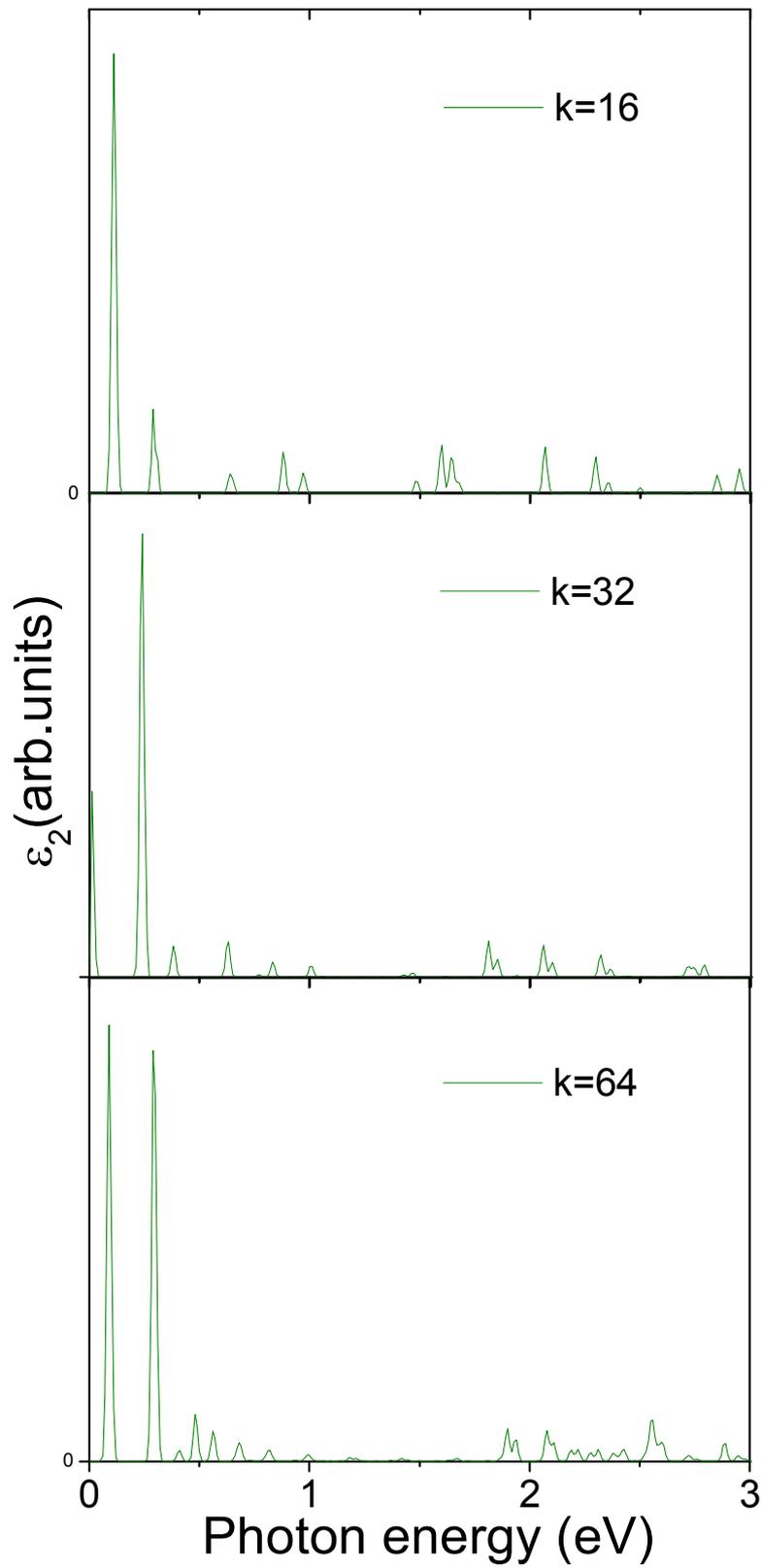


FIG. S5: (color online) Convergence of the optical absorption spectrum with respect to the k-grid. The longitudinal optical absorption spectra of 3-ZSiCNR including the effect of the electron-hole (e-h) interaction. A Gaussian broadening of 0.01 eV has been used.

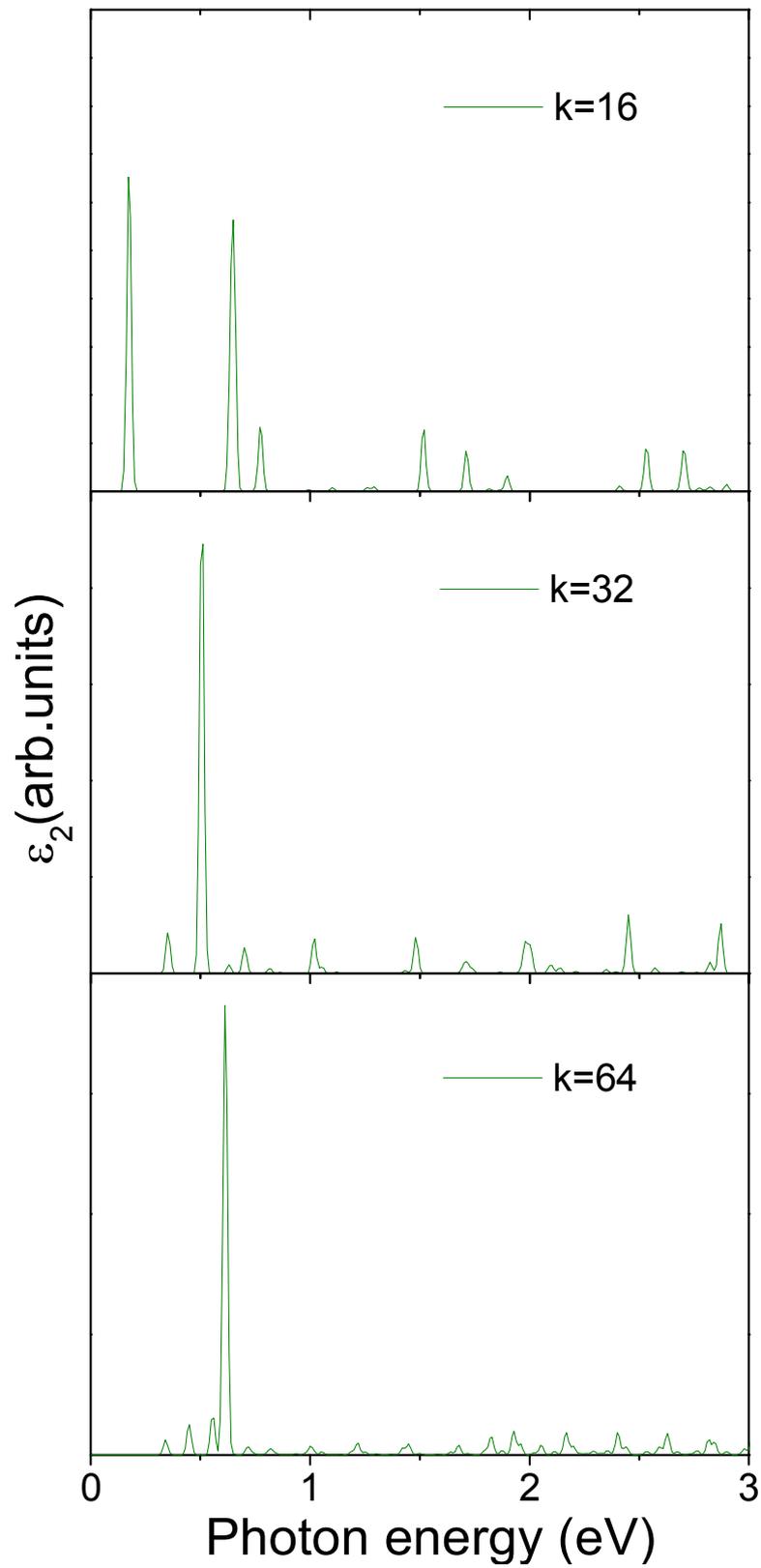


FIG. S6: (color online) Convergence of the optical absorption spectrum with respect to the k-grid. The transverse optical absorption spectra of 3-ZSiCNR including the effect of the electron-hole (e-h) interaction. A Gaussian broadening of 0.01 eV has been used.

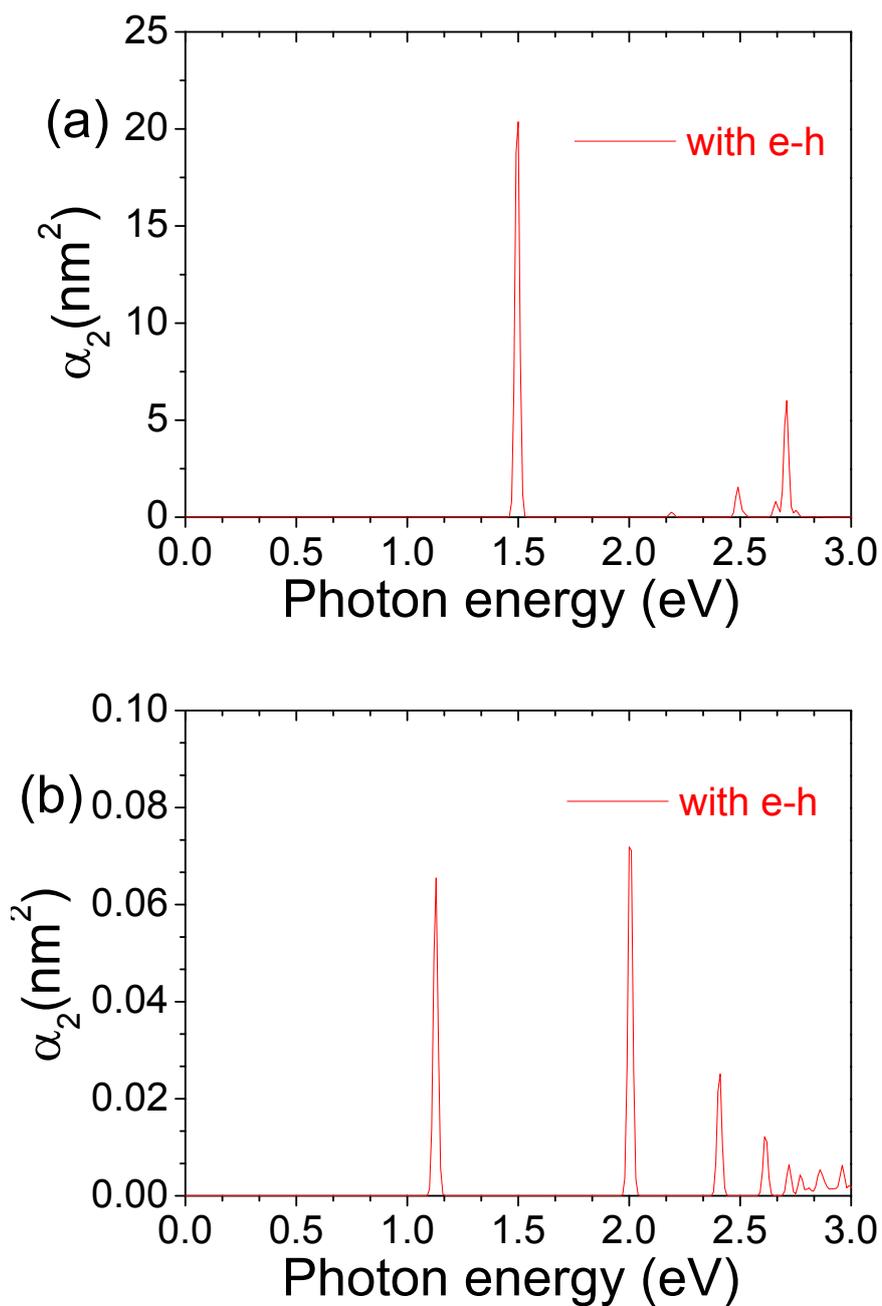


FIG. S7: (color online) The optical spectra in the polarizability per unit area: (a) the longitudinal optical absorption spectra of 2-ZSiCNR including the effect of the electron-hole (e-h) interaction, (b) the transverse optical absorption spectra of 2-ZSiCNR including the effect of the electron-hole (e-h) interaction. Where different Gaussian broadening  $\delta$  have been used.

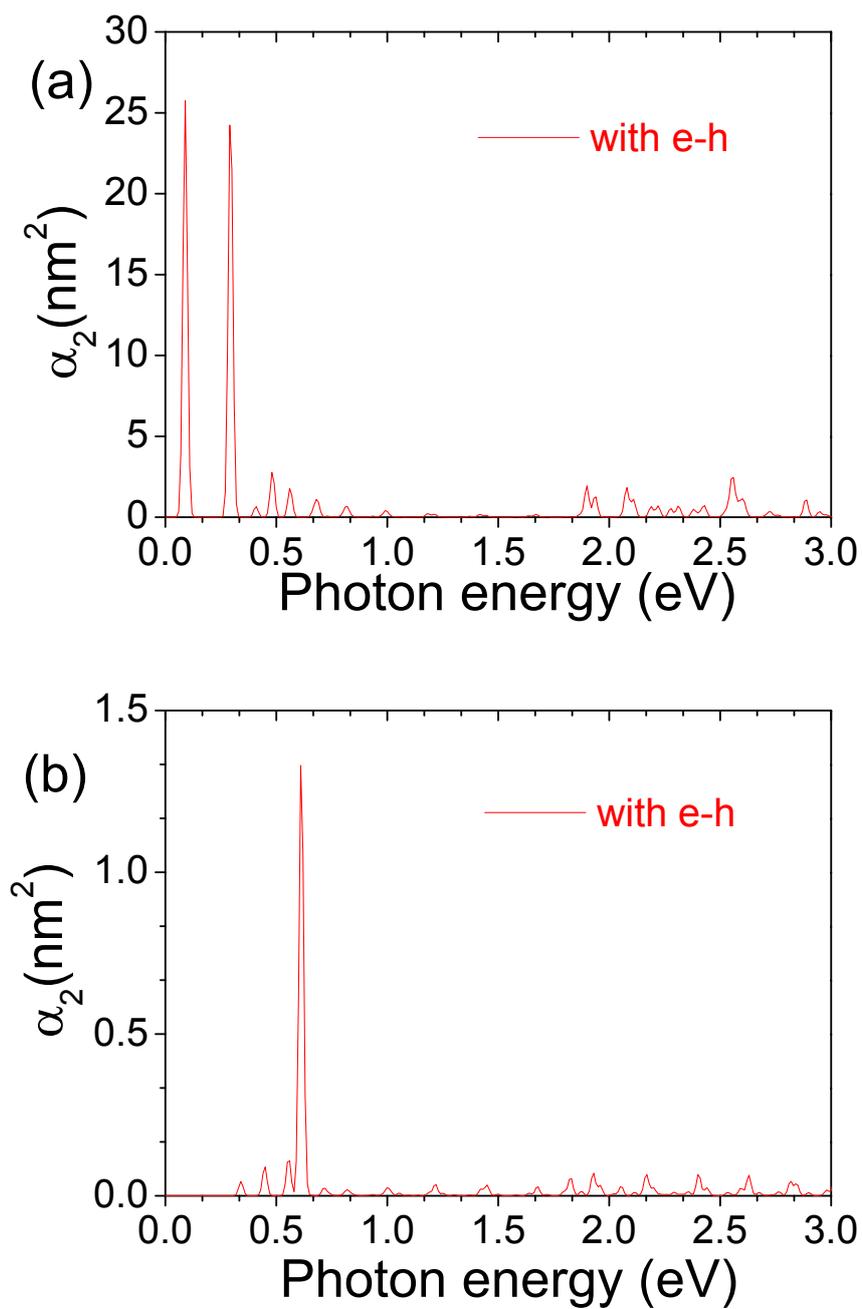


FIG. S8: (color online) The optical spectra in the polarizability per unit area: (a) the longitudinal optical absorption spectra of 3-ZSiCNR including the effect of the electron-hole (e-h) interaction, (b) the transverse optical absorption spectra of 3-ZSiCNR including the effect of the electron-hole (e-h) interaction. A Gaussian broadening of 0.01 eV has been used.