

Supporting Information
**Utilizing FBR to produce olefins from CO reduction using Fe-Mn
nanoparticles on reduced graphene oxide catalysts and comparing the
performance with SBR**

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1. FBR results

Table S 1: The effect of Mn loading and Temperature on the FBR FTS performance

	Fe	FeMn1	FeMn2	Fe	FeMn1	FeMn2	Fe	FeMn1	FeMn2
		6	9		6	9		6	9
T (°C)	300			320			340		
CO conv %	43	60	33	70	93	72	82	98	91
Fraction	Selectivity C mol%								
CO₂	14	25	16	29	37	23	38	41	36
CH₄	31	11	10	39	8.3	12	40	17	24
C 2-4 olefin	12	23	20	6.4	20	28	2.6	22	40
C 5-9 olefin	5.8	20	25	2.7	25	28	1.1	14	14
Total olefin	18	47	55	10	49	63	3.8	40	54
C9+ HC	1.7	16	17	0.9	21	5.21	0.2	18	0.32
				1			9		
Total Paraffin	71	33	35	86	26	32	92	39	46
Total iso	11	19	11	4.0	25	5.8	3.8	20	2.5
Total par + iso	82	52	45	90	51	37	96	60	47
O/P	0.2	0.90	1.22	0.1	0.96	1.7	0.0	0.67	1.1
	2			1			4		
Olefin yield	6.6	21	15	4.6	29	35	1.9	23	31
α	0.5	0.71	0.75	0.5	0.77	0.66	0.4	0.71	0.48
	5			1			2		

Reaction conditions: H₂/CO = 1, 4.2 l/gh, 2MPa

Table S 2: Effect of space velocity on the FBR FTS performance

	FeMn16		
GHSV (l/gh)	4.2	6.2	8.2
CO conversion %	92	93	94
Fraction	Selectivity C mol%		
CO₂	37	37	44
CH₄	8.3	17	23
C 2-4 olefin	20	27	30
C 5-9 olefin	25	15	14
Total olefin	49	45	46
C9+ HC	21	19	7.4
Total Paraffin	26	39	45
Total iso	25	16	8.9
Total par + iso	51	55	54
O/P	0.96	0.82	0.84
Olefin yield	29	26	24
α	0.77	0.61	0.58
Reaction conditions: H₂/CO = 1, 320°C, 2MPa			

Table S 3: Effect of pressure on the FBR FTS performance

FeMn16		
P (MPa)	1	2
CO conversion %	84	93
Fraction	Selectivity C mol%	
CO₂	35	37
CH₄	18	8.3
C 2-4 olefin	30	20
C 5-9 olefin	19	25
Total olefin	52	49
C9+ HC	8.58	21
Total Paraffin	40	26
Total iso	11	25
Total par + iso	50	51
O/P	1.0	0.96
-Olefin yield	28	29
α	0.63	0.77
Reaction conditions: H₂/CO=1, 320 °C, 4.2 L/g.h		

2. Calculation scheme

The equations used to calculate the catalyst performance are summarized as follows:

For the inlet conditions the molar rate is calculated by using the Gas Law:

$$F_{0t} = \frac{\dot{V} \times P_r \times 100 \times 60}{10^6 \times 8.314 \times (T_r + 273)} \frac{\text{mol}}{\text{h}}$$

At any time during the reaction the molar rate is measured by the same law but using the instantaneous flow rate as measured from the bubble flow meter:

$$F_{0 \text{ or } F} = \frac{P_r \times 100 \times 10 \times 3600}{t_{0 \text{ or } t} \times 10^6 \times 8.314 \times (T_r + 273)} \frac{\text{mol}}{\text{h}}$$

Where P_r and T_r are the room temperature and pressure, \dot{V} is the volumetric flow rate of the feed, and t is the time in s/10ml gas (bubble flow meter reading).

The product molar rates for any gas species i are calculated as follows utilizing the GC-TCD data:

$$F_i = \frac{F \times EAT_i \times x_i}{SAT_i} \frac{\text{C mol}}{\text{h}} \quad i = \text{CH}_4, \text{CO or CO}_2, \text{TCD Area}$$

EAT_i is the TCD area for component (i) in the exit stream

SAT_i is the TCD area for component (i) in the standard gas

The TCD data is used to calculate the CO conversion from the following equation if Ar is used as an internal standard

$$f_{\text{CO}} \% = 1 - \frac{EAT_{\text{CO}} / EAT_{\text{Ar}}}{FAT_{\text{CO}} / FAT_{\text{Ar}}} \times 100$$

If an external standard is used like CO or CH₄ then the conversion can be calculated as follows

$$f_{CO\%} = 1 - \frac{F_{CO}}{y_{0\ CO} F_0} \times 100$$

From the gas FID data we can compute the light hydrocarbon mole rates as follows

$$FG_{N,(o/p/i/t)} = \frac{F \times AG_{N,(o/p/i/t)} \times x_{CH_4}}{SAF_{CH_4}} \frac{C\ mol}{h}$$

$FG_{N,(o/p/i/t)}$ is the mole rate of the component N in the exit gas stream

$AG_{N,(o/p/i/t)}$ is the FID peak area for component N in the gas product, it can be calculated for olefins, paraffins, iso-paraffins or for the total hydrocarbon fraction, hence the subscript (o/p/i/t).

SAF_{CH_4} is the FID peak area for methane in the standard gas

x_{CH_4} is the methane mol fraction in the standard gas

And from the liquid FID data the heavy hydrocarbons' molar rate is produced from the following equation

$$FL_{N,(o/p/i/t)} = \frac{AL_{N,(o/p/i/t)} \times W_{12} \times N_{12}}{A_{C12} \times M_{12} \times TOS} \frac{C\ mol}{h}$$

$FL_{N,(o/p/i/t)}$ is the mole rate of the component N in the liquid product.

$AL_{N,(o/p/i/t)}$ is the FID peak area for component N in the liquid product, it can be calculated for olefins, paraffins, iso-paraffins or for the total hydrocarbon fraction, hence the subscript (o/p/i/t).

W_{12} : is the mass of the n-dodecane external standard used for the FID area calibration.

N_{12} is the number of carbon atoms in n-dodecane

A_{C12} is the FID peak area for the C12 fraction, since the amount of n-dodecane is very big compared to the C-12 fraction products in the liquid products, therefore the area can be assumed to represent n-dodecane only.

M_{12} : is the Molecular weight of n-dodecane

TOS: is the total Time On Stream

Then we can calculate the total molar rate in Cmol or mol/h of each carbon number as follows

$$F_{N,t} \text{ Cmol} = FG_{N,t} + FL_{N,t} \frac{\text{Cmol}}{h}$$

$$F_{N,t} = \frac{FG_{N,t} + FL_{N,t}}{N_N} \frac{\text{mol}}{h}$$

N_N : is the number of carbon atoms in an alkane of chain length N

The selectivities for the hydrocarbon fractions can be computed from the following equations:

$$S \text{ Cmol}_{N,(o/p/i/t)} \% = \frac{FG_{N,(o/p/i/t)} + FL_{N,(o/p/i/t)}}{\sum_N F_{N,t}} \frac{\text{Cmol HC}}{\text{Cmol CO reacted}}$$

$$S \text{ mol}_{N,(o/p/i/t)} \% = \frac{FG_{N,(o/p/i/t)} + FL_{N,(o/p/i/t)}}{\sum_N F_{N,t} \times N_N} \frac{\text{mol HC}}{\text{mol THC}}$$

If the selectivity are summed up across the carbon numbers by family (paraffins or olefins or isoparaffins), then the total family selectivity can be obtained:

$$S \text{ Cmol}_{(o/p/t)} \% = \sum_N S \text{ Cmol}_{N,(o/p/t)} \%$$

When the total olefin selectivity is divided by the total paraffin and iso paraffins selectivity we get the olefin to paraffin ratio as follows:

$$O/P = \frac{S Cmol_o \%}{S Cmol_p \% + S Cmol_i \%}$$

The total carbon balance of the system must be $\leq 100\%$ and is calculated as follows:

$$CB\% = \frac{\sum_N F_{N,t} Cmol + F_{CO_2}}{F_0 \times y_{CO} \times f_{CO}\%} \times 100$$

The hydrocarbons' molar rate is then used to calculate the mass rates according to the following equation:

$$W_N = F_{N,t} \times M_N \quad \frac{g}{h}$$

From the mass rates the ASF probability factor α can be calculated from the gradient of the plot between $\log(W_N/N)$ and $(N-1)$ by using single variable regression.