*Electronic Supplementary Information* 

## **Giant Enhancement of Electronic Polarizability and the First Hyperpolarizability of Fluorides-Decorated Graphene** *versus* **Graphyne**

**and Graphdiyne: Insights from Ab Initio Calculations**

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## **Contents:**



## **Calculation of nonlinear optical properties**

The energy of a system is a function of homogeneous electric field, and its Taylor expansion with respect to the field can be expressed as the following equation:<sup>[1]</sup>

$$
E(F) = E^0 - \mu_i F_i - \frac{1}{2} \alpha_{ij} F_i F_j - \frac{1}{6} \beta_{ijk} F_i F_j F_k - \frac{1}{24} \gamma_{ijkl} F_i F_j F_k F_l \cdots
$$
 (1)

where  $E^0$  is the system energy in the absence of an electric field,  $F_i$  is the electric field component along the *i* direction. The  $\mu_i$ ,  $\alpha_{ij}$ , and  $\beta_{ijk}$  terms are the dipole moment, polarizability, and the first hyperpolarizability, respectively, of which *βijk* is recognized as second-order nonlinear optical (NLO) response coefficient.<sup>[2]</sup> The mean dipole moment ( $\mu_0$ ), static polarizability ( $\alpha_0$ ), and the static first hyperpolarizability  $(\beta_{tot})$  are defined as follows:

$$
\mu_0 = (\mu_x^2 + \mu_y^2 + \mu_z^2)^{1/2} \tag{2}
$$

$$
\alpha_0 = (\alpha_{xx} + \alpha_{yy} + \alpha_{zz})/3 \tag{3}
$$

$$
\beta_{\text{tot}} = (\beta_x^2 + \beta_y^2 + \beta_z^2)^{1/2}
$$
 (4)

where 
$$
\beta_i = (1/3) \sum_j (\beta_{ijj} + \beta_{jji} + \beta_{ijj})
$$
  $i, j = \{x, y, z\}$ 

The linear and nonlinear optical properties of these complexes, e.g., polarizability (*α*) and first hyperpolarizability ( $\beta$ ), were calculated by using the long-range corrected CAM-B3LYP functional<sup>[3]</sup> with the all-electron 6-311++ $G(2d, 2p)$  basis sets, because the method has been confirmed to be much reliable for the evaluation of various species.<sup>[4]</sup>



**Figure S1.** Optimized geometries of (a)  $M_3F@GE^{0/+}$ , (b)  $M_3F@GY^{0/+}$ , and (c)  $M_3F@GDY^{0/+}$  (M = Li, Na, and K) complexes. The top and side views are labeled.



Figure S2. Simulated optical absorption spectra of neutral (a) Li<sub>3</sub>F@GDY, (b) Na<sub>3</sub>F@GDY, and (c) K<sub>3</sub>F@GDY complexes using the CAM-B3LYP method. The oscillator strengths of them are inserted.



**Figure S3.** Simulated optical absorption spectra of the cationic (a)  $Li_3F@GDY^+$ , (b)  $Na_3F@GDY^+$ , and (c)  $K_3F@GDY^+$  complexes using the CAM-B3LYP method. The oscillator strengths of them are inserted.

## **References**

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