

Supporting information

KBi(IO₃)₃(OH) and NaBi(IO₃)₄: From Centrosymmetric Chain to Noncentrosymmetric Double Layer

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Table S1. Crystal data and structure refinement for NaBi(IO₃)₄ and KBi(IO₃)₃(OH).

| | | |
|--|---|-------------------------------------|
| Empirical formula | KBi(IO ₃) ₃ (OH) | NaBi(IO ₃) ₄ |
| Formula weight | 789.28 | 931.57 |
| Crystal system | triclinic | monoclinic |
| Space group | <i>P</i> -1 | <i>Cc</i> |
| <i>a</i> /Å | 7.2662(4) | 31.5437(19) |
| <i>b</i> /Å | 8.1678(5) | 5.6122(3) |
| <i>c</i> /Å | 8.8629(5) | 12.7289(8) |
| <i>α</i> /° | 101.6212(10) | 90 |
| <i>β</i> /° | 93.8011(11) | 90.7346(12) |
| <i>γ</i> /° | 109.3178(10) | 90 |
| Volume/Å ³ | 481.16(5) | 2253.2(2) |
| <i>Z</i> | 2 | 8 |
| ρ_{calc} g/cm ³ | 5.448 | 5.492 |
| μ /mm ⁻¹ | 28.417 | 26.709 |
| <i>F</i> (000) | 683.0 | 3216.0 |
| Crystal size/mm ³ | 0.25×0.21×0.15 | 0.3×0.15×0.08 |
| Goodness-of-fit on <i>F</i> ² | 1.180 | 1.074 |
| <i>R</i> ₁ , <i>wR</i> ₂ [<i>I</i> >=2σ(<i>I</i>)] ^a | 0.0170, 0.0488 | 0.0412, 0.0960 |
| all data [<i>I</i> >=2σ(<i>I</i>)] ^a | 0.0171, 0.0489 | 0.0412, 0.0960 |
| Flack parameter | — | 0.4248(14) |

^a $R_1 = \sum ||F_o| - |F_c|| / \sum |F_o|$. $wR_2 = [\sum (F_o^2 - F_c^2)^2 / \sum (F_o^2)^2]^{1/2}$.

Table S2. Selected bond distances (Å) and angles (°) for $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

$\text{KBi}(\text{IO}_3)_3(\text{OH})$

| | | | |
|------------------|------------|------------------|-----------|
| Bi(1)-O(10) | 2.137(3) | I(2)-O(9)#2 | 1.828(4) |
| Bi(1)-O(9) | 2.338(4) | I(3)-O(8) | 1.793(4) |
| Bi(1)-O(1)#1 | 2.351(4) | I(3)-O(7) | 1.820(4) |
| Bi(1)-O(6) | 2.354(4) | I(3)-O(6) | 1.831(4) |
| Bi(1)-O(3) | 2.413(4) | K(1)-O(10)#3 | 2.719(3) |
| Bi(1)-O(8)#2 | 2.457(4) | K(1)-O(1)#7 | 2.758(4) |
| Bi(1)-O(4) | 2.665(4) | K(1)-O(7)#8 | 2.820(4) |
| I(1)-O(3) | 1.828(4) | K(1)-O(8)#8 | 2.951(5) |
| I(1)-O(1) | 1.830(4) | K(1)-O(2)#5 | 2.958(4) |
| I(1)-O(2) | 1.790(4) | K(1)-O(1)#1 | 3.032(4) |
| I(2)-O(4) | 1.805(4) | K(1)-O(4)#1 | 3.051(4) |
| I(2)-O(5) | 1.805(4) | K(1)-O(9)#3 | 3.089(4) |
| O(2)-I(1)-O(3) | 102.15(19) | O(5)-I(2)-O(9)#2 | 99.25(18) |
| O(2)-I(1)-O(1) | 101.27(18) | O(8)-I(3)-O(7) | 96.59(19) |
| O(3)-I(1)-O(1) | 96.23(18) | O(8)-I(3)-O(6) | 95.57(19) |
| O(4)-I(2)-O(5) | 100.99(19) | O(7)-I(3)-O(6) | 96.62(18) |
| O(4)-I(2)-O(9)#2 | 101.45(19) | | |

Symmetry codes:

#1 -x+1, -y, -z #2 -x+1, -y, -z+1 #3 -x, -y, -z #4 x, y, z+1
 #5 -x+1, -y+1, -z #6 x+1, y, z #7 x-1, y, z #8 x, y, z-1

NaBi(IO₃)₄

| | | | |
|---------------|----------|---------------|----------|
| Bi(1)-O(9)#1 | 2.365(5) | Na(2)-O(24)#5 | 2.539(6) |
| Bi(1)-O(8)#2 | 2.388(5) | Na(2)-O(4)#6 | 2.609(6) |
| Bi(1)-O(10)#3 | 2.395(5) | Na(2)-O(13)#5 | 2.904(6) |
| Bi(1)-O(5) | 2.411(5) | I(1)-O(2) | 1.799(5) |
| Bi(1)-O(3) | 2.449(5) | I(1)-O(1) | 1.804(5) |
| Bi(1)-O(12)#3 | 2.470(5) | I(1)-O(3) | 1.825(5) |
| Bi(1)-O(6) | 2.552(5) | I(2)-O(6) | 1.812(5) |
| Bi(1)-O(4) | 2.660(5) | I(2)-O(7) | 1.813(5) |
| Bi(2)-O(15)#2 | 2.319(5) | I(2)-O(8) | 1.839(5) |
| Bi(2)-O(17) | 2.350(5) | I(3)-O(9) | 1.791(5) |
| Bi(2)-O(24)#4 | 2.427(5) | I(3)-O(5) | 1.813(5) |
| Bi(2)-O(19) | 2.429(5) | I(3)-O(10) | 1.826(5) |
| Bi(2)-O(18) | 2.498(5) | I(4)-O(11) | 1.780(5) |
| Bi(2)-O(21)#5 | 2.512(5) | I(4)-O(13) | 1.798(5) |
| Bi(2)-O(14)#3 | 2.523(5) | I(4)-O(4) | 1.830(5) |
| Bi(2)-O(16) | 2.549(5) | I(5)-O(24) | 1.808(5) |
| Na(1)-O(11) | 2.480(7) | I(5)-O(12) | 1.819(5) |
| Na(1)-O(13) | 2.673(6) | I(5)-O(14) | 1.822(5) |
| Na(1)-O(14) | 2.496(6) | I(6)-O(17)#6 | 1.805(5) |
| Na(1)-O(16) | 2.811(7) | I(6)-O(15) | 1.820(5) |
| Na(1)-O(24) | 2.836(6) | I(6)-O(16) | 1.825(5) |

| | | | |
|------------------|----------|--------------------|----------|
| Na(1)-O(15)#2 | 2.374(6) | I(7)-O(23) | 1.785(5) |
| Na(1)-O(21)#8 | 2.609(6) | I(7)-O(22) | 1.804(5) |
| Na(1)-O(17)#8 | 2.744(6) | I(7)-O(18) | 1.809(5) |
| Na(2)-O(10) | 2.518(6) | I(8)-O(20) | 1.802(5) |
| Na(2)-O(11) | 2.355(6) | I(8)-O(21) | 1.818(5) |
| Na(2)-O(14) | 2.463(6) | I(8)-O(19) | 1.823(5) |
| Na(2)-O(12)#5 | 2.516(5) | | |
| O(2)-I(1)-O(1) | 101.3(2) | O(24)-I(5)-O(12) | 91.9(2) |
| O(2)-I(1)-O(3) | 97.2(2) | O(24)-I(5)-O(14) | 95.8(2) |
| O(1)-I(1)-O(3) | 98.2(2) | O(12)-I(5)-O(14) | 99.0(2) |
| O(6)-I(2)-O(7) | 100.3(2) | O(17)#6-I(6)-O(15) | 90.2(2) |
| O(6)-I(2)-O(8) | 98.5(3) | O(17)#6-I(6)-O(16) | 96.5(2) |
| O(7)-I(2)-O(8) | 96.5(2) | O(15)-I(6)-O(16) | 99.3(2) |
| O(9)-I(3)-O(5) | 93.0(2) | O(23)-I(7)-O(22) | 101.7(2) |
| O(9)-I(3)-O(10) | 96.6(2) | O(23)-I(7)-O(18) | 98.7(3) |
| O(5)-I(3)-O(10) | 97.0(2) | O(22)-I(7)-O(18) | 96.6(3) |
| O(11)-I(4)-O(13) | 95.6(3) | O(20)-I(8)-O(21) | 97.6(2) |
| O(11)-I(4)-O(4) | 97.9(3) | O(20)-I(8)-O(19) | 99.2(2) |
| O(13)-I(4)-O(4) | 102.4(2) | O(21)-I(8)-O(19) | 97.4(2) |

Symmetry codes:

#1 x, -y-2, z+1/2 #2 x, y+1, z #3 x, -y-1, z+1/2
#4 x, -y, z+1/2 #5 x, y-1, z #6 x, -y-1, z-1/2
#7 x, -y-2, z-1/2 #8 x, -y, z-1/2

Table S3. Energy-Dispersive Spectrometry (EDS) for $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

$\text{KBi}(\text{IO}_3)_3(\text{OH})$

| Point 1 | | | | Point 2 | | | |
|---------|--------|--------|---------|---|--------|--------|--------|
| Element | Weight | Atomic | Formula | Element | Weight | Atomic | Formul |
| O K | 19.08 | 65.05 | | O K | 15.71 | 59.52 | |
| K K | 4.82 | 6.73 | 1.0 | K K | 5.06 | 7.84 | 1.0 |
| I L | 49.43 | 21.25 | 3.16 | I L | 51.53 | 24.61 | 3.14 |
| Bi M | 26.67 | 6.96 | 1.03 | Bi M | 27.69 | 8.03 | 1.02 |
| Totals | 100 | | | Totals | 100 | | |
| Point 3 | | | | Average ratio: $\text{K}_{1.0}\text{Bi}_{1.0}\text{I}_{3.1}$ | | | |
| Element | Weight | Atomic | Formula | | | | |
| O K | 20.56 | 67.09 | | | | | |
| K K | 4.83 | 6.45 | 1.0 | | | | |
| I L | 48.41 | 19.92 | 3.09 | | | | |
| Bi M | 26.21 | 6.55 | 1.02 | | | | |
| Totals | 100 | | | | | | |

NaBi(IO₃)₄

| Point 1 | | | | Point 2 | | | |
|---------|--------|--------|---------|---------|--------|--------|---------|
| Element | Weight | Atomic | Formula | Element | Weight | Atomic | Formula |
| O K | 22.23 | 69.28 | | O K | 20.59 | 66.93 | |
| Na K | 2.01 | 4.96 | 1.0 | Na K | 2.14 | 4.83 | 1.0 |
| I L | 53.74 | 21.11 | 4.26 | I L | 56.04 | 20.96 | 4.34 |
| Bi M | 22.03 | 5.26 | 1.06 | Bi M | 21.23 | 5.28 | 1.09 |
| Totals | 100 | | | Totals | 100 | | |

| Point 3 | | | |
|---------|--------|--------|---------|
| Element | Weight | Atomic | Formula |
| O K | 21.28 | 67.38 | |
| Na K | 2.48 | 5.47 | 1.0 |
| I L | 55.36 | 22.10 | 4.04 |
| Bi M | 20.88 | 5.06 | 0.93 |
| Totals | 100 | | |

Average ratio:
 $\text{Na}_{1.0}\text{Bi}_{1.03}\text{I}_{4.2}$

Table S4. Dipole moments of IO₃ groups BiO_n (n = 7, 8) polyhedra units for KBi(IO₃)₃(OH) and NaBi(IO₃)₄.

KBi(IO₃)₃(OH)

| Species | x-component | y-component | z -component | total magnitude | debye |
|-----------|-------------|-------------|--------------|---|----------|
| | | | | $\times 10^{-18}$ esu·cm/Å ³ | |
| I(1)O3 | 9.0659 | 7.6012 | 11.4177 | 13.2684 | |
| | 9.0659 | -7.6012 | -11.4177 | 13.2684 | |
| | 0 | 0 | 0 | 0 | 0 |
| I(2)O3 | -13.1435 | -6.6366 | 3.7756 | 13.7845 | |
| | 13.1435 | 6.6366 | -3.7756 | 13.7845 | |
| | 0 | 0 | 0 | 0 | 0 |
| BiO7 | -5.8118 | 3.0999 | -3.1368 | 8.1638 | |
| | 5.8118 | -3.0999 | 3.1368 | 8.1638 | |
| | 0 | 0 | 0 | 0 | 0 |
| Unit cell | | 0 | 0 | 0 | 0 |

NaBi(IO₃)₄

| Species | x- component | y- component | z -component | total magnitude debye ×10⁻¹⁸ | |
|---------|-----------------|-----------------|-----------------|---|---------------|
| I(1)O3 | -0.5591 | 14.3608 | 0.6727 | 14.3877 | |
| | -0.5591 | 14.3608 | 0.6727 | 14.3877 | |
| | -0.5591 | -14.3608 | 0.6727 | 14.3877 | |
| | -0.5591 | -14.3608 | 0.6727 | 14.3877 | |
| | -2.2364 | 0 | 2.6908 | 3.4988 | 0.0016 |
| I(2)O3 | -12.4146 | 6.3674 | -4.5046 | 14.6614 | |
| | -12.4146 | 6.3674 | -4.5046 | 14.6614 | |
| | -12.4146 | -6.3674 | -4.5046 | 14.6614 | |
| | -12.4146 | -6.3674 | -4.5046 | 14.6614 | |
| | -49.6584 | 0 | -18.0184 | 52.8263 | 0.0234 |
| I(3)O3 | -15.5891 | 5.5097 | -0.7776 | 16.5430 | |
| | -15.5891 | -5.5097 | -0.7776 | 16.5430 | |
| | -15.5891 | 5.5097 | -0.7776 | 16.5430 | |
| | -15.5891 | -5.5097 | -0.7776 | 16.5430 | |
| | -62.3564 | 0 | -3.1104 | 62.434 | 0.0277 |
| I(4)O3 | -13.2951 | 4.0339 | 5.5183 | 15.0121 | |
| | -13.2951 | -4.0339 | 5.5183 | 15.0121 | |
| | -13.2951 | -4.0339 | 5.5183 | 15.0121 | |
| | -13.2951 | 4.0339 | 5.5183 | 15.0121 | |
| | -53.1804 | 0 | 22.0732 | 57.5793 | 0.0256 |
| I(5)O3 | -0.6315 | -4.2770 | 15.4451 | 16.0466 | |
| | -0.6315 | 4.2770 | 15.4451 | 16.0466 | |
| | -0.6315 | 4.2770 | 15.4451 | 16.0466 | |
| | -0.6315 | -4.2770 | 15.4451 | 16.0466 | |

| | | | | | |
|-----------|-----------------|----------|----------------|-----------------|---------------|
| | -2.5260 | 0 | 61.7804 | 61.8320 | 0.0274 |
| I(6)O3 | 15.3016 | -6.0531 | -0.5152 | 16.4695 | |
| | 15.3016 | 6.0531 | -0.5152 | 16.4695 | |
| | 15.3016 | -6.0531 | -0.5152 | 16.4695 | |
| | 15.3016 | 6.0531 | -0.5152 | 16.4695 | |
| I(7)O3 | 61.2064 | 0 | -2.0608 | 61.2411 | 0.0272 |
| | 2.7175 | 14.1671 | 2.5253 | 14.6387 | |
| | 2.7175 | 14.1671 | 2.5253 | 14.6387 | |
| | 2.7175 | -14.1671 | 2.5253 | 14.6387 | |
| | 2.7175 | -14.1671 | 2.5253 | 14.6387 | |
| | 10.8700 | 0 | 10.1012 | 14.8388 | 0.0066 |
| I(8)O3 | 12.8470 | 6.5269 | 2.4567 | 14.5902 | |
| | 12.8470 | 6.5269 | 2.4567 | 14.5902 | |
| | 12.8470 | -6.5269 | 2.4567 | 14.5902 | |
| | 12.8470 | -6.5269 | 2.4567 | 14.5902 | |
| | 51.3880 | 0 | 9.8268 | 52.3191 | 0.0232 |
| Bi(1)O8 | -0.8130 | 1.3457 | 1.7533 | 2.3627 | |
| | -0.8130 | -1.3457 | 1.7533 | 2.3627 | |
| | -0.8130 | 1.3457 | 1.7533 | 2.3627 | |
| | -0.8130 | -1.3457 | 1.7533 | 2.3627 | |
| | -3.2520 | 0 | 7.0132 | 7.7305 | 0.0034 |
| Bi(2)O8 | 1.0198 | -1.2673 | -0.0191 | 1.6270 | |
| | 1.0198 | 1.2673 | -0.0191 | 1.6270 | |
| | 1.0198 | -1.2673 | -0.0191 | 1.6270 | |
| | 1.0198 | 1.2673 | -0.0191 | 1.6270 | |
| | 4.0792 | 0 | -0.0764 | 4.0799 | 0.0018 |
| Unit cell | -45.6660 | 0 | 90.2196 | 101.1185 | 0.0449 |

Table S5. Calculation of dipole moment for $\text{NaM}(\text{IO}_3)_4$ ($M = \text{Ce}, \text{Sm}, \text{La}, \text{Eu}, \text{Bi}, \text{Y}$).

| $\text{NaM}(\text{IO}_3)_4$ | Space group | Ionic Radius (M^{3+}) | MO_8 (debye) | Total (debye) | $V/\text{\AA}^3$ | Total ($\text{D}\cdot\text{\AA}^{-3}$) | SHG |
|------------------------------|-------------|---------------------------|-----------------------|---------------|------------------|--|--------------------------------|
| $\text{NaCe}(\text{IO}_3)_4$ | <i>Cc</i> | 1.14 | 0.85–1.34 | 100.39 | 2318.58 | 0.0433 | $50\times\alpha\text{-SiO}_2$ |
| $\text{NaSm}(\text{IO}_3)_4$ | <i>Cc</i> | 1.27 | 0.96–1.60 | 99.01 | 2248.44 | 0.0440 | $60\times\alpha\text{-SiO}_2$ |
| $\text{NaLa}(\text{IO}_3)_4$ | <i>Cc</i> | 1.16 | 1.19–1.75 | 98.38 | 2316.8 | 0.0425 | $120\times\alpha\text{-SiO}_2$ |
| $\text{NaEu}(\text{IO}_3)_4$ | <i>Cc</i> | 1.25 | 1.11–1.62 | 97.69 | 2231.4 | 0.0438 | $130\times\alpha\text{-SiO}_2$ |
| $\text{NaBi}(\text{IO}_3)_4$ | <i>Cc</i> | 1.17 | 1.63–2.33 | 101.11 | 2253.2 | 0.0449 | $5.0\times\text{KDP}$ |
| $\text{NaY}(\text{IO}_3)_4$ | <i>Cc</i> | 1.02 | 0.84–1.61 | 100.46 | 2181.3 | 0.0460 | $400\times\alpha\text{-SiO}_2$ |

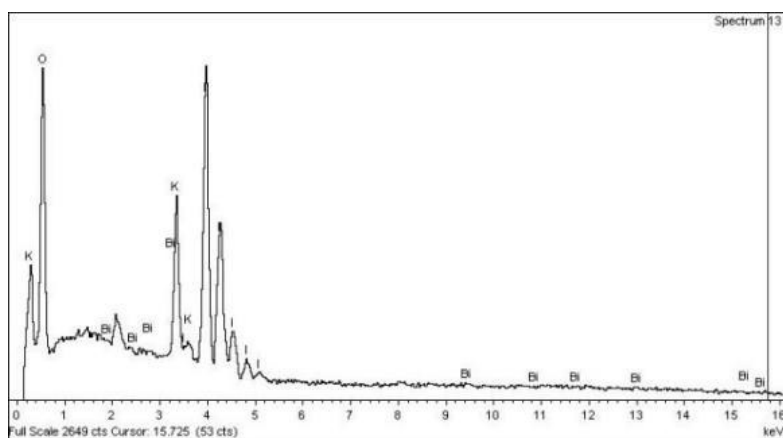


$\text{KBi}(\text{IO}_3)_3(\text{OH})$

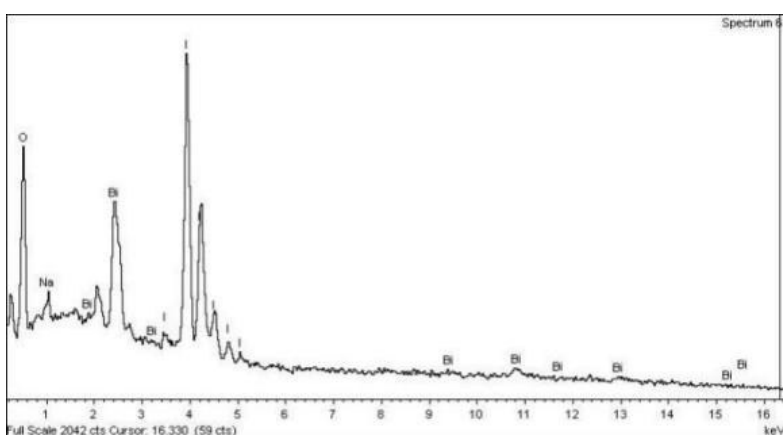


$\text{NaBi}(\text{IO}_3)_4$

Fig. S1. Morphology for $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.



$\text{KBi}(\text{IO}_3)_3(\text{OH})$



$\text{NaBi}(\text{IO}_3)_4$

Fig. S2. Energy-Dispersive Spectrometry (EDS) plot of $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

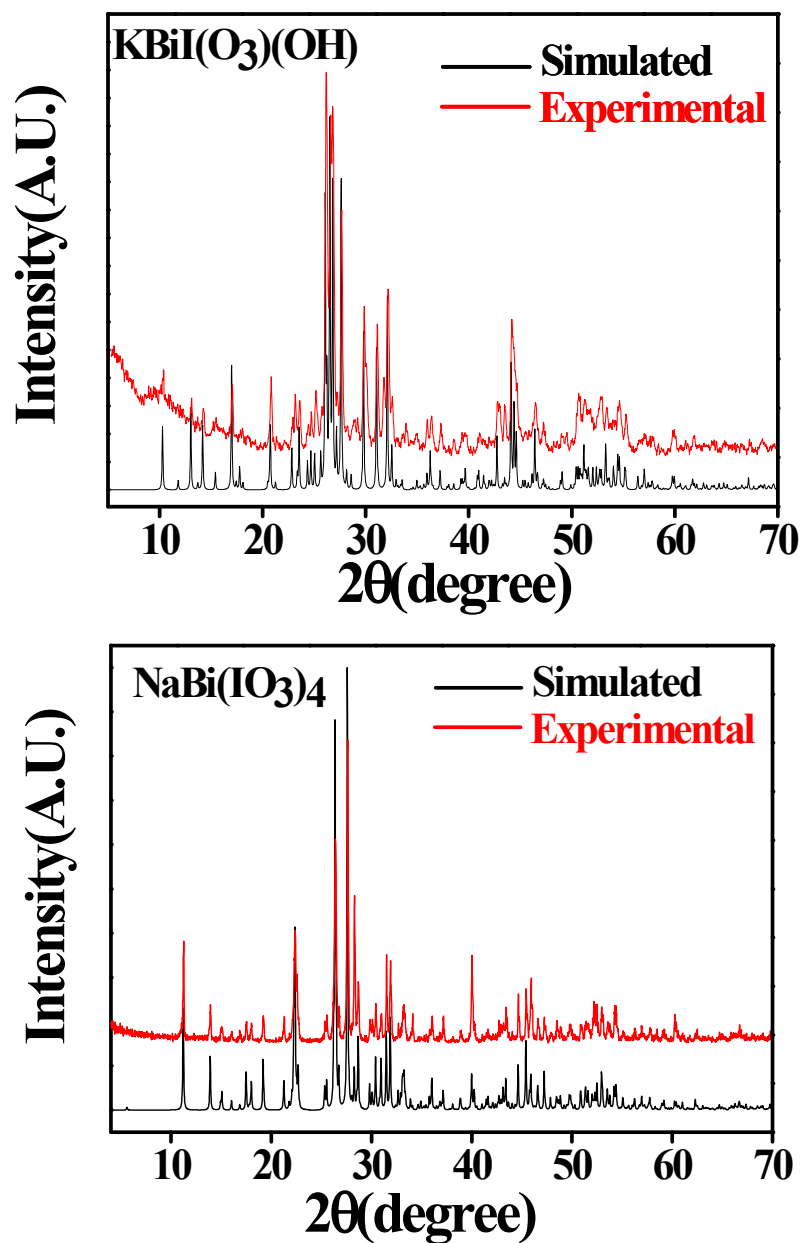


Fig. S3. Experimental and simulated PXRD patterns of $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

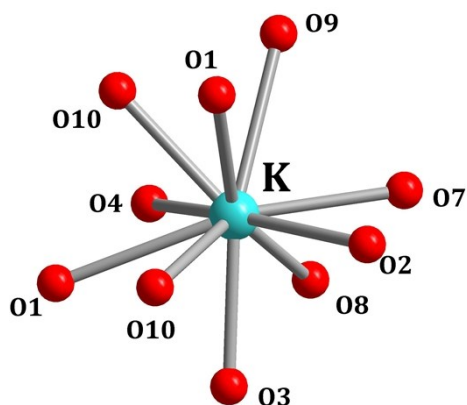


Fig. S4. Coordinate environments of the K^+ in $KBi(IO_3)_3(OH)$.

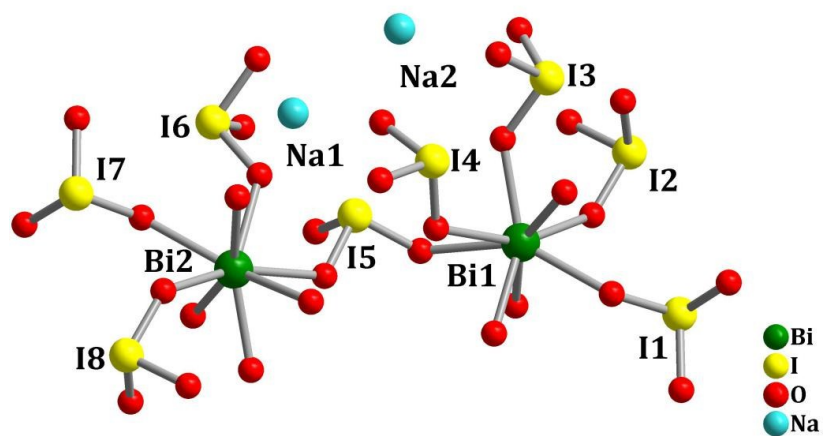


Fig. S5. Asymmetric unit of $NaBi(IO_3)_4$.

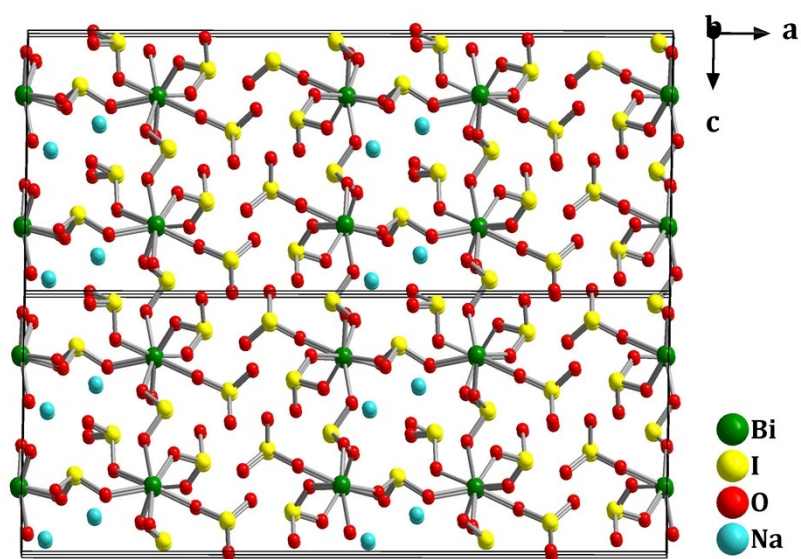


Fig. S6. Structure of $NaBi(IO_3)_4$ along the b -axis.

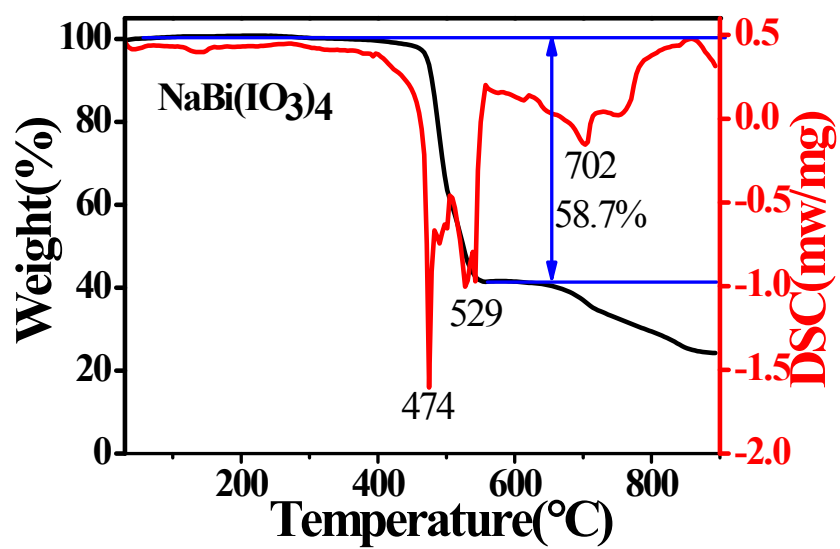
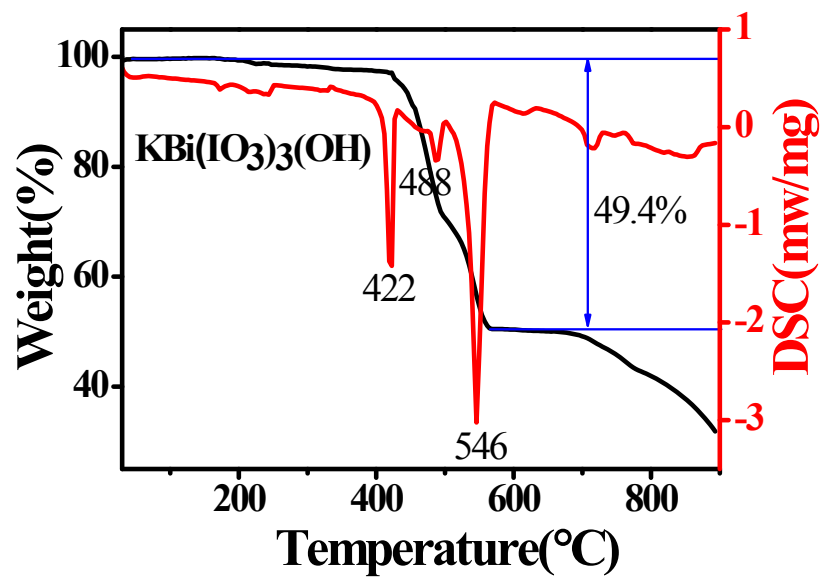


Fig. S7. TGA and DSC curves of $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

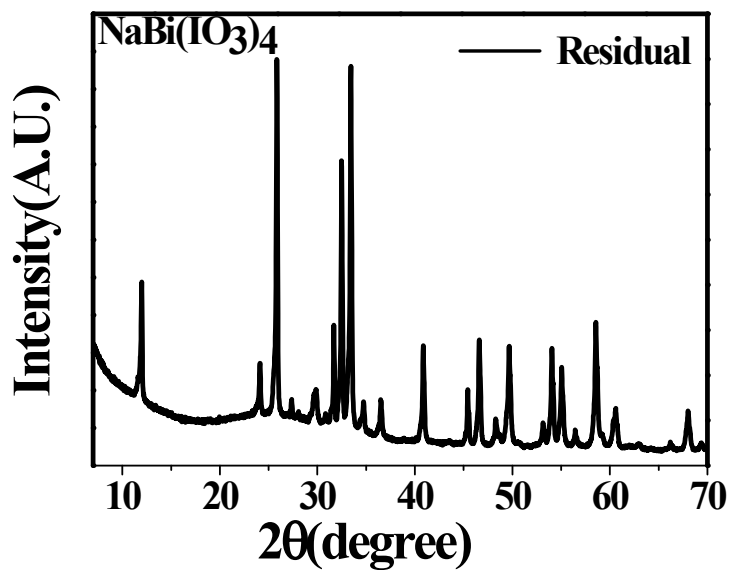
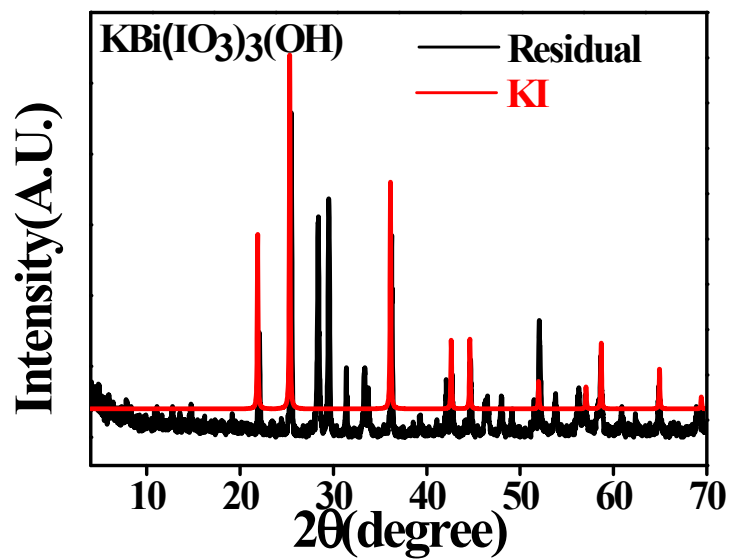


Fig. S8. PXRD patterns for the residual of $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

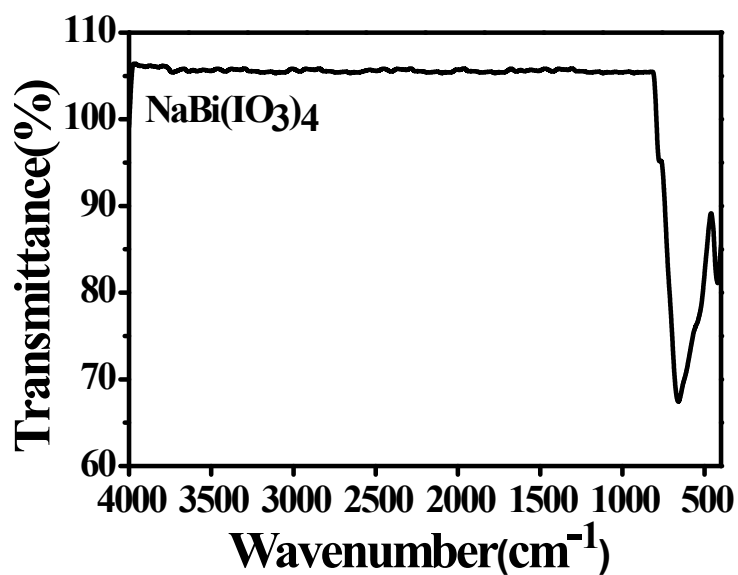
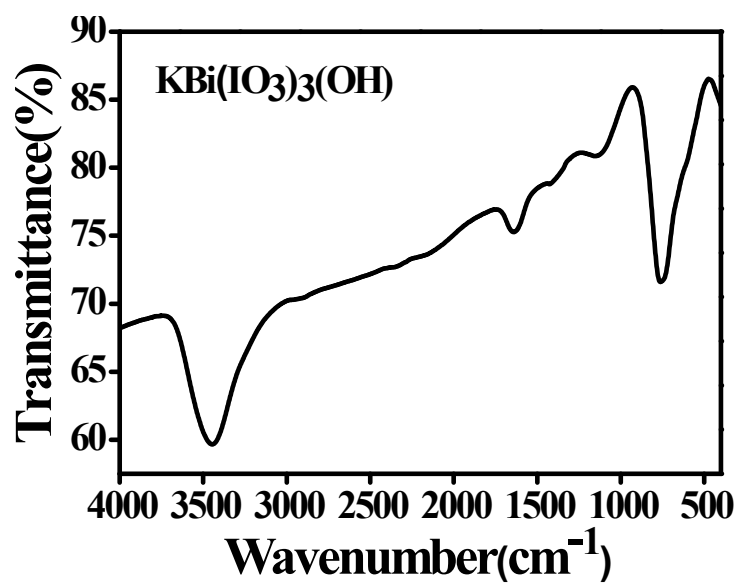


Fig. S9. IR spectrum of $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$.

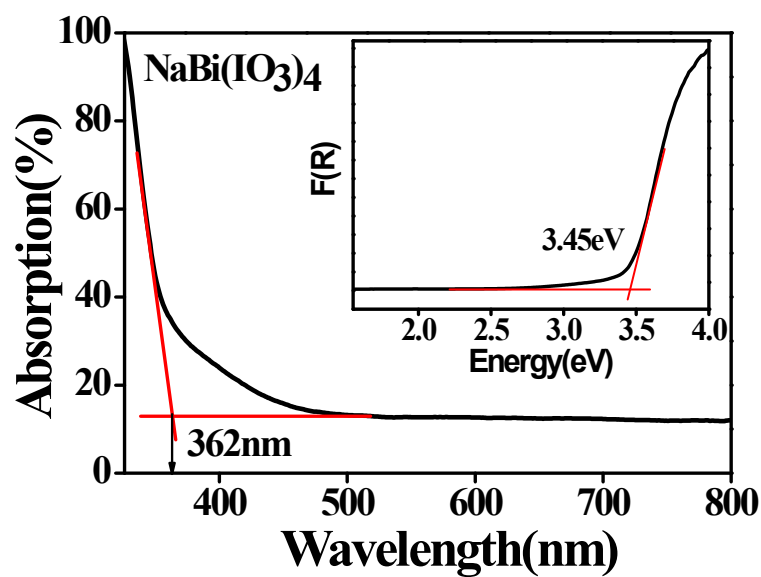
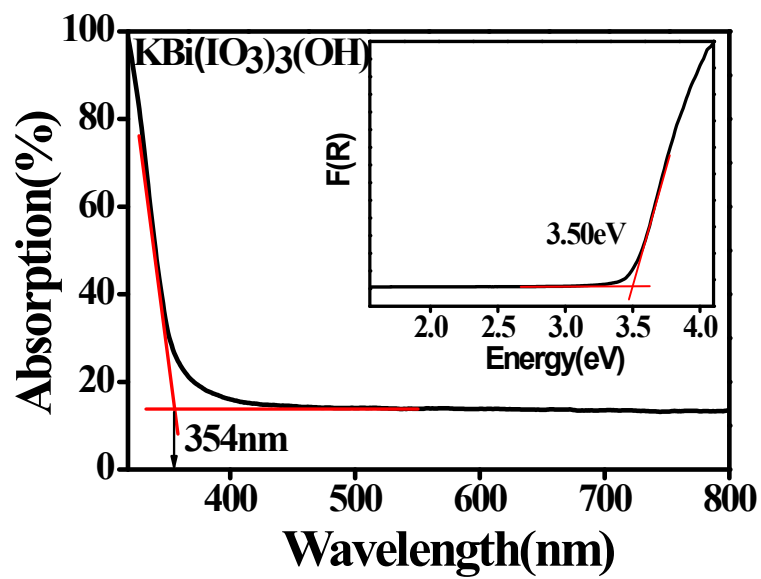
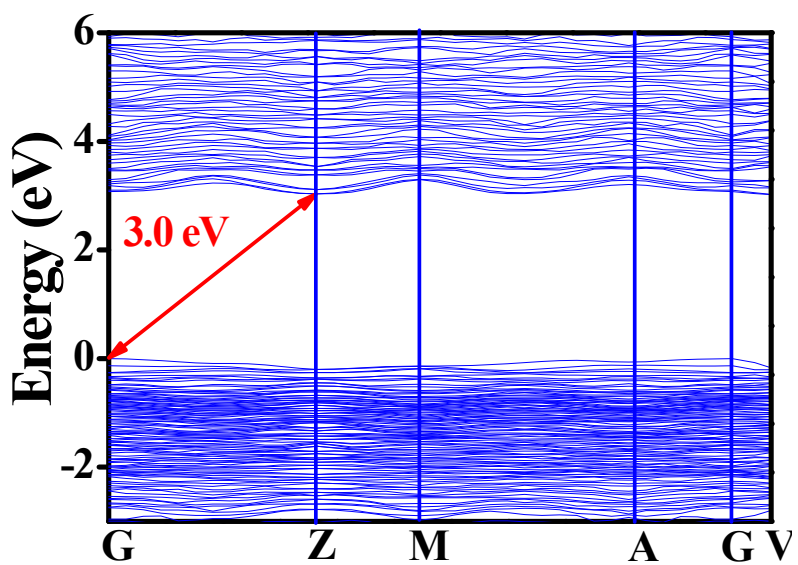
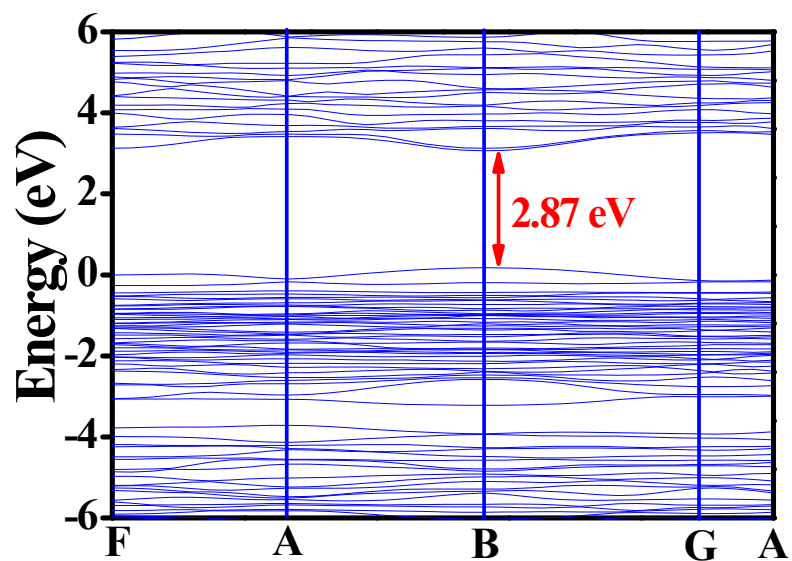


Fig. S10. UV-vis diffuse spectra of $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and $\text{NaBi}(\text{IO}_3)_4$



(a)

(b)

Fig. S11. Calculated band structures of (a) $\text{KBi}(\text{IO}_3)_3(\text{OH})$ and (b) $\text{NaBi}(\text{IO}_3)_4$.

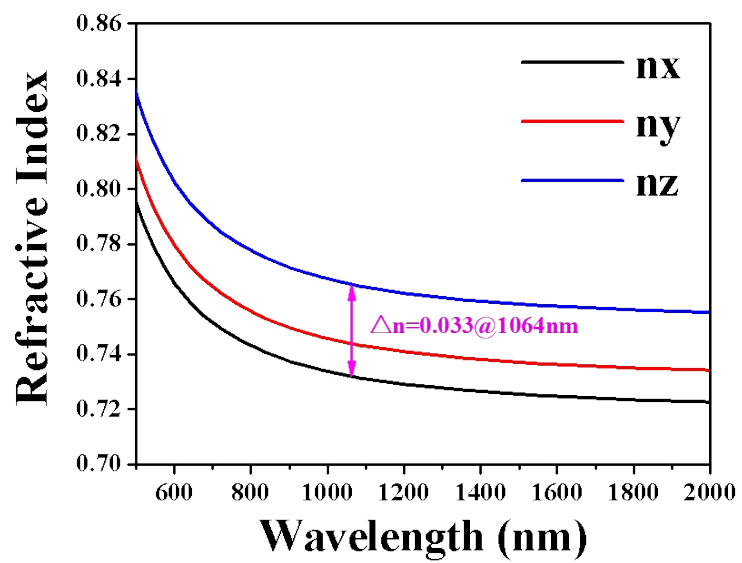


Fig. S12. Calculated refractive indices and birefringence of NaBi(IO₃)₄.