

Electronic supplementary information for:
Energetic and electron density analysis of hydrogen
dissociation of protonated benzene

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1 Nuclear Coordinates, molecular energies and summary of imaginary vibrational frequencies

Nuclear coordinates of the benzenium cation, transition state of 1-2 proton migration, two-fold saddle point, and dissociation products constrained to C_s symmetry: $[C_6H_6]^+ + H$ and $[C_6H_5]^+ + H_2$. Geometry optimizations performed at the MCSCF(6,6)/6-311++G(d,p) level with the GAMESS quantum chemistry program. The geometry optimization criterion was OPTTOL=1.0D-6 except for the partial optimizations during the dissociations which were carried out with OPTTOL=1.0D-5.

In the case of $[C_6H_6]^+ + H$ as dissociation products, one significant and one small imaginary frequencies was obtained for a C1-Ha distance of ca. 10 Å. From this geometry, the system

was further optimized without any symmetry constraint and with explicit Hessian calculation (option HESS=CALC) to yield a true minimum. In the case of $[\text{C}_6\text{H}_5]^+ + \text{H}_2$ at the same C1-Ha separation, unconstrained geometry optimization plus Hessian calculation does not change the molecular geometry.

Table 1: Benzenium cation

| atom | x | y | z |
|------|---------------|---------------|---------------|
| C | -1.2389977479 | 2.1229687044 | -0.0000689141 |
| C | 1.2390093242 | 2.1229508467 | -0.0000652984 |
| C | -1.2500708245 | 0.7570756452 | 0.0000418852 |
| C | 1.2500630450 | 0.7570575339 | 0.0000459073 |
| C | -0.0000096722 | -0.0217378769 | 0.0001060692 |
| C | 0.0000106932 | 2.7942725928 | -0.0001215181 |
| H | -2.1508552001 | 2.6893243222 | -0.0001156048 |
| H | 2.1508743772 | 2.6892943899 | -0.0001091593 |
| H | -0.0000124408 | -0.7068271379 | -0.8551297819 |
| H | -2.1803778243 | 0.2174444422 | 0.0000846788 |
| H | 2.1803632687 | 0.2174147462 | 0.0000914883 |
| H | -0.0000148689 | -0.7066933412 | 0.8554484680 |
| H | 0.0000178714 | 3.8711751325 | -0.0002082200 |

Table 2: Transition state of 1-2 proton migration

| atom | x | y | z |
|------|---------------|---------------|---------------|
| C | -0.7142053861 | 0.0522454765 | 0.0060582971 |
| C | 0.7142060824 | 0.0522454641 | 0.0060576687 |
| C | -1.4203392479 | 1.2917835318 | 0.0031250984 |
| C | 1.4203396651 | 1.2917831874 | 0.0031255695 |
| C | -0.7117080536 | 2.4665207328 | -0.0025378041 |
| C | 0.7117083844 | 2.4665205047 | -0.0025372610 |
| H | -0.0000025435 | -0.0124757368 | 1.0920708089 |
| H | -1.2340685472 | -0.8881089796 | -0.0384772122 |
| H | 1.2340687018 | -0.8881094543 | -0.0384768275 |
| H | -2.4932226625 | 1.2793569655 | -0.0068154219 |
| H | 2.4932230818 | 1.2793568421 | -0.0068135034 |
| H | -1.2351616072 | 3.4044408875 | -0.0073903098 |
| H | 1.2351621325 | 3.4044405783 | -0.0073891026 |

Table 3: Two-fold saddle point

| atom | x | y | z |
|------|---------------|---------------|---------------|
| C | -1.4012471289 | 0.0000006104 | -0.0960944193 |
| C | 1.4012471296 | 0.0000006119 | -0.0960944251 |
| C | -0.7006361957 | -1.2135503875 | -0.0958910763 |
| C | 0.7006362031 | -1.2135503725 | -0.0958910781 |
| C | -0.7006361435 | 1.2135515195 | -0.0958903315 |
| C | 0.7006361697 | 1.2135515139 | -0.0958903420 |
| H | -2.4675362071 | 0.0000000855 | -0.2235092789 |
| H | 2.4675362126 | 0.0000000823 | -0.2235092509 |
| H | -0.0000000783 | -0.0000048125 | -1.1012755562 |
| H | -1.2338126905 | -2.1370258220 | -0.2228705398 |
| H | 1.2338127070 | -2.1370257988 | -0.2228705323 |
| H | -1.2338129227 | 2.1370263830 | -0.2228698898 |
| H | 1.2338129447 | 2.1370263870 | -0.2228698788 |

Table 4: $[\text{C}_6\text{H}_6]^+ + \text{H}$ (dissociation constrained to C_s symmetry)

| atom | x | y | z |
|------|---------------|---------------|---------------|
| C | -1.2416840142 | 1.6896263357 | -1.0621324073 |
| C | 1.2416840142 | 1.6896263357 | -1.0621324073 |
| C | -1.2427831136 | 0.5269009151 | -0.3422838702 |
| C | 1.2427831136 | 0.5269009151 | -0.3422838702 |
| C | 0.0000000000 | -0.0606761497 | 0.0214727805 |
| C | 0.0000000000 | 2.2846923910 | -1.4304707809 |
| H | -2.1619288916 | 2.1597254346 | -1.3531921172 |
| H | 2.1619288916 | 2.1597254346 | -1.3531921172 |
| H | 0.0000000000 | -7.7541567843 | -7.8269720491 |
| H | -2.1567200793 | 0.0477954876 | -0.0457375813 |
| H | 2.1567200793 | 0.0477954876 | -0.0457375813 |
| H | 0.0000000000 | -0.9760643215 | 0.5880671347 |
| H | 0.0000000000 | 3.1982269410 | -1.9959660781 |

Table 5: $[\text{C}_6\text{H}_6]^+ + \text{H}$ (unconstrained optimization using coordinates of Table 4 as initial

| geometry) | | | |
|-----------|---------------|---------------|---------------|
| atom | x | y | z |
| C | -1.2407619955 | 1.6889026901 | -1.0873135371 |
| C | 1.2378659093 | 1.6637550904 | -1.0653269266 |
| C | -1.2271566172 | 0.5140447015 | -0.3624959315 |
| C | 1.2510122625 | 0.5022284272 | -0.3487342456 |
| C | 0.0113355665 | -0.0822730718 | 0.0086124160 |
| C | -0.0228974066 | 2.2712544412 | -1.4433935321 |
| H | -2.1688381217 | 2.1463904993 | -1.3719662320 |
| H | 2.1528696067 | 2.1432823938 | -1.3587637695 |
| H | -0.0049140492 | -7.5574223599 | -7.6644977055 |
| H | -2.1425940187 | 0.0335672253 | -0.0684753982 |
| H | 2.1676880838 | 0.0287803279 | -0.0542656528 |
| H | -0.0045418615 | -0.9980513928 | 0.5735221277 |
| H | -0.0090673584 | 3.1856594500 | -2.0074625577 |

Table 6: $[\text{C}_6\text{H}_5]^+ + \text{H}_2$

| atom | x | y | z |
|------|---------------|----------------|---------------|
| C | -1.2219189945 | 1.7342175324 | 0.0428557658 |
| C | 1.2219189945 | 1.7342175324 | 0.0428557658 |
| C | -1.2783445363 | 0.3095345544 | 0.0258818358 |
| C | 1.2783445363 | 0.3095345544 | 0.0258818358 |
| C | 0.0000000000 | -0.0606761497 | 0.0214727805 |
| C | 0.0000000000 | 2.4139420237 | 0.0509542076 |
| H | -2.1592317915 | 2.2592773863 | 0.0491109889 |
| H | 2.1592317915 | 2.2592773863 | 0.0491109889 |
| H | 0.0000000000 | -10.6841567843 | -0.2754062473 |
| H | -2.1661953586 | -0.2901638524 | 0.0187359356 |
| H | 2.1661953586 | -0.2901638524 | 0.0187359356 |
| H | 0.0000000000 | -10.6671702003 | 0.4598359972 |
| H | 0.0000000000 | 3.4868410319 | 0.0637369721 |

Table 7: MCSCF and MRMP2 molecular energies (in a.u.) and imaginary vibrational frequency magnitudes (in cm^{-1}).

| Molecule | MCSCF energy | MCSCF Imaginary frequency | MRMP2 energy |
|---|-----------------|---------------------------|-----------------|
| $[\text{C}_6\text{H}_7]^+$ | -231.1200862920 | — | -231.8689858764 |
| TS 1-2 mig | -231.1013074788 | 568.54 | -231.8538407563 |
| two-fold saddle | -231.0125220925 | 2082.72, 2081.53 | -231.7891051390 |
| C_s constrained $[\text{C}_6\text{H}_6]^+ + \text{H}$ | -231.0053514045 | 378.03 , 13.10 | -231.7409779789 |
| unconstrained $[\text{C}_6\text{H}_6]^+ + \text{H}$ | -231.0054146686 | — | -231.7406383582 |
| $[\text{C}_6\text{H}_5]^+ + \text{H}_2$ | -231.0133268418 | — | -231.7536547583 |

2 Topological properties of the electron density

This section contains:

1. Atomic charge, energy and localization index defined as $\lambda(A) = \delta(A,A)$. For pairs of atoms: delocalization index $\delta(A,B)$
2. Electron density and its Laplacian at bond critical points of $\rho(r)$.

Values for non equivalent atoms or pairs of atoms are reported. The atomic labels are the same as in Scheme 1 of the paper.

In addition:

3. Electron density profiles along the C_6 axis of the molecular graphs of Figure 2(b) of the paper.

Table 8: Atomic properties for benzenium

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C1 | 0.056 | -37.816 | 3.903 |
| C2 | 0.003 | -37.878 | 4.106 |
| C3 | 0.123 | -37.802 | 3.974 |
| C4 | -0.025 | -37.897 | 4.127 |
| Ha | 0.113 | -0.562 | 0.364 |
| H2 | 0.099 | -0.584 | 0.373 |
| H3 | 0.089 | -0.587 | 0.379 |
| H4 | 0.113 | -0.580 | 0.365 |

Table 9: Delocalization index and properties at bcp for benzenium

| A-B | ρ_b | $\delta(A,B)$ | $\nabla^2\rho_b$ |
|-------|----------|---------------|------------------|
| C1-C2 | 0.282 | 1.052 | -0.836 |
| C2-C3 | 0.337 | 1.395 | -1.103 |
| C3-C4 | 0.315 | 1.242 | -1.007 |
| C1-Ha | 0.273 | 0.891 | -0.962 |
| C2-H2 | 0.300 | 0.954 | -1.155 |
| C3-H3 | 0.298 | 0.952 | -1.133 |
| C4-H4 | 0.303 | 0.949 | -1.185 |

Table 10: Atomic properties for 1-2 proton migration TS

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C1 | -0.049 | -37.905 | 4.094 |
| C3 | 0.087 | -37.814 | 4.027 |
| C4 | 0.062 | -37.834 | 4.041 |
| H2 | 0.133 | -0.568 | 0.347 |
| H3 | 0.093 | -0.585 | 0.375 |
| H4 | 0.086 | -0.589 | 0.382 |
| Ha | 0.174 | -0.508 | 0.290 |

Table 11: Delocalization index and properties at bcp for 1-2 proton migration TS

| A-B | ρ_b | $\delta(A,B)$ | $\nabla^2\rho_b$ |
|------------|----------|---------------|------------------|
| C1-C2 | 0.292 | 1.066 | -0.824 7 |
| C2-C3 | 0.302 | 1.167 | -0.942 |
| C3-C4 | 0.332 | 1.370 | -1.069 |
| C4-C5 | 0.306 | 1.197 | -0.946 |
| C1-Hb | 0.300 | 0.934 | -1.160 |
| C3-H3 | 0.298 | 0.955 | -1.134 |
| C4-H4 | 0.299 | 0.957 | -1.143 |
| C1-Ha | — | 0.478 | — |
| (C1-C2)-Ha | 0.189 | — | -0.257 |

Table 12: Atomic properties for $[\text{C}_6\text{H}_6]^+ + \text{H}$ (dissociation constrained to C_s symmetry)

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C1 | -0.015 | -37.888 | 4.136 |
| C2 | 0.082 | -37.821 | 3.992 |
| C3 | 0.090 | -37.821 | 4.020 |
| C4 | 0.018 | -37.855 | 4.175 |
| Hb | 0.134 | -0.570 | 0.349 |
| H2 | 0.106 | -0.580 | 0.367 |
| H3 | 0.099 | -0.583 | 3.725 |
| H4 | 0.110 | -0.580 | 0.364 |
| Ha | 0.000 | -0.500 | 1.000 |

Table 13: Delocalization index and properties at bcp for $[\text{C}_6\text{H}_6]^+ + \text{H}$ (dissociation constrained

| to C_s symmetry) | | | |
|--------------------|----------|---------------|------------------|
| A-B | ρ_b | $\delta(A,B)$ | $\nabla^2\rho_b$ |
| C1-C2 | 0.309 | 1.270 | -0.985 |
| C2-C3 | 0.337 | 1.386 | -1.098 |
| C3-C4 | 0.306 | 1.202 | -0.953 |
| C1-Ha | 0.304 | 0.943 | -1.195 |
| C2-H2 | 0.299 | 0.949 | -1.149 |
| C3-H3 | 0.299 | 0.953 | -1.145 |
| C4-H4 | 0.301 | 0.958 | -1.164 |
| C1-Hb | 0.000 | 0.000 | 0.000 |

Table 14: Atomic properties for the asymmetric $[\text{C}_6\text{H}_6]^+ + \text{H}$ (unconstrained optimization using

coordinates of Table 4 as initial geometry)

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C1 | -0.005 | -37.879 | 4.125 |
| C2 | 0.118 | -37.801 | 3.976 |
| C3 | 0.056 | -37.841 | 4.073 |
| C4 | 0.020 | -37.857 | 4.159 |
| C5 | 0.122 | -37.800 | 3.974 |
| C6 | 0.037 | -37.851 | 4.034 |
| Hb | 0.130 | -0.572 | 0.351 |
| H2 | 0.097 | -0.583 | 0.373 |
| H3 | 0.101 | -0.583 | 0.371 |
| H4 | 0.109 | -0.580 | 0.365 |
| H5 | 0.097 | -0.583 | 0.373 |
| H6 | 0.117 | -0.576 | 0.359 |
| Ha | 0.000 | -0.500 | 1.000 |

Table 15: Delocalization index and properties at bcp for the asymmetric $[\text{C}_6\text{H}_6]^+ \text{H}$
(unconstrained optimization using coordinates of Table 4 as initial geometry)

| A-B | ρ_b | $\delta(\text{A,B})$ | $\nabla^2\rho_b$ |
|-------|----------|----------------------|------------------|
| C1-C2 | 0.310 | 1.243 | -0.990 |
| C2-C3 | 0.337 | 1.390 | -1.100 |
| C3-C4 | 0.294 | 1.145 | -0.897 |
| C4-C5 | 0.321 | 1.284 | -1.024 |
| C5-C6 | 0.330 | 1.350 | -1.075 |
| C6-C1 | 0.311 | 1.301 | -0.984 |
| C1-Hb | 0.303 | 0.945 | -1.189 |
| C2-H2 | 0.298 | 0.952 | -1.136 |
| C3-H3 | 0.300 | 0.955 | -1.151 |
| C4-H4 | 0.301 | 0.957 | -1.164 |
| C5-H5 | 0.298 | 0.951 | -1.139 |
| C6-H6 | 0.301 | 0.946 | -1.169 |
| C1-Ha | 0.000 | 0.000 | 0.000 |

Table 16: Atomic properties for $[\text{C}_6\text{H}_5]^+ + \text{H}_2$

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C1 | -0.563 | -38.396 | 4.979 |
| C2 | 0.282 | -37.674 | 3.933 |
| C3 | 0.081 | -37.780 | 4.050 |
| C4 | 0.112 | -37.789 | 4.001 |
| Ha | 0.000 | -0.564 | 0.500 |
| H2 | 0.198 | -0.529 | 0.298 |
| H3 | 0.117 | -0.574 | 0.357 |
| H4 | 0.094 | -0.585 | 0.375 |

Table 17: Delocalization index and properties at bcp for $[\text{C}_6\text{H}_5]^+ + \text{H}_2$

| A-B | ρ_b | $\delta(\text{A,B})$ | $\nabla^2\rho_b$ |
|------------|----------|----------------------|------------------|
| C1-C2 | 0.333 | 1.306 | -0.807 |
| C2-C3 | 0.287 | 1.160 | -0.821 |
| C3-C4 | 0.317 | 1.285 | -0.984 |
| C1-Ha | — | 0.000 | — |
| C2-H2 | 0.293 | 0.902 | -1.125 |
| C3-H3 | 0.297 | 0.941 | -1.127 |
| C4-H4 | 0.298 | 0.953 | -1.134 |
| Ha-Hb | 0.266 | 1.000 | -1.120 |
| (Ha-Hb)-C1 | 0.000 | — | 0.000 |

Table 18: Atomic properties for the two-fold saddle point

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C | -0.020 | -37.870 | 4.055 |
| H | 0.109 | -0.578 | 0.364 |
| Ha | 0.463 | -0.321 | 0.169 |

Table 19: Delocalization index and properties at bcp for the two-fold saddle point

| A-B | ρ_b | $\delta(A,B)$ | $\nabla^2\rho_b$ |
|------|----------|---------------|------------------|
| C-C | 0.316 | 1.277 | -0.9813 |
| C-H | 0.299 | 0.947 | -1.149 |
| C-Ha | 0.066 | 0.121 | 0.064 |

Table 20: Atomic properties for benzene

| Atom | Charge | Energy | Localization index |
|------|--------|---------|--------------------|
| C | 0.016 | -37.840 | 4.068 |
| H | -0.016 | -0.631 | 0.462 |

Table 21: Delocalization index and properties at bcp for benzene

| A-B | ρ_b | $\delta(A,B)$ | $\nabla^2\rho_b$ |
|-----|----------|---------------|------------------|
| C-C | 0.318 | 1.287 | -0.991 |
| C-H | 0.292 | 0.987 | -1.085 |

The electron density profiles along the C_6 axis of each of the molecular graphs of Figure 2(b) of the manuscript are shown below. It can be seen that for the structurally stable molecule **1-2S** the electron density decreases monotonically from the H atom towards the aromatic ring and to infinity. It also shows how the bifurcation mechanism operates as the H atom is removed along the C_6 axis: in (b) a degenerate critical point appears to suddenly bifurcate into a ring and a cage critical points in (c).

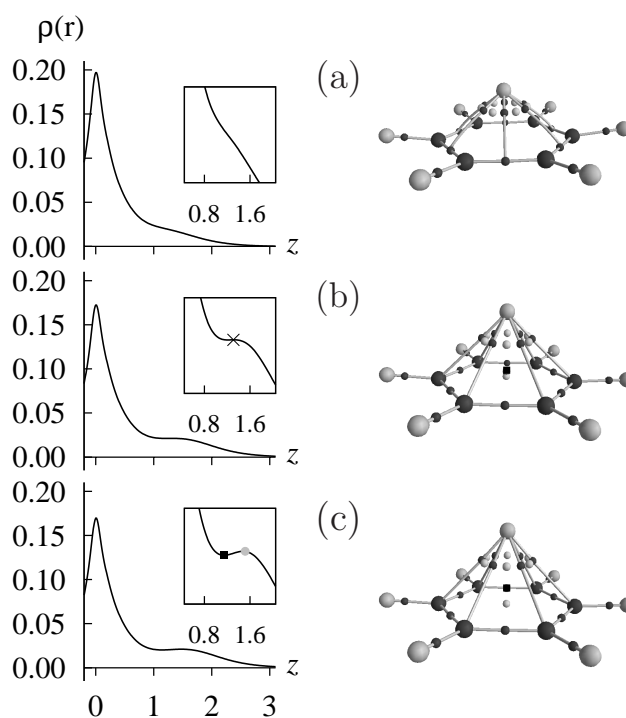


Figure 1: Electron density profiles along the C_6 axis of selected molecular graphs showing the bifurcation mechanism of **1-2S**. In each case the origin is located at the position of the migrating H atom and the z axis is oriented towards the ring of C atoms. The stable critical points are denoted as in Figure 2 and \times refers to the approximate position of the unstable critical point in the inset of (b). Distances are in Å