Formation Mechanism and Twist-angle Dependent Optical Properties of Bilayer MoS $\mathbf{M}_{\mathbf{2}}$ Grown by Chemical Vapor Deposition<br>Jinglei Han, ${ }^{\mathrm{a}} \mathrm{Fa} \mathrm{Cao}^{\mathrm{a}}$ and Xiaohong Ji*a

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Fig. S1. The stacking configurations with twist angles of (a) $0^{\circ}$ (with the nucleation sites of top layers moving along $0^{\circ}, 30^{\circ}$ and $60^{\circ}$ direction relative to that of the bottom layers), (b) $30^{\circ}$ (with the nucleation sites of top layers moving along $0^{\circ}, 30^{\circ}, 60^{\circ}, 90^{\circ}$ and $120^{\circ}$ direction relative to that of the bottom layers) and (c) $60^{\circ}$ (along $0^{\circ}, 30^{\circ}$ and $60^{\circ}$ direction relative to that of the bottom layers) simulated in our study, regardless of the temperature.

(c)


Fig. S2. The corresponding stacking configurations with twist angles of (a) $0^{\circ}$, (b) $30^{\circ}$ and (c) $60^{\circ}$ after fully relaxed at 300 K .
(a)

(b)

$0^{\circ}$



Fig. S3. The corresponding stacking configurations with twist angles of (a) $0^{\circ}$, (b) $30^{\circ}$ and (c) $60^{\circ}$ after fully relaxed at 0.3 K .

Table S1 $0^{\circ}$ stacking configurations simulated in our study at minimized state, 300 K and 0.3 K .

| $0^{\circ}$ stacking configurations | Minimized state | 300 K | 0.3 K |
| :---: | :---: | :---: | :---: |
| Structure 1 (along $0^{\circ}$ direction) | $A B$ stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 2 (along $0^{\circ}$ direction) | $A B$ stacking | $t w i s t e d$ | twisted |
| Structure 3 (along $0^{\circ}$ direction) | $A B$ stacking | $A B^{\prime \prime}$ | $A B^{\prime \prime}$ |
| Structure 4 (along $0^{\circ}$ direction) | $A B$ stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 5 (along $0^{\circ}$ direction) | $A B$ stacking | twisted | twisted |
| Structure 2 (along $30^{\circ}$ direction) | $A B$ stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 3 (along $30^{\circ}$ direction) | $A B$ stacking | twisted | twisted |
| Structure 2 (along $60^{\circ}$ direction) | $A B$ stacking | $t w i s t e d$ | $t w i s t e d$ |
| Structure 3 (along $60^{\circ}$ direction) | $A B$ stacking | $A B^{\prime \prime}$ | $A B^{\prime \prime}$ |
| Structure 4 (along $60^{\circ}$ direction) | $A B$ stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 5 (along $60^{\circ}$ direction) | $A B$ stacking | $A B^{\prime \prime}$ | $A B^{\prime \prime}$ |

Table S2 $30^{\circ}$ stacking configurations simulated in our study at minimized state, 300 K and 0.3 K .

| $30^{\circ}$ stacking configurations | Minimized state | 300 K | 0.3 K |
| :---: | :---: | :---: | :---: |
| Structure 1 (along $0^{\circ}$ direction) | AC stacking | twisted | twisted |
| Structure 2 (along $0^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 3 (along $0^{\circ}$ direction) | AC stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 4 (along $0^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 5 (along $0^{\circ}$ direction) | AC stacking | $A A^{\prime \prime}$ | $A A^{\prime \prime}$ |
| Structure 2 (along $30^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 3 (along $30^{\circ}$ direction) | AC stacking | $A A^{\prime \prime}$ | $A A^{\prime \prime}$ |
| Structure 2 (along 60 ${ }^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 3 (along $60^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 4 (along 60 ${ }^{\circ}$ direction) | AC stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 5 (along 60 ${ }^{\circ}$ direction) | AC stacking | twisted | twisted |
| Structure 2 (along $90^{\circ}$ direction) | AC stacking | twisted | twisted |
| Structure 3 (along 90 ${ }^{\circ}$ direction) | AC stacking | twisted | twisted |
| Structure 2 (along $120^{\circ}$ direction) | AC stacking | $A B^{\prime}$ | $A B^{\prime}$ |
| Structure 3 (along $120^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 4 (along $120^{\circ}$ direction) | AC stacking | $A A^{\prime}$ | $A A^{\prime}$ |
| Structure 5 (along $120^{\circ}$ direction) | AC stacking | $A B^{\prime}$ | $A B^{\prime}$ |

Table S3 $60^{\circ}$ stacking configurations simulated in our study at minimized state, 300 K and 0.3 K .

| $60^{\circ}$ stacking configurations | Minimized state | 300 K | 0.3 K |
| :---: | :---: | :---: | :---: |
| Structure 1 (along $0^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 2 (along $0^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 3 (along $0^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 4 (along $0^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 5 (along $0^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 2 (along $30^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA}^{\prime \prime}$ stacking | $\mathrm{AA}^{\prime \prime}$ stacking |
| Structure 3 (along $30^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA} A^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 2 (along $60^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | twisted | twisted |
| Structure 3 (along $60^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | twisted | twisted |
| Structure 4 (along $60^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA} A^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |
| Structure 5 (along $60^{\circ}$ direction) | $\mathrm{AA}^{\prime}$ stacking | $\mathrm{AA} A^{\prime}$ stacking | $\mathrm{AA}^{\prime}$ stacking |

