## Formation Mechanism and Twist-angle Dependent Optical Properties of Bilayer MoS<sub>2</sub> Grown by Chemical Vapor Deposition

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**Fig. S1.** The stacking configurations with twist angles of  $(a)0^{\circ}$  (with the nucleation sites of top layers moving along 0°, 30° and 60° direction relative to that of the bottom layers), (b)30° (with the nucleation sites of top layers moving along 0°, 30°, 60°, 90° and 120° direction relative to that of the bottom layers) and (c)60° (along 0°, 30° and 60° direction relative to that of the bottom layers) simulated in our study, regardless of the temperature.





**Fig. S2.** The corresponding stacking configurations with twist angles of (a)  $0^{\circ}$ , (b)  $30^{\circ}$  and (c)  $60^{\circ}$  after fully relaxed at 300 K.





**Fig. S3.** The corresponding stacking configurations with twist angles of (a)  $0^{\circ}$ , (b)  $30^{\circ}$  and (c)  $60^{\circ}$  after fully relaxed at 0.3 K.

| Tuble S1 0 Stacking comparations simulated in our study at minimized state, soo k and 0.5 k. |  |   |  |  |  |  |
|--|--|---|--|--|--|--|
| Minimized state  | 300 K  | 0.3 K   |  |  |  |  |
| AB stacking  | AB'  | AB'   |  |  |  |  |
| AB stacking  | twisted  | twisted   |  |  |  |  |
| AB stacking  | AB"  | AB''  |  |  |  |  |
| AB stacking  | AB'  | AB'   |  |  |  |  |
| AB stacking  | twisted  | twisted   |  |  |  |  |
| AB stacking  | AB'  | AB'   |  |  |  |  |
| AB stacking  | twisted  | twisted   |  |  |  |  |
| AB stacking  | twisted  | twisted   |  |  |  |  |
| AB stacking  | AB"  | AB''  |  |  |  |  |
| AB stacking  | AB'  | AB'   |  |  |  |  |
| AB stacking  | AB"  | AB''  |  |  |  |  |
|  | Minimized state<br>AB stacking<br>AB stacking | Minimized state300 KAB stackingAB'AB stackingtwistedAB stackingAB''AB stackingAB'AB stackingtwistedAB stackingtwistedAB stackingAB'AB stackingtwistedAB stackingtwistedAB stackingtwistedAB stackingtwistedAB stackingtwistedAB stackingAB''AB stackingAB''AB stackingAB''AB stackingAB''AB stackingAB''AB stackingAB''AB stackingAB''AB stackingAB'' |  |  |  |  |

 Table S1 0° stacking configurations simulated in our study at minimized state, 300 K and 0.3 K.

| 5 5                                |                 | ,       | ·       |  |
|------------------------------------|-----------------|---------|---------|--|
| 30° stacking configurations        | Minimized state | 300 K   | 0.3 K   |  |
| Structure 1 (along 0° direction)   | AC stacking     | twisted | twisted |  |
| Structure 2 (along 0° direction)   | AC stacking     | AA'     | AA'     |  |
| Structure 3 (along 0° direction)   | AC stacking     | AB'     | AB'     |  |
| Structure 4 (along 0° direction)   | AC stacking     | AA'     | AA'     |  |
| Structure 5 (along 0° direction)   | AC stacking     | AA''    | AA"     |  |
| Structure 2 (along 30° direction)  | AC stacking     | AA'     | AA'     |  |
| Structure 3 (along 30° direction)  | AC stacking     | AA"     | AA"     |  |
| Structure 2 (along 60° direction)  | AC stacking     | AA'     | AA'     |  |
| Structure 3 (along 60° direction)  | AC stacking     | AA'     | AA'     |  |
| Structure 4 (along 60° direction)  | AC stacking     | AB'     | AB'     |  |
| Structure 5 (along 60° direction)  | AC stacking     | twisted | twisted |  |
| Structure 2 (along 90° direction)  | AC stacking     | twisted | twisted |  |
| Structure 3 (along 90° direction)  | AC stacking     | twisted | twisted |  |
| Structure 2 (along 120° direction) | AC stacking     | AB'     | AB'     |  |
| Structure 3 (along 120° direction) | AC stacking     | AA'     | AA'     |  |
| Structure 4 (along 120° direction) | AC stacking     | AA'     | AA'     |  |
| Structure 5 (along 120° direction) | AC stacking     | AB'     | AB'     |  |

 Table S2 30° stacking configurations simulated in our study at minimized state, 300 K and 0.3 K.

| 60° stacking configurations       | Minimized state | 300 K        | 0.3 K        |  |
|-----------------------------------|-----------------|--------------|--------------|--|
| Structure 1 (along 0° direction)  | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 2 (along 0° direction)  | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 3 (along 0° direction)  | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 4 (along 0° direction)  | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 5 (along 0° direction)  | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 2 (along 30° direction) | AA' stacking    | AA" stacking | AA" stacking |  |
| Structure 3 (along 30° direction) | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 2 (along 60° direction) | AA' stacking    | twisted      | twisted      |  |
| Structure 3 (along 60° direction) | AA' stacking    | twisted      | twisted      |  |
| Structure 4 (along 60° direction) | AA' stacking    | AA' stacking | AA' stacking |  |
| Structure 5 (along 60° direction) | AA' stacking    | AA' stacking | AA' stacking |  |
|                                   |                 |              |              |  |

 Table S3 60° stacking configurations simulated in our study at minimized state, 300 K and 0.3 K.