## **Electronic Supplementary Information (ESI)**

## Motional freedom of dimethylammonium ions in a cyanoelpasolite [(CH<sub>3</sub>)<sub>2</sub>NH<sub>2</sub>]<sub>2</sub>KCo(CN)<sub>6</sub> which exhibit phase transition associated with a distinct change of dielectric property

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## Contents

**Fig. S1** Powder X-ray diffraction of [(CH<sub>3</sub>)<sub>2</sub>NH<sub>2</sub>]<sub>2</sub>KCo(CN)<sub>6</sub> by Cu Kα radiation.

**Fig. S2** Powder X-ray diffraction of [(CD<sub>3</sub>)<sub>2</sub>NH<sub>2</sub>]<sub>2</sub>KCo(CN)<sub>6</sub> by Cu Kα radiation.

**Fig. S3** Powder X-ray diffraction of [(CH<sub>3</sub>)<sub>2</sub>NH<sub>2</sub>]<sub>2</sub>KCr(CN)<sub>6</sub> by Cu Kα radiation.

Fig. S4 Crystal structure of low-temperature phase of [(CH<sub>3</sub>)<sub>2</sub>NH<sub>2</sub>]<sub>2</sub>KCo(CN)<sub>6</sub>.

**Fig. S5** <sup>1</sup>H NMR line of  $[(CD_3)_2NH_2]_2KCo(CN)_6$  observed at 120 K (red line) and the simulated Pake doublet F(x) (blue line).

**Fig. S6a-i** <sup>14</sup>N NQR spectra of (DMA)<sub>2</sub>KCo(CN)<sub>6</sub>. The disappearance of the NQR signals under a sufficiently strong magnetic field was checked at room and liquid nitrogen temperatures in order to eliminate the possibility of false signal. The results are shown in Fig. S6b-i.

**Fig. S7** <sup>2</sup>H NMR spectra simulation.

References



**Fig. S1** Powder X-ray diffraction of  $[(CH_3)_2NH_2]_2KCo(CN)_6$  by Cu K $\alpha$  radiation. The abbreviation "DMA" stands for dimethylammonium. Theoretical pattern was calculated for *P4/mnc*, a = b = 8.2895(13), c = 11.621(3) Å, Z = 2 at 293 K [1]. The small peaks were observed at around 7.7 ° and 11.0 °, which are close to the forbidden reflections  $(0\ 0\ 1)$  and  $(1\ 0\ 0)$  at 7.61 ° and 10.67 °, respectively, calculated by the crystal data. This may indicate that the strict symmetry of the present crystals is lower than *P4/mnc*.



**Fig. S2** Powder X-ray diffraction of  $[(CD_3)_2NH_2]_2KCo(CN)_6$  by Cu K $\alpha$  radiation. The abbreviation "DMA" stands for dimethylammonium. Theoretical pattern was calculated for *P4/mnc*, a = b = 8.2895(13), c = 11.621(3) Å, Z = 2 at 293 K [1]. The small peaks were observed at around 7.7 ° and 10.9 °, which are close to the forbidden reflections (0 0 1) and (1 0 0) at 7.61 ° and 10.67 °, respectively, calculated by the crystal data. This may indicate that the strict symmetry of the present crystals is lower than *P4/mnc*. There observed at room temperature no appreciable change of the crystal parameters by deuteration of the methyl groups.



**Fig. S3** Powder X-ray diffraction of  $[(CH_3)_2NH_2]_2KCr(CN)_6$  by Cu K $\alpha$  radiation. The abbreviation "DMA" stands for dimethylammonium. Theoretical pattern was calculated for *P4/mnc*, a = b = 8.40300(10), c = 11.8999(3) Å, Z = 2 at 230 K [2]. In the experimental pattern, the (2 0 0) and (2 2 0) reflections from KCl crystals can be recognized at 28.30 ° and 40.44 °. Due to this contamination, the (2 1 2) reflection at 27.92 ° of the title compound looks like to be split.



**Fig. S4** Crystal structure of low-temperature phase of  $[(CH_3)_2NH_2]_2KCo(CN)_6$ according to Zhang *et al* [1]. Space group *P4/mnc*, a = b = 8.242(6), c = 11.584(10) Å, Z = 2 at 113 K. Three two-fold rotation axes C<sub>2</sub> along [0 0 1], [1 1 0], and [ $\overline{1}$  1 0] directions go through the (CH<sub>3</sub>)<sub>2</sub>NH<sub>2</sub><sup>+</sup> ion site.



**Fig. S5** <sup>1</sup>H NMR line of  $[(CD_3)_2NH_2]_2KCo(CN)_6$  observed at 120 K (red line) and the simulated Pake doublet F(x) (blue line). The argument *x* is the frequency deflection (Hz) from the center of the resonance. F(x) is given by the following equations [3].

$$F(x) = N \int_{-\infty}^{+\infty} f(x') \exp\left(-\frac{(x-x')^2}{2\beta^2}\right) dx'$$

$$f(x) = \left(-\frac{x}{\alpha} + 1\right)^{-\frac{1}{2}} - 2\alpha \le x \le -\alpha$$
$$= \left(-\frac{x}{\alpha} + 1\right)^{-\frac{1}{2}} + \left(\frac{x}{\alpha} + 1\right)^{-\frac{1}{2}} - \alpha < x < \alpha$$
$$= \left(\frac{x}{\alpha} + 1\right)^{-\frac{1}{2}} \qquad \alpha \le x \le 2\alpha$$

where  $\alpha$  is given as

$$\alpha = \frac{3\gamma^2\hbar}{8\pi r^3} \tag{7}$$

by the proton-magnetogyric ratio  $\gamma$  and the distance *r* between the two protons,  $\beta$  represents line-broadening due to the dipolar interaction outside the pair protons, and *N* is a normalization factor.



**Fig. S6a** <sup>14</sup>N NQR spectra of (DMA)<sub>2</sub>KCo(CN)<sub>6</sub> at 298 K. Free induction decay (blue) and Fourier transform spectra (red) accumulated by 1024 times with the repetition time of 0.5 s. Since spectrometer frequency is 2618.0 kHz,  $v_{\pm}$  = 2625.0 kHz,  $v_{-}$  = 2606.5 kHz, and  $v_{\pm}$  = 2635.0 kHz.



**Fig. S6b** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 297.5 K. Spectrometer frequency RF = 2640.0 kHz, number of accumulation N = 2048, repetition time t = 0.2 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6c** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2680.0 kHz, number of accumulation N = 256, repetition time t = 5 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6d** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2740.0 kHz, number of accumulation N = 1024, repetition time t = 1 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6e** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2710.0 kHz, number of accumulation N = 1024, repetition time t = 1 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6f** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2774.0 kHz, number of accumulation N = 512, repetition time t = 3 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6g** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2600.0 kHz, number of accumulation N = 256, repetition time t = 3 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6h** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2640.0 kHz, number of accumulation N = 256, repetition time t = 3 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S6i** Effect of magnetic field on <sup>14</sup>N NQR spectra of  $(DMA)_2KCo(CN)_6$  at 77.3 K. Spectrometer frequency RF = 2580.0 kHz, number of accumulation N = 256, repetition time t = 3 s. With (right) and without (left) magnetic field of *ca*. 110 G.



**Fig. S7** <sup>2</sup>H NMR spectra simulation. The D-N-D bond angle was set at 107°. The quadrupole coupling constant of 128 kHz and the asymmetry parameter  $\eta = 0$  were used. The calculation was done by use of "NMR Weblab, A Tool for Simulation of Solid State NMR Spectra 6.6.2" [4]. As for the axis notation, see Fig. 7 in the text. (a) <sup>2</sup>H NMR line-shape calculated assuming very fast C<sub>2</sub> flip about the C<sub>2, $\eta$ </sub> axis and fast rotational oscillation about the C<sub>2, $\zeta$ </sub> axis (pseudo C<sub>4</sub> axis) with Gaussian jump angle distribution full width of 35°. (b) <sup>2</sup>H NMR line-shape calculated assuming very fast C<sub>2</sub> flip about the C<sub>2, $\eta$ </sub> axis and fast four sites reorientation among A, B, A', B' sites with population of 0.91 at A or A' and 0.09 at B or B' (pseudo C<sub>4</sub> reorientation about the C<sub>2, $\zeta$ </sub> axis).

## References

- [1] W. Zhang, H.-Y. Ye, R. Graf, H. W. Spiess, Y.-F. Yao, R.-Q. Zhu, and R.-G. Xiong, J. Am. Chem. Soc., 2013, 135, 5230-5233.
- [2] M. Rok, G. Bator, B. Zarychta, B. Dziuk, J. Repeć, W. Medycki, M. Zamponi, G. Usevičius, M. Šimėnas, and J. Banys, *Dalton Trans.*, 2019, 48, 4190-4202.
- [3] T. Asaji and K. Ashitomi, J. Phys. Chem. C, 2013, 117, 10185-10190; A. Abragam, The Principles of Nuclear Magnetism, Oxford University Press, London, 1961.
- [4] V. Macho, L. Brombacher, and H. W. Spiess, *Appl. Magn. Reson.* 2001, 20, 405-432.