

**Fluorooxoborate Layers: Second Harmonic Generation and Raman
Spectra Anisotropy**

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Calculations details and methods

Properties of fluorooxoborate and KBBF functional layers were obtained on the basis of *ab initio* calculations implemented in the CASTEP package through density functional theory (DFT).¹ The generalized gradient approximation (GGA)² was adopted, and Perdew-Burke-Ernzerhof (PBE)³ functional was chosen to calculate the exchange-correlation potential, with an energy cutoff of 780 eV under the Norm conserving pseudopotentials. The numerical integration of the Brillouin zone was performed using a $3 \times 3 \times 1$ Monkhorst-Pack k-point sampling. We set the layer in the *xy* plane, and adopted a 20 Å supercell length in the *z* direction to avoid the interaction between the layers.

The SHG anisotropy of functional layers in C_1 , C_{2v} and C_3 point groups can be calculated by the following equations:

$$I_{C_1}^{\parallel} = |d_{11}\cos^3\theta + (d_{12} + 2d_{26})\cos\theta\sin^2\theta + (2d_{16} + d_{21})\cos^2\theta\sin\theta + d_{22}\sin^3\theta|^2 \quad (1)$$

$$I_{C_3}^{\perp} = |d_{12}\sin^3\theta + (d_{22} - 2d_{16})\cos\theta\sin^2\theta + (2d_{26} - d_{11})\cos^2\theta\sin\theta - d_{21}\sin\cos^3\theta|^2 \quad (2)$$

$$I_{C_{2v}}^{\parallel} = |d_{22}\sin^3\theta + (d_{16} + 2d_{21})\sin\theta\cos^2\theta|^2 \quad (3)$$

$$I_{C_{2v}}^{\perp} = |d_{21}\cos^3\theta + (d_{22} - 2d_{16})\cos\theta\sin^2\theta|^2 \quad (4)$$

$$I_{C_3}^{\parallel} = |d_{22}\sin^3\theta - 2d_{22}\sin\theta\cos^2\theta|^2 \quad (5)$$

$$I_{C_3}^{\perp} = |2d_{22}\cos\theta\sin^2\theta - d_{22}\cos^3\theta|^2 \quad (6)$$

Raman scattering intensities of C_1 , C_{2v} and C_3 point groups can be calculated as following equations:

$$C_1: S_{A_g}^{\parallel} = |a\cos^2\theta + b\sin^2\theta + 2d\sin\theta\cos\theta|^2 \quad (7)$$

$$S_{A_g}^{\perp} = |d\cos^2\theta - d\sin^2\theta + (b - a)\sin\theta\cos\theta|^2 \quad (8)$$

C_{2v} :

$$S_{A_{1g}}^{\parallel} = |a\cos^2\theta + b\sin^2\theta|^2 \quad (9)$$

$$S_{A_{1g}}^{\perp} = |b\sin\theta\cos\theta - a\sin\theta\cos\theta|^2 \quad (10)$$

$$S_{A_{2g}}^{\parallel} = |2d\sin\theta\cos\theta|^2 \quad (11)$$

$$S_{A_{2g}}^{\perp} = |d\cos^2\theta - d\sin^2\theta|^2 \quad (12)$$

C_3 :

$$S_{A_g}^{\parallel} = |a\cos^2\theta + a\sin^2\theta|^2 \quad (13)$$

$$S_{A_g}^{\perp} = 0 \quad (14)$$

$$S_{E_g}^{\parallel} = |c\cos^2\theta - c\sin^2\theta + 2d\sin\theta\cos\theta|^2 \quad (15)$$

$$S_{E_g}^{\perp} = |d\cos^2\theta - d\sin^2\theta - 2c\sin\theta\cos\theta|^2 \quad (16)$$

$$S_{E_g}^{\parallel} = |d\cos^2\theta - d\sin^2\theta - 2c\sin\theta\cos\theta|^2 \quad (17)$$

$$S_{E_g}^{\perp} = |c\sin^2\theta - c\cos^2\theta - 2d\sin\theta\cos\theta|^2 \quad (18)$$

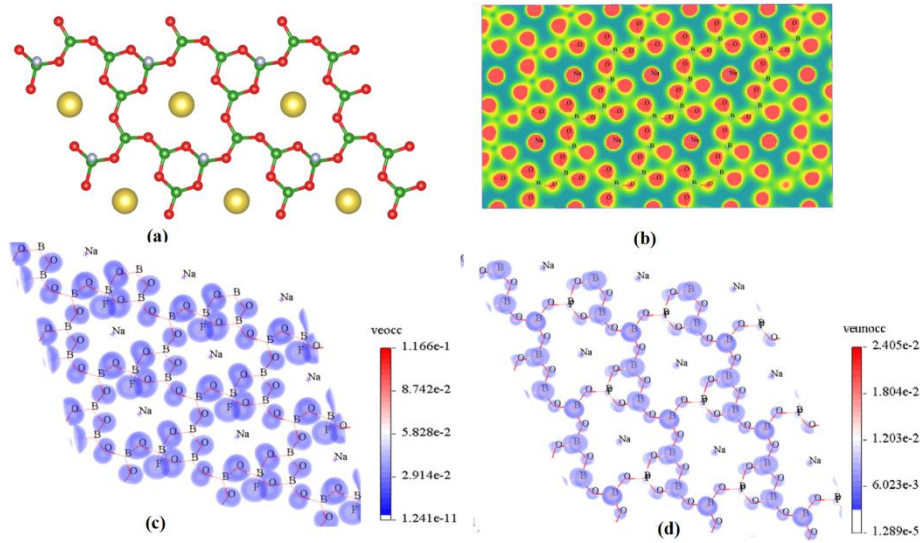


Fig. S1 (a) The $\text{NaB}_4\text{O}_6\text{F}$ layer, (b) the electronic density of $\text{NaB}_4\text{O}_6\text{F}$ layer. The SHG densities of the $\text{NaB}_4\text{O}_6\text{F}$ layer, (c) virtual-electron (VE) occupied states and (d) VE unoccupied states.

The highlighted electronic density of the $\text{NaB}_4\text{O}_6\text{F}$ layer shows the anisotropy of bonding electron distributions of the B-O-F layer, which indicates its significant role in the birefringence (Fig. S1b). The SHG-density of virtual-electron(VE) occupied (veocc) and unoccupied (veunocc) states are shown in Fig. 1c, 1d. For the occupied states, O-2*p* and F-2*p* orbitals make significant contribution to the SHG effects. In unoccupied states, the B-2*p*, O-2*p* and F-2*p* orbitals contribute to the SHG response. Therefore, the $\text{NaB}_4\text{O}_6\text{F}$ layer plays a key role both in SHG response and birefringence, which exhibits the characteristic of functional layers for the nonlinear optical performances.

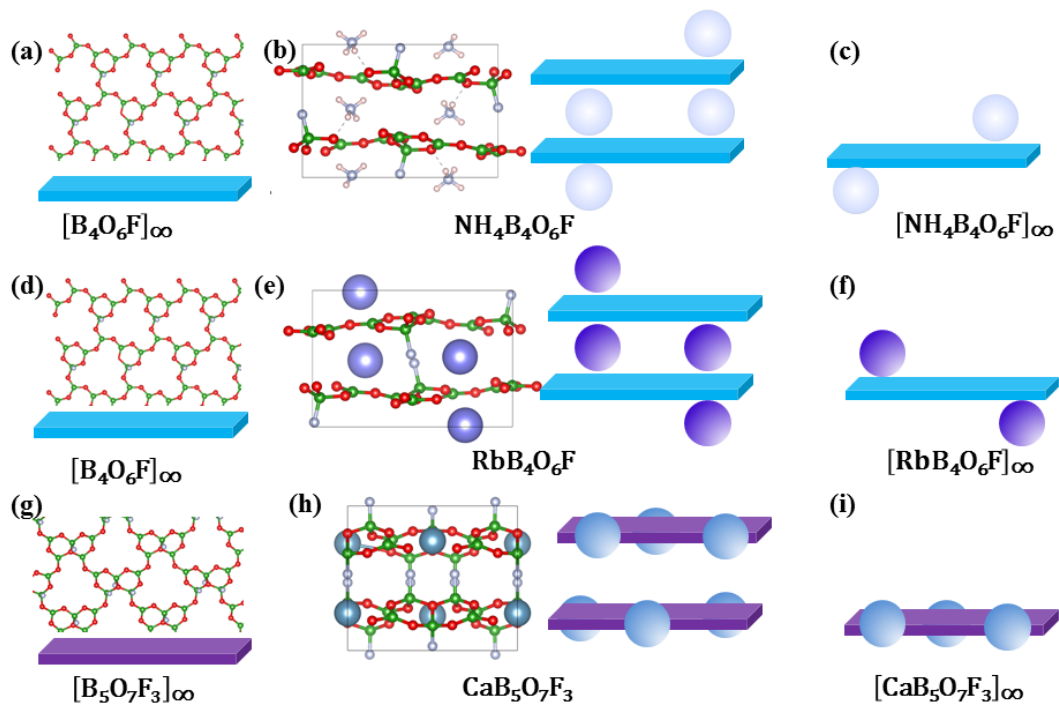


Fig. S2 (a) The $[B_4O_6F]_\infty$ functional layer, (b) the unit cell of $NH_4B_4O_6F$, (c) the $[NH_4B_4O_6F]_\infty$ layer, (d) the $[B_4O_6F]_\infty$ functional layer, (e) the unit cell of RbB_4O_6F , (f) the $[RbB_4O_6F]_\infty$ layer, (g) $[B_5O_7F_3]_\infty$ functional layer, (h) the unit cell of $CaB_5O_7F_3$, (i) the $[CaB_5O_7F_3]_\infty$ layer.

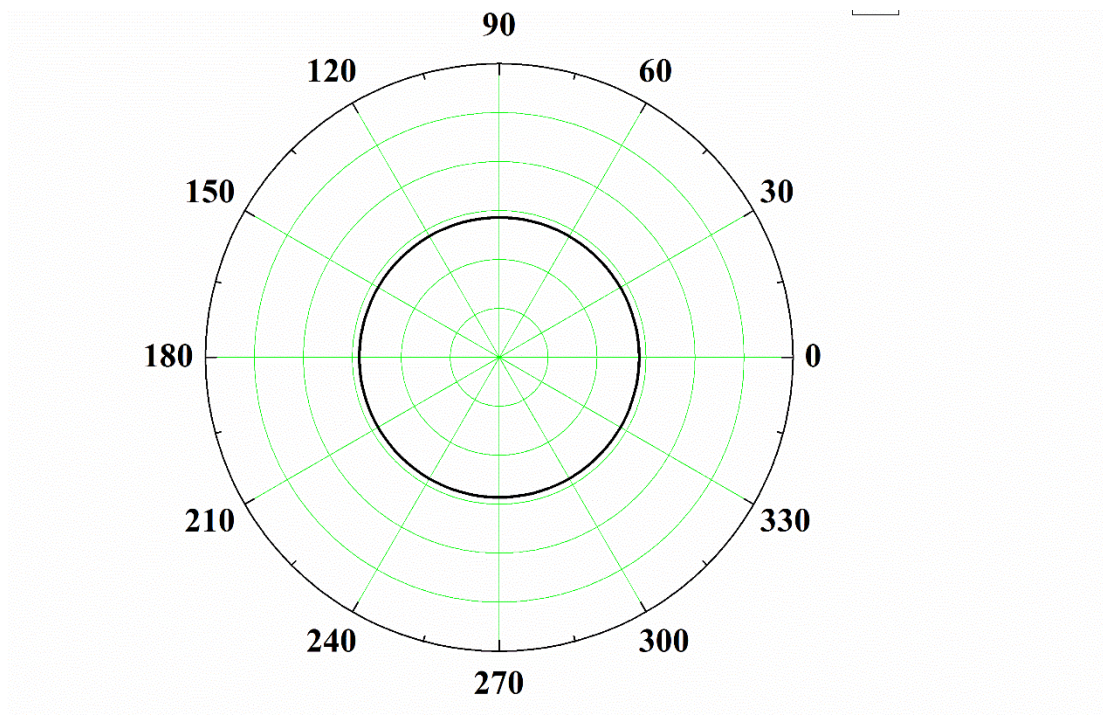


Fig. S3. The angle dependence of the Raman intensities under parallel polarization configurations of the KBBF functional layer (A_g modes).

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