

Supplementary Information – Influence of M/A substitution on material properties of intermetallic compounds MSn₂ (M = Fe, Co; A = Li, Na): A first-principles study

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Table S1. Lattice constants and their relative error, total energy and total energy difference of alloy compounds with different magnetic states such as ferromagnetic (FM), non-magnetic (NM) and anti-ferromagnetic (AFM) states. For the case of CoSn₂, only NM state was observed although initial magnetization were differently imposed.

	Mag. state	<i>a</i> (Å)	error (%)	<i>c</i> (Å)	error (%)	<i>E</i> _{tot} (Ry)	Δ <i>E</i> (Ry)
FeSn ₂	FM	6.3430	-0.294	5.4759	0.324	-2304.670759	0.013
	NM	6.3879	-2.222	5.4386	2.226	-2304.602940	0.081
	AFM	6.5333	0.003	5.3271	0.130	-2304.683929	0.000
CoSn ₂	NM	6.3442	-0.275	5.4723	0.258	-2489.977319	

Table S2. Magnetic moment of transition atom (M = Fe or Co), alkali atom (A = Li or Na) and Sn atom, and total magnetization of alloy compounds with different magnetic states in μ_B unit.

	Mag. state	μ _{M1}	μ _{M2}	μ _A	μ _{Sn}	μ _{tot}
FeSn ₂	FM	1.72	1.72	-	0.00	6.00
	NM	0.00	0.00	-	0.00	0.00
	AFM	1.89	-1.89	-	0.00	0.00
FeLiSn ₂	FM	2.30, 1.64	0.04	0.00	-0.03	3.40
FeNaSn ₂	FM	2.38, 1.79	-1.78	0.02	-0.01	2.29
CoSn ₂	NM	0.00	0.00	-	0.00	0.00
CoLiSn ₂	NM	0.00	0.00	0.00	0.00	0.00
CoNaSn ₂	NM	0.00	0.00	0.00	0.00	0.00

Table S3. Inter-atomic distance in Å unit for the inter-metallics. M = Fe or Co and A = Li or Na.

	M-Sn	M-M	Sn-Sn	M-A	Sn-A
FeSn ₂	2.787	2.663	3.117		
FeLiSn ₂	2.806	2.736	3.078	2.736	2.855
FeNaSn ₂	2.843	2.837	3.108	2.837	2.994
CoSn ₂	2.731	2.736	3.116		
CoLiSn ₂	2.778	2.798	3.111	2.798	2.856
CoNaSn ₂	2.802	2.869	3.124	2.869	2.984

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Table S4. Elastic compliance constants in 1/GPa unit.

	S_{11}	S_{12}	S_{13}	S_{33}	S_{44}	S_{66}
FeSn ₂	0.00588	-0.00063	-0.00216	0.00738	0.01872	0.01444
Fe _{3/4} Li _{1/4} Sn ₂	0.00692	-0.00123	-0.00183	0.00824	0.02211	0.01822
Fe _{3/4} Na _{1/4} Sn ₂	0.00794	-0.00177	-0.00203	0.00941	0.02348	0.01961
CoSn ₂	0.00557	-0.00105	-0.00138	0.00611	0.02343	0.01492
Co _{3/4} Li _{1/4} Sn ₂	0.00757	-0.00127	-0.00214	0.00911	0.03558	0.02173
Co _{3/4} Na _{1/4} Sn ₂	0.00855	-0.00147	-0.00275	0.01142	0.03901	0.02521

Table S5. Elastic moduli within the Reuss (B_R and G_R) and Voigt (B_V and G_V) approximation in GPa unit, and longitudinal (v_l) and transverse (v_t) elastic wave velocities in m/s unit.

	B_R	G_R	B_V	G_V	v_l	v_t
FeSn ₂	108.271	59.530	108.278	61.047	4693.0629	2652.9847
Fe _{3/4} Li _{1/4} Sn ₂	81.486	50.807	81.722	51.533	4367.6808	2552.4578
Fe _{3/4} Na _{1/4} Sn ₂	73.489	46.264	73.989	46.653	4261.6229	2493.7009
CoSn ₂	104.087	55.637	104.144	59.067	4495.3979	2533.3857
Co _{3/4} Li _{1/4} Sn ₂	76.015	37.706	76.144	40.847	4003.8153	2213.9901
Co _{3/4} Na _{1/4} Sn ₂	68.549	33.211	69.122	35.553	3859.7698	2113.4270

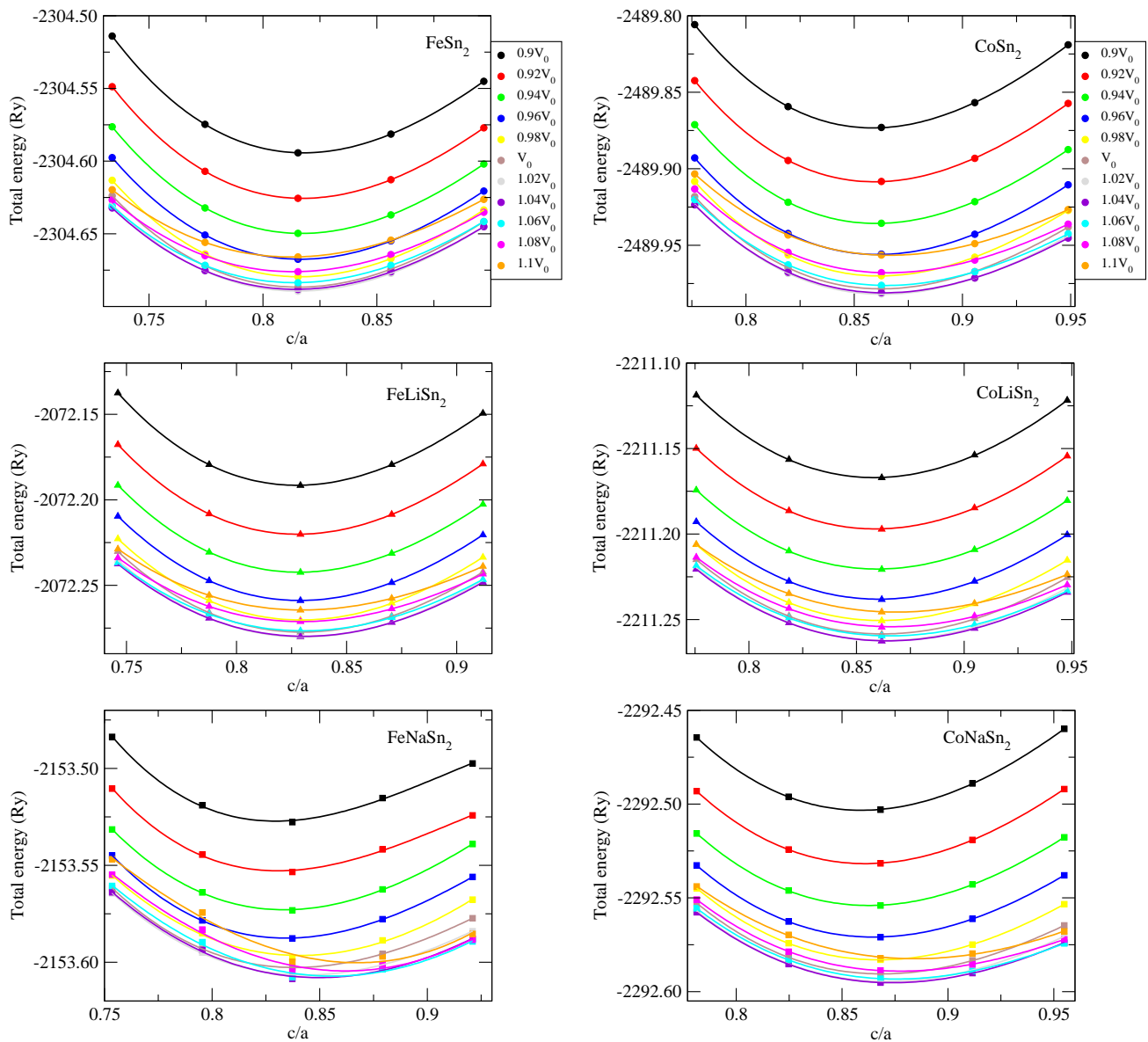


Figure S1. Total energy as a function of tetragonal lattice constants ratio c/a with gradually varying the cell volume from $0.9V_0$ to $1.1V_0$ in FeSn_2 , $\text{Fe}_{3/4}\text{Li}_{1/4}\text{Sn}_2$, $\text{Fe}_{3/4}\text{Na}_{1/4}\text{Sn}_2$, CoSn_2 , $\text{Co}_{3/4}\text{Li}_{1/4}\text{Sn}_2$ and $\text{Co}_{3/4}\text{Na}_{1/4}\text{Sn}_2$ in tetragonal phase.

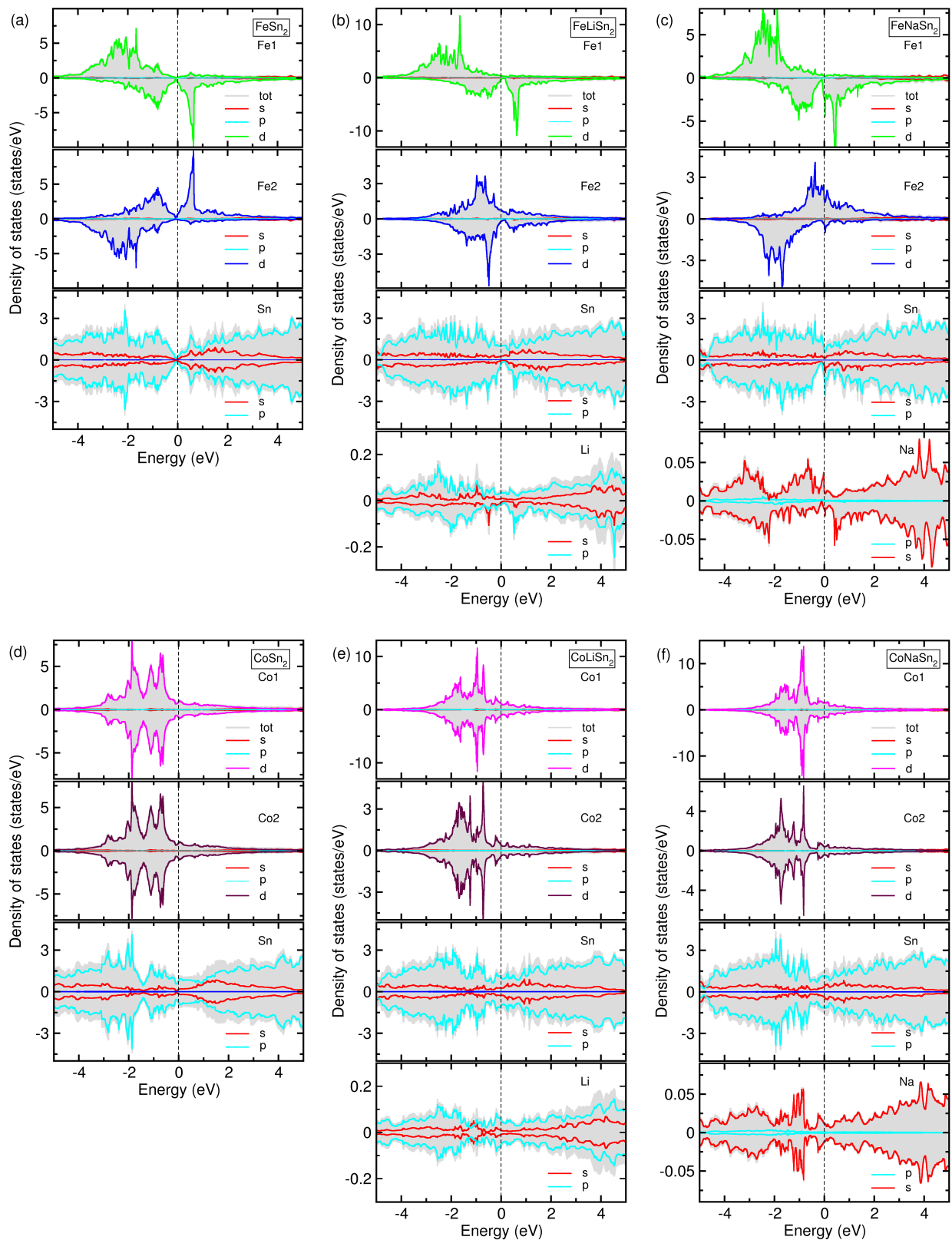


Figure S2. Partial density of states in (a) FeSn_2 , (b) FeLiSn_2 , (c) FeNaSn_2 , (d) CoSn_2 , (e) CoLiSn_2 and (f) CoNaSn_2 . The Fermi energy is set to zero as denoted by vertical dotted line.

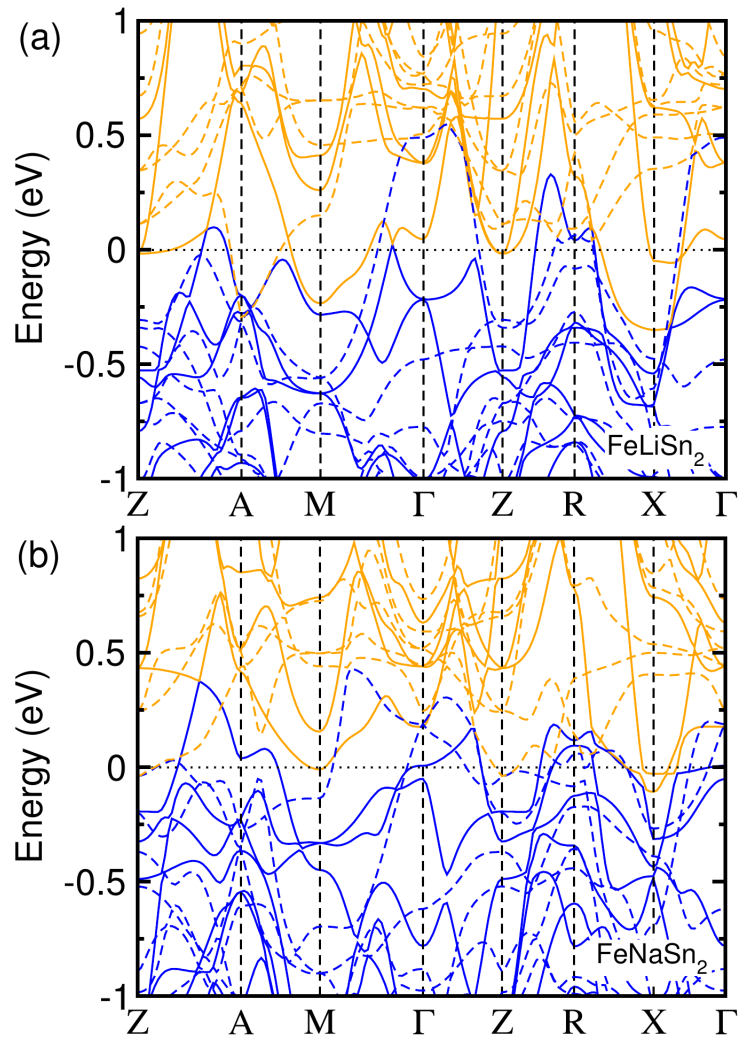


Figure S3. Both spin-up and spin-down energy band structures of (a) $\text{Fe}_{3/4}\text{Li}_{1/4}\text{Sn}_2$ and (b) $\text{Fe}_{3/4}\text{Na}_{1/4}\text{Sn}_2$. Blue and orange colors denote the occupied and empty spin-up bands, and dashed lines indicate the corresponding spin-down bands.

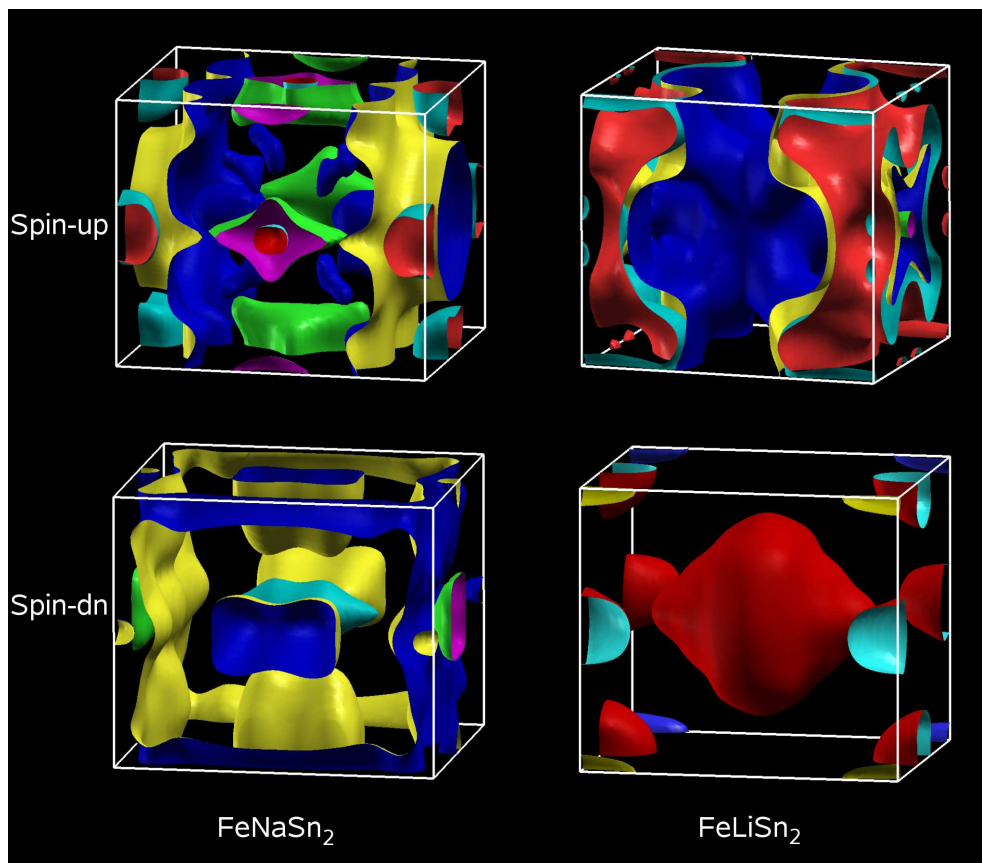


Figure S4. Fermi surface for spin-up and spin-down electronic energy bands of $\text{Fe}_{3/4}\text{Na}_{1/4}\text{Sn}_2$ and $\text{Fe}_{3/4}\text{Li}_{1/4}\text{Sn}_2$.