

SUPPLEMENTARY INFORMATION

The Al≡Al triple bond in Al₂X₅⁺ and Al₂X₆²⁺ (X=Li, Na) clusters with multiple alkali metals coordination

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Table of Contents

S4 Figure S1. Optimized GEM structures together with important bond distances (in/Å) and WBIs of D_{4h} - Al_2Li_4 (a) and D_{4h} - Al_2Na_4 (b) at the CCSD/6-311G(d) level.

S4 Figure S2. The lowest-lying isomers of $Al_2Li_5^+$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

S5 Figure S3. The lowest-lying isomers of $Al_2Li_6^{2+}$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

S6 Figure S4. The lowest-lying isomers of $Al_2Na_5^+$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

S7 Figure S5. The lowest-lying isomers of $Al_2Na_6^{2+}$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

S8 Table S1. Important results information of the clusters, including the spin states, relative energies (kcal/mol), Al-Al bond length (R/Å), Wiberg Bond Indices (WBI_{Al-Al}) and NPA charge (NPA/|e|). They all calculated at the B3LYP/def2-TZVP level.

S9 Figure S6. Optimized GEM structures at the CCSD/6-311G(d) level for C_1 - Al_2Li_5 (a), C_1 - Al_2Li_6 (b), C_1 - Al_2Na_5 (c) and C_1 - Al_2Na_6 (d). Together with important bond distances (in/Å) and Wiberg bond indices (WBIs) at the same level.

S10 Figure S7. The lowest-lying isomers of Al_2Li_5 . Optimized structures at B3LYP/def2-TZVP level, relative energies (kcal/mol) at the CCSD/6-311G(d) level.

S11 Figure S8. The lowest-lying isomers of Al_2Li_6 . Optimized structures at B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

S12 Figure S9. The lowest-lying isomers of Al_2Na_5 . Optimized structures at B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at CCSD/6-311G(d) level.

S13 Figure S10. The lowest-lying isomers of Al_2Na_6 . Optimized structures at B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

S14 Table S2. Important results information of the clusters, including the spin states, relative energies (kcal/mol), Al-Al bond length (R/Å), Wiberg Bond Indices (WBI_{Al-Al}) and NPA charge (NPA/|e|). They all calculated at the B3LYP/def2-TZVP level.

S15 Figure S11. Root-mean-square deviations (RMSD) of $Al_2Li_5^+$ (a), $Al_2Li_6^{2+}$ (b), $Al_2Na_5^+$ (c) and $Al_2Na_6^{2+}$ (d) during Born-Oppenheimer molecular dynamics (BOMD) simulations at 298K. The initial and final structural snapshots are also shown here.

S16 Figure S12. The global minimum of C_{4v} - $Al_2Li_5^+$ (a), D_{4h} - $Al_2Li_6^{2+}$ (b) and D_{4h} - $Al_2Na_6^{2+}$ (c) and their important FMOs under the CCSD/6-311G(d) level.

S17 Figure S13. The dominant FMO correlation diagram in $Al_2Na_6^{2+}$ between Al_2 and Na_6^{2+} fragments calculated at the CCSD/6-311G(d) level. The horizontal dashed and solid lines represent virtual and occupied molecular orbitals, respectively. (the

orbital energies are also given, unit: eV).

S17 Figure S14. a) AdNDP orbitals. b) LOL profile. c) ELF profile for Al_2Li_5^+ at the CCSD/6-311G(d) level. ON stands for the occupation number.

S18 Figure S15. a) AdNDP orbitals. b) LOL profile. c) ELF profile for $\text{Al}_2\text{Li}_6^{2+}$ at the CCSD/6-311G(d) level. ON stands for the occupation number.

S18 Figure S16. a) AdNDP orbitals. b) LOL profile. c) ELF profile for $\text{Al}_2\text{Na}_6^{2+}$ at the CCSD/6-311G(d) level. ON stands for the occupation number.

S19 Figure S17. Laplacian plot of the electron density $\nabla^2\rho(r)$, of Al_2Li_5^+ (a), $\text{Al}_2\text{Li}_6^{2+}$ (b), $\text{Al}_2\text{Na}_6^{2+}$ (c) in different perspectives. Solid and dashed lines correspond to positive and negative regions of $\nabla^2\rho$, respectively.

S20 Scheme 1. Several potential reactions and thermodynamic values for the generation of $C_1\text{-Al}_2\text{Li}_5$, $C_{4v}\text{-Al}_2\text{Li}_5^+$, $C_1\text{-Al}_2\text{Li}_6$, $D_{4h}\text{-Al}_2\text{Li}_6^{2+}$, $C_1\text{-Al}_2\text{Na}_5$, $D_{3h}\text{-Al}_2\text{Na}_5^+$, $C_1\text{-Al}_2\text{Na}_6$ and $D_{4h}\text{-Al}_2\text{Na}_6^{2+}$.

S21 Table S3. Cartesian coordinates for optimized structures of Al_2Li_5^+ , $\text{Al}_2\text{Li}_6^{2+}$, Al_2Na_5^+ , and $\text{Al}_2\text{Na}_6^{2+}$ at the CCSD/6-311G(d) level.

S22 Table S4. Cartesian coordinates for optimized structures of Al_2Li_5 , Al_2Li_6 , Al_2Na_5 , and Al_2Na_6 at the CCSD/6-311G(d) level.

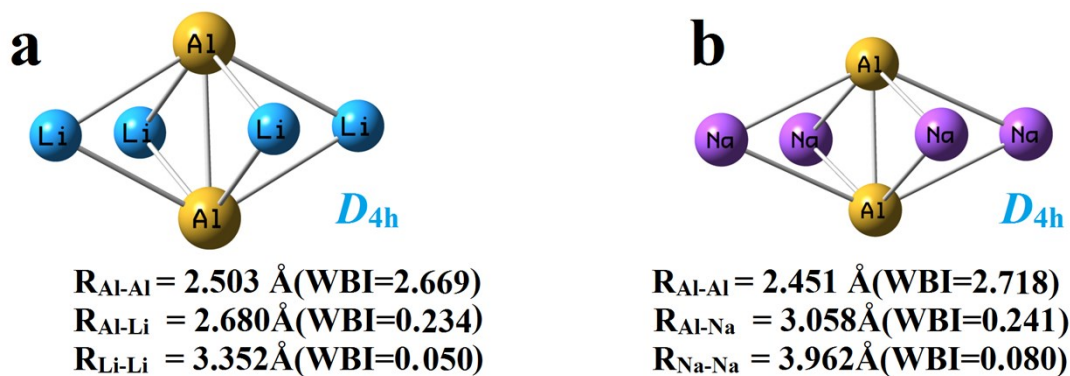


Figure S1. Optimized GEM structures together with important bond distances (in/Å) and WBIs of $D_{4h}\text{-Al}_2\text{Li}_4$ (a), and $D_{4h}\text{-Al}_2\text{Na}_4$ (b) at the CCSD/6-311G(d) level.

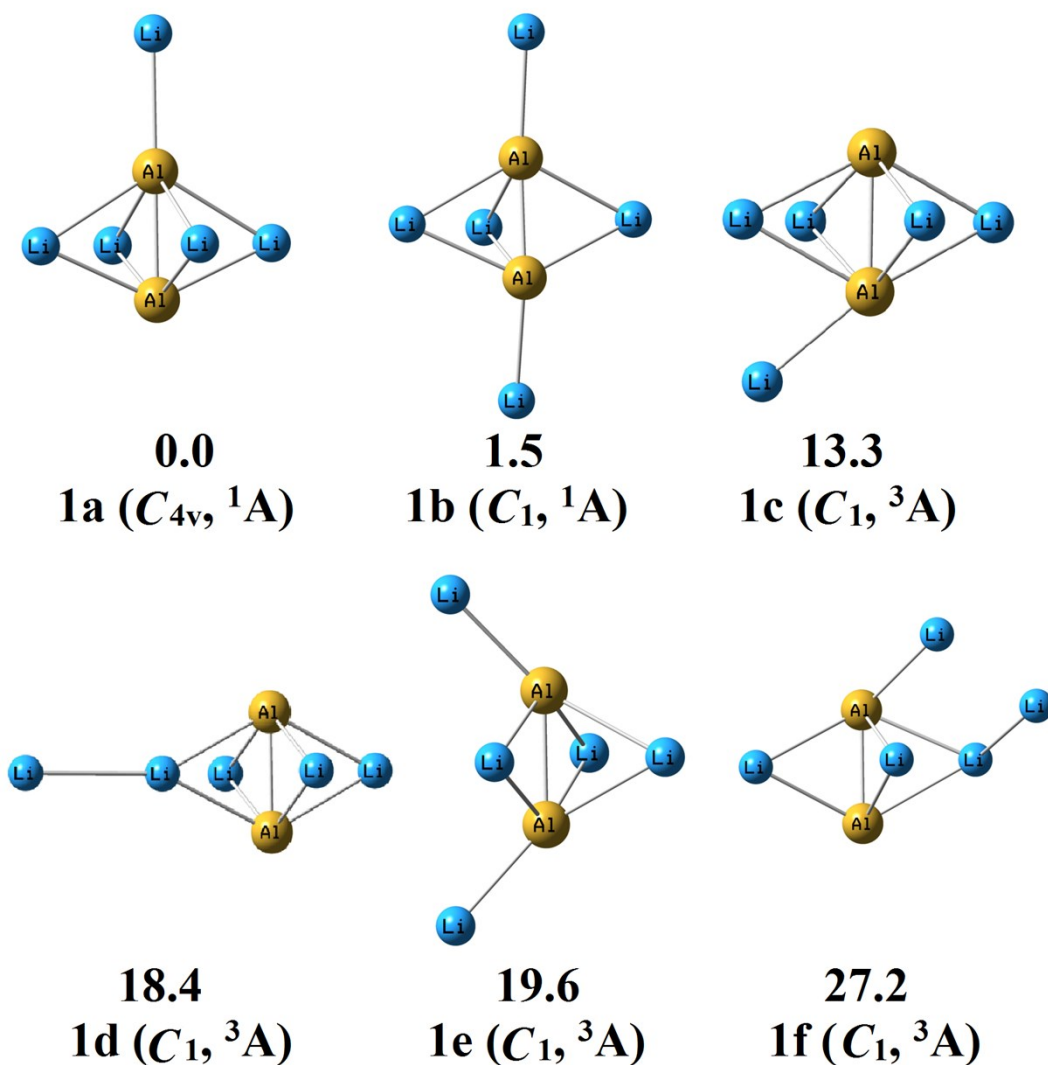


Figure S2. The lowest-lying isomers of Al_2Li_5^+ . Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

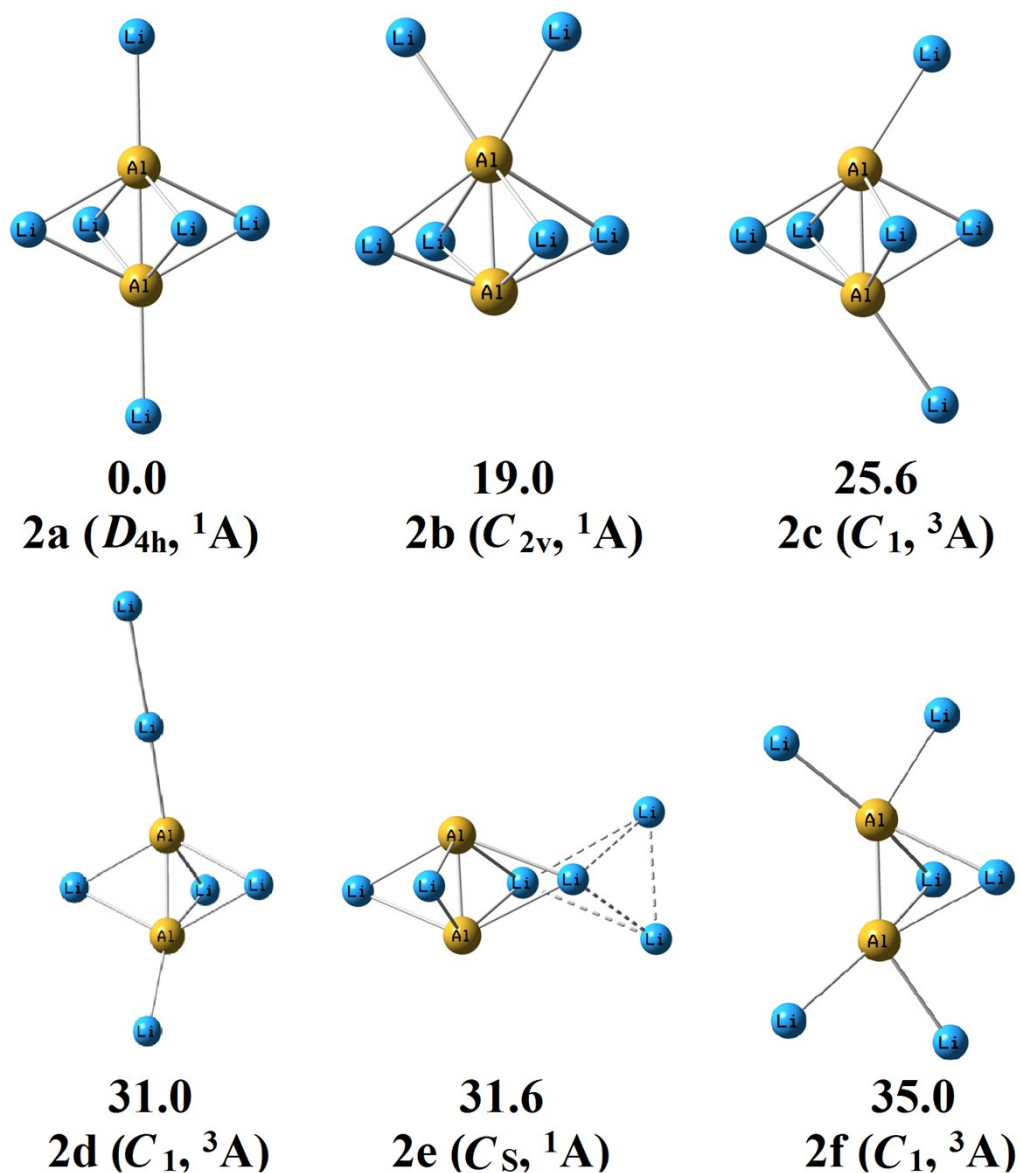


Figure S3. The lowest-lying isomers of $Al_2Li_6^{2+}$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

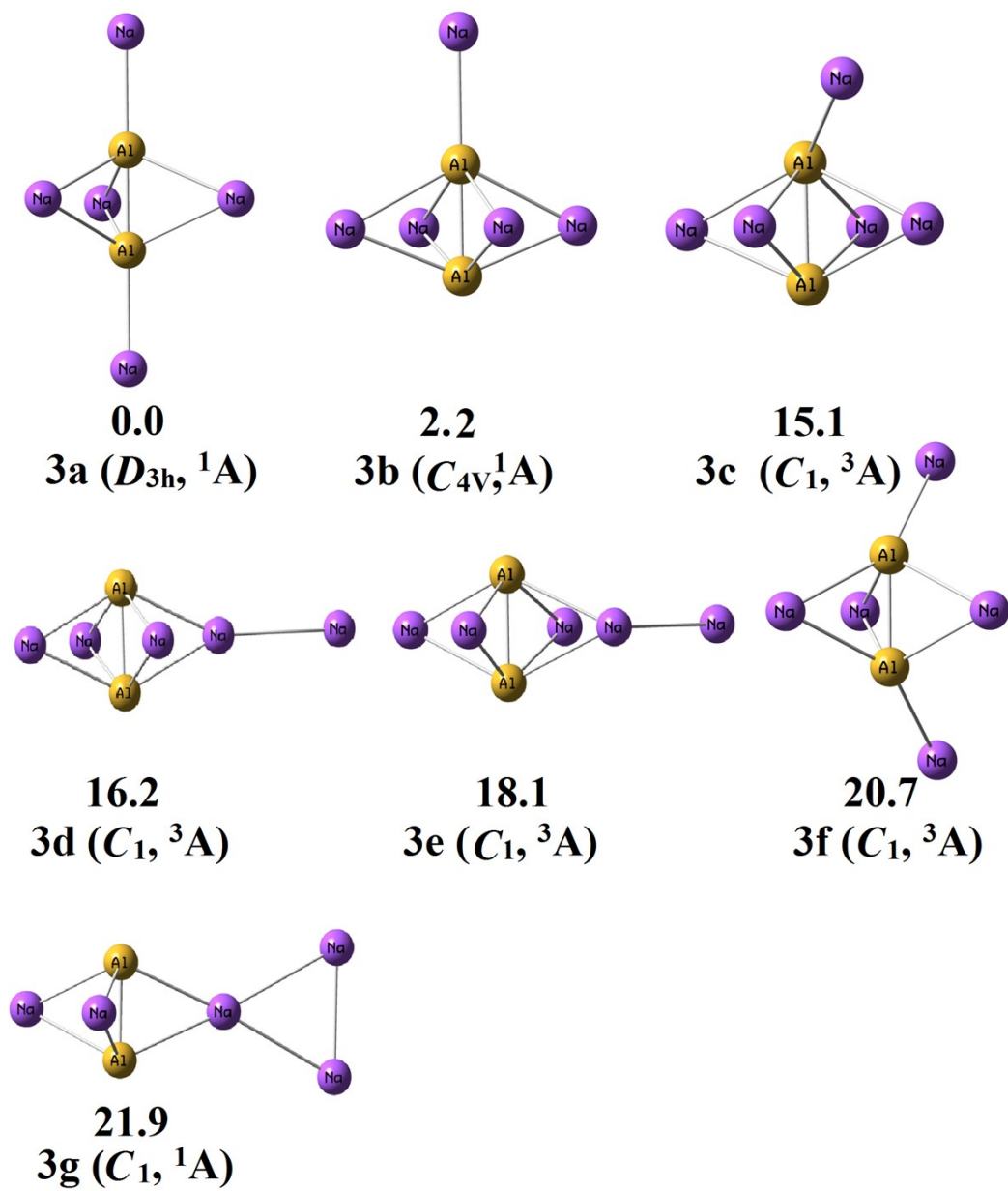


Figure S4. The lowest-lying isomers of $Al_2Na_5^+$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

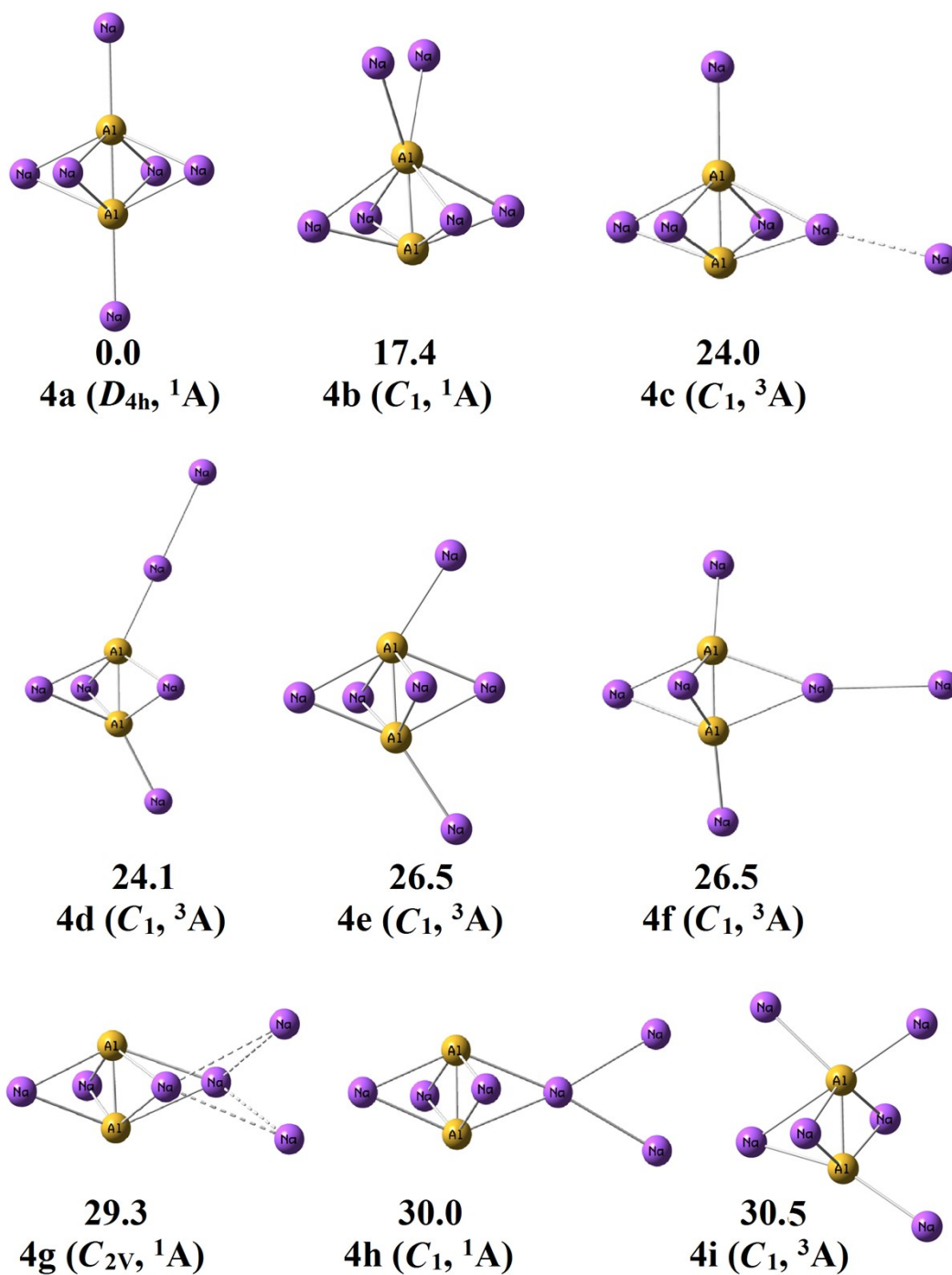


Figure S5. The lowest-lying isomers of $Al_2Na_6^{2+}$. Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

Table S1. Important results information of the structures of clusters, including the spin states, relative energies (kcal/mol), Al-Al bond length ($R_{\text{Al-Al}}$), Wiberg Bond Indices ($\text{WBI}_{\text{Al-Al}}$) and NPA charge ($\text{NPA}_{\text{Al-Al}}(|e|)$). They all calculated at the B3LYP/def2-TZVP level.

Molecule- Al_2Li_5^+	Spin States	Relative Energies(kcal/mol)	$R_{\text{Al-Al}}(\text{\AA})$	$\text{WBI}_{\text{Al-Al}}$	$\text{NPA}_{\text{Al-Al}}(e)$
I	Singlet	0.0	2.52	2.50	-1.529
II	Singlet	1.5	2.43	2.76	-0.795
III	Triplet	13.3	2.54	1.61	-1.031
IV	Triplet	18.4	2.48	1.30	-1.199
V	Triplet	19.6	2.54	1.60	-1.223
VI	Triplet	27.2	2.49	1.55	-0.558

Molecule- $\text{Al}_2\text{Li}_6^{2+}$	Spin States	Relative Energies(kcal/mol)	$R_{\text{Al-Al}}(\text{\AA})$	$\text{WBI}_{\text{Al-Al}}$	$\text{NPA}_{\text{Al-Al}}(e)$
I	Singlet	0.0	2.45	2.73	-1.708
II	Singlet	19.0	2.50	2.29	-1.364
III	Triplet	25.6	2.52	1.70	-1.340
IV	Triplet	31.0	2.45	2.18	-1.111
V	Singlet	31.6	2.36	2.47	-0.558
VI	Triplet	35.0	2.48	1.76	-1.045

Molecule- Al_2Na_5^+	Spin States	Relative Energies(kcal/mol)	$R_{\text{Al-Al}}(\text{\AA})$	$\text{WBI}_{\text{Al-Al}}$	$\text{NPA}_{\text{Al-Al}}(e)$
I	Singlet	0.0	2.44	2.64	-1.547
II	Singlet	2.2	2.51	2.29	-1.247
III	Triplet	15.1	2.55	1.92	-1.034
IV	Triplet	16.2	2.51	2.01	-0.932
V	Triplet	18.1	2.53	2.02	-0.901
VI	Triplet	20.7	2.54	1.79	-1.127
VI	Singlet	21.9	2.42	2.54	-0.650

Molecule- Al ₂ Na ₆ ²⁺	Spin States	Relative Energies(kcal/mol)	R _{Al-Al} (Å)	WBI _{Al-Al}	NPA _{Al-Al} (e)
I	Singlet	0.0	2.47	2.55	-1.551
II	Singlet	17.4	2.49	2.40	-1.318
III	Triplet	24.0	2.45	2.35	-1.092
IV	Triplet	24.1	2.48	2.19	-1.101
V	Triplet	26.5	2.56	1.82	-1.327
VI	Triplet	26.5	2.46	2.16	-1.087
VII	Singlet	29.3	2.40	2.68	-0.714
VIII	Singlet	30.0	2.41	2.64	-0.716
IX	Triplet	30.5	2.55	1.80	-1.357

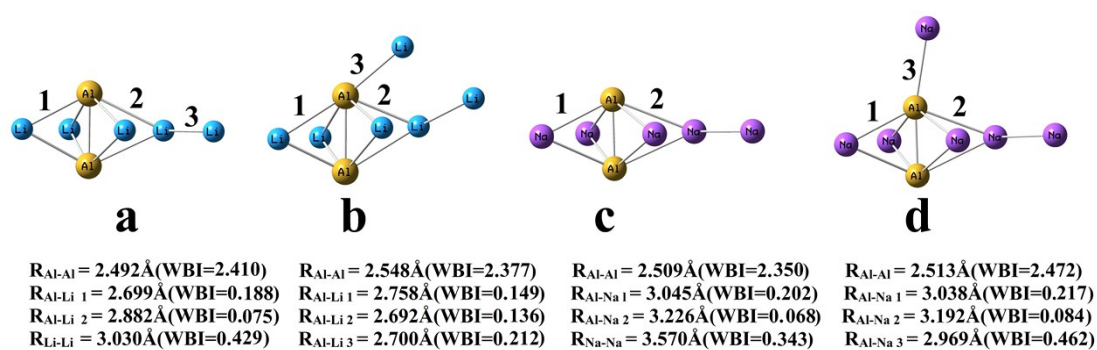


Figure S6. Optimized GEM structures at the CCSD/6-311G(d) level for C_1 -Al₂Li₅ (a), C_1 -Al₂Li₆ (b), C_1 -Al₂Na₅ (c) and C_1 -Al₂Na₆ (d). Together with important bond distances (in/Å) and Wiberg bond indices (WBIs) at the same level.

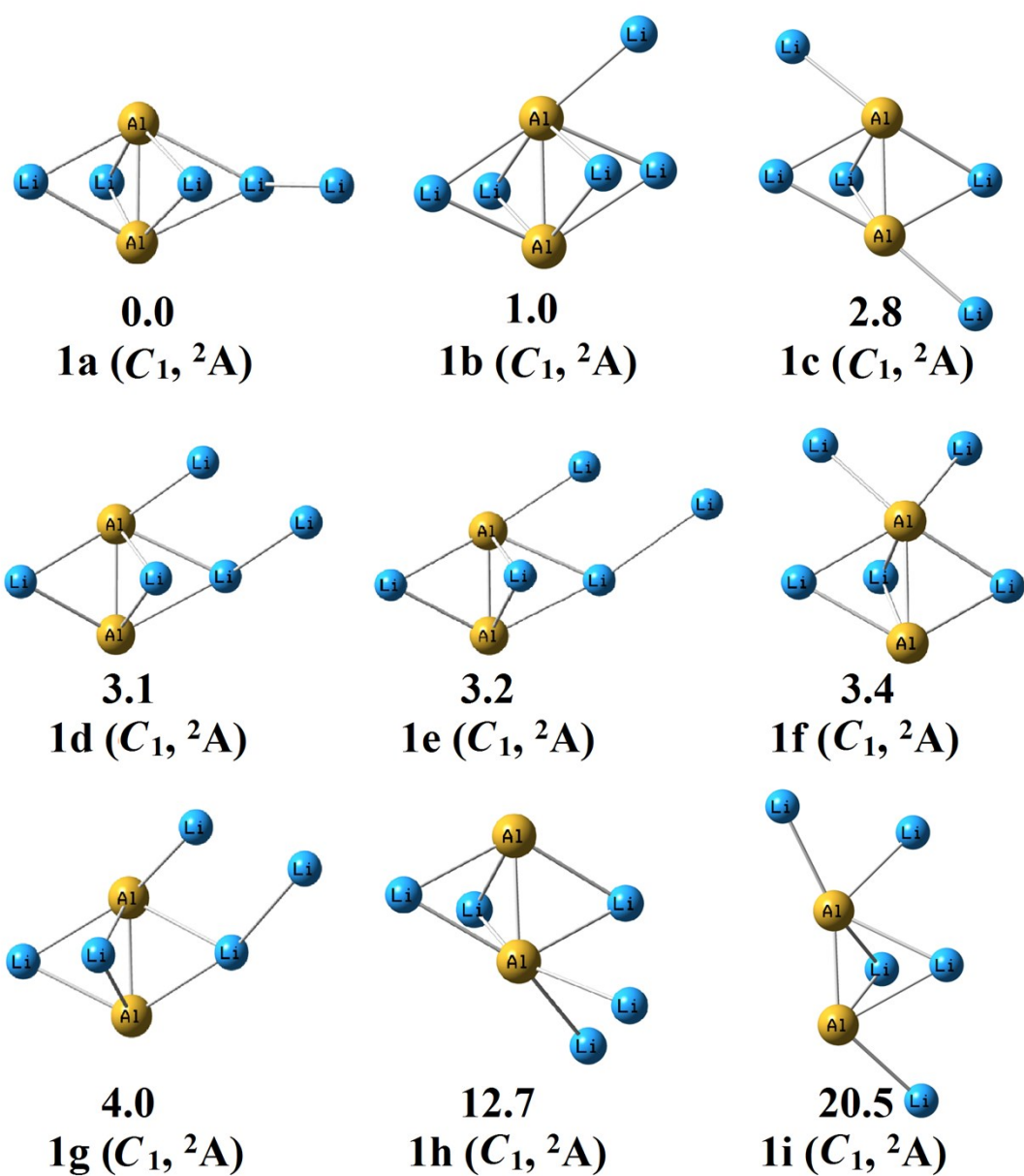


Figure S7. The lowest-lying isomers of Al_2Li_5 . Optimized structures at the B3LYP/def2-TZVP level, relative energies (kcal/mol) at the CCSD/6-311G(d) level.

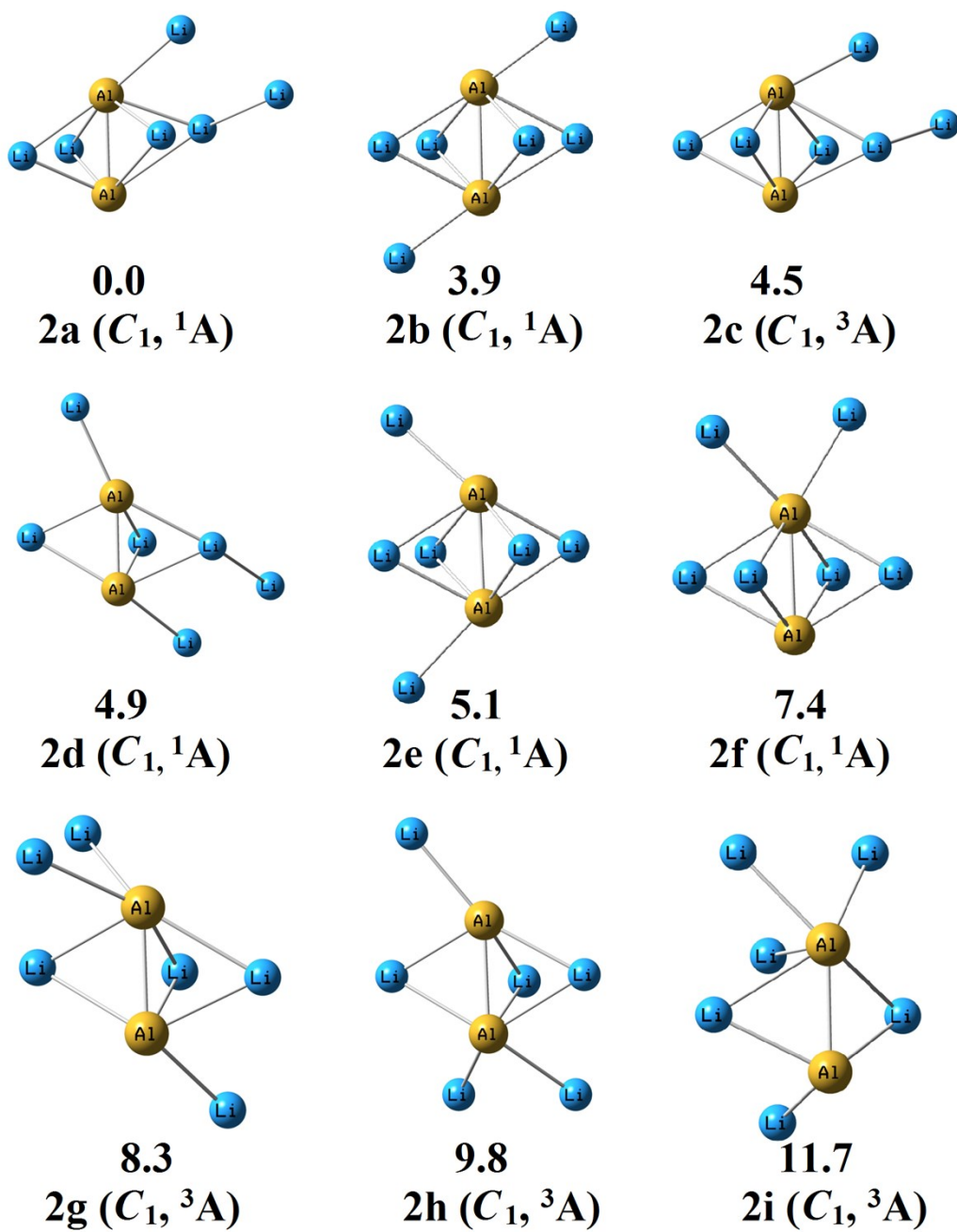


Figure S8. The lowest-lying isomers of Al_2Li_6 . Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

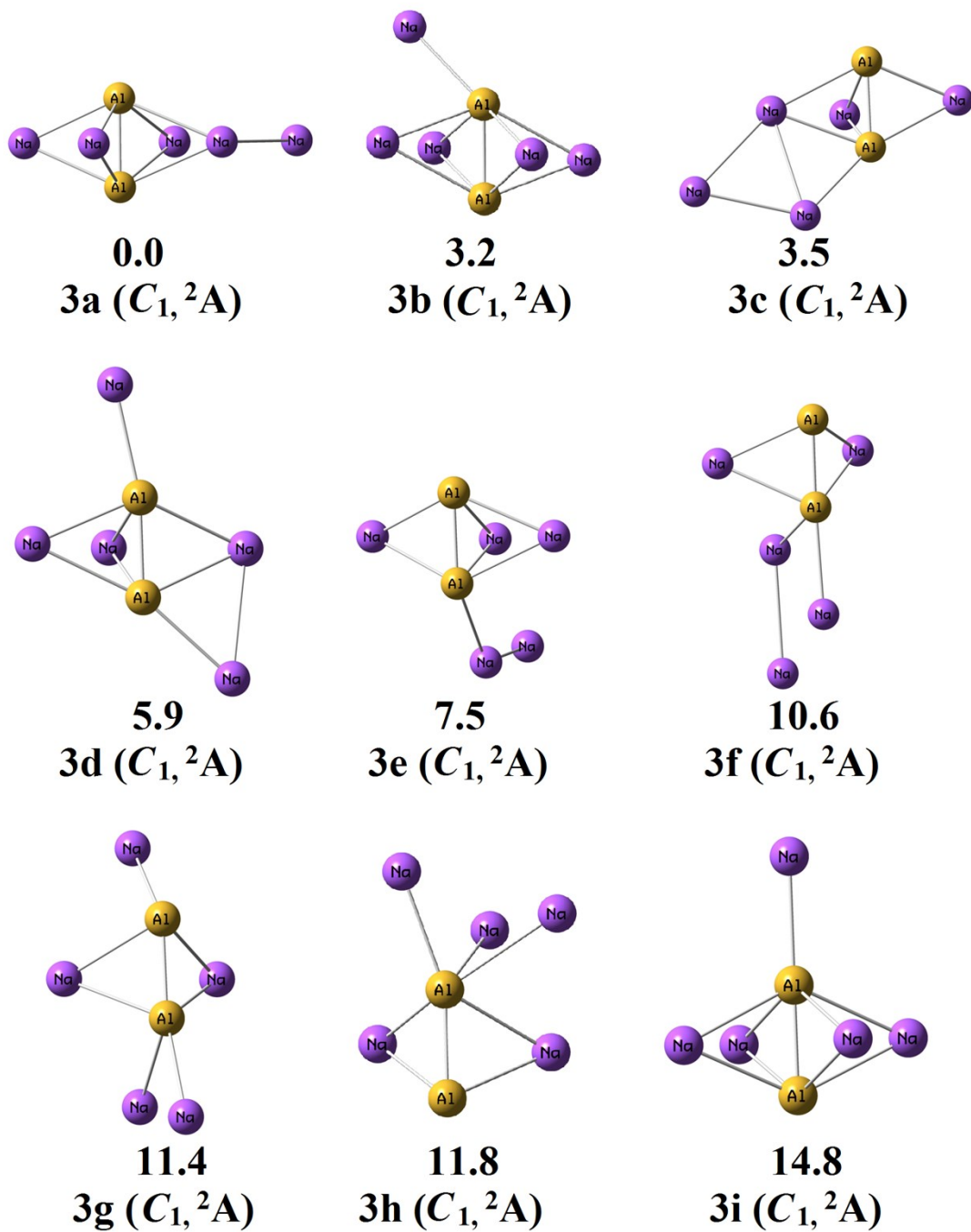


Figure S9. The lowest-lying isomers of Al_2Na_5 . Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

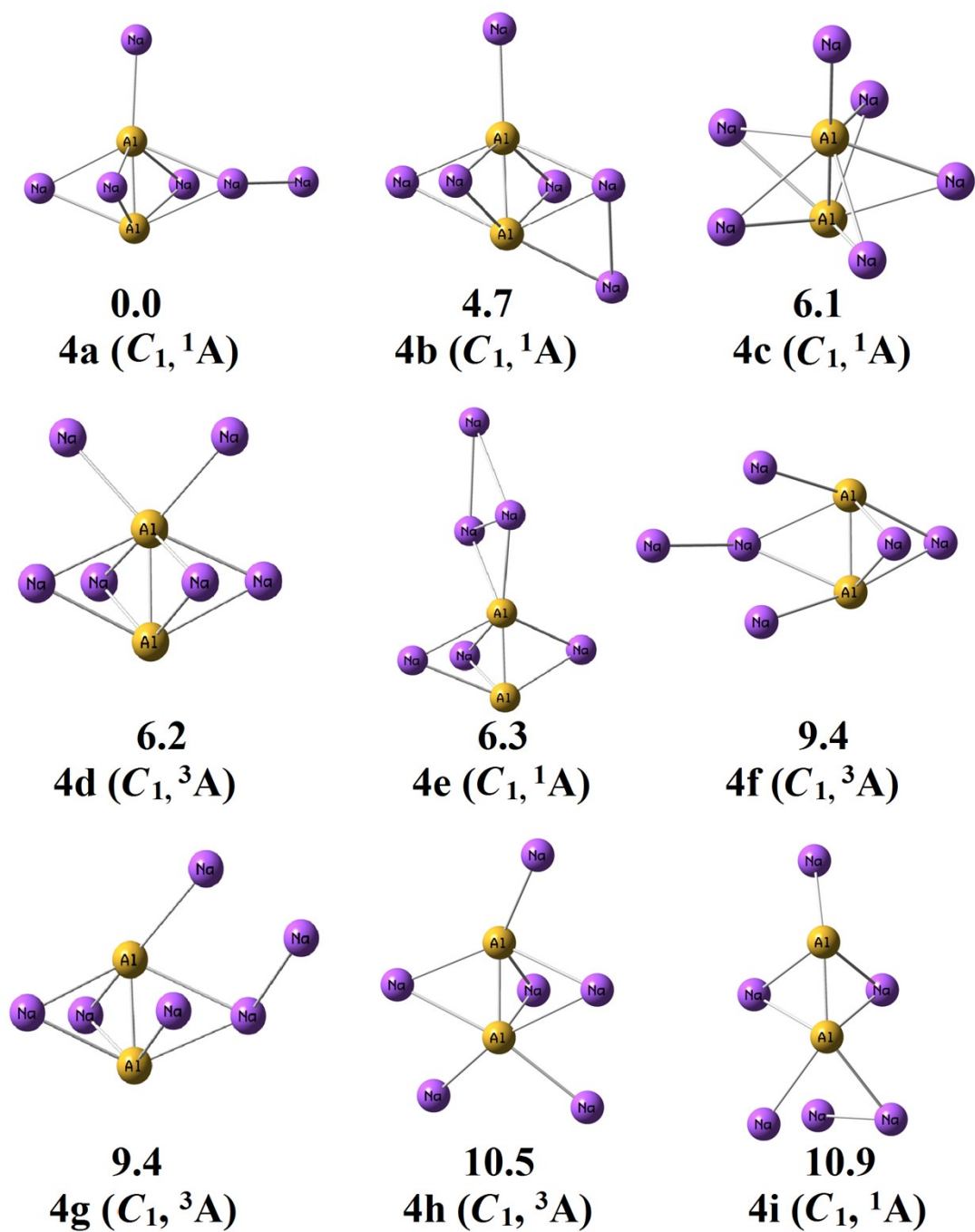


Figure S10. The lowest-lying isomers of Al_2Na_6 . Optimized structures at the B3LYP/def2-TZVP level, relative single-point energies (kcal/mol) at the CCSD/6-311G(d) level.

Table S2. Important results information of the structures of clusters, including the spin states, relative energies (kcal/mol), Al-Al bond length ($R_{\text{Al-Al}}$), Wiberg Bond Indices ($\text{WBI}_{\text{Al-Al}}$) and NPA charge ($\text{NPA}_{\text{Al-Al}}(|e|)$). They all calculated at the B3LYP/def2-TZVP level.

Molecule- Al_2Li_5	Spin States	Relative Energies(Kcal/mol)	$R_{\text{Al-Al}}(\text{\AA})$	WBI	$\text{NPA}_{\text{Al-Al}}(e)$
I	Doublet	0.0	2.47	2.41	-1.172
II	Doublet	1.0	2.57	1.69	-1.063
III	Doublet	2.8	2.56	1.58	-1.085
IV	Doublet	3.1	2.45	1.81	-0.679
V	Doublet	3.2	2.46	1.80	-0.698
VI	Doublet	3.4	2.67	1.14	-0.993
VII	Doublet	4.0	2.55	1.60	-1.010
VIII	Doublet	12.7	2.49	1.58	-0.982
IX	Doublet	20.5	2.51	1.50	-0.719

Molecule- Al_2Li_6	Spin States	Relative Energies(Kcal/mol)	$R_{\text{Al-Al}}(\text{\AA})$	WBI	$\text{NPA}_{\text{Al-Al}}(e)$
I	Singlet	0.0	2.54	2.38	-1.548
II	Singlet	3.9	2.71	1.52	-1.237
III	Triplet	4.5	2.57	1.41	-0.891
IV	Singlet	4.9	2.45	2.00	-0.998
V	Singlet	5.1	2.66	1.44	-1.326
VI	Singlet	7.4	2.70	1.26	-1.388
VII	Triplet	8.3	2.56	1.39	-1.069
VIII	Triplet	9.8	2.59	1.37	-1.189
IX	Triplet	11.7	2.63	1.10	-0.9569

Molecule- Al_2Na_5	Spin States	Relative Energies(Kcal/mol)	$R_{\text{Al-Al}}(\text{\AA})$	WBI	$\text{NPA}_{\text{Al-Al}}(e)$
I	Doublet	0.0	2.52	2.35	-1.133
II	Doublet	3.2	2.54	1.98	-1.066
III	Doublet	3.5	2.50	1.89	-0.805
IV	Doublet	5.9	2.50	1.92	-1.034
V	Doublet	7.5	2.51	1.86	-0.793
VI	Doublet	10.6	2.52	1.62	-0.694
VII	Doublet	11.4	2.51	1.70	-0.896
VIII	Doublet	11.8	2.57	1.42	-0.866
IX	Doublet	14.8	2.53	2.13	-1.116

Molecule- Al ₂ Na ₆	Spin States	Relative Energies(Kcal/mol)	R _{Al-Al} (Å)	WBI	NPA _{Al-Al} (e)
I	Singlet	0.0	2.53	2.47	-1.4329
II	Singlet	4.7	2.57	1.94	-1.1685
III	Singlet	6.1	2.56	1.92	-1.0862
IV	Triplet	6.2	2.60	1.69	-1.2637
V	Singlet	6.3	2.54	1.84	-0.9441
VI	Triplet	9.4	2.56	1.67	-0.9472
VII	Triplet	9.4	2.52	1.86	-0.9623
VIII	Triplet	10.5	2.55	1.71	-1.1620
IX	Singlet	10.9	2.56	1.48	-0.7725

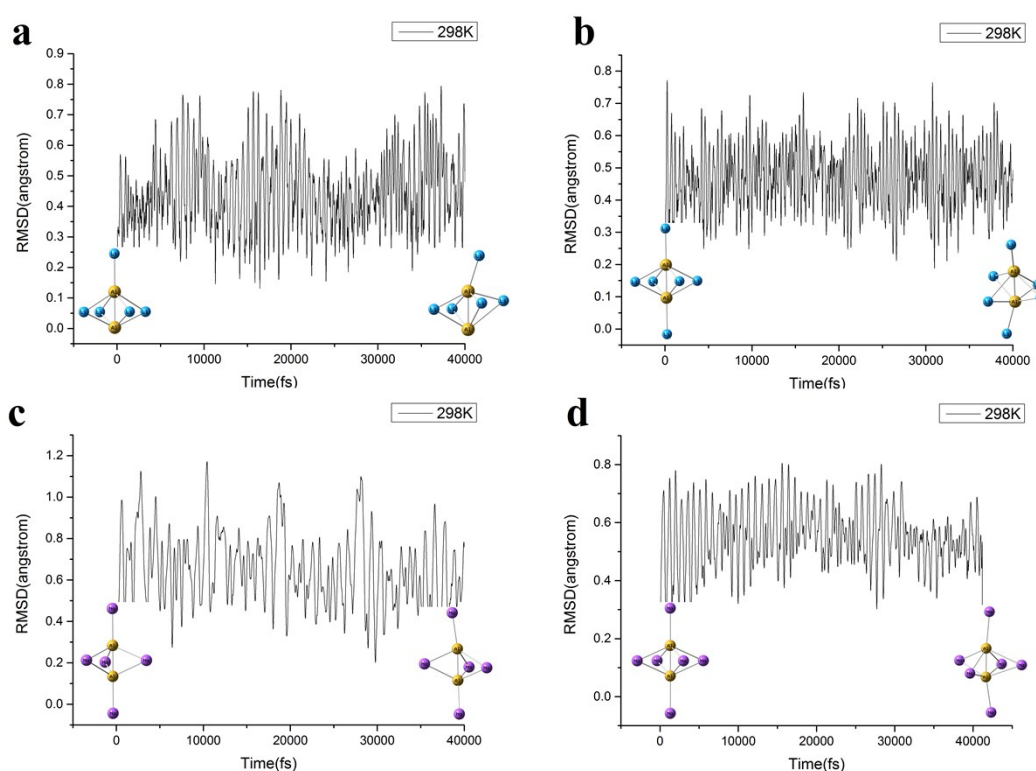


Figure S11. Root-mean-square deviations (RMSD) of Al₂Li₅⁺ (a), Al₂Li₆²⁺ (b), Al₂Na₅⁺ (c) and Al₂Na₆²⁺ (d) during Born-Oppenheimer molecular dynamics (BOMD) simulations at 298K. The initial and final structural snapshots are also shown here.

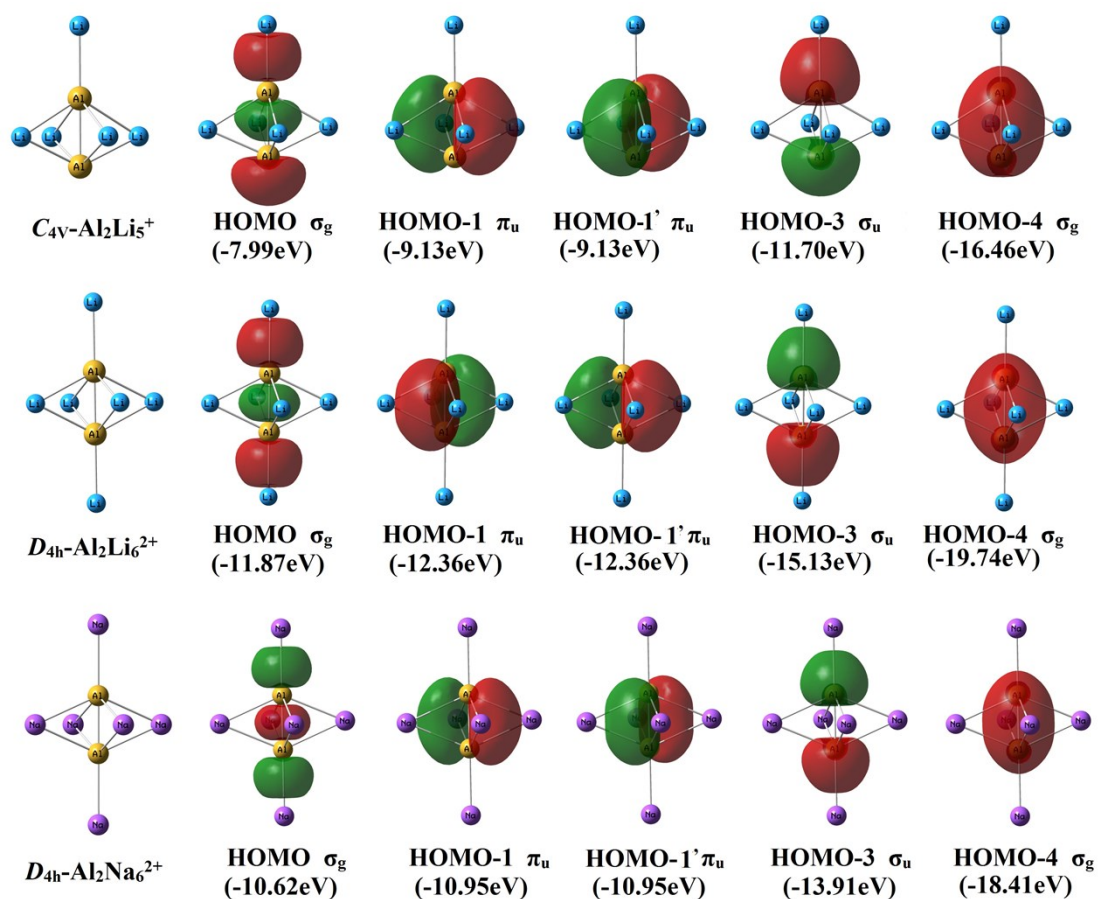


Figure S12. The global minimum of $C_{4v}\text{-Al}_2\text{Li}_5^+$ (a), $D_{4h}\text{-Al}_2\text{Li}_6^{2+}$ (b) and $D_{4h}\text{-Al}_2\text{Na}_6^{2+}$ (c) and their important FMOs at the CCSD/6-311G(d) level.

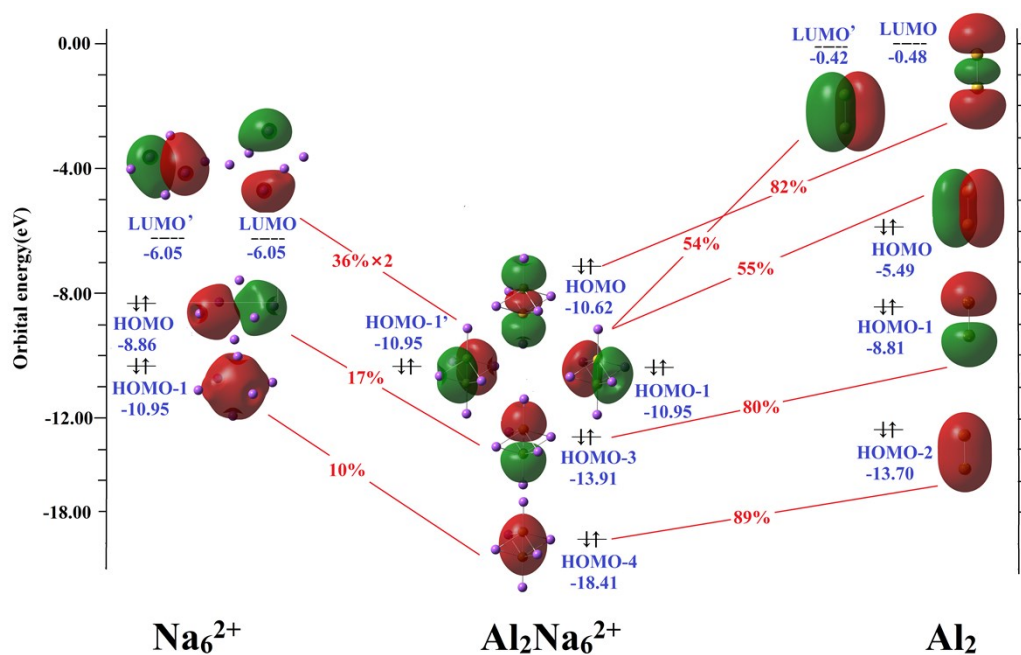


Figure S13. The dominant FMO correlation diagram in $\text{Al}_2\text{Na}_6^{2+}$ between Al_2 and Na_6^{2+} fragments calculated at the CCSD/6-311G(d) level. The horizontal dashed and solid lines represent virtual and occupied molecular orbitals, respectively. (the orbital energies are also given, unit: eV).

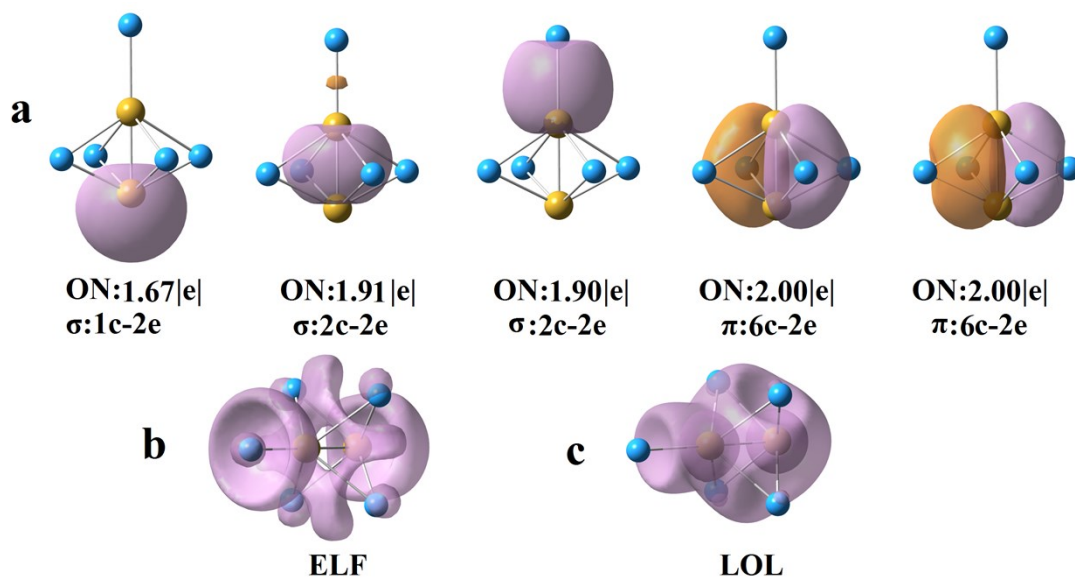


Figure S14. a) AdNDP orbitals. b) LOL profile. c) ELF profile for Al_2Li_5^+ at the CCSD/6-311G(d) level. ON stands for the occupation number.

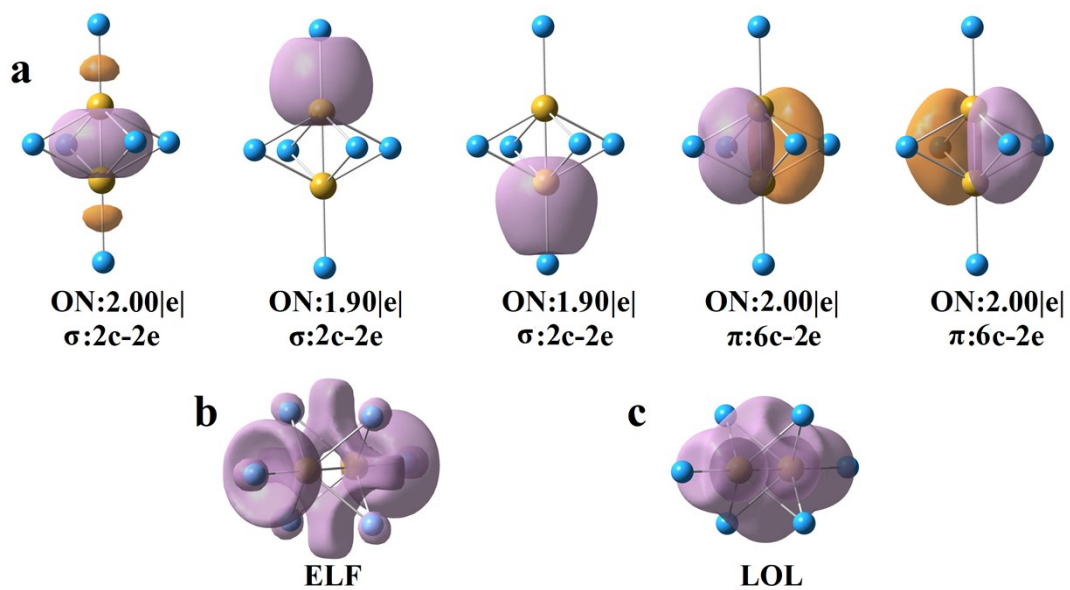


Figure S15. a) AdNDP orbitals. b) LOL profile. c) ELF profile for $\text{Al}_2\text{Li}_6^{2+}$ at the CCSD/6-311G(d) level. ON stands for the occupation number.

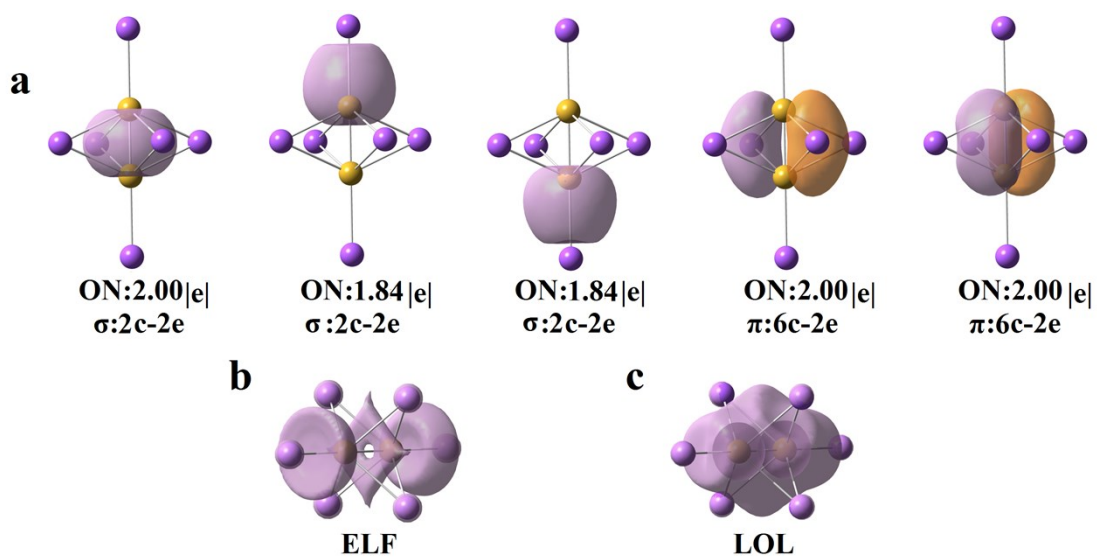


Figure S16. a) AdNDP orbitals. b) LOL profile. c) ELF profile for $\text{Al}_2\text{Na}_6^{2+}$ at the CCSD/6-311G(d) level. ON stands for the occupation number.

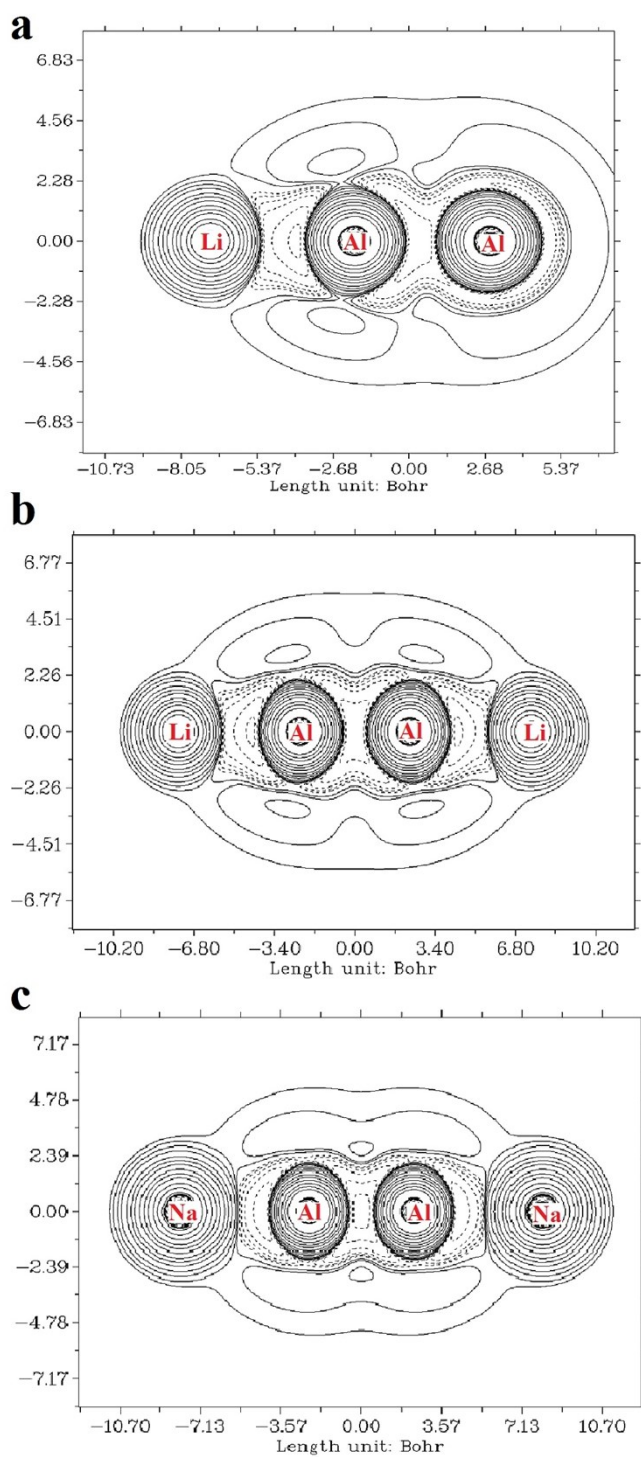


Figure S17. Laplacian plot of the electron density $\nabla^2\rho(r)$, of Al_2Li_5^+ (a), $\text{Al}_2\text{Li}_6^{2+}$ (b), $\text{Al}_2\text{Na}_6^{2+}$ (c) in different perspectives. Solid and dashed lines correspond to positive and negative regions of $\nabla^2\rho$, respectively.

Scheme 1. Several potential reactions and thermodynamic values for the generation of $C_1\text{-Al}_2\text{Li}_5$, $C_{4V}\text{-Al}_2\text{Li}_5^+$, $C_1\text{-Al}_2\text{Li}_6$, $D_{4h}\text{-Al}_2\text{Li}_6^{2+}$, $C_1\text{-Al}_2\text{Na}_5$, $D_{3h}\text{-Al}_2\text{Na}_5^+$, $C_1\text{-Al}_2\text{Na}_6$ and $D_{4h}\text{-Al}_2\text{Na}_6^{2+}$.

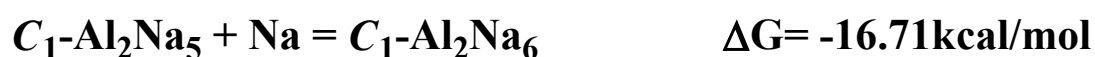
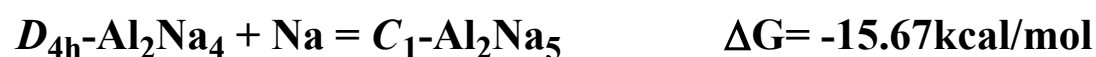
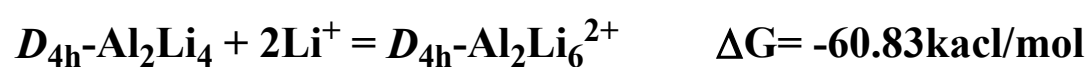


Table S3. Cartesian coordinates for optimized structures of Al_2Li_5^+ , $\text{Al}_2\text{Li}_6^{2+}$, Al_2Na_5^+ , and $\text{Al}_2\text{Na}_6^{2+}$ at the CCSD/6-311G(d) level.

Al_2Li_5^+ (C_{4v} , ^1A)

Li	0.00000000	2.42444450	0.39986648
Li	0.00000000	-2.42444450	0.39986648
Li	0.00000000	-0.00000000	-3.71594610
Li	-2.42444450	-0.00000000	0.39986648
Li	2.42444450	0.00000000	0.39986648
Al	0.00000000	-0.00000000	-1.02113346
Al	0.00000000	0.00000000	1.51055521

$\text{Al}_2\text{Li}_6^{2+}$ (D_{4h} , ^1A)

Li	-0.00000000	2.53027834	0.00000000
Li	-2.53027834	-0.00000000	0.00000000
Li	-0.00000000	-0.00000000	-3.95040198
Li	0.00000000	-0.00000000	3.95040198
Li	2.53027834	0.00000000	0.00000000
Li	0.00000000	-2.53027834	0.00000000
Al	0.00000000	0.00000000	1.23073334
Al	-0.00000000	0.00000000	-1.23073334

Al_2Na_5^+ (D_{3h} , ^1A)

Na	-0.00000000	2.79534858	0.00000000
Na	0.00000000	-0.00000000	-4.13069466
Na	-2.42084289	-1.39767429	0.00000000
Na	2.42084289	-1.39767429	0.00000000
Na	0.00000000	-0.00000000	4.13069466
Al	0.00000000	0.00000000	1.21780642
Al	-0.00000000	0.00000000	-1.21780642

$\text{Al}_2\text{Na}_6^{2+}$ (D_{4h} , ^1A)

Na	0.00000000	0.00000000	4.25676351
Na	-2.88787913	0.00000000	-0.00000000
Na	0.00000000	2.88787913	-0.00000000
Na	0.00000000	-2.88787913	-0.00000000
Na	2.88787913	0.00000000	-0.00000000
Na	-0.00000000	0.00000000	-4.25676351
Al	0.00000000	-0.00000000	-1.23073033
Al	0.00000000	-0.00000000	1.23073033

Table S4. Cartesian coordinates for optimized structures of Al_2Li_5 , Al_2Li_6 , Al_2Na_5 , and Al_2Na_6 at the CCSD/6-311G(d) level.

Al_2Li_5 ($C_1, {}^2A$)			
Li	-1.740339	0.001070	-1.362101
Li	2.123506	-0.001946	1.663363
Li	-4.469773	0.000267	0.000118
Li	-1.740226	-0.001222	1.361546
Al	0.426721	-1.237231	-0.000855
Al	0.427333	1.237518	0.000513
Li	2.125933	0.000588	-1.661446
Al_2Li_6 ($C_1, {}^1A$)			
Li	-1.318905	-0.782612	-1.412557
Li	2.175948	0.669665	1.609724
Li	2.176645	0.670054	-1.609066
Li	-2.686713	1.536697	-0.000032
Li	-4.189791	-1.230047	-0.000014
Li	-1.318715	-0.782506	1.412696
Al	1.211967	-1.124332	-0.000104
Al	-0.020845	1.105582	-0.000069
Al_2Na_5 ($C_1, {}^2A$)			
Na	-1.560299	-1.675054	0.001077
Na	2.857283	1.960853	0.000726
Na	-4.713753	0.000281	-0.000359
Na	-1.559958	1.673405	-0.000185
Al	0.894843	-0.000946	1.254129
Al	0.894688	-0.000418	-1.254557
Na	2.861826	-1.957872	-0.000752
Al_2Na_6 ($C_1, {}^1A$)			
Na	1.585168	-0.448075	1.674544
Na	1.586491	-0.463263	-1.673604
Na	4.769903	-0.352065	0.001093
Na	-0.290169	3.637125	-0.010148
Na	-2.823095	-0.565076	-1.935132
Na	-2.815274	-0.549277	1.943168
Al	-0.863198	0.723637	-0.004620
Al	-0.840131	-1.789257	0.004687