

Supplementary Information (SI)

Synthesis, crystal structure and theoretical calculations of two rare-earth borates with DUV cut-off edges

Qin Ma,^a Tinghao Tong,^b and Zhi Su^{a,*}

^a College of Chemistry and Chemical Engineering, Xinjiang Normal University, Urumqi, 102
Xinyi Road, Xinjiang 830054, P.R. China.

^b Department of Physical Science and Technology, Xinjiang University, Urumqi, Xinjiang 830046,
P. R China.

* Corresponding author, E-mail: suzhixj@sina.com

Table S1. Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{YZnB}_5\text{O}_{10}$. $U(\text{eq})$ is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Atoms	<i>x/a</i>	<i>y/b</i>	<i>z/c</i>	U(e q)	BVS
Y(1)	8154(1)	6813(1)	7597(1)	6(1)	3.00
Zn(1)	8943(1)	5915(1)	3728(1)	7(1)	1.89
B(1)	5648(2)	6877(2)	888(2)	6(1)	2.92
B(2)	7772(2)	4680(2)	577(2)	6(1)	3.00
B(3)	5825(2)	4270(2)	2466(2)	6(1)	3.00
B(4)	4815(2)	1758(2)	3973(2)	5(1)	3.03
B(5)	6613(2)	3971(2)	5096(2)	6(1)	3.05
O(1)	4917(1)	8481(2)	709(1)	7(1)	1.81
O(2)	6808(1)	6253(2)	96(1)	7(1)	1.89
O(3)	8233(1)	3911(2)	-791(1)	6(1)	2.09
O(4)	6818(1)	3515(2)	1400(1)	6(1)	2.01
O(5)	5106(1)	5932(2)	1997(1)	7(1)	2.15
O(6)	4609(1)	2980(2)	2750(1)	6(1)	2.06
O(7)	6839(1)	4680(2)	3782(1)	7(1)	2.04
O(8)	5832(1)	300(2)	3493(1)	6(1)	1.87
O(9)	7459(1)	4423(2)	6293(1)	7(1)	1.87
O(10)	5476(1)	2677(2)	5236(1)	6(1)	2.09

Table S2. Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for $\text{GdZnB}_5\text{O}_{10}$. $U(\text{eq})$ is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Atoms	x/a	y/b	z/c	$U(\text{e q})$	BVS
Gd(1)	4463(1)	6825(1)	2624(1)	5(1)	2.94
Zn(1)	9824(1)	5898(1)	8748(1)	7(1)	1.91
B(1)	7753(7)	4677(7)	5540(5)	5(1)	2.96
B(2)	5887(8)	6739(6)	6062(6)	4(1)	3.06
B(3)	10193(8)	6877(6)	5870(6)	5(1)	3.09
B(4)	11583(8)	4243(6)	7406(5)	5(1)	3.09
B(5)	6530(8)	8990(6)	4960(5)	5(1)	3.05
O(1)	7323(4)	5276(4)	6480(3)	5(1)	1.82
O(2)	9521(5)	3505(4)	6347(3)	5(1)	2.09
O(3)	5239(5)	7718(4)	4813(3)	4(1)	1.94
O(4)	6967(5)	7915(4)	7316(3)	5(1)	2.10
O(5)	11890(5)	4663(4)	8721(3)	6(1)	2.04
O(6)	10751(5)	8477(4)	5708(3)	6(1)	2.13
O(7)	6160(5)	9495(4)	3772(3)	7(1)	2.06
O(8)	5924(5)	3929(4)	4175(3)	5(1)	2.03
O(9)	8259(5)	6272(4)	5096(3)	7(1)	1.94
O(10)	11837(5)	5893(4)	6945(3)	6(1)	1.94

Table S3. Bond lengths [Å] and angles [deg] for YZnB₅O₁₀.

Y(1)-O(9)	2.2444(12)	B(1)-O(5)	1.366(2)
Y(1)-O(9)#1	2.3124(12)	B(1)-O(1)	1.373(2)
Y(1)-O(6)#2	2.3598(12)	B(2)-O(4)	1.455(2)
Y(1)-O(10)#1	2.3637(12)	B(2)-O(3)	1.482(2)
Y(1)-O(1)#3	2.4024(12)	B(2)-O(2)	1.501(2)
Y(1)-O(5)#3	2.4768(12)	B(2)-O(8)#4	1.502(2)
Y(1)-O(3)#4	2.5545(12)	B(3)-O(5)	1.458(2)
Y(1)-O(3)#5	2.6678(12)	B(3)-O(6)	1.462(2)
Y(1)-O(2)#5	2.7034(12)	B(3)-O(4)	1.466(2)
Y(1)-O(8)#6	2.8689(12)	B(3)-O(7)	1.490(2)
Zn(1)-O(7)	2.0265(12)	B(4)-O(10)	1.454(2)
Zn(1)-O(1)#3	2.0318(13)	B(4)-O(3)#8	1.471(2)
Zn(1)-O(4)#4	2.0794(12)	B(4)-O(6)	1.474(2)
Zn(1)-O(1)#7	2.1374(12)	B(4)-O(8)	1.493(2)
Zn(1)-O(8)#4	2.1503(12)	B(5)-O(9)	1.337(2)
Zn(1)-O(6)#4	2.4731(12)	B(5)-O(7)	1.366(2)
B(1)-O(2)	1.359(2)	B(5)-O(10)	1.391(2)
O(9)-Y(1)-O(9)#1	151.341(13)	O(3)#4-Y(1)-O(8)#6	150.04(4)
O(9)-Y(1)-O(6)#2	75.74(4)	O(3)#5-Y(1)-O(8)#6	51.91(3)
O(9)#1-Y(1)-O(6)#2	75.65(4)	O(2)#5-Y(1)-O(8)#6	91.92(3)
O(9)-Y(1)-O(10)#1	142.01(4)	O(7)-Zn(1)-O(1)#3	113.01(5)
O(9)#1-Y(1)-O(10)#1	59.39(4)	O(7)-Zn(1)-O(4)#4	99.66(5)
O(6)#2-Y(1)-O(10)#1	122.09(4)	O(1)#3-Zn(1)-O(4)#4	86.88(5)
O(9)-Y(1)-O(1)#3	71.39(4)	O(7)-Zn(1)-O(1)#7	88.97(5)
O(9)#1-Y(1)-O(1)#3	125.44(4)	O(1)#3-Zn(1)-O(1)#7	79.57(5)
O(6)#2-Y(1)-O(1)#3	124.81(4)	O(4)#4-Zn(1)-O(1)#7	165.99(5)
O(10)#1-Y(1)-O(1)#3	111.02(4)	O(7)-Zn(1)-O(8)#4	93.34(5)
O(9)-Y(1)-O(5)#3	126.38(4)	O(1)#3-Zn(1)-O(8)#4	150.81(5)
O(9)#1-Y(1)-O(5)#3	71.57(4)	O(4)#4-Zn(1)-O(8)#4	101.39(5)
O(6)#2-Y(1)-O(5)#3	126.94(4)	O(1)#7-Zn(1)-O(8)#4	89.00(5)
O(10)#1-Y(1)-O(5)#3	72.62(4)	O(7)-Zn(1)-O(6)#4	141.42(5)
O(1)#3-Y(1)-O(5)#3	55.69(4)	O(1)#3-Zn(1)-O(6)#4	100.23(4)
O(9)-Y(1)-O(3)#4	92.93(4)	O(4)#4-Zn(1)-O(6)#4	62.00(4)
O(9)#1-Y(1)-O(3)#4	69.75(4)	O(1)#7-Zn(1)-O(6)#4	116.80(4)
O(6)#2-Y(1)-O(3)#4	56.89(4)	O(8)#4-Zn(1)-O(6)#4	61.21(4)
O(10)#1-Y(1)-O(3)#4	125.06(4)	O(2)-B(1)-O(5)	121.62(15)
O(1)#3-Y(1)-O(3)#4	81.73(4)	O(2)-B(1)-O(1)	125.69(16)
O(5)#3-Y(1)-O(3)#4	72.96(4)	O(5)-B(1)-O(1)	112.68(15)
O(9)-Y(1)-O(3)#5	68.59(4)	O(4)-B(2)-O(3)	113.94(14)
O(9)#1-Y(1)-O(3)#5	116.90(4)	O(4)-B(2)-O(2)	109.19(13)
O(6)#2-Y(1)-O(3)#5	96.93(4)	O(3)-B(2)-O(2)	103.05(13)
O(10)#1-Y(1)-O(3)#5	75.67(4)	O(4)-B(2)-O(8)#4	109.38(14)

O(1)#3-Y(1)-O(3)#5	110.17(4)	O(3)-B(2)-O(8)#4	112.27(13)
O(5)#3-Y(1)-O(3)#5	134.97(4)	O(2)-B(2)-O(8)#4	108.71(13)
O(3)#4-Y(1)-O(3)#5	151.89(2)	O(5)-B(3)-O(6)	110.24(13)
O(9)-Y(1)-O(2)#5	103.34(4)	O(5)-B(3)-O(4)	112.54(14)
O(9)#1-Y(1)-O(2)#5	68.04(4)	O(6)-B(3)-O(4)	108.01(13)
O(6)#2-Y(1)-O(2)#5	69.75(4)	O(5)-B(3)-O(7)	106.09(13)
O(10)#1-Y(1)-O(2)#5	61.07(4)	O(6)-B(3)-O(7)	111.68(14)
O(1)#3-Y(1)-O(2)#5	160.36(4)	O(4)-B(3)-O(7)	108.31(13)
O(5)#3-Y(1)-O(2)#5	129.33(4)	O(10)-B(4)-O(3)#8	110.72(14)
O(3)#4-Y(1)-O(2)#5	117.76(4)	O(10)-B(4)-O(6)	110.40(13)
O(3)#5-Y(1)-O(2)#5	51.54(4)	O(3)#8-B(4)-O(6)	105.69(13)
O(9)-Y(1)-O(8)#6	83.28(4)	O(10)-B(4)-O(8)	113.48(13)
O(9)#1-Y(1)-O(8)#6	123.15(4)	O(3)#8-B(4)-O(8)	110.14(13)
O(6)#2-Y(1)-O(8)#6	147.59(4)	O(6)-B(4)-O(8)	106.02(13)
O(10)#1-Y(1)-O(8)#6	64.31(4)	O(9)-B(5)-O(7)	123.52(15)
O(1)#3-Y(1)-O(8)#6	68.86(4)	O(9)-B(5)-O(10)	116.25(15)
O(5)#3-Y(1)-O(8)#6	85.42(4)	O(7)-B(5)-O(10)	120.22(15)

Symmetry transformations used to generate equivalent atoms:

#1 $-x+3/2, y+1/2, -z+3/2$	#2 $-x+1, -y+1, -z+1$
#3 $x+1/2, -y+3/2, z+1/2$	#4 $-x+3/2, y+1/2, -z+1/2$
#5 $x, y, z+1$	#6 $x+1/2, -y+1/2, z+1/2$
#7 $-x+3/2, y-1/2, -z+1/2$	#8 $x-1/2, -y+1/2, z+1/2$
#9 $-x+2, -y+1, -z+1$	#10 $x-1/2, -y+3/2, z-1/2$
#11 $-x+3/2, y-1/2, -z+3/2$	#12 $x, y, z-1$
#13 $x+1/2, -y+1/2, z-1/2$	#14 $x-1/2, -y+1/2, z-1/2$

Table S4. Bond lengths [\AA] and angles [deg] for $\text{GdZnB}_5\text{O}_{10}$.

Gd(1)-O(1)	2.2778(17)	B(1)-O(5)	1.472(3)
Gd(1)-O(1)#1	2.3580(17)	B(1)-O(4)	1.474(3)
Gd(1)-O(2)#1	2.4175(17)	B(1)-O(3)	1.487(3)
Gd(1)-O(5)#2	2.4201(18)	B(2)-O(1)	1.336(3)
Gd(1)-O(10)#3	2.4512(18)	B(2)-O(6)	1.365(3)
Gd(1)-O(7)#3	2.5124(17)	B(2)-O(2)	1.392(3)
Gd(1)-O(4)#2	2.5782(17)	B(3)-O(7)	1.459(3)
Gd(1)-O(4)#4	2.6358(17)	B(3)-O(8)	1.463(3)
Gd(1)-O(9)#5	2.6742(18)	B(3)-O(5)	1.467(3)
Gd(1)-O(3)#4	2.8841(17)	B(3)-O(6)	1.495(3)
Zn(1)-O(6)	2.0304(17)	B(4)-O(8)	1.453(3)
Zn(1)-O(10)#3	2.0491(18)	B(4)-O(4)#8	1.483(3)
Zn(1)-O(8)#6	2.0813(18)	B(4)-O(3)#6	1.496(3)
Zn(1)-O(10)#7	2.1147(18)	B(4)-O(9)	1.501(3)
Zn(1)-O(3)#6	2.1962(17)	B(5)-O(9)	1.359(3)
Zn(1)-O(5)#6	2.4216(18)	B(5)-O(7)	1.369(3)
B(1)-O(2)	1.456(3)	B(5)-O(10)	1.374(3)
O(1)-Gd(1)-O(1)#1	150.685(19)	O(4)#2-Gd(1)-O(3)#4	150.42(5)
O(1)-Gd(1)-O(2)#1	145.14(6)	O(4)#4-Gd(1)-O(3)#4	51.85(5)
O(1)#1-Gd(1)-O(2)#1	58.32(6)	O(9)#5-Gd(1)-O(3)#4	91.87(5)
O(1)-Gd(1)-O(5)#2	74.96(6)	O(6)-Zn(1)-O(10)#3	116.87(7)
O(1)#1-Gd(1)-O(5)#2	76.03(6)	O(6)-Zn(1)-O(8)#6	99.50(7)
O(2)#1-Gd(1)-O(5)#2	121.64(6)	O(10)#3-Zn(1)-O(8)#6	86.52(7)
O(1)-Gd(1)-O(10)#3	71.09(6)	O(6)-Zn(1)-O(10)#7	89.52(7)
O(1)#1-Gd(1)-O(10)#3	124.89(6)	O(10)#3-Zn(1)-O(10)#7	79.28(8)
O(2)#1-Gd(1)-O(10)#3	110.23(6)	O(8)#6-Zn(1)-O(10)#7	165.53(7)
O(5)#2-Gd(1)-O(10)#3	125.83(6)	O(6)-Zn(1)-O(3)#6	91.27(7)
O(1)-Gd(1)-O(7)#3	124.37(6)	O(10)#3-Zn(1)-O(3)#6	149.06(7)
O(1)#1-Gd(1)-O(7)#3	71.19(6)	O(8)#6-Zn(1)-O(3)#6	102.04(7)
O(2)#1-Gd(1)-O(7)#3	73.50(6)	O(10)#7-Zn(1)-O(3)#6	88.95(7)
O(5)#2-Gd(1)-O(7)#3	125.74(6)	O(6)-Zn(1)-O(5)#6	139.93(7)
O(10)#3-Gd(1)-O(7)#3	54.88(6)	O(10)#3-Zn(1)-O(5)#6	98.55(7)
O(1)-Gd(1)-O(4)#2	89.69(6)	O(8)#6-Zn(1)-O(5)#6	62.76(7)
O(1)#1-Gd(1)-O(4)#2	70.56(6)	O(10)#7-Zn(1)-O(5)#6	116.37(7)
O(2)#1-Gd(1)-O(4)#2	125.16(5)	O(3)#6-Zn(1)-O(5)#6	61.27(6)
O(5)#2-Gd(1)-O(4)#2	56.15(6)	O(2)-B(1)-O(5)	110.55(19)
O(10)#3-Gd(1)-O(4)#2	82.57(6)	O(2)-B(1)-O(4)	110.1(2)
O(7)#3-Gd(1)-O(4)#2	72.51(5)	O(5)-B(1)-O(4)	106.2(2)
O(1)-Gd(1)-O(4)#4	70.66(6)	O(2)-B(1)-O(3)	114.0(2)
O(1)#1-Gd(1)-O(4)#4	117.62(6)	O(5)-B(1)-O(3)	105.8(2)
O(2)#1-Gd(1)-O(4)#4	76.52(6)	O(4)-B(1)-O(3)	109.83(19)
O(5)#2-Gd(1)-O(4)#4	97.54(5)	O(1)-B(2)-O(6)	122.9(2)

O(10)#3-Gd(1)-O(4)#4	109.06(6)	O(1)-B(2)-O(2)	117.1(2)
O(7)#3-Gd(1)-O(4)#4	135.82(5)	O(6)-B(2)-O(2)	120.0(2)
O(4)#2-Gd(1)-O(4)#4	151.30(3)	O(7)-B(3)-O(8)	112.6(2)
O(1)-Gd(1)-O(9)#5	104.63(6)	O(7)-B(3)-O(5)	110.7(2)
O(1)#1-Gd(1)-O(9)#5	68.45(6)	O(8)-B(3)-O(5)	107.5(2)
O(2)#1-Gd(1)-O(9)#5	61.57(6)	O(7)-B(3)-O(6)	105.93(19)
O(5)#2-Gd(1)-O(9)#5	69.40(6)	O(8)-B(3)-O(6)	108.4(2)
O(10)#3-Gd(1)-O(9)#5	159.84(6)	O(5)-B(3)-O(6)	111.7(2)
O(7)#3-Gd(1)-O(9)#5	130.58(5)	O(8)-B(4)-O(4)#8	113.7(2)
O(4)#2-Gd(1)-O(9)#5	117.43(5)	O(8)-B(4)-O(3)#6	109.6(2)
O(4)#4-Gd(1)-O(9)#5	52.23(5)	O(4)#8-B(4)-O(3)#6	112.6(2)
O(1)-Gd(1)-O(3)#4	86.37(6)	O(8)-B(4)-O(9)	109.1(2)
O(1)#1-Gd(1)-O(3)#4	121.49(5)	O(4)#8-B(4)-O(9)	103.11(19)
O(2)#1-Gd(1)-O(3)#4	63.79(5)	O(3)#6-B(4)-O(9)	108.49(19)
O(5)#2-Gd(1)-O(3)#4	148.56(5)	O(9)-B(5)-O(7)	121.3(2)
O(10)#3-Gd(1)-O(3)#4	68.42(5)	O(9)-B(5)-O(10)	125.6(2)
O(7)#3-Gd(1)-O(3)#4	85.67(5)	O(7)-B(5)-O(10)	113.1(2)

Symmetry transformations used to generate equivalent atoms:

#1 $-x+1/2, y+1/2, -z+1/2$	#2 $-x+1, -y+1, -z+1$
#3 $x-1/2, -y+3/2, z-1/2$	#4 $x-1/2, -y+1/2, z-1/2$
#5 $x, y, z-1$	#6 $-x+1/2, y+1/2, -z+3/2$
#7 $-x+1/2, y-1/2, -z+3/2$	#8 $x-1/2, -y+1/2, z+1/2$
#9 $-x, -y+1, -z+1$	#10 $-x+1/2, y-1/2, -z+1/2$
#11 $x+1/2, -y+3/2, z+1/2$	#12 $x+1/2, -y+1/2, z+1/2$
#13 $x+1/2, -y+1/2, z-1/2$	#14 $x, y, z+1$

Fig. S1. The picture is under a microscope of (a) $\text{YZnB}_5\text{O}_{10}$, (b) $\text{GdZnB}_5\text{O}_{10}$.

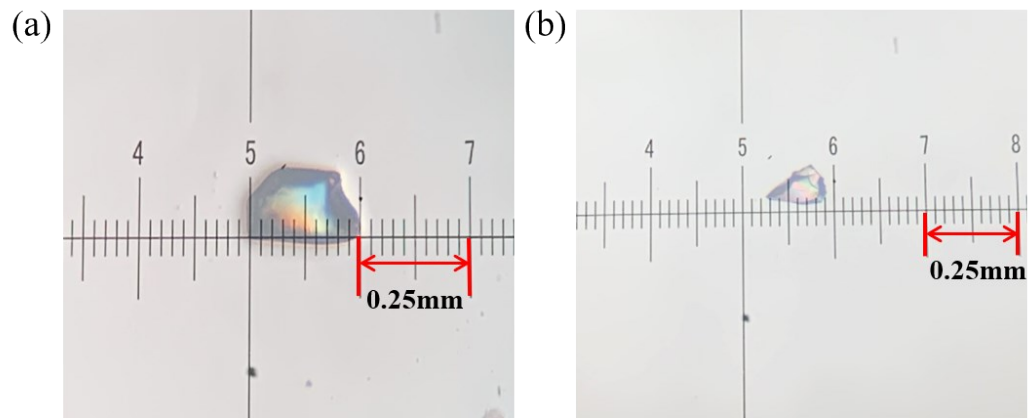


Fig. S2. Calculated and experimental XRD patterns of (a) $\text{YZnB}_5\text{O}_{10}$, (b) $\text{GdZnB}_5\text{O}_{10}$.

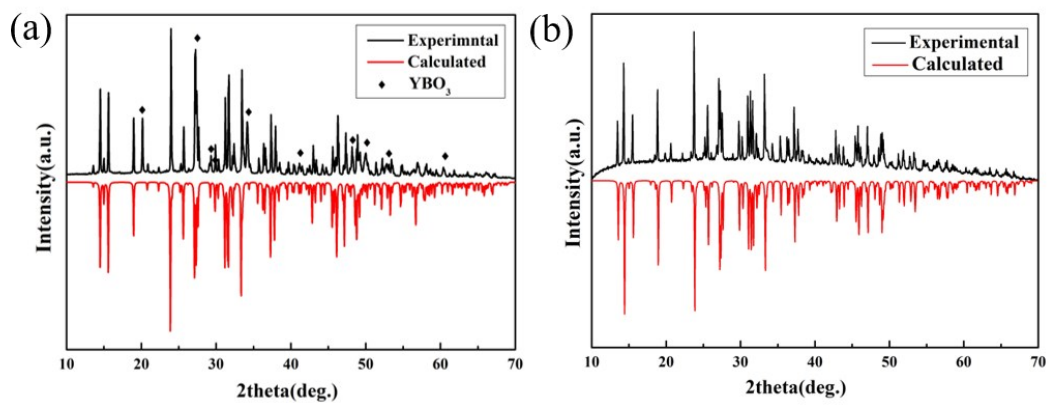


Fig. S3. (a) Cation coordination environment of Zn in the $\text{YZnB}_5\text{O}_{10}$, (b) Cation coordination environment of Y in the $\text{YZnB}_5\text{O}_{10}$.

