

## Supporting Information

### **Evolutionary structure predicted assisted design of anode materials for Ca-ion battery based on phosphorene**

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1. Cartesian coordinates for the allotropes of phosphorene.

(A)  $\alpha$  Pn

P 1.675407887 0.382691860 6.375204086

P 0.000000000 1.862238646 6.375204086

P 1.675407887 4.107169151 4.263043404

P 0.000000000 2.627622366 4.263043404

a=3.35 Å, b= 4.49 Å.

(B)  $\beta$  Pn

P 0.66481257 1.72061050 4.78454992

P -0.97963745 2.67011927 3.54986464

a=3.28897 Å, b= 3.28897 Å.

(C)  $\gamma$  Pn

P 0.00000000 0.08571784 10.35762000

P 0.00000000 2.42022295 10.35762000

P 1.63500000 2.84991784 11.84238000

P 1.63500000 5.18442295 11.84238000

a=3.27 Å, b= 5.528 Å.

(D)  $\delta$  Pn

P 0.03061958 0.47983824 10.40284000

P 0.03061958 2.79288784 10.40284000

P 2.21229374 5.61129348 10.40284000

P 2.21229374 3.29823260 10.40284000

P 2.80061404 0.47983260 12.52716000

P 2.80061404 2.79289348 12.52716000

P	4.98228820	5.61128784	12.52716000
P	4.98228820	3.29823824	12.52716000

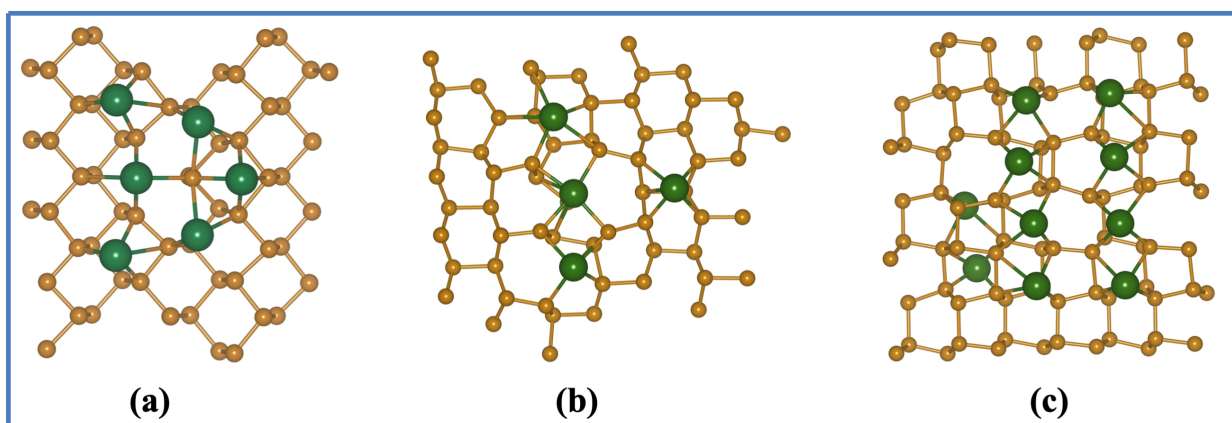
a=5.54 Å, b= 5.5368 Å.

(E)  $\zeta$  Pn

P	0.58378578	3.69027624	6.74649000
P	2.30621422	3.69027624	8.25351000
P	5.19621422	5.63972376	6.74649000
P	3.47378578	5.63972376	8.25351000
P	5.19621422	2.52972376	8.25351000
P	3.47378578	2.52972376	6.74649000
P	0.58378578	0.58027624	8.25351000
P	2.30621422	0.58027624	6.74649000

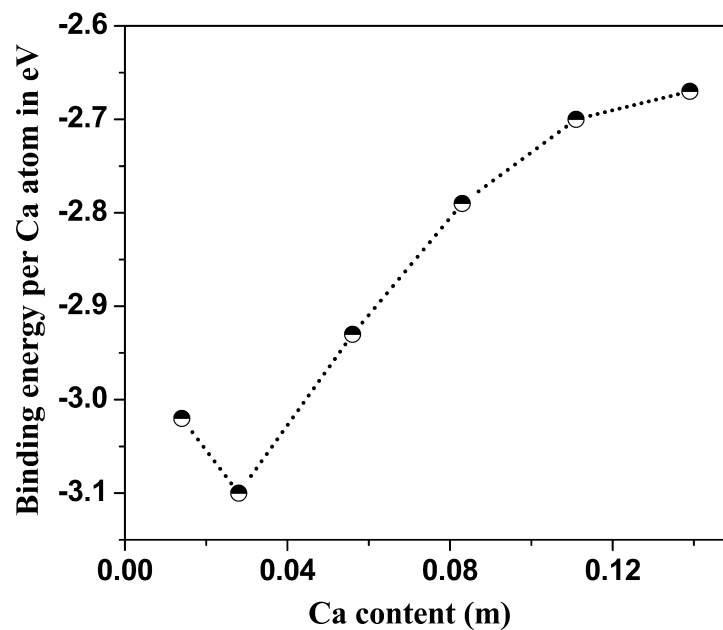
a=5.78 Å, b= 6.22 Å.

2. Fully calcinated structures of alpha, gamma and delta phases of phosphorene.



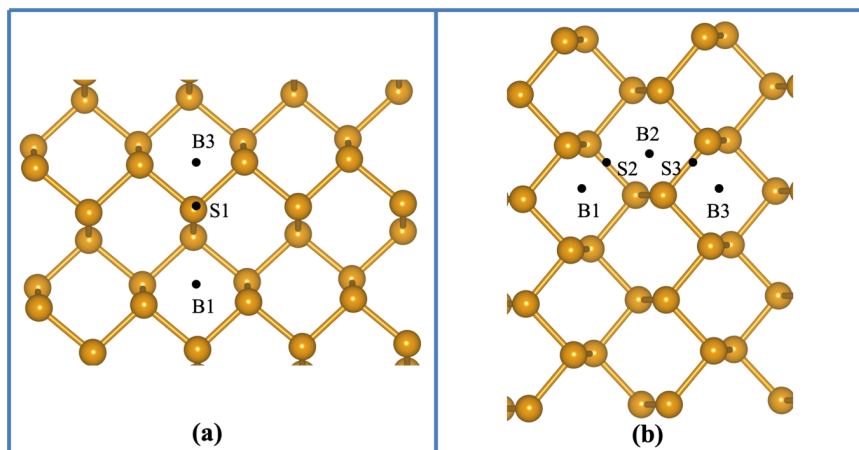
**Figure S1:** Fully calcium intercalated (a) alpha ( $Ca_{0.125}P$ ) (b) gamma ( $Ca_{0.083}P$ ) and (c) delta-phases ( $Ca_{0.139}P$ ) of phosphorene.

3. Variation of binding energy with Ca content of  $\delta$ -phase of phosphorene.



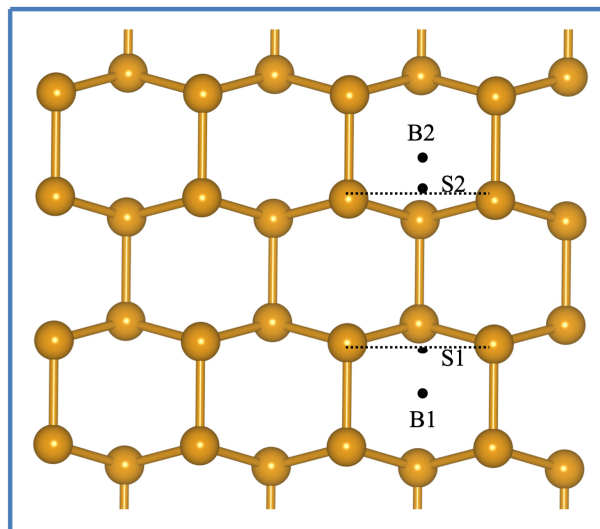
**Figure S2:** Variation of binding energy with Ca content of  $\delta$ -phase of phosphorene.

4. Detailed minimum energy pathway for Ca diffusion along armchair and zigzag direction of  $\alpha$ -allotrope.



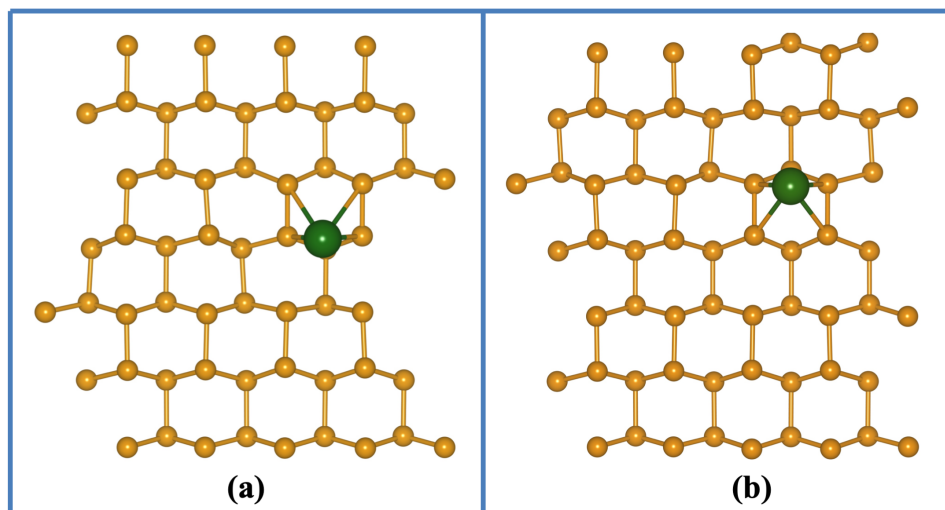
**Figure S3:** Detailed minimum energy pathway for Ca diffusion along (a) armchair and (b) zigzag direction of  $\alpha$ -allotrope.

5. Detailed minimum energy pathway for Ca diffusion along zigzag direction of  $\gamma$ -phase.



*Figure S4: Detailed minimum energy pathway for Ca diffusion along zigzag direction of  $\gamma$ -phase.*

6. Structures of saddle points during diffusion of Ca along zigzag direction of  $\gamma$ -allotrope.



*Figure S5: Structures of saddle points during diffusion of Ca along zigzag direction of  $\gamma$ -allotrope.*

7. Convergence test of  $k$ -point mesh for  $\alpha$ -phase.

**Table S1:**

k-point grid	Binding energy of Ca (eV)
$4 \times 4 \times 1$	-2.47
$5 \times 5 \times 1$	-2.56
$6 \times 6 \times 1$	-2.57
$7 \times 7 \times 1$	-2.57

8. Cartesian co-ordinates for the structures generated using evolutionary structure prediction algorithm with lattice parameters and their corresponding energies calculated using plane wave methods (DFT-D2).

**(A)  $\text{Ca}_3\text{P}_2$**

Ca	1.15787216	2.04312495	3.51284057
Ca	-1.21243905	3.37523322	5.92647873
Ca	3.52124304	0.69305972	1.10052338
P	3.45642802	0.65932947	5.13576165
P	-1.15249264	3.41000164	1.89283692

$a=4.71587 \text{ \AA}$ ,  $b=4.67724 \text{ \AA}$ ,  $c=7.06422 \text{ \AA}$ ;  $\alpha=90.01012^\circ$ ,  $\beta=90.37836^\circ$ ,  $\gamma=119.66444^\circ$

**(B)  $\text{Ca}_4\text{P}_4$**

Ca	3.53996500	1.24847404	1.42515848
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Ca	1.75432561	2.88798059	6.27057140
Ca	-0.70083202	1.82703063	8.41881815
Ca	1.08728531	0.19583187	3.57674680
P	0.76903033	2.49117517	1.62606960
P	2.06712885	0.59418142	8.22343758
P	0.72005110	0.11943845	6.47468850
P	2.13234752	2.94530734	3.36984990

a=5.40778 Å, b= 4.34652 Å, c= 9.89737 Å;  $\alpha$ = 88.64252°,  $\beta$ = 101.36213°,  $\gamma$ = 113.32098°

**(C) Ca<sub>4</sub>P<sub>7</sub>**

Ca	2.43790297	1.63109014	2.24649235
Ca	4.89066066	4.44336398	0.89155278
Ca	0.34790886	3.98183007	4.40389390
Ca	2.95420825	6.56919385	5.93952265
P	1.54885006	1.23747806	5.14160296
P	1.96770702	4.52512333	1.96137314
P	2.08493941	2.79519410	6.61037958
P	5.15645472	1.55999543	0.26268710
P	3.50280414	5.49559017	3.22926379
P	5.34513193	1.90943731	2.42031792
P	4.06142577	3.82922666	6.30830911

a=6.0205 Å, b= 5.858445 Å, c= 7.36062 Å;  $\alpha$ = 79.61485°,  $\beta$ = 84.77111°,  $\gamma$ = 104.7499°

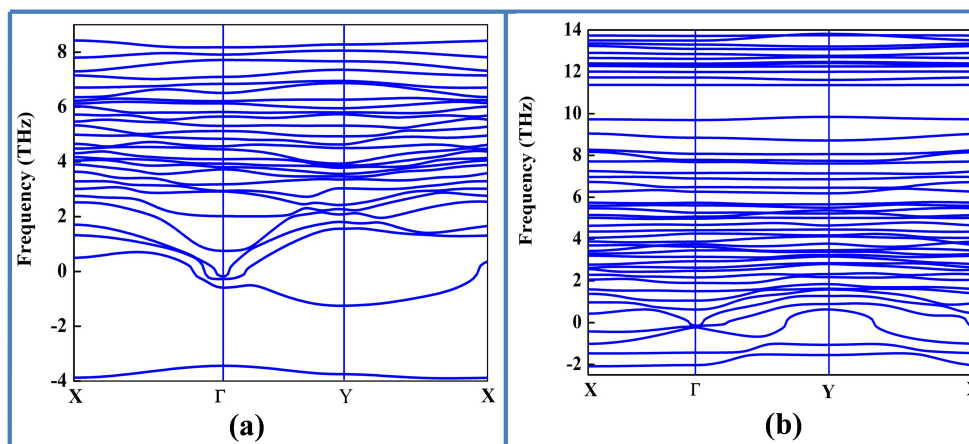
**(D) Ca<sub>4</sub>P<sub>12</sub>**

Ca	1.85884834	1.69035540	0.68039477
Ca	4.34027544	1.78972195	4.03322197
Ca	3.68179458	5.19632801	8.25901051
Ca	0.55540068	5.48701196	4.82032306
P	4.29303965	1.51282094	7.42753719
P	2.42073687	1.89949357	6.29955982
P	1.13844544	5.57178922	1.50840706
P	3.02821616	5.45302699	2.72776458
P	3.95486646	7.25046115	1.76534884
P	0.29556184	3.72378196	2.43016009
P	1.42706901	3.44108877	7.48613515
P	4.12683387	7.13289026	6.11379995
P	1.90642946	-0.23829308	6.76185625
P	5.20786590	3.26846986	6.48848787
P	3.92635182	3.69291687	1.66874164
P	0.31699858	7.35776711	2.54443631



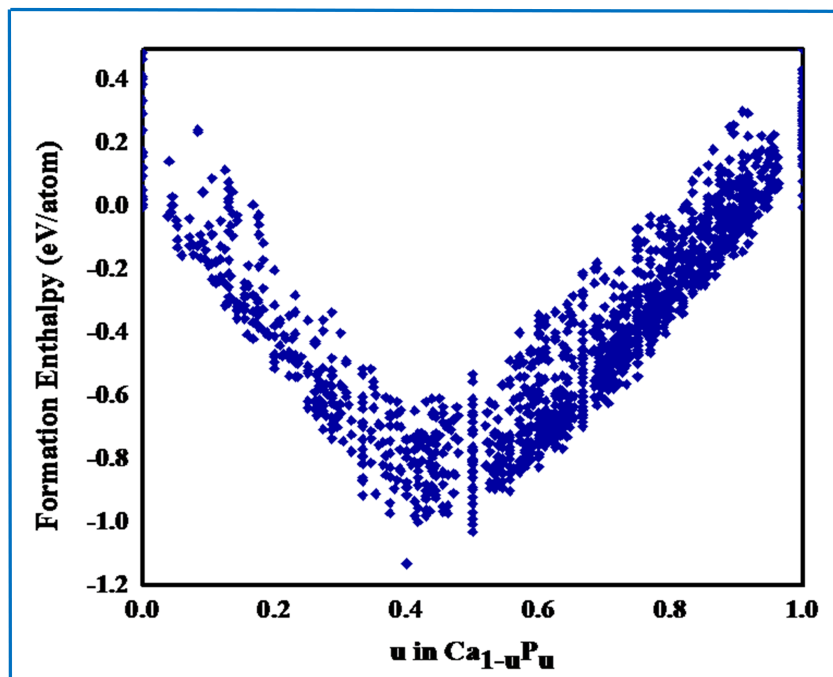
$a=5.7076 \text{ \AA}$ ,  $b= 7.47315 \text{ \AA}$ ,  $c= 8.89302 \text{ \AA}$ ;  $\alpha= 92.2923^\circ$ ,  $\beta= 92.92014^\circ$ ,  $\gamma= 89.69074^\circ$

9. Phonon spectrums of other two structures originated from evolutionary structure prediction algorithm.



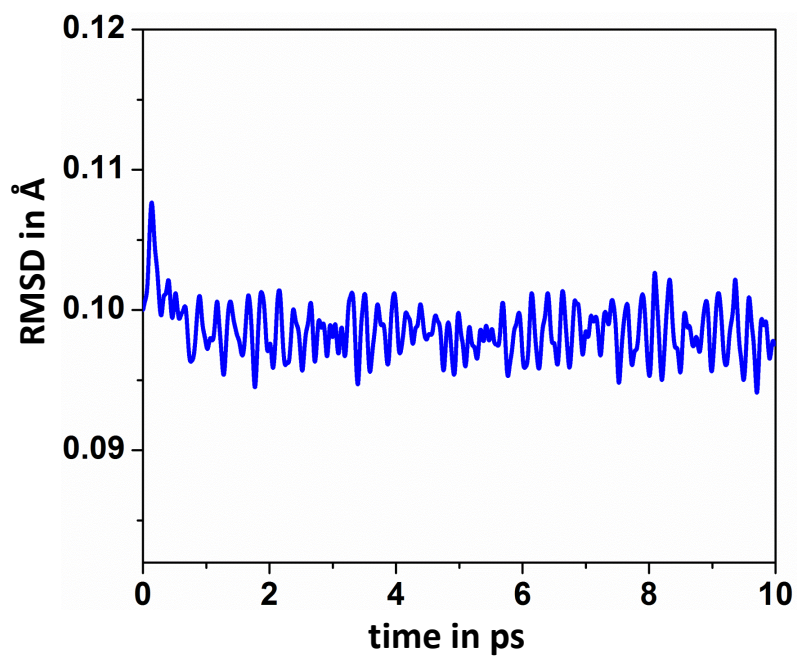
*Figure S6: Phonon dispersion curve of (a)  $\text{Ca}_4\text{P}_7$  and (b)  $\text{Ca}_4\text{P}_{12}$  phases*

10. Convex curve taking possible phases of all the 2319 structures.

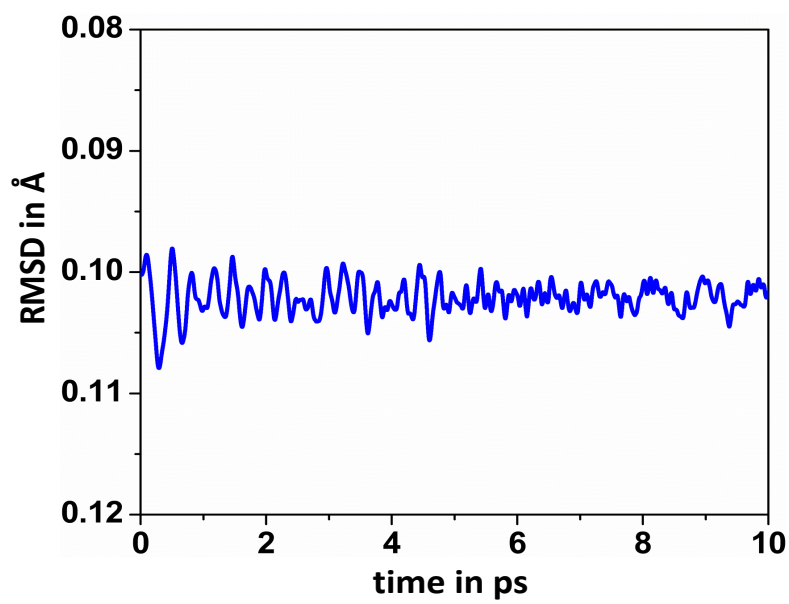


*Figure S7: Convex curve taking all possible 2319 structures.*

## 11. RMSD plots for $\text{Ca}_3\text{P}_2$ and $\text{Ca}_4\text{P}_4$



*Figure S8:* Plot of RMSD with time for  $\text{Ca}_3\text{P}_2$  at 300 K.



*Figure S9:* RMSD plot for  $\text{Ca}_4\text{P}_4$  at 300 K.