

**Supplementary Materials for
Catalytic sulfate formation mechanism influenced by important
constituents of cloud water via the reaction of SO₂ oxidized by
hypobromic acid in marine areas**

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Section 1. Theoretical method

1.1 Aqueous concentration of S(IV)

For reactant S(IV), the ratio of the distribution of different forms (HOSO_2^- , SO_3^{2-}) is important for identifying the possible oxidation reaction, and thus should be calculated. The corresponding computational methods about the ratio of the distribution of different forms (HOSO_2^- , SO_3^{2-}) has been discussed in our previous work.¹

1.2 Aqueous concentration of hypobromic acid

For the reactant HOBr, the aqueous $[\text{HOBr}]$ can also estimate based on the gas-phase mixing ratio using Henry's law

$$[\text{HOBr}] = p(\text{HOBr}) \times H(\text{HOBr}) \quad (1)$$

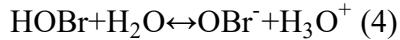
where $p(\text{HOBr})$ is the partial pressure of HOBr in the gas phase and $H(\text{HOBr})$ is the Henry's constant which has been measured from laboratory experiment and reported to be about $1900 \text{ M}^1 \text{ atm}^{-1}$.²

Moreover, according to measurement results, the gas phase ground-level mixing ratio HOBr varies between about 0.01 ppbv and 0.310 ppbv. The corresponding partial pressures $p(\text{HOBr})$ are $1.00 \times 10^{-11} \text{ atm}$ - $3.10 \times 10^{-10} \text{ atm}$

$$[\text{HOBr}] = 1.00 \times 10^{-11} \text{ atm} \times 1900 \text{ M}^1 \text{ atm}^{-1} = 1.90 \times 10^{-8} \text{ M} \quad (2)$$

$$[\text{HOBr}] = 3.10 \times 10^{-10} \text{ atm} \times 1900 \text{ M}^1 \text{ atm}^{-1} = 5.89 \times 10^{-7} \text{ M} \quad (3)$$

we thus obtain a range of 1.90×10^{-8} - $5.89 \times 10^{-7} \text{ M}$ for $[\text{HOBr}]$. The concentration of OBr^- anion can be obtained from the equilibrium expression:



$$\frac{[\text{HOBr}]}{[\text{OBr}^-]} = \frac{[\text{H}_3\text{O}^+]}{K_{a3}} \quad (5)$$

$$[\text{OBr}^-] = K_{a3} \times [\text{HOBr}] / [\text{H}_3\text{O}^+] \quad (6)$$

where K_{a3} ($10^{-8.9}$) is the acidity constant for HOBr. Concentrations of OBr^- corresponding to the $[\text{HOBr}]$ range given above at different pH are shown in Table S2.

The distributions fraction of the two anions can be computed as:

$$\delta_{\text{HOBr}} = [\text{HOBr}] / ([\text{HOBr}] + [\text{OBr}^-]) \quad (7)$$

$$= [\text{HOBr}] / ([\text{HOBr}] + K_{a3} \times [\text{HOBr}] / [\text{H}_3\text{O}^+]) \quad (8)$$

$$= 1 / (1 + K_{a3} / [\text{H}_3\text{O}^+]) = [\text{H}_3\text{O}^+] / ([\text{H}_3\text{O}^+] + K_{a3}) \quad (9)$$

$$\delta_{\text{OBr}^-} = [\text{OBr}^-] / (\text{HOBr} + [\text{OBr}^-]) \quad (10)$$

$$= [\text{OBr}^-] / ([\text{OBr}^-] + [\text{H}_3\text{O}^+] \times [\text{OBr}^-] / K_{a3}) \quad (11)$$

$$= 1 / (1 + [\text{H}_3\text{O}^+] / K_{a3}) = K_{a3} / ([\text{H}_3\text{O}^+] + K_{a3}) \quad (12)$$

Table S1. Calculated aqueous $[\text{OBr}^-]$ under the different aqueous $[\text{HOBr}]$ ($[\text{HOBr}] = 1.90 \times 10^{-8}$ M and $[\text{HOBr}] = 5.89 \times 10^{-7}$ M) and pH.

| pH | $[\text{OBr}^-]$ | $[\text{OBr}^-]$ |
|------|------------------------|------------------------|
| 3 | 2.39×10^{-14} | 7.42×10^{-13} |
| 4 | 2.39×10^{-13} | 7.42×10^{-12} |
| 5 | 2.39×10^{-12} | 7.42×10^{-11} |
| 6 | 2.39×10^{-11} | 7.42×10^{-10} |
| 6.97 | 2.23×10^{-10} | 6.92×10^{-9} |
| 7 | 2.39×10^{-10} | 7.42×10^{-9} |
| 7.5 | 2.39×10^{-9} | 7.42×10^{-8} |
| 8 | 1.90×10^{-8} | 5.89×10^{-7} |
| 9 | 2.39×10^{-8} | 7.42×10^{-7} |

Section 2. Figures

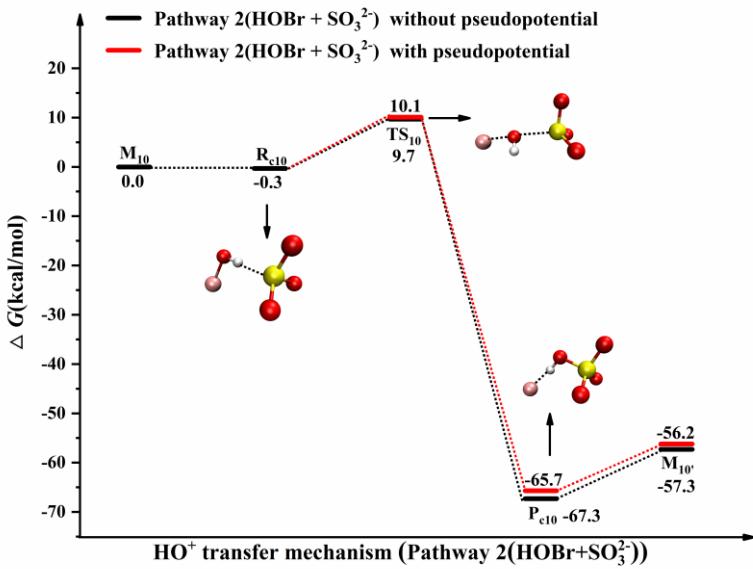


Fig. S1 The Gibbs free energy profile (kcal/mol, at 298.15 K and a reference concentration of 1 mol/L) for the reaction of HOBr with SO_3^{2-} through Pathway 2($\text{HOBr} + \text{SO}_3^{2-}$) at the DLPNO-CCSD(T)/aug-cc-pVTZ//M06-2X/6-311++G (3df, 3pd) level of theory with or without pseudopotential. Solvent corrections are included in the M06-2X calculations using the SMD model. The white, pink, red, and yellow spheres represent H, Br, O, and S atoms, respectively.

In order to investigate the effect of pseudopotential on the reactions studied in the present work, we calculated the energy barrier of Pathway 2 between HOBr and SO_3^{2-} , the most competitive mechanism in the studied system, with and without pseudopotential. As shown in Fig. S1, the reaction energy barrier with pseudopotential at the M06-2X/6-311++G(3df,3pd)//DLPNO-CCSD(T)/aug-cc-pVTZ (aug-cc-pVTZ-PP for the optimization of Br) level of theory is 10.4 kcal/mol, and that without pseudopotential at the M06-2X/6-311++G(3df,3pd)//DLPNO-CCSD(T)/aug-cc-pVTZ level of theory is 10.0 kcal/mol, with a low deviation of 0.4 kcal/mol. It is suggested that the effect of ignoring pseudopotential on the reaction energy barrier is very unobvious.

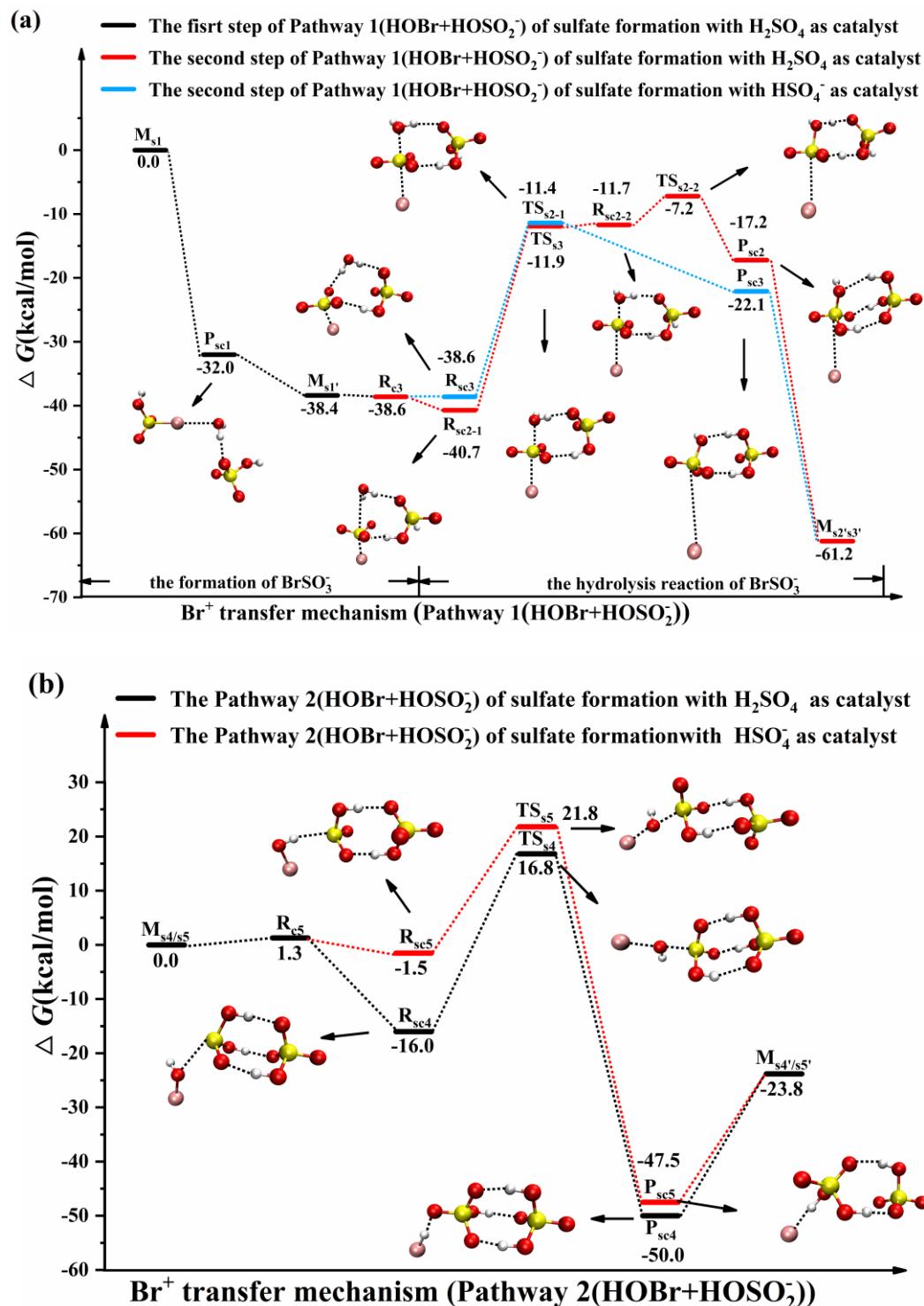
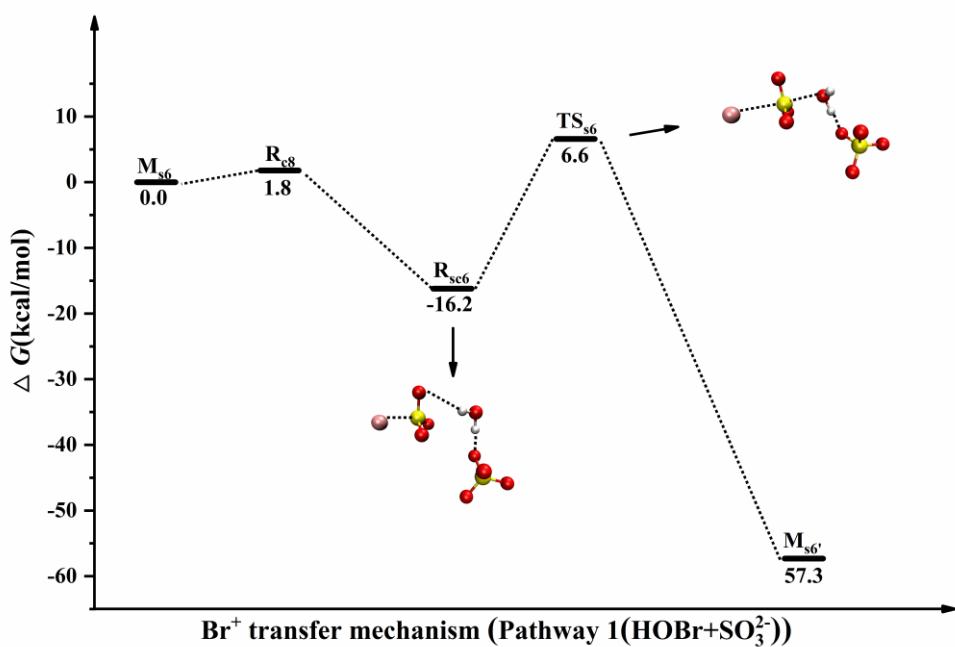


Fig. S2 The Gibbs free energy profile (kcal/mol, at 298.15 K and a reference concentration of 1 mol/L) for the reaction of HOBr with HOSO₂⁻ through (a) Pathway 1(HOBr + HOSO₂⁻) and (b) Pathway 2(HOBr + HOSO₂⁻) at the DLPNO-CCSD(T)/aug-cc-pVTZ//M06-2X/6-311++G (3df, 3pd) level of theory. Solvent corrections are included in the M06-2X calculations using the SMD model. The white, pink, red, and yellow spheres represent H, Br, O, and S atoms, respectively.

(a) — The second step of Pathway 1(HOBr+SO₃²⁻) of sulfate formation with HSO₄⁻ as catalyst



(b) — The Pathway 2(HOBr+SO₃²⁻) of sulfate formation with HSO₄⁻ as catalyst

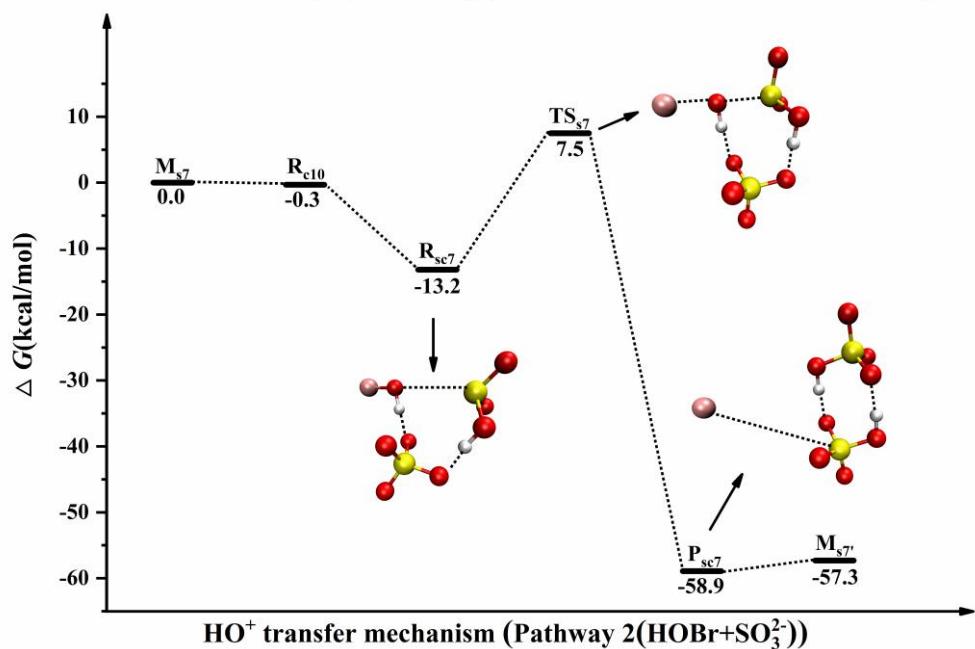


Fig. S3 The Gibbs free energy profile (kcal/mol, at 298.15 K and a reference concentration of 1 mol/L) for the reaction of HOBr with SO₃²⁻ through (a) Pathway 1(HOBr + SO₃²⁻) and (b) Pathway 2(HOBr + SO₃²⁻) at the DLPNO-CCSD(T)/aug-cc-pVTZ//M06-2X/6-311++G (3df, 3pd) level of theory. Solvent corrections are included in the M06-2X calculations using the SMD model. The white, pink, red, and yellow spheres represent H, Br, O, and S atoms, respectively.

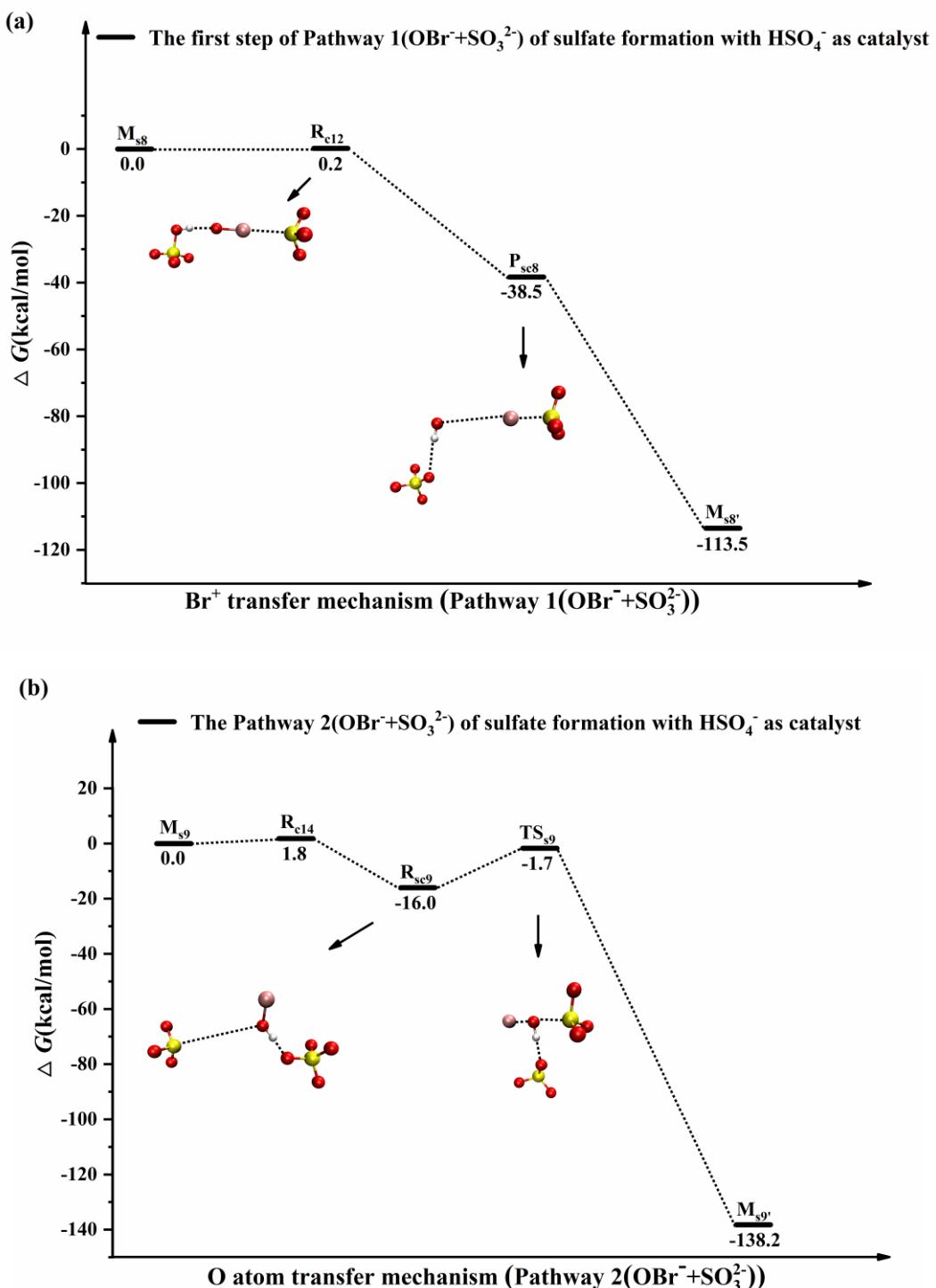
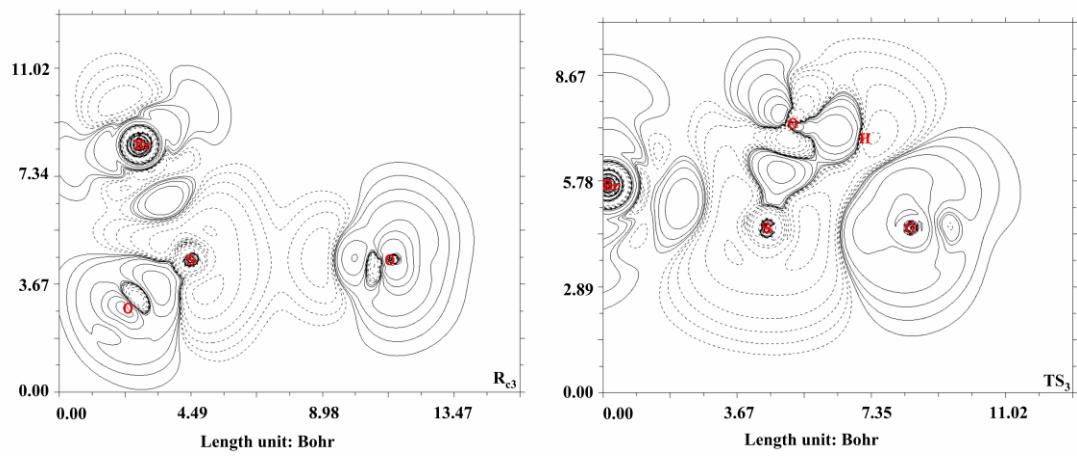
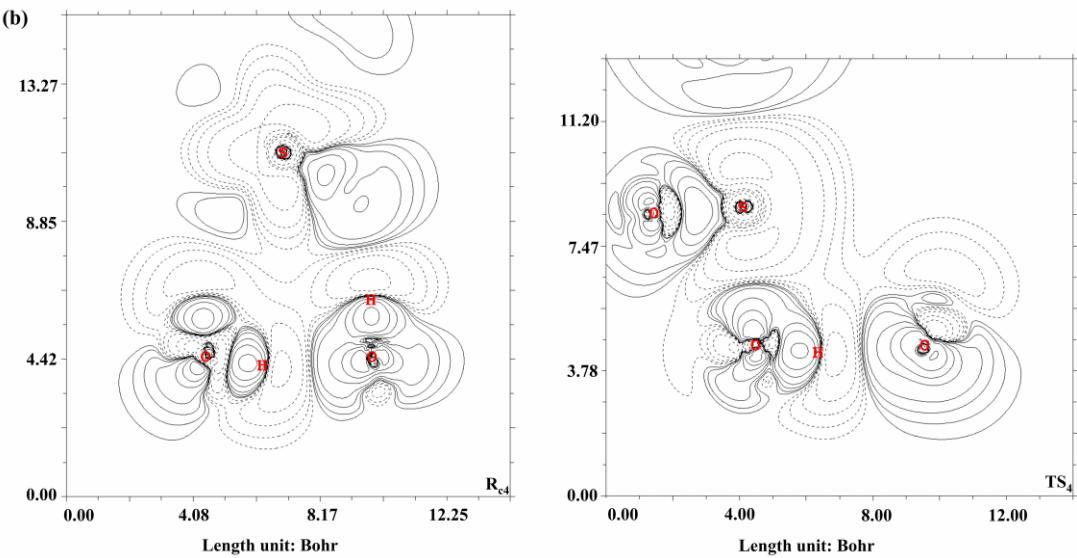


Fig. S4 The Gibbs free energy profile (kcal/mol, at 298.15 K and a reference concentration of 1 mol/L) for the reaction of OBr^- with SO_3^{2-} through (a) Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$) and (b) Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$) at the DLPNO-CCSD(T)/aug-cc-pVTZ//M06-2X/6-311++G (3df, 3pd) level of theory. Solvent corrections are included in the M06-2X calculations using the SMD model. The white, pink, red, and yellow spheres represent H, Br, O, and S atoms, respectively.

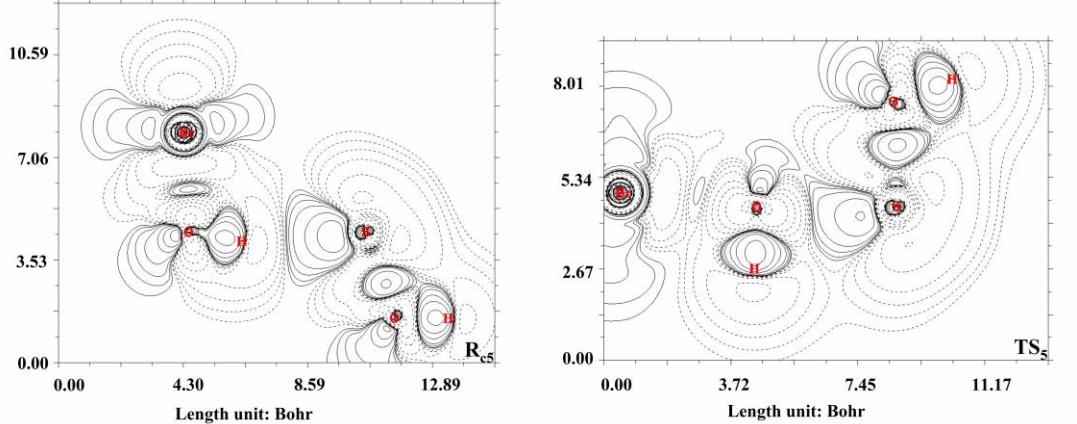
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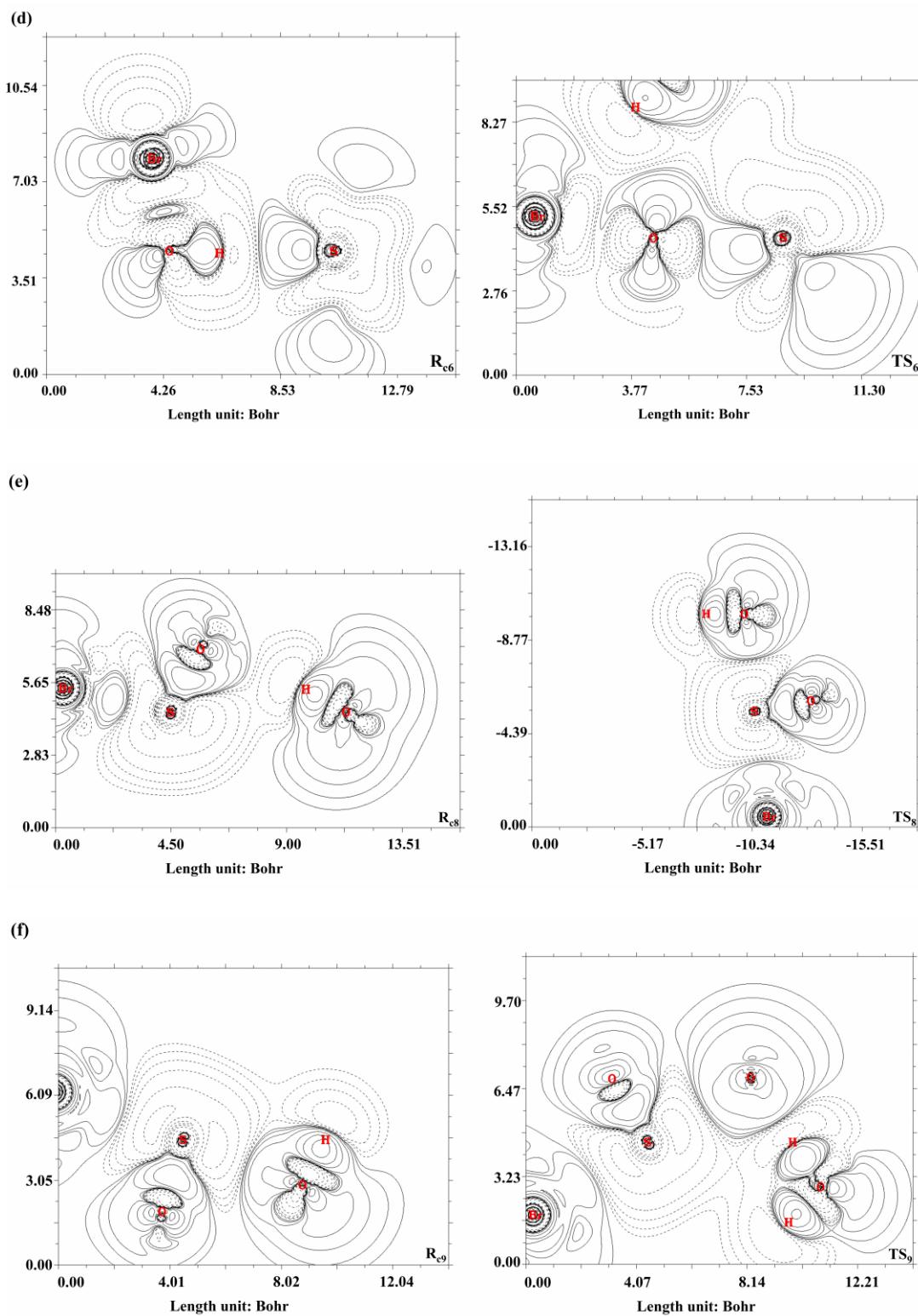


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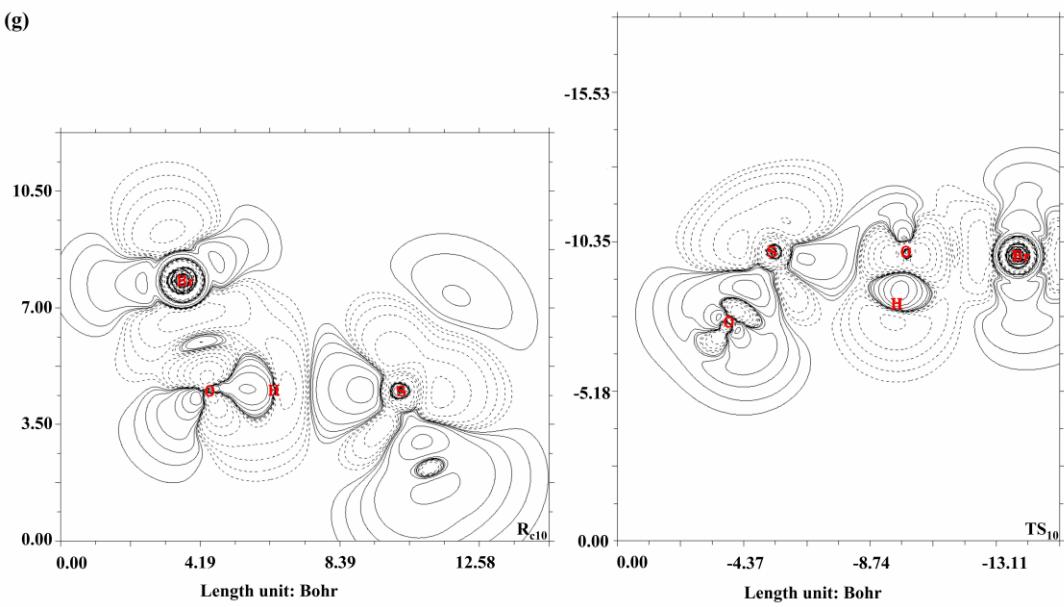


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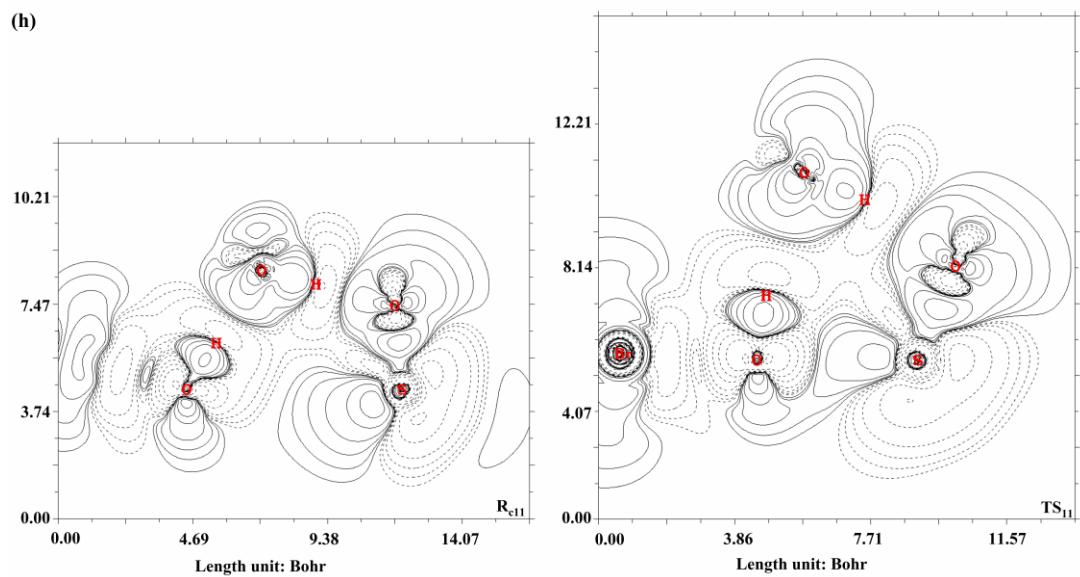




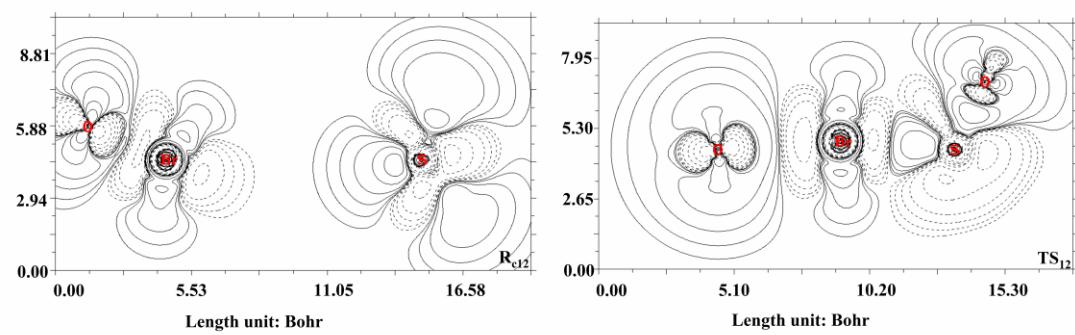
(g)



(h)



(i)



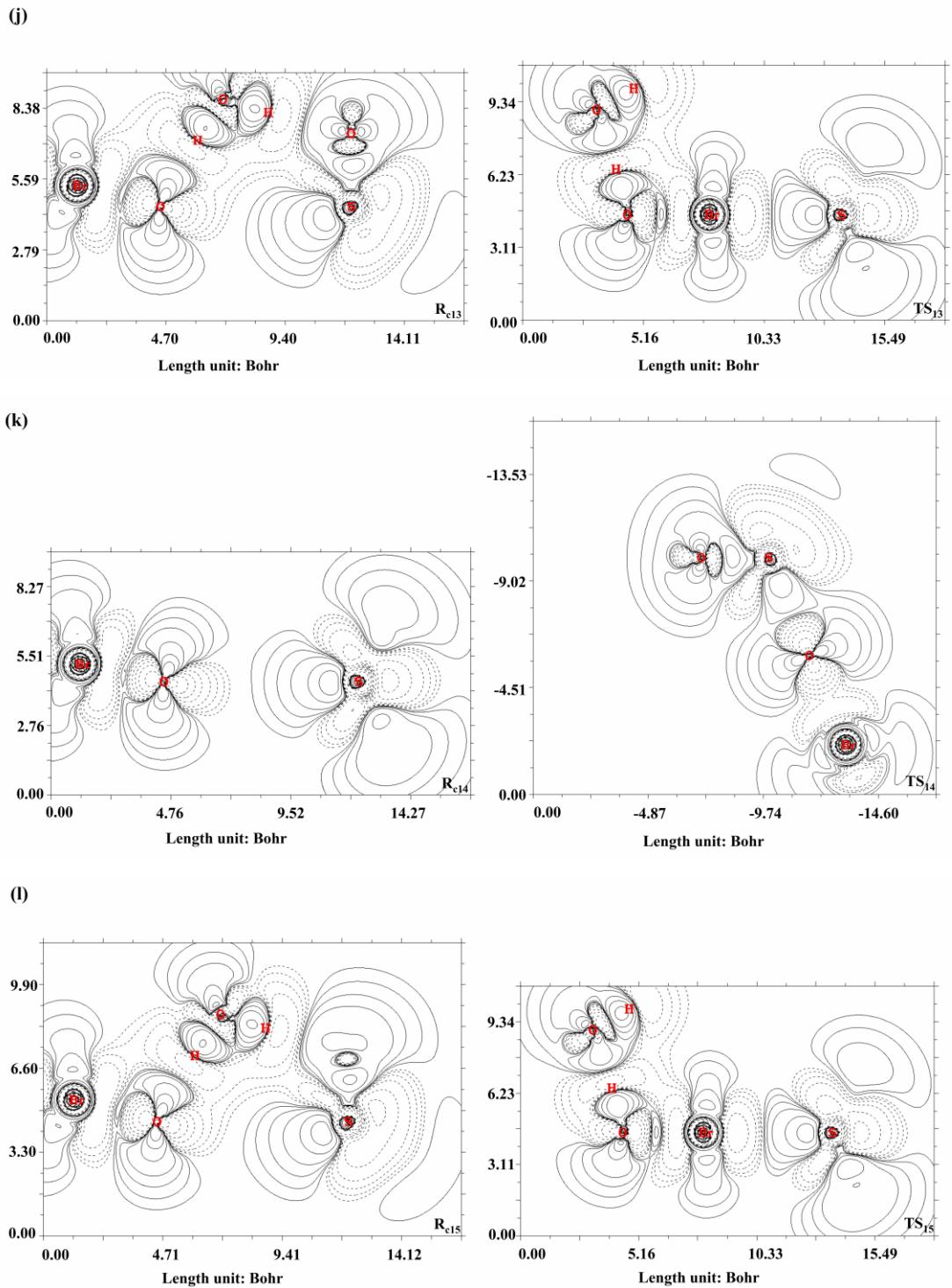


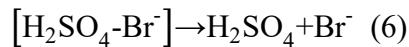
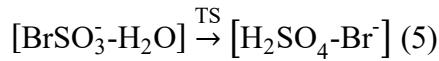
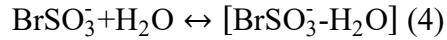
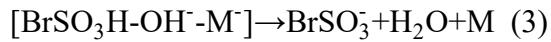
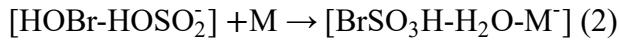
Fig. S5. Contour maps of the electron density differences between (a) R_{c3} and TS_3 , (b) R_{c4} and TS_4 , (c) R_{c5} and TS_5 (d) R_{c6} and TS_6 , (e) R_{c8} and TS_8 , (f) R_{c9} and TS_9 , (g) R_{c10} and TS_{10} , (h) R_{c11} and TS_{11} , (i) R_{c12} and TS_{12} , (j) R_{c13} and TS_{13} , (k) R_{c14} and TS_{14} , (l) R_{c15} and TS_{15} . Solid and dashed lines represent areas where electron density increases and decreases, respectively.

Section 3. Results

3.1 The reaction rates between HOBr and HOSO₂⁻ leading to sulfate formation

3.1.1 The reaction rate via Pathway 1(HOBr + HOSO₂⁻)

The detailed formation process of sulfate from HOBr and HOSO₂⁻ through Pathway 1(HOBr + HOSO₂⁻) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex, and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($v_{1\text{HOBr} + \text{HOSO}_2^-, \text{un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{HOBr} + \text{HOSO}_2^-, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_5 [\text{BrSO}_3^-\text{-H}_2\text{O}] \quad (7)$$

$$k_4 [\text{BrSO}_3^-][\text{H}_2\text{O}] - k_{-4} [\text{BrSO}_3^-\text{-H}_2\text{O}] - k_5 [\text{BrSO}_3^-\text{-H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^-\text{-H}_2\text{O}] = \frac{k_4 [\text{BrSO}_3^-][\text{H}_2\text{O}]}{k_{-4} + k_5} \quad (7-1)$$

$$k_3 [\text{BrSO}_3\text{H}-\text{OH}^-\text{-M}^-] - k_4 [\text{BrSO}_3^-][\text{H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^-] = \frac{k_3 [\text{BrSO}_3\text{H}-\text{OH}^-\text{-M}^-]}{k_4 [\text{H}_2\text{O}]} \quad (7-2)$$

$$k_2 [\text{HOBr-HOSO}_2^-][\text{M}] - k_3 [\text{BrSO}_3\text{H}-\text{OH}^-\text{-M}^-] = 0$$

$$[\text{BrSO}_3\text{H}-\text{OH}^-\text{-M}^-] = \frac{k_2 [\text{HOBr-HOSO}_2^-][\text{M}]}{k_3} \quad (7-3)$$

$$k_1 [\text{HOBr}][\text{HOSO}_2^-] - k_{-1} [\text{HOBr-HOSO}_2^-] - k_2 [\text{HOBr-HOSO}_2^-][\text{M}] = 0$$

$$[\text{HOBr-HOSO}_2^-] = \frac{k_1 [\text{HOBr}][\text{HOSO}_2^-]}{k_{-1} + k_2 [\text{M}]} \quad (7-4)$$

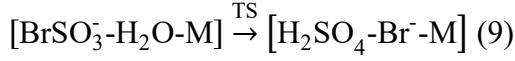
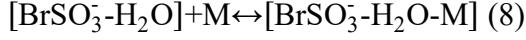
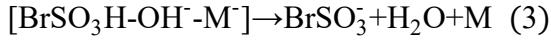
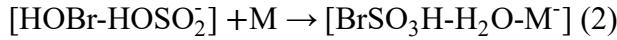
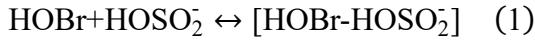
$$v_{1\text{HOBr} + \text{HOSO}_2^-, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_5}{k_{-4} + k_5} \times \frac{k_1 \times k_2}{k_{-1} + k_2 [\text{M}]} \times [\text{HOBr}][\text{HOSO}_2^-][\text{M}] \quad (7-5)$$

The pseudo-unimolecular uncatalyzed S(IV) oxidation rates through Pathway 1(HOBr + HOSO₂⁻) can then be written as

$$v_{1\text{HOBr+HOSO}_2^{\text{-}},\text{un-S(IV)}} = \frac{k_5}{k_{-4} + k_5} \times \frac{k_1 \times k_2}{k_{-1} + k_2[M]} \times [\text{HOBr}][\text{M}] \quad (7-6)$$

where k_1/k_{-1} are the forward/reverse rate coefficients for the reaction 1, k_{-4} is the reverse rate coefficient for the reaction 4, k_2 is the diffusion rate constant for the reaction 2, and k_5 is the unimolecular rate constants for the uncatalyzed reaction 5. $[M]$ is the concentration of catalyst M.

The catalyzed formation process of sulfate from HOBr and HOSO₂⁻ through Pathway 1(HOBr + HOSO₂⁻) is similarly described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($v_{1\text{HOBr+HOSO}_2^{\text{-}},\text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{HOBr+HOSO}_2^{\text{-}},\text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_9[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}-\text{M}] \quad (10)$$

$$k_8[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}][\text{M}] - k_{-8}[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}-\text{M}] - k_9[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}-\text{M}] = 0$$

$$[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}-\text{M}] = \frac{k_8[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}][\text{M}]}{k_{-8} + k_9} \quad (11-1)$$

$$k_4[\text{BrSO}_3^{\text{-}}][\text{H}_2\text{O}] - k_{-4}[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}] - k_8[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}][\text{M}] = 0$$

$$[\text{BrSO}_3^{\text{-}}\text{-H}_2\text{O}] = \frac{k_4[\text{BrSO}_3^{\text{-}}][\text{H}_2\text{O}]}{k_{-4} + k_8[\text{M}]} \quad (11-2)$$

$$k_3[\text{BrSO}_3^{\text{-}}\text{H}-\text{OH}^{\text{-}}-\text{M}^-] - k_4[\text{BrSO}_3^{\text{-}}][\text{H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^{\text{-}}] = \frac{k_3[\text{BrSO}_3^{\text{-}}\text{H}-\text{OH}^{\text{-}}-\text{M}^-]}{k_4[\text{H}_2\text{O}]} \quad (11-3)$$

$$k_2[\text{HOBr-HOSO}_2^-][\text{M}] - k_3[\text{BrSO}_3\text{H-OH}^-\text{M}^-] = 0$$

$$[\text{BrSO}_3\text{H-OH}^-\text{M}^-] = \frac{k_2[\text{HOBr-HOSO}_2^-][\text{M}]}{k_3} \quad (11-4)$$

$$k_1[\text{HOBr}][\text{HOSO}_2^-] - k_{-1}[\text{HOBr-HOSO}_2^-] - k_2[\text{HOBr-HOSO}_2^-][\text{M}] = 0$$

$$[\text{HOBr-HOSO}_2^-] = \frac{k_1[\text{HOBr}][\text{HOSO}_2^-]}{k_{-1} + k_2[\text{M}]} \quad (11-5)$$

$$\nu_{1\text{HOBr+HOSO}_2\text{,cat}} = \frac{d[\text{SO}_4^{2-}]}{dt}$$

$$= \frac{k_9 \times k_8}{k_{-8} + k_9} \times \frac{1}{k_{-4} + k_8[\text{M}]} \times \frac{k_1 \times k_2}{k_{-1} + k_2[\text{M}]} [\text{HOBr}][\text{HOSO}_2^-][\text{M}][\text{M}] \quad (11-6)$$

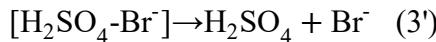
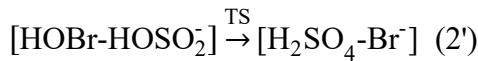
The pseudo-unimolecular uncatalyzed S(IV) oxidation rates through Pathway 1(HOBr + HOSO₂⁻) can then be written as

$$\nu_{1\text{HOBr+HOSO}_2\text{,un-S(IV)}} = \frac{k_9 \times k_8}{k_{-8} + k_9} \times \frac{1}{k_{-4} + k_8[\text{M}]} \times \frac{k_1 \times k_2}{k_{-1} + k_2[\text{M}]} [\text{HOBr}][\text{M}][\text{M}] \quad (11-7)$$

where k_8/k_{-8} symbolize the forward/reverse rate coefficients for the reaction 8 and k_9 is the unimolecular rate constant for the catalyzed reaction 9. [M] is the concentration of catalysts M.

3.1.2 The reaction rate via Pathway 2(HOBr + HOSO₂⁻)

The detailed formation process of sulfate from HOBr and HOSO₂⁻ through Pathway 2(HOBr + HOSO₂⁻) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($\nu_{2\text{HOBr+HOSO}_2\text{,un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$\nu_{2\text{HOBr+HOSO}_2\text{,un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_2'[\text{HOBr-HOSO}_2^-] \quad (4')$$

$$k_{1'}[\text{HOBr}][\text{HOSO}_2^-] - k_{-1'}[\text{HOBr-HOSO}_2^-] - k_2'[\text{HOBr-HOSO}_2^-] = 0$$

$$[\text{HOBr-HOSO}_2^-] = \frac{k_{1'}}{k_{-1'} + k_2'} [\text{HOBr}][\text{HOSO}_2^-] \quad (4'-1)$$

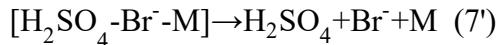
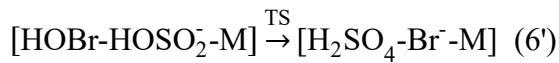
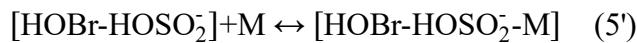
$$\nu_{2\text{HOBr+HOSO}_2\text{,un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{1'} \times k_2'}{k_{-1'} + k_2'} [\text{HOBr}][\text{HOSO}_2^-] \quad (4'-2)$$

The pseudo-unimolecular uncatalyzed S(IV) oxidation rate through Pathway 2(HOBr + HOSO₂⁻) can be written as

$$v_{2\text{HOBr}+\text{HOSO}_2^{\cdot},\text{un-S(IV)}} = \frac{k_{1'} \times k_{2'}}{k_{-1'} + k_{2'}} [\text{HOBr}] \quad (4'-3)$$

where $k_{1'}/k_{-1'}$ symbolize the forward/reverse rate coefficients for the reaction 1' and $k_{2'}$ is the unimolecular rate constant for the uncatalyzed reaction 2'.

The catalyzed formation process of sulfate from HOBr and HOSO₂⁻ through Pathway 2(HOBr + HOSO₂⁻) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($v_{2\text{HOBr}+\text{HOSO}_2^{\cdot},\text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{2\text{HOBr}+\text{HOSO}_2^{\cdot},\text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_6' [\text{HOSO}_2^{\cdot}-\text{HOBr-M}] \quad (8')$$

$$k_5' [\text{HOBr-HOSO}_2^{\cdot}] [\text{M}] - k_{-5'} [\text{HOSO}_2^{\cdot}-\text{HOBr-M}] - k_6' [\text{HOSO}_2^{\cdot}-\text{HOBr-M}] = 0$$

$$[\text{HOSO}_2^{\cdot}-\text{HOBr-M}] = \frac{k_5' [\text{HOBr-HOSO}_2^{\cdot}] [\text{M}]}{k_{-5'} + k_6'} \quad (8'-1)$$

$$k_{1'} [\text{HOBr}] [\text{HOSO}_2^{\cdot}] - k_{-1'} [\text{HOBr-HOSO}_2^{\cdot}] - k_5' [\text{HOBr-HOSO}_2^{\cdot}] [\text{M}] = 0$$

$$[\text{HOBr-HOSO}_2^{\cdot}] = \frac{k_{1'}}{k_{-1'} + k_5' [\text{M}]} [\text{HOBr}] [\text{HOSO}_2^{\cdot}] \quad (8'-2)$$

$$v_{2\text{HOBr}+\text{HOSO}_2^{\cdot},\text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{1'}}{k_{-1'} + k_5' [\text{M}]} \times \frac{k_5' \times k_6'}{k_{-5'} + k_6'} [\text{M}] [\text{HOBr}] [\text{HOSO}_2^{\cdot}] \quad (8'-3)$$

The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 2(HOBr + HOSO₂⁻) can be written as

$$v_{2\text{HOBr}+\text{HOSO}_2^{\cdot},\text{cat-S(IV)}} = \frac{k_{1'}}{k_{-1'} + k_5' [\text{M}]} \times \frac{k_5' \times k_6'}{k_{-5'} + k_6'} [\text{M}] [\text{HOBr}] \quad (8'-4)$$

where $k_5'/k_{-5'}$ symbolize the forward/reverse rate coefficients for the reaction 5' and k_6' is the unimolecular rate constant for the catalyzed reaction 6'. [M] is the concentration

of catalyst M.

3.1.3 S(IV) oxidation rates, related reaction rate constants and S(IV) lifetimes through Pathway 1(HOBr + HOSO₂⁻) and Pathway 2(HOBr + HOSO₂⁻)

Table S2. Calculated forward/reverse rate coefficients (k_1/k_{-1} , k_4/k_{-4} , k_8/k_{-8}), diffusion rate constant k_2 , the unimolecular rate constants (k_5 , k_9) for the sulfate formation between HOBr and HOSO₂⁻ through Pathway 1(HOBr + HOSO₂⁻).

| Catalyst | Rate constants | | Rate constants | |
|---|----------------|--|----------------|--------------------------------------|
| Without catalyst | k_1 | $7.44 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-1} | $5.65 \times 10^{10} \text{ s}^{-1}$ |
| | k_4 | $7.81 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-4} | $5.57 \times 10^9 \text{ s}^{-1}$ |
| | k_5 | $8.05 \times 10^{-28} \text{ s}^{-1}$ | | |
| (H ₂ O-catalyzed) | k_8 | $7.81 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-8} | $1.38 \times 10^{11} \text{ s}^{-1}$ |
| | k_9 | $2.27 \times 10^{-8} \text{ s}^{-1}$ | | |
| (H ₂ SO ₄ -catalyzed) | k_2 | $7.48 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | | |
| | k_8 | $7.44 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-8} | $2.14 \times 10^8 \text{ s}^{-1}$ |
| | k_9 | $4.96 \times 10^{-9} \text{ s}^{-1}$ | | |
| (HSO ₄ ⁻ -catalyzed) | k_2 | $3.24 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | | |
| | k_8 | $3.23 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-8} | $3.23 \times 10^9 \text{ s}^{-1}$ |
| | k_9 | $7.39 \times 10^{-8} \text{ s}^{-1}$ | | |

Table S3. Calculated forward/reverse rate coefficients (k_1/k_{-1} , k_5/k_{-5}), the unimolecular rate constants (k_2 , k_6) for the sulfate formation between HOBr and HOSO₂⁻ through Pathway 2(HOBr + HOSO₂⁻).

| Catalyst | Rate constants | | Rate constants | |
|---|----------------|--|----------------|--------------------------------------|
| Without catalyst | k_1 | $7.44 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-1} | $6.68 \times 10^{10} \text{ s}^{-1}$ |
| | k_2 | $1.21 \times 10^{-4} \text{ s}^{-1}$ | | |
| (H ₂ O-catalyzed) | k_5 | $7.92 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} | $1.63 \times 10^8 \text{ s}^{-1}$ |
| | k_6 | $1.61 \times 10^{-5} \text{ s}^{-1}$ | | |
| (H ₂ SO ₄ -catalyzed) | k_5 | $7.48 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} | $1.54 \times 10^{-3} \text{ s}^{-1}$ |
| | k_6 | $7.00 \times 10^{-12} \text{ s}^{-1}$ | | |
| (HSO ₄ ⁻ -catalyzed) | k_5 | $3.24 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} | $2.86 \times 10^7 \text{ s}^{-1}$ |
| | k_6 | $6.43 \times 10^{-5} \text{ s}^{-1}$ | | |

Table S4. Calculated overall rate constant, effective rate constant, S(IV) oxidation rate and the S(IV) lifetimes for Pathway 1(HOBr + HOSO₂⁻) and Pathway 2(HOBr + HOSO₂⁻) from HOSO₂⁻ and HOBr respectively, assuming [HOBr] = $5.89 \times 10^{-7} \text{ M}$ (corresponding to a Henry's law equilibrium with a gas phase HOBr mixing ratio of 0.31 ppbv), and [H₂O] = 55.56 M (corresponding to the known bulk concentration of

H_2O).

| Rate constants | Catalysts | Overall rate constant $\text{M}^{-2}\text{s}^{-1}$ | Effective rate constant ^c ($\text{M}^{-1}\text{s}^{-1}$) | S(IV) oxidation rate (s^{-1}) | S(IV) lifetime (s) |
|--|--|--|---|--|-----------------------|
| | Without catalyst | 6.61×10^{-36} | 6.61×10^{-36} | 3.89×10^{-42} | 2.57×10^{41} |
| (HOBr+HOSO ₂ ⁻) | Pathway1 H ₂ O-catalyzed | 1.34×10^{-19} | 7.43×10^{-18} | 4.38×10^{-24} | 2.28×10^{23} |
| | H ₂ SO ₄ -catalyzed ^a | 7.06×10^{-16} | 3.78×10^{-23} | 2.23×10^{-29} | 4.49×10^{28} |
| | HSO ₄ ⁻ -catalyzed ^b | 6.07×10^{-16} | 6.50×10^{-23} | 3.83×10^{-29} | 2.61×10^{28} |
| Pathway 2 (HOBr+HOSO ₂ ⁻) | Without catalyst | 1.35×10^{-5} | 1.35×10^{-5} | 7.94×10^{-12} | 1.26×10^{11} |
| | H ₂ O-catalyzed | 1.15×10^{-5} | 6.39×10^{-4} | 3.76×10^{-10} | 2.66×10^9 |
| | H ₂ SO ₄ -catalyzed ^a | 3.79×10^0 | 2.03×10^{-7} | 1.20×10^{-13} | 8.35×10^{12} |
| | HSO ₄ ⁻ -catalyzed ^b | 8.10×10^{-4} | 8.68×10^{-11} | 5.11×10^{-17} | 1.96×10^{16} |

^a Assuming a half of general concentration of H⁺ act as the possible high limit for the concentration of H₂SO₄ in cloud water.

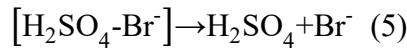
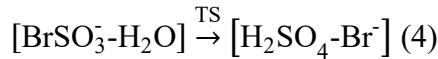
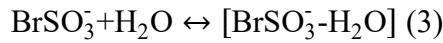
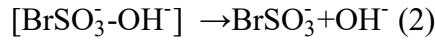
^b Assuming a general concentration of H⁺ act as the possible high limit for the concentration of HSO₄⁻ in cloud water.

^c Effective rate constant = Overall rate constant \times [M], where [M] is the concentration of catalyst M.

3.2 The reaction rates between HOBr and SO₃²⁻ leading to sulfate formation.

3.2.1 The reaction rate via Pathway 1(HOBr + SO₃²⁻)

The detailed formation process of sulfate from HOBr and SO₃²⁻ through the Pathway 1(HOBr + SO₃²⁻) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_4 [\text{BrSO}_3^{\cdot-}\text{-H}_2\text{O}] \quad (6)$$

$$k_3 [\text{BrSO}_3^{\cdot-}] [\text{H}_2\text{O}] - k_{-3} [\text{BrSO}_3^{\cdot-}\text{-H}_2\text{O}] - k_4 [\text{BrSO}_3^{\cdot-}\text{-H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^{\cdot-}\text{-H}_2\text{O}] = \frac{k_3 [\text{BrSO}_3^{\cdot-}] [\text{H}_2\text{O}]}{k_{-3} + k_4} \quad (6-1)$$

$$k_2 [\text{BrSO}_3^{\cdot-}\text{-OH}^-] - k_3 [\text{BrSO}_3^{\cdot-}] [\text{H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^{\cdot-}] = \frac{k_2 [\text{BrSO}_3^{\cdot-}\text{-OH}^-]}{k_3 [\text{H}_2\text{O}]} \quad (6-2)$$

$$k_1 [\text{HOBr}] [\text{SO}_3^{2-}] - k_2 [\text{BrSO}_3^{\cdot-}\text{-OH}^-] = 0$$

$$[\text{BrSO}_3^{\cdot-}\text{-OH}^-] = \frac{k_1 [\text{HOBr}] [\text{SO}_3^{2-}]}{k_2} \quad (6-3)$$

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_4 \times k_1}{k_{-3} + k_4} [\text{HOBr}] [\text{SO}_3^{2-}] \quad (6-4)$$

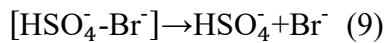
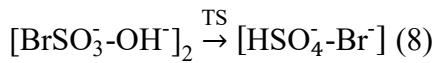
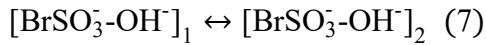
The pseudo-unimolecular uncatalyzed S(IV) oxidation rates through Pathway 1(HOBr + SO₃²⁻) can be written as

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un-S(IV)}} = \frac{k_4 \times k_1}{k_{-3} + k_4} [\text{HOBr}] \quad (6-6)$$

where k_1 is the diffusion rate constant between HOBr and SO₃²⁻, k_{-3} is the reverse rate

coefficients for the reaction 3 and k_4 is the unimolecular rate constant for the uncatalyzed reaction 4.

The possible formation process of sulfate from BrSO_3^- and OH^- is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_8 [\text{BrSO}_3^-\text{-OH}^-] \quad (10)$$

$$k_7 [\text{BrSO}_3^-\text{-OH}^-]_1 - k_{-7} [\text{BrSO}_3^-\text{-OH}^-]_2 - k_8 [\text{BrSO}_3^-\text{-OH}^-]_2 = 0$$

$$[\text{BrSO}_3^-\text{-OH}^-]_2 = \frac{k_7 [\text{BrSO}_3^-\text{-OH}^-]_1}{k_{-7} + k_8} \quad (10-1)$$

$$k_1 [\text{HOBr}] [\text{SO}_3^{2-}] - k_7 [\text{BrSO}_3^-\text{-OH}^-]_1 = 0$$

$$[\text{BrSO}_3^-\text{-OH}^-]_1 = \frac{k_1 [\text{HOBr}] [\text{SO}_3^{2-}]}{k_7} \quad (10-2)$$

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_8 \times k_1}{k_{-7} + k_8} [\text{HOBr}] [\text{SO}_3^{2-}] \quad (10-3)$$

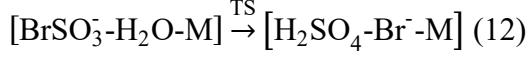
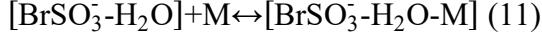
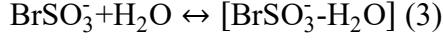
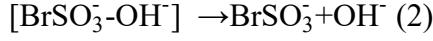
The pseudo-unimolecular uncatalyzed S(IV) oxidation rate through Pathway 1($\text{HOBr} + \text{SO}_3^{2-}$) can be written as

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{un-S(IV)}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_8 \times k_1}{k_{-7} + k_8} [\text{HOBr}] \quad (10-4)$$

where k_7/k_{-7} symbolize the forward/reverse rate coefficients for the reaction 7 and k_8 is the unimolecular rate constant for the reaction 8.

The catalyzed formation process of sulfate from HOBr and SO_3^{2-} through Pathway

1(HOBr + SO₃²⁻) is similarly described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_{12}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O} - \text{M}] \quad (14)$$

$$k_{11}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O}][\text{M}] - k_{-11}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O} - \text{M}] - k_{12}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O} - \text{M}] = 0$$

$$[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O} - \text{M}] = \frac{k_{11}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O}][\text{M}]}{k_{-11} + k_{12}} \quad (14-1)$$

$$k_3[\text{BrSO}_3^{\cdot}][\text{H}_2\text{O}] - k_{-3}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O}] - k_{11}[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O}][\text{M}] = 0$$

$$[\text{BrSO}_3^{\cdot} - \text{H}_2\text{O}] = \frac{k_3[\text{BrSO}_3^{\cdot}][\text{H}_2\text{O}]}{k_{-3} + k_{11}[\text{M}]} \quad (14-2)$$

$$k_2[\text{BrSO}_3^{\cdot} - \text{OH}^-] - k_3[\text{BrSO}_3^{\cdot}][\text{H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^{\cdot}] = \frac{k_2[\text{BrSO}_3^{\cdot} - \text{OH}^-]}{k_3[\text{H}_2\text{O}]} \quad (14-3)$$

$$k_1[\text{HOBr}][\text{SO}_3^{2-}] - k_2[\text{BrSO}_3^{\cdot} - \text{OH}^-] = 0$$

$$[\text{BrSO}_3^{\cdot} - \text{OH}^-] = \frac{k_1[\text{HOBr}][\text{SO}_3^{2-}]}{k_2} \quad (14-4)$$

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{12} \times k_{11}}{k_{-11} + k_{12}} \times \frac{k_1}{k_{-3} + k_{11}[\text{M}]} \times [\text{HOBr}][\text{SO}_3^{2-}][\text{M}] \quad (14-5)$$

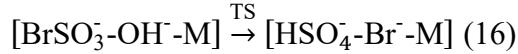
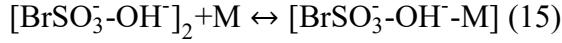
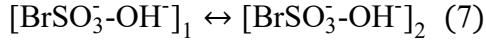
The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 1(HOBr + SO₃²⁻) can then be written as

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat-S(IV)}} = \frac{k_{12} \times k_{11}}{k_{-11} + k_{12}} \times \frac{k_1}{k_{-3} + k_{11}[\text{M}]} \times [\text{HOBr}][\text{M}] \quad (14-6)$$

where k_{11}/k_{-11} symbolize the forward/reverse rate coefficients for the reaction 11 and

k_{12} is the unimolecular rate constant for the catalyzed reaction 12.

The catalyzed formation process of sulfate from BrSO_3^- and OH^- is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_{16}[\text{BrSO}_3^-\text{-OH}^- \text{-M}] \quad (18)$$

$$k_{15}[\text{BrSO}_3^-\text{-OH}^-]_2[\text{M}] - k_{-15}[\text{BrSO}_3^-\text{-OH}^- \text{-M}] - k_{16}[\text{BrSO}_3^-\text{-OH}^- \text{-M}] = 0$$

$$[\text{BrSO}_3^-\text{-OH}^- \text{-M}] = \frac{k_{15}[\text{BrSO}_3^-\text{-OH}^-]_2[\text{M}]}{k_{-15} + k_{16}} \quad (18-1)$$

$$k_7[\text{BrSO}_3^-\text{-OH}^-]_1 - k_{-7}[\text{BrSO}_3^-\text{-OH}^-]_2 - k_{15}[\text{BrSO}_3^-\text{-OH}^-]_2[\text{M}]$$

$$[\text{BrSO}_3^-\text{-OH}^-]_2 = \frac{k_7[\text{BrSO}_3^-\text{-OH}^-]_1}{k_{-7} + k_{15}[\text{M}]} \quad (18-2)$$

$$k_1[\text{HOBr}][\text{SO}_3^{2-}] - k_7[\text{BrSO}_3^-\text{-OH}^-]_1 = 0$$

$$[\text{BrSO}_3^-\text{-OH}^-]_1 = \frac{k_1[\text{HOBr}][\text{SO}_3^{2-}]}{k_8} \quad (18-3)$$

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{16} \times k_{15}}{k_{-15} + k_{16}} \times \frac{k_1}{k_{-7} + k_{15}[\text{M}]} \times [\text{HOBr}][\text{SO}_3^{2-}][\text{M}] \quad (18-4)$$

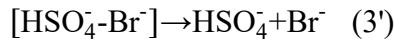
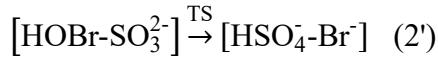
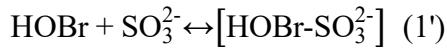
The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 1($\text{HOBr} + \text{SO}_3^{2-}$) can be written as

$$v_{1\text{HOBr} + \text{SO}_3^{2-}, \text{cat-S(IV)}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{16} \times k_{15}}{k_{-15} + k_{16}} \times \frac{k_1}{k_{-7} + k_{15}[\text{M}]} \times [\text{HOBr}][\text{M}] \quad (18-5)$$

where k_{15}/k_{-15} symbolize the forward/reverse rate coefficients for the reaction 15 and k_{16} is the unimolecular rate constant for the reaction 16.

3.2.2 The reaction rate via Pathway 2(HOBr + SO₃²⁻)

The detailed formation process of sulfate from HOBr and SO₃²⁻ through the Pathway 2(HOBr + SO₃²⁻) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the formation reaction rate ($v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_2' [\text{HOBr-SO}_3^{2-}] \quad (4')$$

$$k_1' [\text{HOBr}] [\text{SO}_3^{2-}] - k_{-1}' [\text{HOBr-SO}_3^{2-}] - k_2' [\text{HOBr-SO}_3^{2-}] = 0$$

$$[\text{HOBr-SO}_3^{2-}] = \frac{k_1' [\text{HOBr}] [\text{SO}_3^{2-}]}{k_{-1}' + k_2'} \quad (4'-1)$$

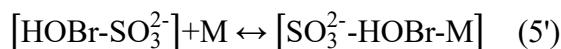
$$v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_1' \times k_2'}{k_{-1}' + k_2'} [\text{HOBr}] [\text{SO}_3^{2-}] \quad (4'-2)$$

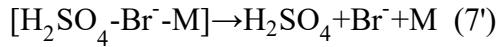
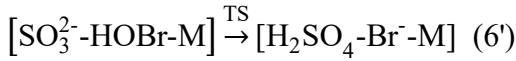
The pseudo-unimolecular catalyzed S(IV) oxidation rates through Pathway 2(HOBr + SO₃²⁻) can be written as

$$v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{un-S(IV)}} = \frac{k_1' \times k_2'}{k_{-1}' + k_2'} [\text{HOBr}] \quad (4'-3)$$

where k_1'/k_{-1}' symbolize the forward/reverse rate coefficients for the reaction 1', and k_2' is the unimolecular rate constant for the reaction 2'.

The catalyzed formation process of sulfate from HOBr and SO₃²⁻ through Pathway 2(HOBr + SO₃²⁻) is described by the following reaction equations:





Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_6' [\text{SO}_3^{2-}\text{-HOBr-M}] \quad (8')$$

$$k_5' [\text{HOBr-SO}_3^{2-}] [\text{M}] - k_{-5'} [\text{SO}_3^{2-}\text{-HOBr-M}] - k_6' [\text{SO}_3^{2-}\text{-HOBr-M}] = 0$$

$$[\text{SO}_3^{2-}\text{-HOBr-M}] = \frac{k_5' [\text{HOBr-SO}_3^{2-}] [\text{M}]}{k_{-5'} + k_6'} \quad (8'-1)$$

$$k_{-1'} [\text{HOBr}] [\text{SO}_3^{2-}] - k_{-1'} [\text{HOBr-SO}_3^{2-}] - k_5' [\text{HOBr-SO}_3^{2-}] [\text{M}] = 0$$

$$[\text{HOBr-SO}_3^{2-}] = \frac{k_{-1'} [\text{HOBr}] [\text{SO}_3^{2-}]}{k_{-1'} + k_5' [\text{M}]} \quad (8'-2)$$

$$v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_5' \times k_6'}{k_{-5'} + k_6'} \times \frac{k_{-1'}}{k_{-1'} + k_5' [\text{M}]} \times [\text{M}] [\text{HOBr}] [\text{SO}_3^{2-}] \quad (8'-3)$$

The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 2(HOBr+ SO_3^{2-}) can be written as

$$v_{2\text{HOBr} + \text{SO}_3^{2-}, \text{cat-S(IV)}} = \frac{k_5' \times k_6'}{k_{-5'} + k_6'} \times \frac{k_{-1'}}{k_{-1'} + k_5' [\text{M}]} \times [\text{M}] [\text{HOBr}] \quad (8'-4)$$

where $k_5'/k_{-5'}$ symbolize the forward/reverse rate coefficients for the reaction 5' and k_6' is the unimolecular rate constant for the catalyzed reaction 6'. [M] is the concentration of catalyst M.

3.2.3 S(IV) oxidation rates, related reaction rate constants and S(IV) lifetimes through Pathway 1(HOBr + SO_3^{2-}) and Pathway 2(HOBr + SO_3^{2-})

Table S5. Calculated diffusion rate constant (k_1) between HOBr and SO_3^{2-} , the forward/reverse rate coefficients (k_3/k_{-3} , k_7/k_{-7} , k_{11}/k_{-11} , k_{15}/k_{-15}), and the unimolecular rate constants (k_4 , k_8 , k_{12} , k_{16}) for the sulfate formation between HOBr and SO_3^{2-} through Pathway 1(HOBr + SO_3^{2-}).

| Catalyst | Rate constants | | Rate constants | |
|--|----------------|--|----------------|--------------------------------------|
| Without (H ₂ O-catalyzed) | k_1 | $7.45 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-3} | $5.57 \times 10^9 \text{ s}^{-1}$ |
| | k_3 | $7.81 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | | |
| | k_4 | $8.05 \times 10^{-28} \text{ s}^{-1}$ | k_{-7} | $3.34 \times 10^9 \text{ s}^{-1}$ |
| | k_7 | $1.44 \times 10^9 \text{ s}^{-1}$ | | |
| | k_8 | 1.03 s^{-1} | | |
| (HSO ₄ ⁻ -catalyzed) | k_{11} | $7.81 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-11} | $1.38 \times 10^{11} \text{ s}^{-1}$ |
| | k_{12} | $2.27 \times 10^{-8} \text{ s}^{-1}$ | k_{-15} | $1.26 \times 10^{12} \text{ s}^{-1}$ |
| | k_{15} | $7.98 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | | |
| | k_{16} | 4.70 s^{-1} | | |
| (HOBr + SO ₃ ²⁻) | k_{11} | $3.23 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-11} | $3.23 \times 10^9 \text{ s}^{-1}$ |
| | k_{12} | $7.39 \times 10^{-8} \text{ s}^{-1}$ | k_{-15} | |
| | k_{15} | $3.25 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | | $2.04 \times 10^{-4} \text{ s}^{-1}$ |
| | k_{16} | $1.25 \times 10^{-4} \text{ s}^{-1}$ | | |

Table S6. Calculated forward/reverse rate coefficients (k_1/k_{-1} , k_5/k_{-5}), and the unimolecular rate constant (k_2 , k_6) for the sulfate formation between HOBr and SO₃²⁻ through Pathway 2(HOBr + SO₃²⁻).

| Catalyst | Rate constants | | Rate constants | |
|--|----------------|--|----------------|-----------------------------------|
| Without catalyst | k_1 | $7.45 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-1} | $4.49 \times 10^9 \text{ s}^{-1}$ |
| | k_2 | $3.50 \times 10^5 \text{ s}^{-1}$ | | |
| (H ₂ O-catalyzed) | k_5 | $7.96 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} | $3.42 \times 10^9 \text{ s}^{-1}$ |
| | k_6 | $4.18 \times 10^5 \text{ s}^{-1}$ | | |
| (HSO ₄ ⁻ -catalyzed) | k_5 | $3.24 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} | 1.12 s^{-1} |
| | k_6 | $5.19 \times 10^{-3} \text{ s}^{-1}$ | | |

Table S7. Calculated overall rate constant, effective rate constant, S(IV) oxidation rate and the S(IV) lifetimes for Pathway 1(HOBr + SO₃²⁻) and Pathway 2 (HOBr + SO₃²⁻) from SO₃²⁻ and HOBr respectively, assuming [HOBr] = $5.89 \times 10^{-7} \text{ M}$ (corresponding to a Henry's law equilibrium with a gas phase HOBr mixing ratio of 0.31 ppbv), and [H₂O] = 55.56 M (corresponding to the known bulk concentration of H₂O).

| Rate constants | Catalysts | Overall rate constant M ⁻² s ⁻¹ | Effective rate constant ^d (M ⁻¹ s ⁻¹) | S(IV) oxidation rate (s ⁻¹) | S(IV) lifetime (s) |
|---|---|---|---|---|-----------------------|
| Pathway 1 ^a (HOBr + SO ₃ ²⁻) | Without catalyst | 1.08×10^{-27} | 1.08×10^{-27} | 6.34×10^{-34} | 1.58×10^{33} |
| | H ₂ O-catalyzed | 2.18×10^{-11} | 1.21×10^{-9} | 7.13×10^{-16} | 1.40×10^{15} |
| | HSO ₄ ⁻ -catalyzed ^c | 9.88×10^{-8} | 1.24×10^{-16} | 7.33×10^{-23} | 1.36×10^{22} |
| Pathway 1 ^b (HOBr + SO ₃ ²⁻) | Without catalyst | 2.30 | 2.30 | 1.35×10^{-6} | 7.39×10^5 |
| | H ₂ O-catalyzed | 1.24×10^1 | 6.90×10^2 | 4.07×10^{-4} | 2.46×10^3 |
| | HSO ₄ ⁻ -catalyzed ^c | 2.74×10^9 | 3.45×10^0 | 2.03×10^{-6} | 4.92×10^5 |
| Pathway 2 (HOBr + SO ₃ ²⁻) | Without catalyst | 5.80×10^5 | 5.80×10^5 | 3.42×10^{-1} | 2.93×10^0 |
| | H ₂ O-catalyzed | 1.62×10^4 | 9.01×10^5 | 5.31×10^{-1} | 1.88×10^0 |

| | | | | |
|---|----------------------|-----------------------|-----------------------|----------------------|
| HSO ₄ ⁻ -catalyzed ^c | 2.48×10 ⁷ | 3.12×10 ⁻² | 1.84×10 ⁻⁸ | 5.44×10 ⁷ |
|---|----------------------|-----------------------|-----------------------|----------------------|

^a The second step of Pathway 1(HOBr + SO₃²⁻) leading to sulfate formation through the hydrolysis reaction.

^b The second step of Pathway 1(HOBr + SO₃²⁻) leading to sulfate formation through the reaction of BrSO₃⁻ intermediate with OH⁻.

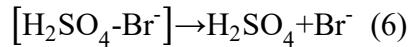
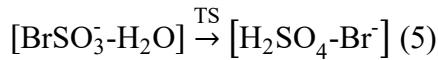
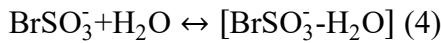
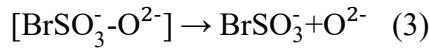
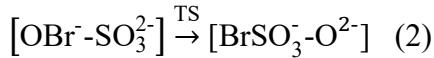
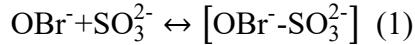
^c Assuming a general concentration of H⁺ act as the possible high limit for the concentration of HSO₄⁻ in cloud water.

^d Effective rate constant = Overall rate constant × [M], where [M] is the concentration of catalyst M.

3.3 The reaction rates between OBr⁻ and SO₃²⁻ leading to sulfate formation.

3.3.1 The reaction rate via Pathway 1(OBr⁻ + SO₃²⁻)

The detailed formation process of sulfate from OBr⁻ and SO₃²⁻ through Pathway 1(OBr⁻ + SO₃²⁻) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($v_{1\text{OBr}^- + \text{SO}_3^{2-}, \text{un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{OBr}^- + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_5 [\text{BrSO}_3^-\text{-H}_2\text{O}] \quad (7)$$

$$k_4 [\text{BrSO}_3^-][\text{H}_2\text{O}] - k_{-4} [\text{BrSO}_3^-\text{-H}_2\text{O}] - k_5 [\text{BrSO}_3^-\text{-H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^-\text{-H}_2\text{O}] = \frac{k_4 [\text{BrSO}_3^-][\text{H}_2\text{O}]}{k_{-4} + k_5} \quad (7-1)$$

$$k_3 [\text{BrSO}_3^-\text{-O}^{2-}] - k_4 [\text{BrSO}_3^-][\text{H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^-] = \frac{k_3 [\text{BrSO}_3^-\text{-O}^{2-}]}{k_4 [\text{H}_2\text{O}]} \quad (7-2)$$

$$k_2 [\text{OBr}^-\text{-SO}_3^{2-}] - k_3 [\text{BrSO}_3^-\text{-O}^{2-}] = 0$$

$$[\text{BrSO}_3^-\text{-O}^{2-}] = \frac{k_2 [\text{OBr}^-\text{-SO}_3^{2-}]}{k_3} \quad (7-3)$$

$$k_1 [\text{OBr}^-][\text{SO}_3^{2-}] - k_{-1} [\text{OBr}^-\text{-SO}_3^{2-}] - k_2 [\text{OBr}^-\text{-SO}_3^{2-}] = 0$$

$$[\text{OBr}^-\text{-SO}_3^{2-}] = \frac{k_1 [\text{OBr}^-][\text{SO}_3^{2-}]}{k_{-1} + k_2} \quad (7-4)$$

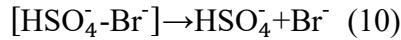
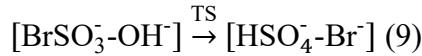
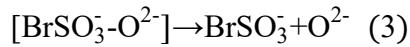
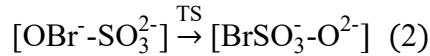
$$v_{1\text{OBr}^- + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_5}{k_{-4} + k_5} \times \frac{k_2 \times k_1}{k_{-1} + k_2} [\text{OBr}^-][\text{SO}_3^{2-}] \quad (7-6)$$

The pseudo-unimolecular uncatalyzed S(IV) oxidation rate through Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$) can be written as

$$v_{1\text{OBr}^- + \text{SO}_3^{2-}, \text{un-S(IV)}} = \frac{k_5}{k_{-4} + k_5} \times \frac{k_2 \times k_1}{k_{-1} + k_2} [\text{OBr}^-][\text{SO}_3^{2-}] \quad (7-7)$$

where k_1/k_{-1} and k_{-4} symbolize the forward/reverse and reverse rate coefficients for the reactions 1 and 4, respectively, as well as k_2 and k_5 are the unimolecular rate constants for the uncatalyzed reactions 2 and 5.

The possible formation process of sulfate from BrSO_3^- and OH^- is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($v_{1\text{OBr}^- + \text{SO}_3^{2-}, 2, \text{un}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{OBr}^- + \text{SO}_3^{2-}, 2, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_9 [\text{BrSO}_3^- - \text{OH}^-] \quad (11)$$

$$k_8 [\text{BrSO}_3^-] [\text{OH}^-] - k_{-8} [\text{BrSO}_3^- - \text{OH}^-] - k_9 [\text{BrSO}_3^- - \text{OH}^-] = 0$$

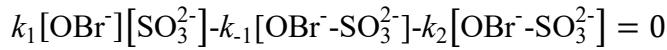
$$[\text{BrSO}_3^- - \text{OH}^-] = \frac{k_8 [\text{BrSO}_3^-] [\text{OH}^-]}{k_{-8} + k_9} \quad (11-1)$$

$$k_3 [\text{BrSO}_3^- - \text{O}^{2-}] - k_8 [\text{BrSO}_3^-] [\text{OH}^-] = 0$$

$$[\text{BrSO}_3^-] = \frac{k_3 [\text{BrSO}_3^- - \text{O}^{2-}]}{k_8 [\text{OH}^-]} \quad (11-2)$$

$$k_2 [\text{OBr}^- - \text{SO}_3^{2-}] - k_3 [\text{BrSO}_3^- - \text{O}^{2-}] = 0$$

$$[\text{BrSO}_3^{\cdot-}\text{-O}^{2-}] = \frac{k_2[\text{OBr}^{\cdot-}\text{-SO}_3^{2-}]}{k_3} \quad (11-3)$$



$$[\text{OBr}^{\cdot-}\text{-SO}_3^{2-}] = \frac{k_1[\text{OBr}^{\cdot-}][\text{SO}_3^{2-}]}{k_{-1} + k_2} \quad (11-4)$$

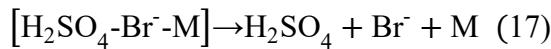
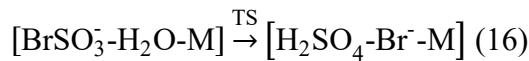
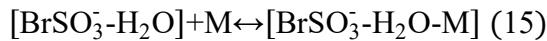
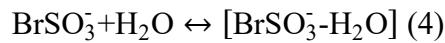
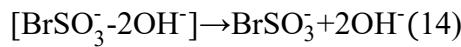
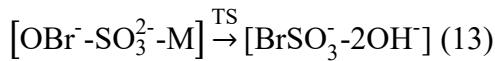
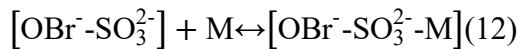
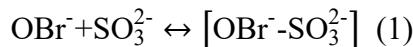
$$\nu_{1\text{OBr}^{\cdot-} + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_9}{k_{-8} + k_9} \times \frac{k_2 \times k_1}{k_{-1} + k_2} [\text{OBr}^{\cdot-}][\text{SO}_3^{2-}] \quad (11-5)$$

The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 1($\text{OBr}^{\cdot-} + \text{SO}_3^{2-}$) can be written as

$$\nu_{1\text{OBr}^{\cdot-} + \text{SO}_3^{2-}, \text{un-S(IV)}} = \frac{k_9}{k_{-8} + k_9} \times \frac{k_2 \times k_1}{k_{-1} + k_2} [\text{OBr}^{\cdot-}] \quad (11-6)$$

where k_{-8} symbolizes the reverse rate coefficients for the reaction 8, and k_9 is the unimolecular rate constant for the reaction 9.

The detailed catalyzed formation process of sulfate from $\text{OBr}^{\cdot-}$ and SO_3^{2-} through Pathway 1($\text{OBr}^{\cdot-} + \text{SO}_3^{2-}$) is similarly described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($\nu_{1\text{OBr}^{\cdot-} + \text{SO}_3^{2-}, \text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{OBr}^- + \text{SO}_3^{2-},\text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_{16}[\text{BrSO}_3^-\text{-H}_2\text{O-M}] \quad (18)$$

$$k_{15}[\text{BrSO}_3^-\text{-H}_2\text{O}][\text{M}] - k_{-15}[\text{BrSO}_3^-\text{-H}_2\text{O-M}] - k_{16}[\text{BrSO}_3^-\text{-H}_2\text{O-M}] = 0$$

$$[\text{BrSO}_3^-\text{-H}_2\text{O-M}] = \frac{k_{15}[\text{BrSO}_3^-\text{-H}_2\text{O}][\text{M}]}{k_{-15} + k_{16}} \quad (18-1)$$

$$k_4[\text{BrSO}_3^-\text{-H}_2\text{O}] - k_{-4}[\text{BrSO}_3^-\text{-H}_2\text{O}] - k_{15}[\text{BrSO}_3^-\text{-H}_2\text{O}][\text{M}] = 0$$

$$[\text{BrSO}_3^-\text{-H}_2\text{O}] = \frac{k_4 [\text{BrSO}_3^-\text{-H}_2\text{O}]}{k_{-4} + k_{15}[\text{M}]} \quad (18-2)$$

$$k_{14}[\text{BrSO}_3^-\text{-2OH}^-] - k_4[\text{BrSO}_3^-\text{-H}_2\text{O}] = 0$$

$$[\text{BrSO}_3^-] = \frac{k_{14}[\text{BrSO}_3^-\text{-2OH}^-]}{k_4[\text{H}_2\text{O}]} \quad (18-3)$$

$$k_{13}[\text{OBr}^-\text{-SO}_3^{2-}\text{-M}] - k_{14}[\text{BrSO}_3^-\text{-2OH}^-] = 0$$

$$[\text{BrSO}_3^-\text{-2OH}^-] = \frac{k_{13}[\text{OBr}^-\text{-SO}_3^{2-}\text{-M}]}{k_{14}} \quad (18-4)$$

$$k_{12}[\text{OBr}^-\text{-SO}_3^{2-}][\text{M}] - k_{-12}[\text{OBr}^-\text{-SO}_3^{2-}\text{-M}] - k_{13}[\text{OBr}^-\text{-SO}_3^{2-}\text{-M}] = 0$$

$$[\text{OBr}^-\text{-SO}_3^{2-}\text{-M}] = \frac{k_{12}[\text{OBr}^-\text{-SO}_3^{2-}][\text{M}]}{k_{-12} + k_{13}} \quad (18-5)$$

$$k_1[\text{OBr}^-][\text{SO}_3^{2-}] - k_{-1}[\text{OBr}^-\text{-SO}_3^{2-}] - k_{12}[\text{OBr}^-\text{-SO}_3^{2-}][\text{M}] = 0$$

$$[\text{OBr}^-\text{-SO}_3^{2-}] = \frac{k_1[\text{OBr}^-][\text{SO}_3^{2-}]}{k_{-1} + k_{12}[\text{M}]} \quad (18-6)$$

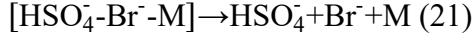
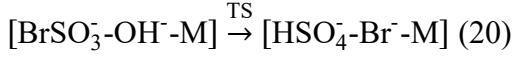
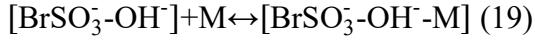
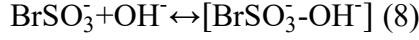
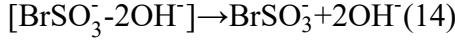
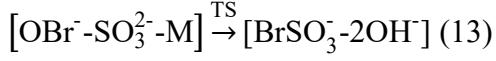
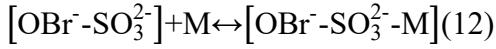
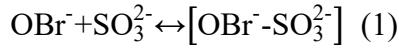
$$\begin{aligned} v_{1\text{OBr}^- + \text{SO}_3^{2-},\text{cat}} &= \frac{d[\text{SO}_4^{2-}]}{dt} \\ &= \frac{k_{16} \times k_{15}}{k_{-15} + k_{16}} \times \frac{1}{k_{-4} + k_{15}[\text{M}]} \times \frac{k_{12} \times k_{13}}{k_{-12} + k_{13}} \times \frac{k_1}{k_{-1} + k_{12}[\text{M}]} [\text{OBr}^-][\text{SO}_3^{2-}][\text{M}][\text{M}] \end{aligned} \quad (18-7)$$

The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 1(OBr⁻ + SO₃²⁻) can be written as

$$\begin{aligned} v_{1\text{OBr}^- + \text{SO}_3^{2-},\text{cat-S(IV)}} &= \\ \frac{k_{16} \times k_{15}}{k_{-15} + k_{16}} \times \frac{1}{k_{-4} + k_{15}[\text{M}]} \times \frac{k_{12} \times k_{13}}{k_{-12} + k_{13}} \times \frac{k_1}{k_{-1} + k_{12}[\text{M}]} [\text{OBr}^-][\text{M}][\text{M}] \end{aligned} \quad (18-8)$$

where k_{12}/k_{-12} and k_{15}/k_{-15} symbolize the forward/reverse rate coefficients for the reactions 12 and 15, respectively, as well as k_{13} and k_{16} are the unimolecular rate constants for the catalyzed reactions 13 and 16. In addition, [M] is the concentration of catalyst M.

The catalyzed formation process of sulfate from BrSO_3^- and OH^- is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($v_{1\text{OBr}^- + \text{SO}_3^{2-} - 2, \text{cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{1\text{OBr}^- + \text{SO}_3^{2-} - 2, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_{20}[\text{BrSO}_3^- \cdot \text{OH}^- \cdot \text{M}] \quad (22)$$

$$k_{19}[\text{BrSO}_3^- \cdot \text{OH}^-][\text{M}] - k_{-19}[\text{BrSO}_3^- \cdot \text{OH}^- \cdot \text{M}] - k_{20}[\text{BrSO}_3^- \cdot \text{OH}^- \cdot \text{M}] = 0$$

$$[\text{BrSO}_3^- \cdot \text{OH}^- \cdot \text{M}] = \frac{k_{19}[\text{BrSO}_3^- \cdot \text{OH}^-][\text{M}]}{k_{-19} + k_{20}} \quad (22-1)$$

$$k_8[\text{BrSO}_3^-][\text{OH}^-] - k_{-8}[\text{BrSO}_3^- \cdot \text{OH}^-] - k_{19}[\text{BrSO}_3^- \cdot \text{OH}^-][\text{M}] = 0$$

$$[\text{BrSO}_3^- \cdot \text{OH}^-] = \frac{k_8[\text{BrSO}_3^-][\text{OH}^-]}{k_{-8} + k_{19}[\text{M}]} \quad (22-2)$$

$$k_{14}[\text{BrSO}_3^- \cdot 2\text{OH}^-] - k_8[\text{BrSO}_3^-][\text{OH}^-] = 0$$

$$[\text{BrSO}_3^-] = \frac{k_{14}[\text{BrSO}_3^- \cdot 2\text{OH}^-]}{k_8[\text{OH}^-]} \quad (22-3)$$

$$k_{13}[\text{OBr}^- \cdot \text{SO}_3^{2-} \cdot \text{M}] - k_{14}[\text{BrSO}_3^- \cdot 2\text{OH}^-] = 0$$

$$[\text{BrSO}_3^- \cdot 2\text{OH}^-] = \frac{k_{13}[\text{OBr}^- \cdot \text{SO}_3^{2-} \cdot \text{M}]}{k_{14}} \quad (22-4)$$

$$k_{12}[\text{OBr}^- \cdot \text{SO}_3^{2-}][\text{M}] - k_{-12}[\text{OBr}^- \cdot \text{SO}_3^{2-} \cdot \text{M}] - k_{13}[\text{OBr}^- \cdot \text{SO}_3^{2-} \cdot \text{M}] = 0$$

$$[\text{OBr}^- \cdot \text{SO}_3^{2-} \cdot \text{M}] = \frac{k_{12} [\text{OBr}^- \cdot \text{SO}_3^{2-}] [\text{M}]}{k_{-12} + k_{13}} \quad (22-5)$$

$$k_1 [\text{OBr}^-] [\text{SO}_3^{2-}] - k_{-1} [\text{OBr}^- \cdot \text{SO}_3^{2-}] - k_{12} [\text{OBr}^- \cdot \text{SO}_3^{2-}] [\text{M}] = 0$$

$$[\text{OBr}^- \cdot \text{SO}_3^{2-}] = \frac{k_1 [\text{OBr}^-] [\text{SO}_3^{2-}]}{k_{-1} + k_{12} [\text{M}]} \quad (22-6)$$

$$\begin{aligned} v_{1\text{OBr}^- + \text{SO}_3^{2-}, \text{cat}} &= \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{20} \times k_{19}}{k_{-19} + k_{20}} \times \frac{1}{k_{-8} + k_{19} [\text{M}]} \times \frac{k_{13} \times k_{12}}{k_{-12} + k_{13}} \\ &\times \frac{k_1}{k_{-1} + k_{12} [\text{M}]} [\text{OBr}^-] [\text{SO}_3^{2-}] [\text{M}] [\text{M}] \end{aligned} \quad (22-7)$$

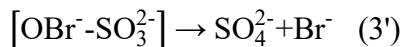
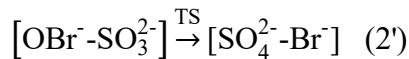
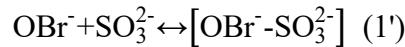
The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$) can be written as

$$\begin{aligned} v_{1\text{OBr}^- + \text{SO}_3^{2-}, \text{cat-S(IV)}} &= \frac{k_{20} \times k_{19}}{k_{-19} + k_{20}} \times \frac{1}{k_{-8} + k_{19} [\text{M}]} \times \frac{k_{13} \times k_{12}}{k_{-12} + k_{13}} \\ &\times \frac{k_1}{k_{-1} + k_{12} [\text{M}]} [\text{OBr}^-] [\text{M}] [\text{M}] \end{aligned} \quad (22-8)$$

where k_{19}/k_{-19} symbolize the forward/reverse rate coefficients for the reaction 19 and k_{20} is the unimolecular rate constant for the catalyzed reaction 20. In addition, $[\text{M}]$ is the concentration of catalyst M.

3.3.2 The reaction rate via Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$)

The detailed formation process of sulfate from OBr^- and SO_3^{2-} through Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the uncatalyzed formation reaction rate ($v_{2\text{OBr}^- + \text{SO}_3^{2-}, \text{un}}$) of (where k_n is the rate constant for reaction n in the scheme given above):

$$v_{2\text{OBr}^- + \text{SO}_3^{2-}, \text{un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_2' [\text{OBr}^- \cdot \text{SO}_3^{2-}] \quad (4')$$

$$k_{1'}[\text{OBr}^-][\text{SO}_3^{2-}] - k_{-1'}[\text{OBr}^-][\text{SO}_3^{2-}] - k_{2'}[\text{OBr}^- \cdot \text{SO}_3^{2-}] = 0$$

$$[\text{OBr}^- \cdot \text{SO}_3^{2-}] = \frac{k_{1'}[\text{OBr}^-][\text{SO}_3^{2-}]}{k_{-1'} + k_{2'}} \quad (4'-1)$$

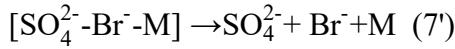
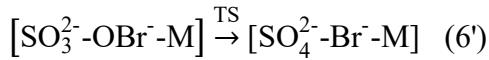
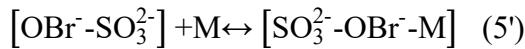
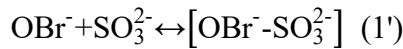
$$\nu_{2\text{OBr}^- + \text{SO}_3^{2-,un}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_{1'} \times k_{2'}}{k_{-1'} + k_{2'}} [\text{OBr}^-][\text{SO}_3^{2-}] \quad (4'-2)$$

The pseudo-unimolecular uncatalyzed S(IV) oxidation rates through Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$) can be written as

$$\nu_{2\text{OBr}^- + \text{SO}_3^{2-,S(IV)}} = \frac{k_{1'} \times k_{2'}}{k_{-1'} + k_{2'}} [\text{OBr}^-] \quad (4'-3)$$

where $k_{1'}/k_{-1'}$ symbolizes the forward/reverse rate coefficients for the reaction 1' and $k_{2'}$ is the unimolecular rate constant for the uncatalyzed reaction 2'.

The detailed catalyzed formation process of sulfate from OBr^- and SO_3^{2-} through Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$) is described by the following reaction equations:



Applying the steady-state approximation to the pre-reactive complex and assuming that the complex is in equilibrium with the reactant, we obtain the following expressions for the catalyzed formation reaction rate ($\nu_{2\text{OBr}^- + \text{SO}_3^{2-,cat}}$) of sulfate (where k_n is the rate constant for reaction n in the scheme given above):

$$\nu_{2\text{OBr}^- + \text{SO}_3^{2-,cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = k_6 [\text{SO}_3^{2-} \cdot \text{OBr}^- \cdot \text{M}] \quad (8')$$

$$k_5 [\text{OBr}^- \cdot \text{SO}_3^{2-}] [\text{M}] - k_{-5'} [\text{SO}_3^{2-} \cdot \text{OBr}^- \cdot \text{M}] - k_6 [\text{SO}_3^{2-} \cdot \text{OBr}^- \cdot \text{M}] = 0$$

$$[\text{SO}_3^{2-} \cdot \text{OBr}^- \cdot \text{M}] = \frac{k_5 [\text{OBr}^- \cdot \text{SO}_3^{2-}] [\text{M}]}{k_{-5'} + k_6} \quad (8'-1)$$

$$k_{1'} [\text{OBr}^-] [\text{SO}_3^{2-}] - k_{-1'} [\text{OBr}^- \cdot \text{SO}_3^{2-}] - k_{5'} [\text{OBr}^- \cdot \text{SO}_3^{2-}] [\text{M}] = 0$$

$$[\text{OBr}^- \cdot \text{SO}_3^{2-}] = \frac{k_{1'} [\text{OBr}^-] [\text{SO}_3^{2-}]}{k_{-1'} + k_{5'} [\text{M}]} \quad (8'-2)$$

$$v_{2\text{OBr}^- + \text{SO}_3^{2-}, \text{cat}} = \frac{d[\text{SO}_4^{2-}]}{dt} = \frac{k_6' \times k_5'}{k_{-5'} + k_6'} \times \frac{k_1'}{k_{-1'} + k_5' [\text{M}]} \times [\text{OBr}^-] [\text{SO}_3^{2-}] [\text{M}] \quad (8'-3)$$

The pseudo-unimolecular catalyzed S(IV) oxidation rate through Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$) can be written as

$$v_{2\text{OBr}^- + \text{SO}_3^{2-}, \text{cat-S(IV)}} = \frac{k_6' \times k_5'}{k_{-5'} + k_6'} \times \frac{k_1'}{k_{-1'} + k_5' [\text{M}]} \times [\text{OBr}^-] [\text{M}] \quad (8'-4)$$

where $k_5'/k_{-5'}$ symbolizes the forward/reverse rate coefficients for the reaction 5' and k_6' is the unimolecular rate constant for the catalyzed reaction 6'.

3.3.3 S(IV) oxidation rate, related reaction rate constants and S(IV) lifetimes through Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$) and Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$)

Table S8. Calculated forward/reverse rate coefficients (k_1/k_{-1} , k_4/k_{-4} , k_8/k_{-8} , k_{12}/k_{-12} , k_{15}/k_{-15} , k_{19}/k_{-19}), and the unimolecular rate constants (k_2 , k_5 , k_9 , k_{13} , k_{16} , k_{20}) for the sulfate formation between OBr^- and SO_3^{2-} through Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$).

| Catalyst | Rate constants | | Rate constants | |
|--|----------------|---|----------------|--------------------------------------|
| Without catalyst | k_1 | $3.23 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-1} | $4.53 \times 10^9 \text{ s}^{-1}$ |
| | k_2 | $1.88 \times 10^{-3} \text{ s}^{-1}$ | | |
| | k_4 | $7.81 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-4} | $5.57 \times 10^9 \text{ s}^{-1}$ |
| | k_5 | $8.05 \times 10^{-28} \text{ s}^{-1}$ | | |
| | k_8 | $7.69 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-8} | $1.61 \times 10^{11} \text{ s}^{-1}$ |
| | k_9 | 1.03 s^{-1} | | |
| | k_{12} | $8.00 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-12} | $4.53 \times 10^8 \text{ s}^{-1}$ |
| | k_{13} | $3.67 \times 10^2 \text{ s}^{-1}$ | | |
| | k_{15} | $7.81 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-15} | $1.38 \times 10^{11} \text{ s}^{-1}$ |
| | k_{16} | $2.27 \times 10^{-8} \text{ s}^{-1}$ | | |
| (H ₂ O-catalyzed) | k_{19} | $7.98 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-19} | $5.03 \times 10^7 \text{ s}^{-1}$ |
| | k_{20} | 4.70 s^{-1} | | |
| | k_{12} | $3.23 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-12} | $4.53 \times 10^9 \text{ s}^{-1}$ |
| | k_{13} | $3.25 \times 10^9 \text{ s}^{-1}$ | | |
| | k_{15} | $3.23 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-15} | $1.64 \times 10^9 \text{ s}^{-1}$ |
| (HSO ₄ ⁻ -catalyzed) | k_{16} | $7.39 \times 10^{-8} \text{ s}^{-1}$ | | |
| | k_{19} | $3.25 \times 10^9 \text{ M}^{-1} \text{s}^{-1}$ | k_{-19} | $2.04 \times 10^{-4} \text{ s}^{-1}$ |
| | k_{20} | $1.25 \times 10^{-4} \text{ s}^{-1}$ | | |

Table S9. Calculated forward/reverse rate coefficients ($k_1'/k_{-1'}$, $k_5'/k_{-5'}$), and the unimolecular rate constants (k_2' , k_6') for the sulfate formation between OBr^- and SO_3^{2-} .

through Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$).

| Rate constant | Rate constants | Rate constants | |
|---------------|--|----------------|--------------------------------------|
| k_1 , | $3.23 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-1} , | $6.75 \times 10^{10} \text{ s}^{-1}$ |
| | $3.32 \times 10^{-5} \text{ s}^{-1}$ | | |
| k_5 , | $8.03 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} , | $3.19 \times 10^5 \text{ s}^{-1}$ |
| | 2.54×10^{-4} | | |
| k_6 , | $3.25 \times 10^9 \text{ M}^{-1}\text{s}^{-1}$ | k_{-5} , | $2.87 \times 10^{-4} \text{ s}^{-1}$ |
| | $2.46 \times 10^2 \text{ s}^{-1}$ | | |

Table S10. Calculated overall rate constant, effective rate constant, S(IV) oxidation rate and the S(IV) lifetimes for Pathway 1($\text{OBr}^- + \text{SO}_3^{2-}$) and Pathway 2($\text{OBr}^- + \text{SO}_3^{2-}$) from SO_3^{2-} and OBr^- respectively, assuming $[\text{OBr}^-] = 7.42 \times 10^{-7} \text{ M}$ (corresponding to a Henry's law equilibrium with a gas phase HOBr mixing ratio of 0.31 ppbv at pH=9), and $[\text{H}_2\text{O}] = 55.56 \text{ M}$ (corresponding to the known bulk concentration of H_2O).

| Rate constants | Catalysts | Overall rate constant $\text{M}^{-2}\text{s}^{-1}$ | Effective rate constant ^d ($\text{M}^{-1}\text{s}^{-1}$) | S(IV) oxidation rate (s^{-1}) | S(IV) lifetime (s) |
|---|--|--|---|--|-----------------------|
| Pathway 1 ^a ($\text{OBr}^- + \text{SO}_3^{2-}$) | Without catalyst | 1.94×10^{-40} | 1.94×10^{-40} | 1.44×10^{-46} | 6.96×10^{45} |
| | H_2O -catalyzed | 1.36×10^{-19} | 4.21×10^{-16} | 3.12×10^{-22} | 3.20×10^{21} |
| | HSO_4^- -catalyzed ^c | 2.51×10^{-8} | 2.51×10^{-26} | 1.86×10^{-32} | 5.37×10^{31} |
| Pathway 1 ^b ($\text{OBr}^- + \text{SO}_3^{2-}$) | Without catalyst | 6.80×10^{-15} | 6.80×10^{-15} | 5.05×10^{-21} | 1.98×10^{20} |
| | H_2O -catalyzed | 4.44×10^{-8} | 1.37×10^{-4} | 1.02×10^{-10} | 9.83×10^9 |
| | HSO_4^- -catalyzed ^c | 1.76×10^7 | 1.76×10^{-11} | 1.31×10^{-17} | 7.64×10^{16} |
| Pathway 2 ($\text{OBr}^- + \text{SO}_3^{2-}$) | Without catalyst | 1.59×10^{-6} | 1.59×10^{-6} | 1.18×10^{-12} | 8.49×10^{11} |
| | H_2O -catalyzed | 4.01×10^{-2} | 2.23 | 1.65×10^{-6} | 6.04×10^5 |
| | HSO_4^- -catalyzed ^c | 1.56×10^8 | 1.56×10^{-1} | 1.15×10^{-7} | 8.66×10^6 |

^a The second step of Pathway 1 ($\text{OBr}^- + \text{SO}_3^{2-}$) leading to sulfate formation through the hydrolysis reaction.

^b The second step of Pathway 1 ($\text{OBr}^- + \text{SO}_3^{2-}$) leading to sulfate formation through the reaction of BrSO_3^- intermediate with OH^- .

^c Assuming a general concentration of H^+ act as the possible higher limit for the concentration of HSO_4^- in cloud water.

^d Effective rate constant = Overall rate constant \times [M], where [M] is the concentration of catalyst M.

Section 4. Cartesian coordinates of the structures.

4.1 Cartesian coordinates of the structures involving in the reaction of HOBr with HOSO₂⁻.

Table S11. Coordinates of HOBr. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|----------|
| O | 0.021200 | 1.437606 | 0.000000 |
| H | -0.911587 | 1.678685 | 0.000000 |
| Br | 0.021200 | -0.376558 | 0.000000 |

Table S12. Coordinates of HOSO₂⁻. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 0.174133 | 0.000070 | -0.381367 |
| O | -1.480647 | -0.001124 | 0.046825 |
| H | -1.462594 | -0.000264 | 1.013624 |
| O | 0.658589 | -1.218452 | 0.294668 |
| O | 0.656617 | 1.219468 | 0.294537 |

Table S13. Coordinates of BrSO₃⁻. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.018881 | -0.000009 | 0.000016 |
| O | -1.298949 | -1.256781 | 0.633168 |
| O | -1.298964 | 1.176750 | 0.771791 |
| O | -1.299024 | 0.080039 | -1.404952 |
| Br | 1.356503 | 0.000003 | -0.000009 |

Table S14. Coordinates of BrSO₃H. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.880751 | 0.120799 | 0.069210 |
| O | -1.289144 | -1.073702 | -0.866719 |
| H | -1.289927 | -1.899639 | -0.361576 |
| O | -1.269048 | -0.181821 | 1.397289 |
| O | -1.259093 | 1.303032 | -0.598161 |
| Br | 1.312006 | -0.011806 | -0.005859 |

Table S15. Coordinates of cis-H₂SO₄. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|----------|----------|
| S | 0.000000 | 0.091216 | 0.120238 |
| O | -0.000020 | 1.494832 | 0.195960 |

| | | | |
|---|-----------|-----------|-----------|
| O | 0.000013 | -0.758497 | 1.259994 |
| O | -1.223808 | -0.312199 | -0.783942 |
| H | -1.556128 | -1.177623 | -0.514162 |
| O | 1.223810 | -0.312168 | -0.783949 |
| H | 1.556168 | -1.177575 | -0.514159 |

Table S16. Coordinates of trans-H₂SO₄. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.000002 | 0.000001 | -0.153840 |
| O | 0.641015 | -1.068244 | -0.819725 |
| O | -0.641020 | 1.068270 | -0.819690 |
| O | 1.029516 | 0.662937 | 0.836058 |
| O | -1.029509 | -0.662963 | 0.836045 |
| H | 1.691785 | 0.010654 | 1.099951 |
| H | -1.691765 | -0.010681 | 1.099974 |

Table S17. Coordinates of SO₄²⁻. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.000002 | 0.000017 | -0.000050 |
| O | 0.374677 | 0.239450 | 1.421658 |
| O | 1.227987 | -0.274813 | -0.797412 |
| O | -0.685196 | 1.206218 | -0.542828 |
| O | -0.917463 | -1.170888 | -0.081318 |

Table S18. Coordinates of H₂O. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| H | -0.000000 | 0.000000 | 0.116661 |
| O | 0.000000 | 0.760848 | -0.466644 |
| O | -0.000000 | -0.760848 | -0.466644 |

Table S19. Coordinates of OH⁻. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|----------|-----------|
| O | -0.000000 | 0.000000 | 0.106625 |
| H | 0.000000 | 0.000000 | -0.853002 |

Table S20. Coordinates of HSO₄⁻. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.142029 | -0.029869 | -0.000006 |
| O | -0.900566 | 1.193776 | -0.000107 |
| O | -0.232877 | -0.817287 | -1.211881 |
| O | -0.233038 | -0.817186 | 1.211922 |

| | | | |
|---|----------|-----------|----------|
| O | 1.405583 | 0.532161 | 0.000068 |
| H | 1.959652 | -0.253800 | 0.000082 |

Table S21. Coordinates of reactant complex (R_{c1}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.427633 | -0.133204 | 0.040985 |
| O | 1.984175 | 1.296588 | -0.572656 |
| H | 1.762363 | 2.010589 | 0.042141 |
| O | 2.052072 | -0.212097 | 1.369052 |
| O | 2.014100 | -1.067179 | -0.926653 |
| O | -3.151990 | 0.106632 | 0.025565 |
| H | -3.440872 | -0.543055 | -0.625659 |
| Br | -1.267156 | -0.009366 | 0.021866 |

Table S22. Coordinates of transition state (P_{c2}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| O | -1.144381 | -1.843517 | 0.007509 |
| H | -1.347257 | -1.861750 | 0.947528 |
| Br | 1.441060 | -0.591378 | -0.024336 |
| S | 3.420095 | 0.327536 | -0.019076 |
| O | 3.107250 | 1.842213 | 0.156205 |
| H | 2.966684 | 2.090686 | 1.088336 |
| O | 4.123158 | -0.156613 | 1.120129 |
| O | 3.970510 | 0.189525 | -1.321330 |
| S | -3.870488 | 0.339355 | -0.000272 |
| O | -4.138490 | 1.790947 | -0.057268 |
| O | -5.113813 | -0.415618 | -0.262991 |
| O | -3.334093 | -0.024582 | 1.330302 |
| O | -2.856848 | -0.012079 | -1.037890 |
| H | -1.756586 | -1.163181 | -0.351873 |

Table S23. Coordinates of product complex (R_{c3}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 0.342745 | 0.690269 | 0.003442 |
| O | 0.941680 | 0.406782 | 1.282483 |
| O | 1.088154 | 0.183042 | -1.128057 |
| O | -0.168271 | 2.024963 | -0.160272 |
| O | 3.413365 | -1.184098 | -0.062709 |
| H | 2.642865 | -0.745384 | -0.450686 |
| H | 3.355970 | -0.974361 | 0.874341 |
| Br | -1.533776 | -0.593430 | 0.001992 |

Table S24. Coordinates of reactant complex (TS_3). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 0.716046 | -0.160474 | 0.024768 |
| O | 0.828803 | -0.877085 | -1.212304 |
| O | 0.834227 | 1.389566 | -0.020218 |
| O | 0.798791 | -0.790021 | 1.307656 |
| O | 2.762989 | 0.191429 | 0.053070 |
| H | 1.890476 | 1.354598 | -0.027653 |
| H | 3.085191 | -0.041956 | -0.822830 |
| Br | -1.663740 | 0.055538 | -0.016327 |

Table S25. Coordinates of transition state (P_{c3}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.566238 | 0.110840 | 0.041666 |
| O | 1.435473 | 0.195213 | 1.462515 |
| O | 0.529932 | -0.850525 | -0.536860 |
| O | 1.611906 | 1.328763 | -0.698770 |
| O | 2.891271 | -0.637893 | -0.313916 |
| H | -0.466335 | -0.543199 | -0.330771 |
| H | 3.040588 | -1.409501 | 0.258348 |
| Br | -2.268078 | -0.003006 | 0.002915 |

Table S26. Coordinates of product complex (R_{c4}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.007458 | -0.439482 | 0.316425 |
| O | 0.581178 | 0.674236 | 1.025632 |
| O | 0.615932 | -0.738344 | -0.951016 |
| O | -0.312041 | -1.582439 | 1.134257 |
| O | 3.133176 | 1.680571 | 0.232594 |
| H | 3.061303 | 2.250234 | -0.539509 |
| H | 2.220600 | 1.434724 | 0.449935 |
| O | 3.532374 | -0.981495 | -0.673097 |
| H | 2.599736 | -1.130289 | -0.872705 |
| H | 3.545202 | -0.057229 | -0.374920 |
| Br | -2.048927 | 0.346115 | -0.282073 |

Table S27. Coordinates of reactant complex (TS_4). Units are in angstrom.

| atom | X | Y | Z |
|------|----------|-----------|-----------|
| S | 0.549142 | 0.449643 | -0.010165 |
| O | 0.723513 | -0.368873 | -1.157271 |
| O | 0.676697 | -0.116827 | 1.286406 |
| O | 0.163766 | 1.807765 | -0.153016 |
| O | 3.575070 | -1.535051 | -0.013867 |

| | | | |
|----|-----------|-----------|-----------|
| H | 3.332726 | -1.898494 | 0.845035 |
| H | 2.970702 | -1.956567 | -0.635498 |
| O | 2.677961 | 0.990897 | -0.088258 |
| H | 2.917195 | 1.471972 | 0.713745 |
| H | 3.114746 | 0.107844 | -0.019547 |
| Br | -2.390220 | -0.318353 | 0.007627 |

Table S28. Coordinates of transition state (P_{c4}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.615124 | -0.594010 | -0.012610 |
| O | -1.237412 | 0.699913 | -0.521949 |
| O | -1.288087 | -0.833345 | 1.371653 |
| O | -1.332044 | -1.702429 | -0.889505 |
| O | -4.285826 | 1.834307 | 0.062815 |
| H | -3.659131 | 2.469530 | 0.449969 |
| H | -4.489010 | 2.119938 | -0.843837 |
| O | -3.255946 | -0.460310 | -0.031933 |
| H | -3.675133 | -1.138295 | 0.519892 |
| H | -3.852918 | 0.894894 | 0.039745 |
| Br | 3.791791 | 0.252943 | 0.003067 |

Table S29. Coordinates of product complex (R_{c5}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.663798 | -0.064638 | 0.000002 |
| O | -2.830060 | 1.106089 | -0.000001 |
| H | -3.702334 | 0.678324 | -0.000009 |
| O | -1.969735 | -0.850822 | -1.214745 |
| O | -1.969751 | -0.850827 | 1.214738 |
| O | 1.230612 | 1.376371 | 0.000001 |
| H | 0.291344 | 1.101905 | 0.000006 |
| Br | 2.124092 | -0.199786 | 0.000001 |

Table S30. Coordinates of reactant complex (TS₅). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.858352 | -0.165624 | 0.008480 |
| O | 1.791103 | 1.453275 | -0.086653 |
| H | 2.694794 | 1.811313 | -0.068148 |
| O | 2.584834 | -0.441692 | 1.252171 |
| O | 2.593166 | -0.589871 | -1.187213 |
| O | -0.311657 | -0.186245 | 0.008596 |
| H | -0.342084 | -1.155452 | 0.010163 |
| Br | -2.438454 | 0.003154 | 0.000774 |

Table S31. Coordinates of transition state (P_{c5}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.646423 | -0.066252 | 0.071228 |
| O | -1.474783 | 1.280283 | -0.719095 |
| H | -1.870957 | 2.026630 | -0.240316 |
| O | -2.892207 | -0.663925 | -0.287792 |
| O | -1.416258 | 0.195703 | 1.457212 |
| O | -0.535877 | -0.889315 | -0.553785 |
| H | 0.446609 | -0.544225 | -0.324029 |
| Br | 2.237717 | 0.005590 | 0.007211 |

Table S32. Coordinates of product complex (R_{c6}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.689482 | -0.562651 | -0.043972 |
| O | 2.509761 | 0.820847 | -0.413508 |
| H | 1.919010 | 1.569443 | -0.179470 |
| O | 1.691389 | -0.578780 | 1.435606 |
| O | 2.618258 | -1.568023 | -0.596455 |
| O | -1.127050 | 0.566290 | -0.976709 |
| H | -0.270441 | 0.094833 | -0.874743 |
| O | 0.553102 | 2.671870 | 0.214998 |
| H | 0.441513 | 2.710033 | 1.170763 |
| H | -0.228160 | 2.205248 | -0.112441 |
| Br | -2.253066 | -0.367850 | 0.096799 |

Table S33. Coordinates of reactant complex (TS_6). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.922238 | -0.395002 | 0.056415 |
| O | 1.898289 | 0.923038 | -0.870401 |
| H | 1.156423 | 1.510337 | -0.566685 |
| O | 2.373114 | 0.061716 | 1.378490 |
| O | 2.909066 | -1.230674 | -0.637011 |
| O | -0.320428 | -0.547812 | -0.001948 |
| H | -0.303256 | -1.246435 | 0.670306 |
| O | -0.186343 | 2.383894 | -0.058873 |
| H | -0.002392 | 2.865784 | 0.754916 |
| H | -0.793121 | 1.675779 | 0.198362 |
| Br | -2.405801 | -0.320192 | -0.012617 |

Table S34. Coordinates of transition state (P_{c6}). Units are in angstrom.

| atom | X | Y | Z |
|------|---|---|---|
| | | | |

| | | | |
|----|-----------|-----------|-----------|
| S | 1.728078 | -0.216876 | 0.065513 |
| O | 1.430815 | 0.949666 | -0.879776 |
| H | 0.648574 | 1.572122 | -0.528750 |
| O | 1.471728 | 0.189932 | 1.415420 |
| O | 3.022655 | -0.726752 | -0.252612 |
| O | 0.724141 | -1.323632 | -0.337102 |
| H | -0.241275 | -1.031739 | -0.189258 |
| O | -0.460709 | 2.343385 | -0.096662 |
| H | -0.277743 | 2.756432 | 0.756309 |
| H | -1.143845 | 1.656424 | 0.064091 |
| Br | -2.175543 | -0.369829 | 0.001579 |

4.2 Cartesian coordinates of the structures involving in the reaction of HOBr with SO₃²⁻.

Table S35. Coordinates of SO₃²⁻. Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.000055 | -0.000023 | 0.332061 |
| O | -0.171848 | 1.409296 | -0.221366 |
| O | -1.134796 | -0.853445 | -0.221340 |
| O | 1.306754 | -0.555805 | -0.221415 |

Table S36. Coordinates of monomer (M₇). Units are in angstrom.

| atom | X | Y | Z |
|------|-------------|-------------|-------------|
| S | -1.05978900 | 0.00994400 | -0.02952400 |
| O | -1.74023800 | 1.37383200 | 0.08497500 |
| O | -1.44002600 | -0.74724400 | 1.24208400 |
| O | -1.77860300 | -0.71314900 | -1.16886200 |
| O | 3.28879445 | 0.93178316 | -1.76698883 |
| H | 3.81448122 | 1.05680239 | -0.96306569 |
| Br | 1.60237850 | 0.67795094 | -1.19116728 |

Table S37. Coordinates of product complex (P_{c7}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.517619 | -0.063942 | 0.004340 |
| O | -1.798264 | -0.498979 | 1.348972 |
| O | -1.763046 | -1.047084 | -1.019481 |
| O | -1.962285 | 1.269939 | -0.310948 |
| O | 4.757766 | -0.149211 | 0.034197 |
| H | 3.866296 | -0.399166 | -0.218029 |
| Br | 0.758350 | 0.137855 | -0.007809 |

Table S38. Coordinates of reactant complex (R_{c8}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 0.478604 | -0.144418 | 0.000202 |
| O | 0.960060 | 1.211467 | -0.095560 |
| O | 0.730443 | -0.792814 | 1.261157 |
| O | 0.712723 | -0.957736 | -1.165307 |
| O | 4.076786 | 0.228760 | 0.000537 |
| H | 3.194267 | 0.605716 | -0.005628 |
| Br | -1.791200 | 0.119645 | -0.000121 |

Table S39. Coordinates of transition state (TS_8). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.805044 | 0.020026 | 0.001853 |
| O | -0.908701 | -0.770179 | -1.185880 |
| O | -0.904517 | -0.617157 | 1.278226 |
| O | -0.889124 | 1.444709 | -0.086122 |
| O | -3.236596 | 0.066687 | -0.004440 |
| H | -3.354624 | -0.886284 | -0.000933 |
| Br | 1.821338 | -0.012189 | -0.001228 |

Table S40. Coordinates of product complex (P_{c8}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 2.214578 | -0.003426 | 0.002085 |
| O | 1.937760 | -0.718536 | 1.232736 |
| O | 1.919999 | -0.781246 | -1.185951 |
| O | 1.701369 | 1.347694 | -0.028589 |
| O | 3.800961 | 0.241372 | -0.017181 |
| H | 4.266137 | -0.607657 | -0.025444 |
| Br | -3.273717 | -0.001480 | -0.000458 |

Table S41. Coordinates of product complex (R_{c9}). Units are in angstrom.

| Atom | X | Y | Z |
|------|----------|-----------|-----------|
| S | 0.099989 | 0.193893 | -0.122658 |
| O | 0.178015 | 1.484651 | -0.756089 |
| O | 0.576831 | 0.149098 | 1.235996 |
| O | 0.509025 | -0.916889 | -0.948145 |
| O | 3.565197 | 1.050631 | 0.152463 |
| H | 2.708483 | 1.355295 | 0.461188 |
| O | 3.298822 | -1.455676 | 0.067919 |
| H | 3.399915 | -0.419514 | 0.104905 |
| H | 2.393865 | -1.584610 | -0.234120 |

| | | | |
|----|-----------|-----------|----------|
| Br | -2.146435 | -0.141371 | 0.103240 |
|----|-----------|-----------|----------|

Table S42. Coordinates of product complex (TS₉). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -0.416334 | 0.372256 | 0.013357 |
| O | -0.141088 | 1.767413 | -0.128730 |
| O | -0.708500 | -0.408842 | -1.149640 |
| O | -0.630845 | -0.186859 | 1.310827 |
| O | -2.712679 | 0.948934 | 0.084185 |
| H | -2.823758 | 1.306087 | -0.800649 |
| O | -3.356177 | -1.496017 | 0.014534 |
| H | -3.094648 | -0.496893 | 0.022570 |
| H | -2.547212 | -1.949180 | -0.237139 |
| Br | 2.157751 | -0.280375 | -0.007083 |

Table S43. Coordinates of product complex (P_{c9}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.803550 | -0.621420 | 0.029320 |
| O | 1.183605 | -1.817192 | -0.498729 |
| O | 1.519515 | 0.562813 | -0.770030 |
| O | 1.627225 | -0.423605 | 1.448062 |
| O | 3.386406 | -0.844040 | -0.087539 |
| H | 3.632852 | -1.003432 | -1.010836 |
| O | 3.358252 | 2.593792 | -0.006868 |
| H | 4.139951 | 2.093188 | 0.244675 |
| H | 2.715140 | 1.920713 | -0.281804 |
| Br | -3.655565 | 0.181660 | -0.002866 |

Table S44. Coordinates of reactant complex (R_{c10}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.762919 | 0.004596 | -0.006057 |
| O | -2.791349 | 1.056405 | -0.368336 |
| O | -1.953122 | -1.149073 | -0.967020 |
| O | -2.115418 | -0.505624 | 1.374949 |
| O | 1.014734 | 1.244662 | -0.019949 |
| H | 0.097153 | 0.820882 | -0.026365 |
| Br | 2.139165 | -0.173297 | -0.000968 |

Table S45. Coordinates of reactant complex (TS₁₀). Units are in angstrom.

| Atom | X | Y | Z |
|------|----------|-----------|-----------|
| S | 1.978718 | 0.024790 | -0.008049 |
| O | 2.399176 | -1.033901 | -0.991108 |

| | | | |
|----|-----------|-----------|-----------|
| O | 2.745377 | 1.285385 | -0.320605 |
| O | 2.374501 | -0.430605 | 1.370218 |
| O | -0.469252 | -0.024219 | -0.007909 |
| H | -0.307053 | 0.909569 | -0.196009 |
| Br | -2.507167 | 0.009157 | -0.002285 |

Table S46. Coordinates of reactant complex (P_{c10}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.754022 | -0.059252 | -0.000000 |
| O | -2.971243 | 0.732127 | -0.000063 |
| O | -1.578224 | -0.846523 | -1.210208 |
| O | -1.578296 | -0.846432 | 1.210276 |
| O | -0.616661 | 1.038607 | -0.000005 |
| H | 0.299226 | 0.625160 | -0.000007 |
| Br | 2.334872 | -0.008553 | 0.000000 |

Table S47. Coordinates of product complex (R_{c11}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -2.634408 | -0.347818 | 0.028644 |
| O | -2.403512 | 1.183851 | 0.017230 |
| O | -3.512993 | -0.615614 | -1.180143 |
| O | -3.495360 | -0.599065 | 1.253707 |
| O | 1.308934 | -0.597938 | -0.311710 |
| H | 0.831738 | 0.285631 | -0.235772 |
| Br | 3.030841 | -0.192045 | 0.063369 |
| O | 0.081799 | 1.674644 | -0.155736 |
| H | -0.918114 | 1.475923 | -0.066061 |
| H | 0.326529 | 2.158114 | 0.638836 |

Table S48. Coordinates of product complex (TS_{11}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.932451 | -0.343078 | 0.006494 |
| O | -2.497382 | 1.063223 | -0.129999 |
| O | -2.429340 | -1.148983 | -1.156352 |
| O | -2.481078 | -0.935078 | 1.270459 |
| O | 0.480756 | -0.347346 | 0.012370 |
| H | 0.346078 | 0.619160 | -0.026424 |
| Br | 2.542389 | -0.249425 | 0.001074 |
| O | -0.224743 | 2.462798 | -0.099816 |
| H | -1.124119 | 2.055332 | -0.080650 |
| H | -0.072078 | 2.787701 | 0.792293 |

Table S49. Coordinates of product complex (P_{c11}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.818543 | -0.144016 | 0.025328 |
| O | 1.598060 | 0.941193 | -0.925433 |
| O | 1.566247 | 0.266097 | 1.394594 |
| O | 3.085081 | -0.819185 | -0.165699 |
| O | 0.758178 | -1.266085 | -0.318662 |
| H | -0.175847 | -0.933869 | -0.194309 |
| Br | -2.259173 | -0.384878 | 0.002879 |
| O | -0.614029 | 2.490254 | 0.005977 |
| H | 0.214372 | 2.086389 | -0.296635 |
| H | -1.212452 | 1.724289 | 0.058735 |

4.3 Cartesian coordinates of the structures involving in the reaction of OBr⁻ with SO₃²⁻.

Table S50. Coordinates of OBr-. Units are in angstrom.

| atom | X | Y | Z |
|------|----------|----------|-----------|
| O | 0.000000 | 0.000000 | -1.461728 |
| Br | 0.000000 | 0.000000 | 0.334109 |

Table S51. Coordinates of reactant complex (R_{c12}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 2.853608 | -0.024325 | -0.027034 |
| O | 3.340422 | -0.209897 | 1.409439 |
| O | 3.741249 | -0.926377 | -0.883550 |
| O | 3.238968 | 1.405373 | -0.407701 |
| O | -4.355405 | 0.494444 | 0.058548 |
| Br | -2.667988 | -0.163404 | -0.028039 |

Table S52. Coordinates of transition state (TS₁₂). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.297174 | -0.022195 | -0.000003 |
| O | -1.686205 | -0.759764 | 1.214203 |
| O | -1.860775 | 1.338720 | -0.000603 |
| O | -1.686046 | -0.760764 | -1.213654 |
| O | 3.429158 | -0.147585 | -0.000029 |
| Br | 1.005306 | 0.085436 | 0.000020 |

Table S53. Coordinates of reactant complex (R_{c13}). Units are in angstrom.

| Atom | X | Y | Z |
|------|----------|----------|-----------|
| | 2.225526 | 0.168093 | -0.001913 |

| | | |
|-----------|-----------|-----------|
| 2.766911 | 1.553194 | -0.361704 |
| 2.838207 | -0.163935 | 1.360741 |
| 2.883470 | -0.795551 | -0.991087 |
| -2.941489 | -0.811399 | 0.002889 |
| -4.032427 | 1.431459 | -0.001775 |
| -3.549279 | 0.500573 | 0.000055 |
| -3.324858 | 2.080082 | -0.000989 |
| -1.167190 | -0.428008 | -0.001170 |

Table S54. Coordinates of transition state (TS₁₃). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 2.200092 | 0.160574 | 0.000273 |
| O | 2.638973 | 1.558353 | -0.384433 |
| O | 2.758057 | -0.146772 | 1.374266 |
| O | 2.812254 | -0.812874 | -0.985825 |
| O | -2.802225 | -0.849052 | -0.001615 |
| O | -4.593387 | 1.073930 | 0.008946 |
| H | -3.425683 | -0.027806 | 0.005266 |
| H | -4.026542 | 1.846462 | -0.057585 |
| Br | -0.978818 | -0.313614 | -0.001222 |

Table S55. Coordinates of product complex (P_{c13}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | 1.680182 | 0.294937 | 0.002518 |
| O | 1.247056 | 1.664175 | -0.109322 |
| O | 2.262447 | -0.060844 | 1.271474 |
| O | 2.366513 | -0.226120 | -1.152215 |
| O | -4.702118 | -0.480589 | 0.008649 |
| O | -2.525596 | 2.110024 | -0.006312 |
| H | -4.011289 | 0.188924 | 0.006819 |
| H | -1.921365 | 1.363421 | -0.004143 |
| Br | -0.289619 | -0.866415 | -0.004033 |

Table S56. Coordinates of reactant complex (R_{c14}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -2.700801 | -0.009142 | -0.007471 |
| O | -3.426318 | -1.004225 | -0.911704 |
| O | -3.267196 | -0.247406 | 1.391073 |
| O | -3.209200 | 1.369546 | -0.428942 |
| O | 1.386490 | -0.230448 | -0.065239 |
| Br | 3.181217 | 0.029901 | 0.006801 |

Table S57. Coordinates of transition state (TS₁₄). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.965569 | -0.001749 | 0.004910 |
| O | -2.581893 | -0.972745 | 1.001481 |
| O | -2.540862 | 1.368806 | 0.331517 |
| O | -2.518632 | -0.382531 | -1.360782 |
| O | 0.401586 | -0.010089 | 0.011996 |
| Br | 2.553358 | 0.000013 | 0.001364 |

Table S58. Coordinates of product complex (P_{c14}). Units are in angstrom.

| Atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -2.737586 | -0.000020 | -0.000480 |
| O | -3.236137 | -0.991822 | -0.982126 |
| O | -3.269488 | -0.328038 | 1.344195 |
| O | -3.189840 | 1.356420 | -0.392233 |
| O | -1.255369 | -0.036244 | 0.030762 |
| Br | 3.754516 | -0.000063 | 0.000083 |

Table S59. Coordinates of reactant complex (R_{c15}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -2.670341 | -0.299962 | 0.054776 |
| O | -3.459629 | -0.995073 | -1.048382 |
| O | -3.581805 | -0.288517 | 1.277370 |
| O | -2.561983 | 1.167557 | -0.385797 |
| O | 1.318766 | -0.535554 | 0.086303 |
| O | 0.128712 | 1.765063 | -0.059203 |
| H | 0.621165 | 0.885025 | -0.006872 |
| H | -0.814677 | 1.531032 | -0.167580 |
| Br | 3.090471 | -0.186413 | 0.009592 |

Table S60. Coordinates of transition state (TS_{15}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -1.923184 | -0.260883 | 0.005550 |
| O | -2.393834 | -1.179550 | -1.103496 |
| O | -2.493103 | -0.806138 | 1.299634 |
| O | -2.592694 | 1.088458 | -0.232432 |
| O | 0.402517 | -0.244062 | 0.021135 |
| O | -0.006298 | 2.291460 | 0.009184 |
| H | 0.271889 | 1.304286 | 0.016765 |
| H | -0.967399 | 2.188663 | -0.060632 |
| Br | 2.518107 | -0.243433 | 0.000082 |

Table S61. Coordinates of reactant complex (P_{c15}). Units are in angstrom.

| atom | X | Y | Z |
|------|-----------|-----------|-----------|
| S | -2.469126 | -0.171390 | -0.000000 |
| O | -3.276439 | -0.441475 | -1.209997 |
| O | -3.276486 | -0.441413 | 1.209979 |
| O | -2.049808 | 1.256881 | -0.000028 |
| O | -1.261647 | -1.027580 | 0.000046 |
| O | 0.647233 | 1.859217 | 0.000001 |
| H | 1.306647 | 1.141179 | 0.000006 |
| H | -0.239866 | 1.454381 | -0.000010 |
| Br | 3.205040 | -0.271382 | -0.000000 |

6 Note and References

- 1 J. Liu, A. Ning, L. Liu, H. Wang, T. Kurtén and X. Zhang, *Sci. Total Environ.*, 2021, **787**, 147551.
- 2 W. F. Mccoy, E. R. B. III and R. W. Johnson, Hypohalous Acid and haloamine flashoff in industrial evaporative cooling systems, Cooling Tower Institute Annual Meeting, 1990.