

Supporting Information

Screening of metal complexes and organic solvents using COSMOSAC-LANL model to enhance the energy density in non-aqueous redox flow cell: an insight into the solubility

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1 Error estimation from coefficient of determination (R^2)

For a linear function, $y = (y_1 \cdots \cdots y_n)$ of input $x = (x_1 \cdots \cdots x_n)$, the a and b of smallest residual is

$$(a, b) = \underset{i}{\operatorname{argmin}} \sum (y_i - ax_i - b)^2, \quad (1)$$

which gives you $a = \operatorname{argmin} \operatorname{var}(y - ax)$, $b = \bar{y} - a\bar{x}$ and $R^2 = \frac{\operatorname{var}(ax)}{\operatorname{var}(y)} = \operatorname{corr}(x, y)$, where for any two vectors u, v, \bar{u} is the empirical mean. $\operatorname{var}(u)$ and $\operatorname{corr}(u, v)$ the correlation.

Now, $\operatorname{var}(y - ax)$ is equal to $(1-R^2)*\operatorname{var}(y)$. By normalizing errors by $\operatorname{var}(y)$, one will obtain

$$\operatorname{Error} = \frac{\operatorname{var}(y - ax)}{\operatorname{var}(y)} = 1 - R^2. \quad (2)$$

Now ‘error’ is the root mean error divided by the standard deviation of the output and which is $\sqrt{\operatorname{Error}}$.

Table S 1: The details of COSMO setting for the metal complexes

<p>XC potential in SCF: GGA: BP XC energy after SCF: Default Relativity (ZORA): Scalar XC: Becke Perdew Basis set: TZP Frozen core: Small Integration: Becke Good Density used in exchange potential: Exact Total charge: 0.0 Spin polarization: 2.0 - 3.0 Coordinates used for optimization: Delocalized Optimization method: new Number of geometry iterations: 100 Maximum no of SCF cycles: 50 Convergence method: DIIS Mixing: 0.2</p>	<p>Solvation method: COSMO Solvent: CRS Default radii: Klamt Surface: Delley Ndiv: 4 Charge determination method: CONJ Convergence: 1.00E-06 Max. iterations: 300 Correct for outlying charge: Yes Calculate coulomb interaction: EXACT Disc scaling: 0.01 Disc Legendre order: 4 Disc tolerance: 0.1 Handle charges: VAR Charges in which SCF cycles: ALL —</p>
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Table S 2: The details of COSMO setting for the organic solvents

XC potential in SCF: GGA: BP XC energy after SCF: Default Relativity (ZORA): Scalar XC: Becke Perdew Basis set: TZP Frozen core: Small Integration: Becke Good Density used in exchange potential: Exact Total charge: 0.0 Spin polarization: 0.0 Coordinates used for optimization: Delocalized Optimization method: new Number of geometry iterations: 100 Maximum no of SCF cycles: 50 Convergence method: DIIS Mixing: 0.2	Solvation method: COSMO Solvent: CRS Default radii: Klamt Surface: Delley Ndiv: 4 Charge determination method: CONJ Convergence: 1.00E-06 Max. iterations: 300 Correct for outlying charge: Yes Calculate coulomb interaction: EXACT Disc scaling: 0.01 Disc Legendre order: 4 Disc tolerance: 0.1 Handle charges: VAR Charges in which SCF cycles: ALL –
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Table S 3: The details of frequency calculations.

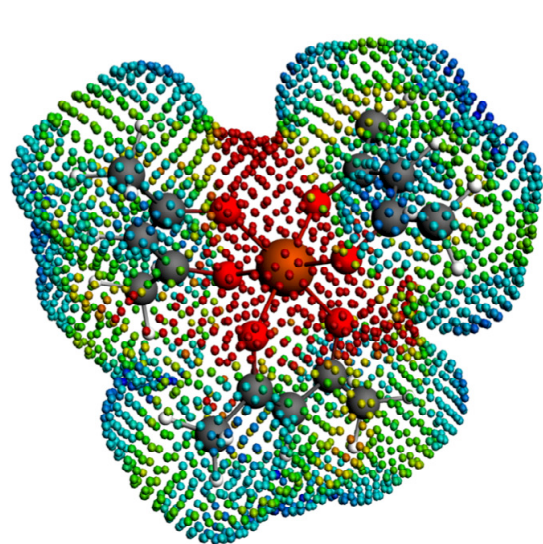
Basis set	TZP
Frozen Core	Small
Task	GO & Frequency calculation
XC	Becke Perdew
Frequency	Analytical
Numerical quality	Excellent

Table S 4: Margules parameters of metal complexes in acetonitrile organic solvent at 297 K , COSMO Volume and COSMO Surface

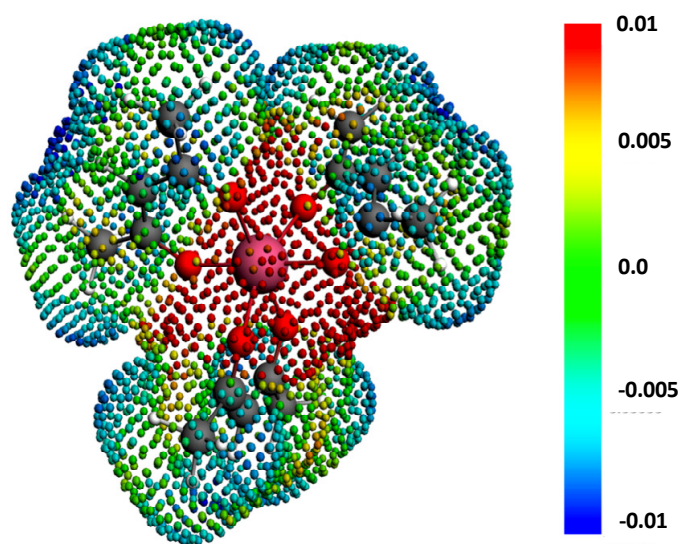
Organic solvents	γ_{12}	A_{12}	γ_{21}	A_{21}	COSMO Volume (\AA^3)	COSMO Surface (\AA^2)
I	1.14	0.08	0.76	-0.16	387.35	357.69
II	1.058	0.03	0.75	-0.17	383.47	357.32
III	1.11	0.06	0.77	-0.16	379.83	353.29
IV	1.08	0.05	0.74	-0.18	393.18	351.10
V	0.96	-0.02	0.73	-0.19	389.56	362.22
VI	0.54	-0.36	0.43	-0.49	769.95	637.70
VII	1.82	0.35	0.47	-0.44	830.02	657.92
VIII	0.12	-1.26	0.32	-0.67	953.15	798.82
IX	0.06	-1.63	0.33	-0.65	866.90	728.61
X	0.02	-2.30	0.27	-0.78	1089.89	921.52
XI	0.26	-0.80	0.56	-0.35	460.46	411.09
XII	3.58	0.753	1.11	0.062	470.97	421.89
XIII	0.12	-1.27	0.45	-0.47	520.23	460.10

Table S 5: Margules parameters of $V(\text{acac})_3$ in 14 different organic solvents at 297 K.

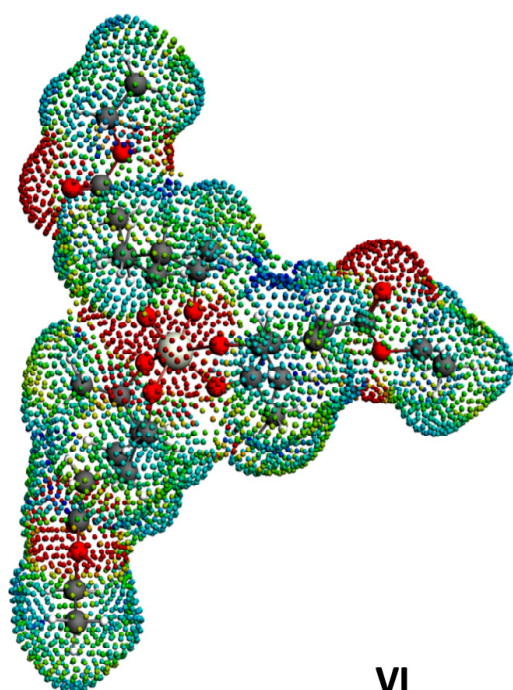
Numbers	Organic solvents	γ_{12}	A_{12}	γ_{21}	A_{21}
1	Cyclohexane	73.63	2.54	2.61	0.57
2	Diisopropyl Ether	1.47	0.23	1.13	0.07
3	1-Butanol	2.07	0.43	1.87	0.37
4	1-Hexanol	2.76	0.60	2.28	0.49
5	1-Hexyne	0.50	-0.41	0.73	-0.19
6	1-Heptyne	0.74	-0.18	0.87	-0.08
7	1-Hexene	8.29	1.25	1.74	0.33
8	Benzene	1.38	0.19	0.90	-0.06
9	1,3do	0.44	-0.48	0.66	-0.25
10	ACN	1.14	0.08	0.76	-0.16
11	DMPU	0.53	-0.38	0.71	-0.20
12	GBL	0.70	-0.21	0.82	-0.11
13	MA	0.54	-0.36	0.71	-0.21
14	PC	1.72	0.32	1.08	0.05



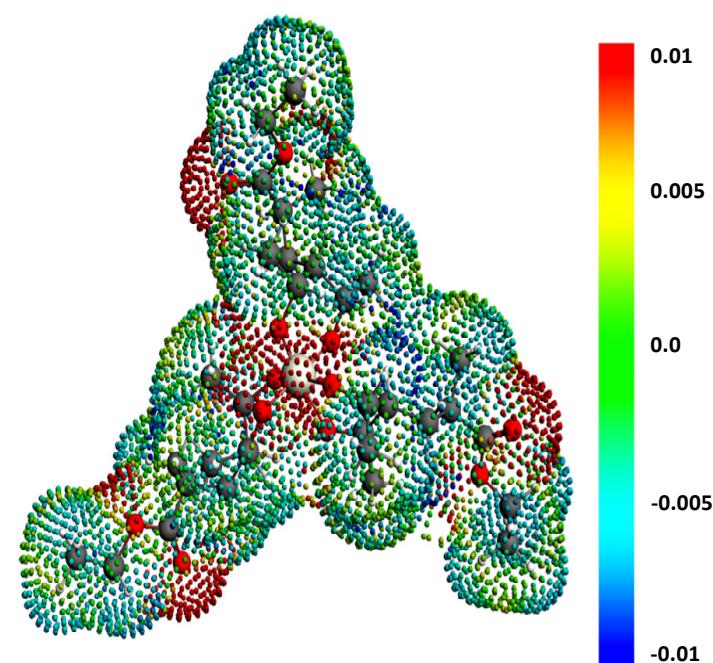
IV



V

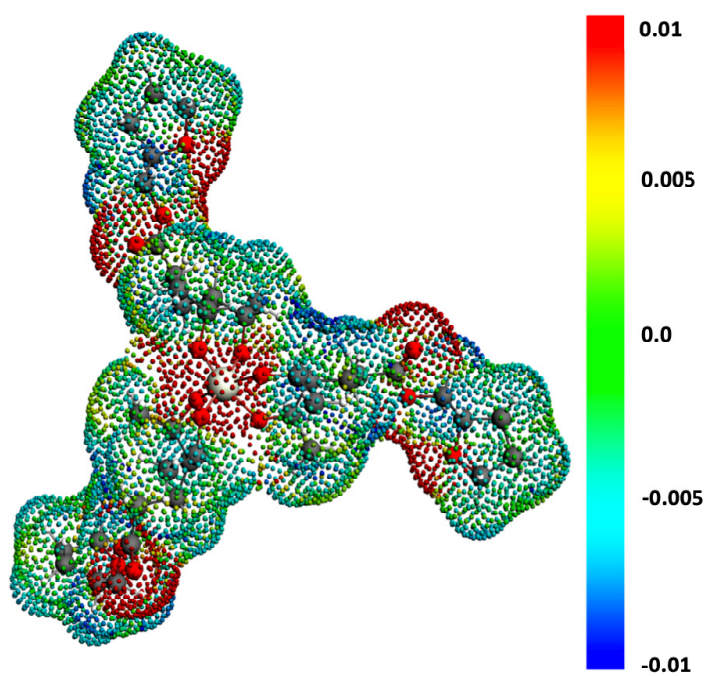


VI

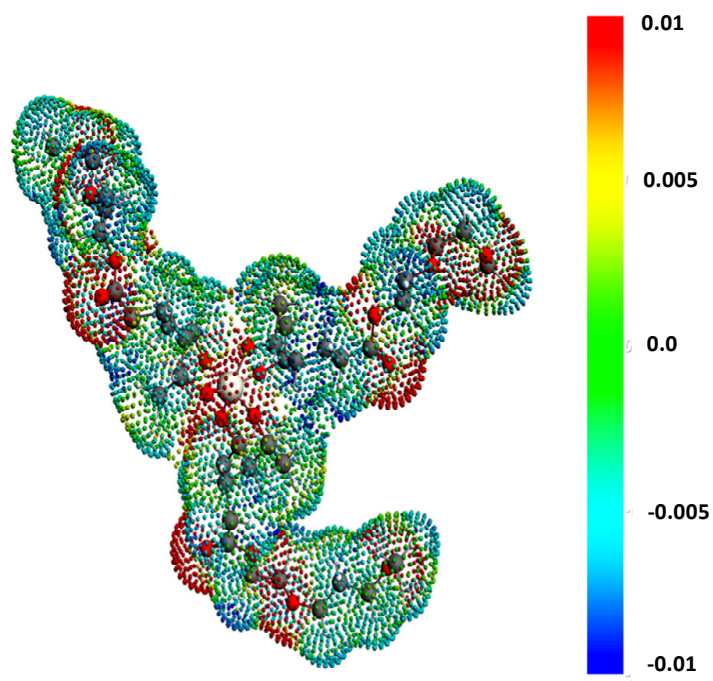


VII

Figure. S 1: COSMO Surface points of metal complexes.

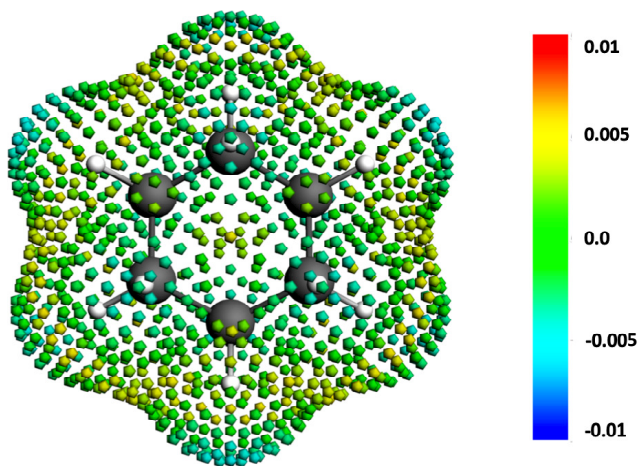


VIII

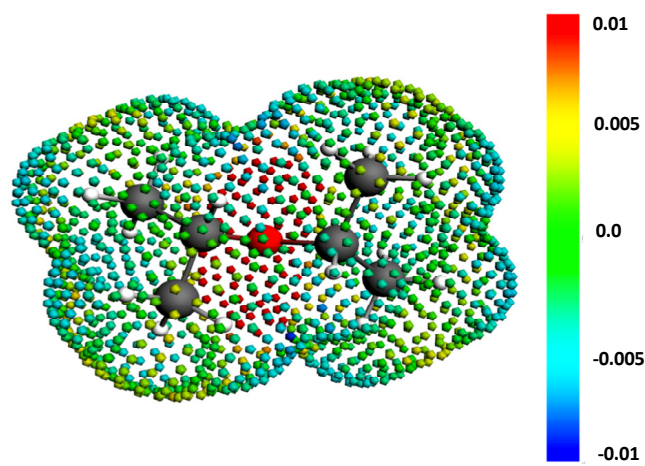


X

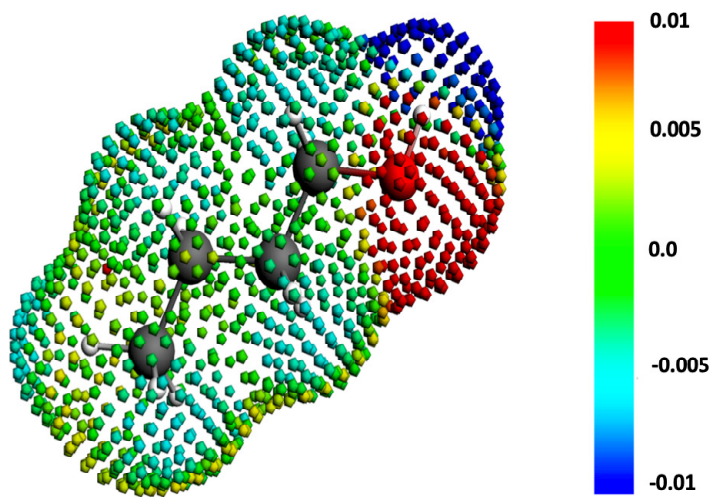
Figure. S 2: COSMO Surface points of metal complexes.



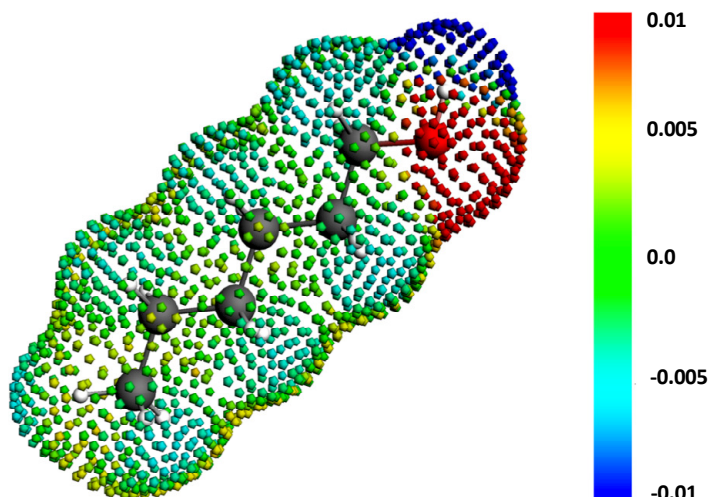
Cyclohexane



Diisopropyl Ether

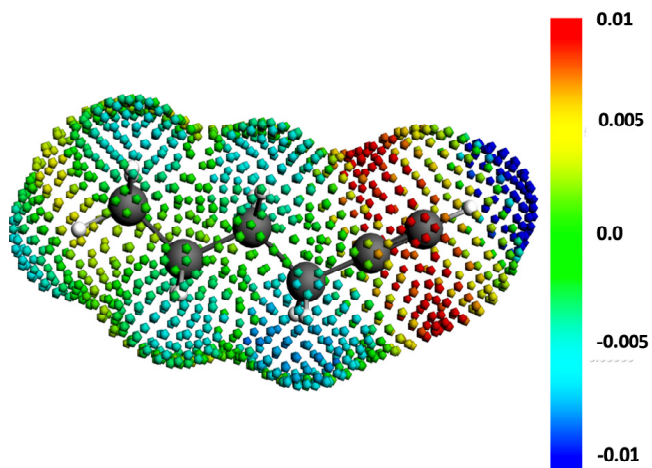


1-Butanol

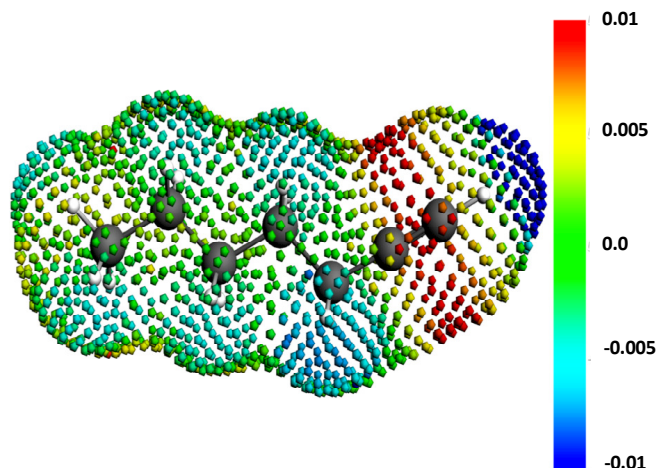


1-Hexanol

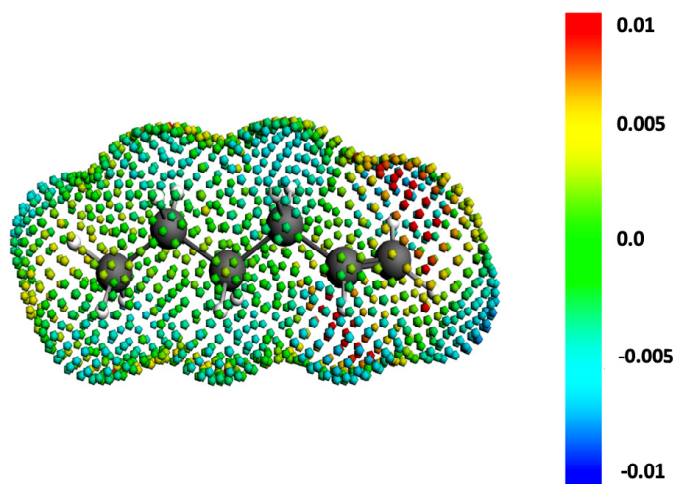
Figure. S 3: COSMO surface points of organic solvents.



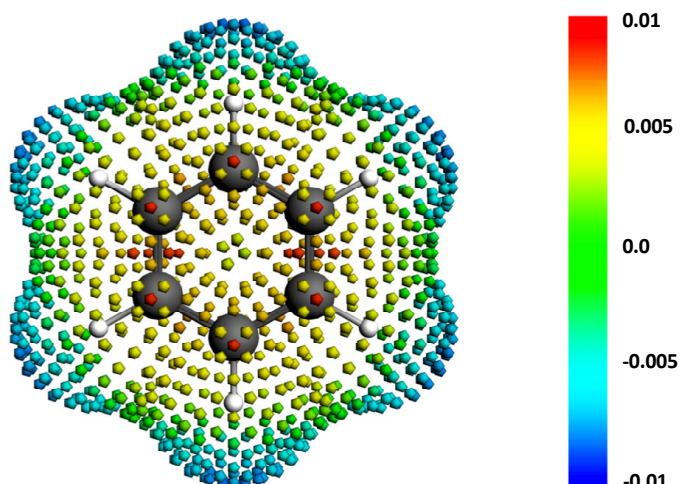
1-Hexyne



1-Heptyne



1-Hexene



Benzene

Figure. S 4: COSMO surface points of organic solvents.

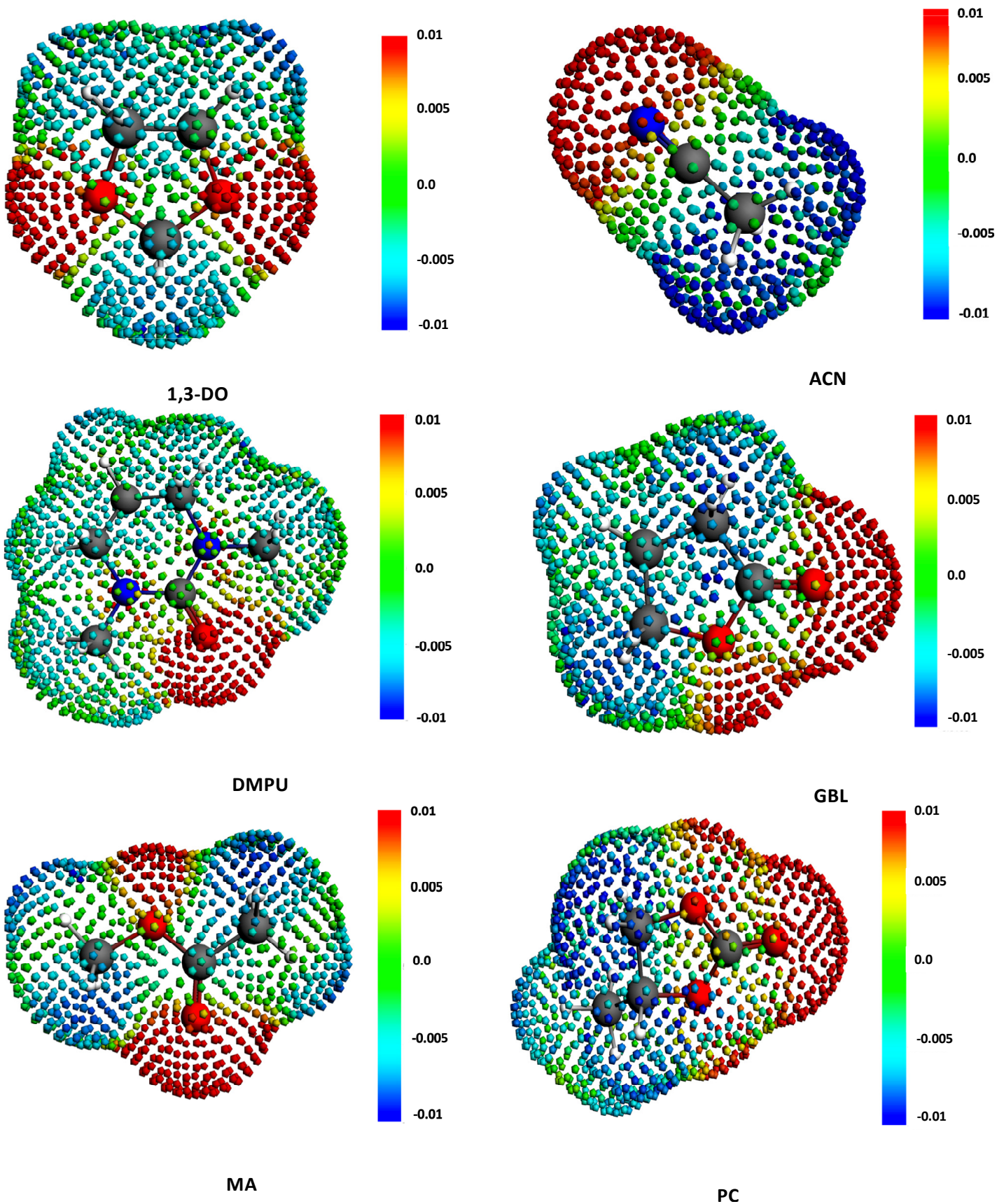


Figure. S 5: COSMO surface points of organic solvents.

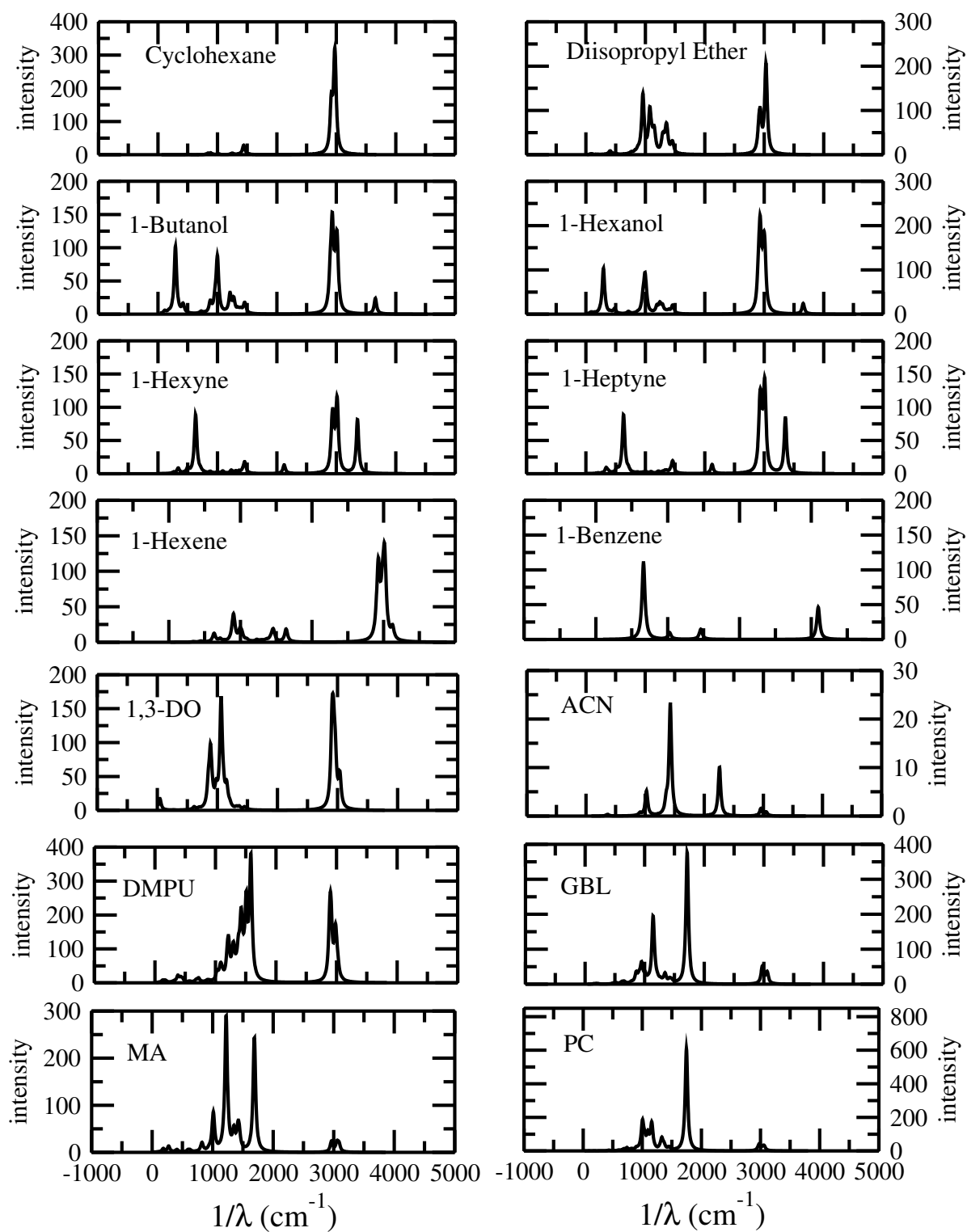


Figure. S 6: Analytical frequency of 14 different organic solvents at ambient condition.

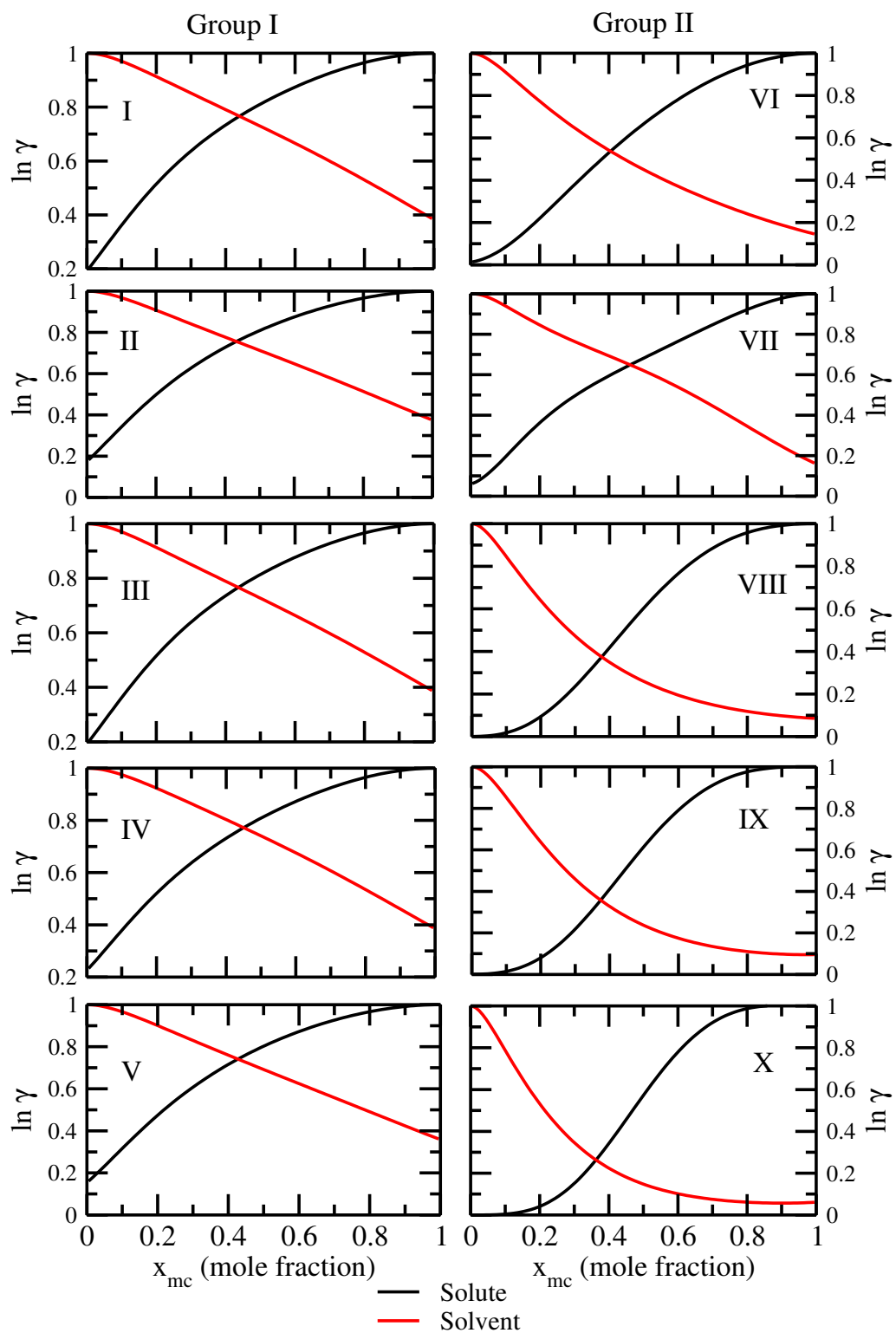


Figure. S 7: Gibbs-Duhem relationship of Group I and II type of metal complexes in acetonitrile solvent. The black curve is for the solute and the red curve is for the solvent.

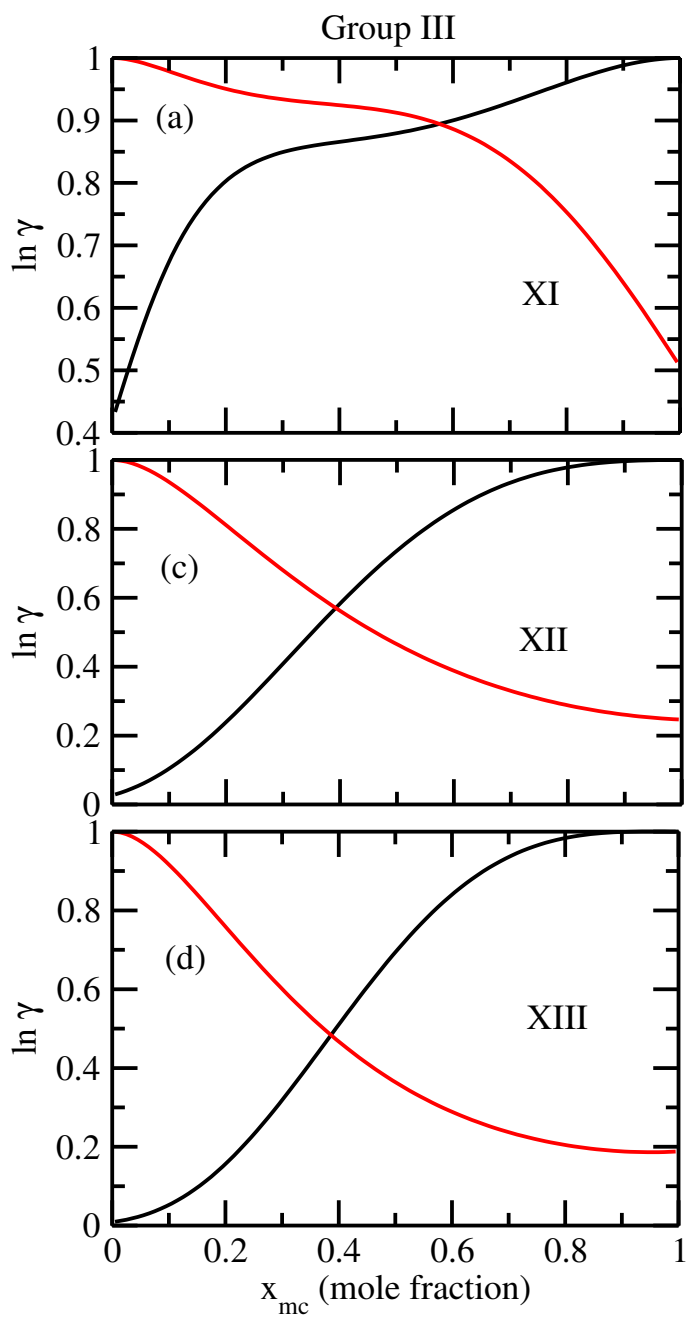


Figure. S 8: Gibbs-Duhem relationship of Group III type of metal complexes in acetonitrile solvent. The black curve is for the solute and the red curve is for the solvent.

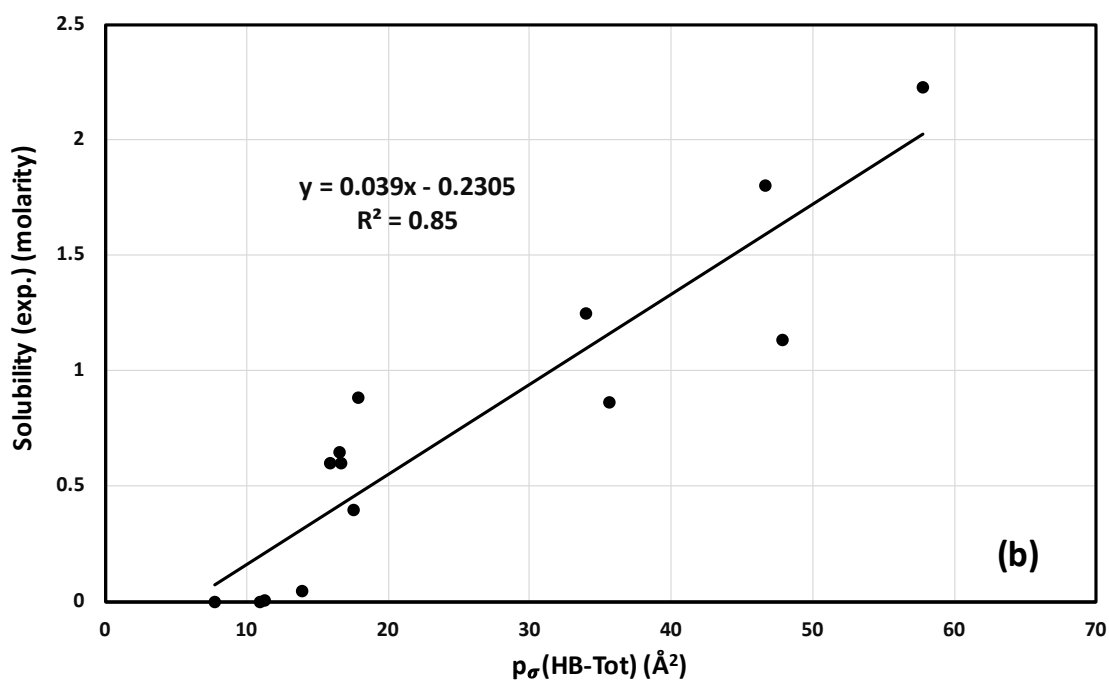
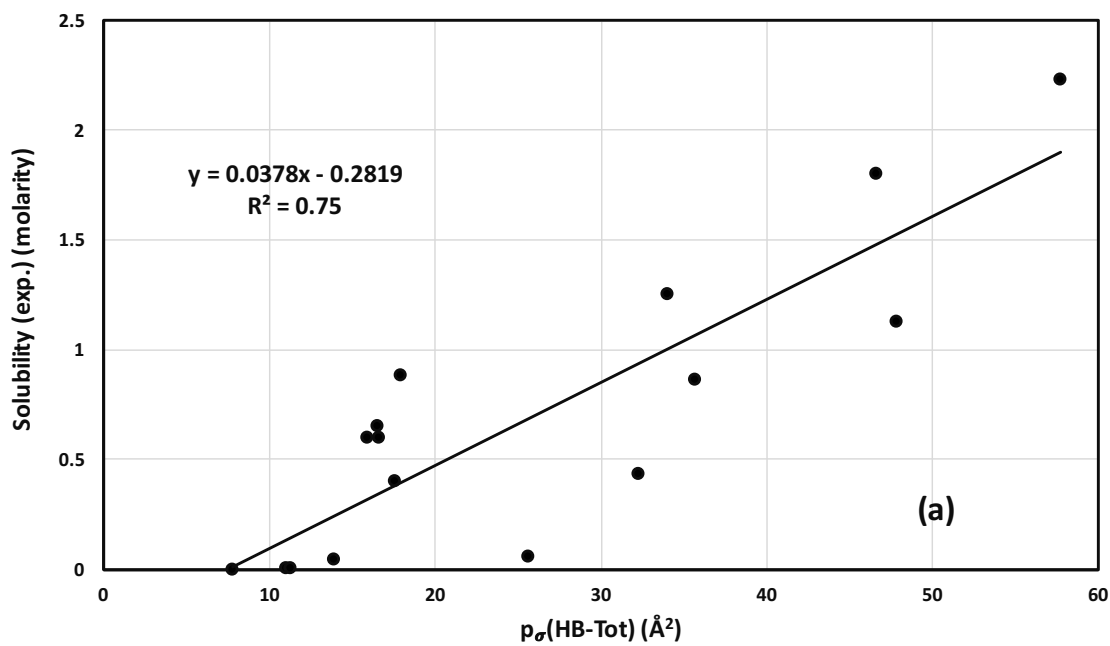


Figure. S 9: The experimental solubility vs $p_{\sigma}(\text{HB-Tot})$ for (a) 16 different metal complexes and for (b) 14 different metal complexes for COSMOSAC-LANL model. The solubility is in molarity.

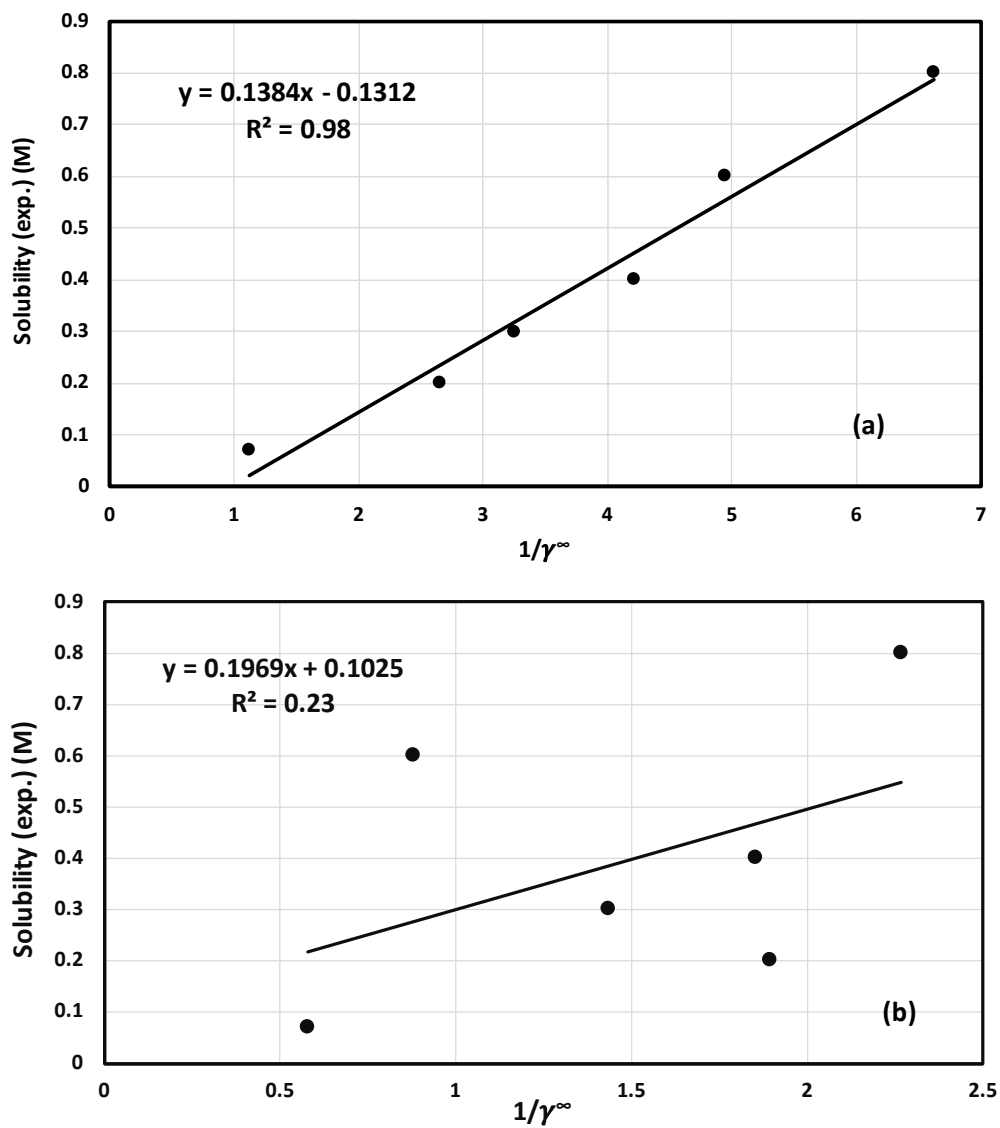


Figure. S 10: In fig. (a) and (b), the experimental solubility has been plotted as a function of $1/\gamma_{i/S}^\infty$ for the COSMOSAC-LANL and COSMOSAC-2013 model, respectively. These results have been shown for a particular metal complex $V(\text{acac})_3$ in 6 different organic solvents. The solubility is in molarity unit.

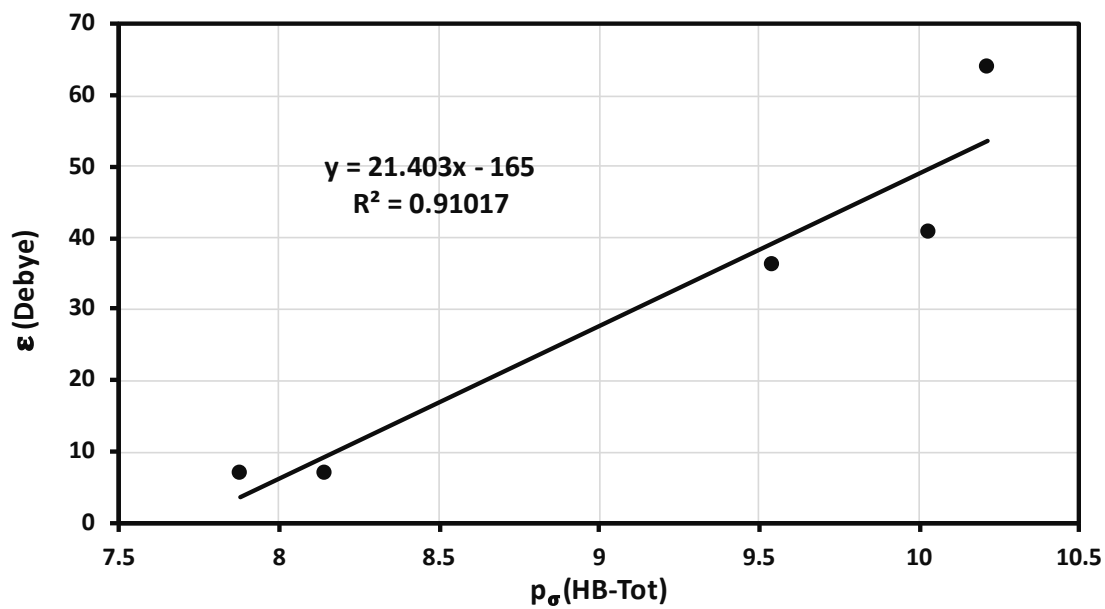


Figure. S 11: ϵ vs $p_{\sigma}(\text{HB-Tot})$ for 1,3do, MA, DMPU, GBL and PC solvents.

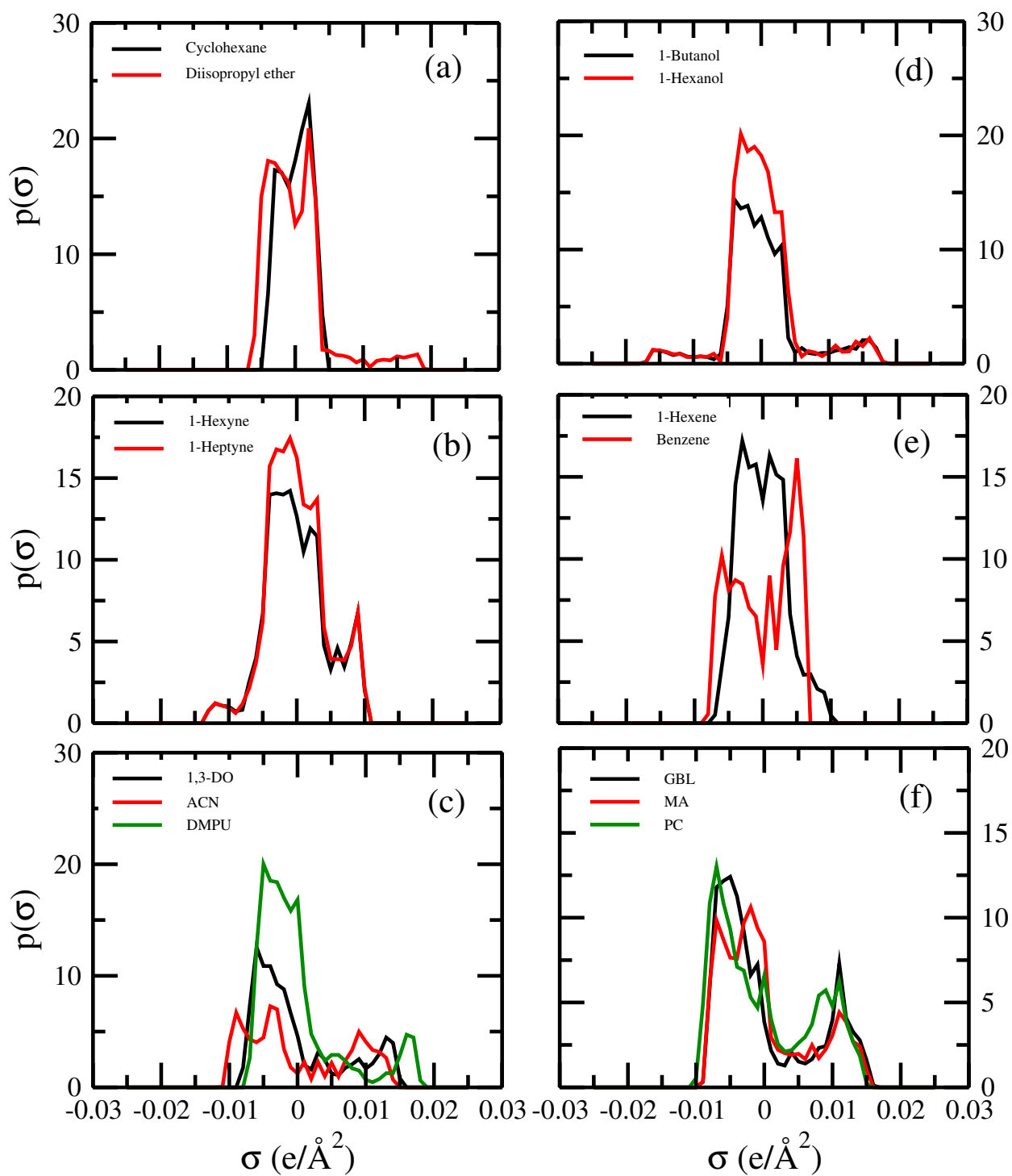


Figure. S 12: Total σ profile of 14 different organic solvents.

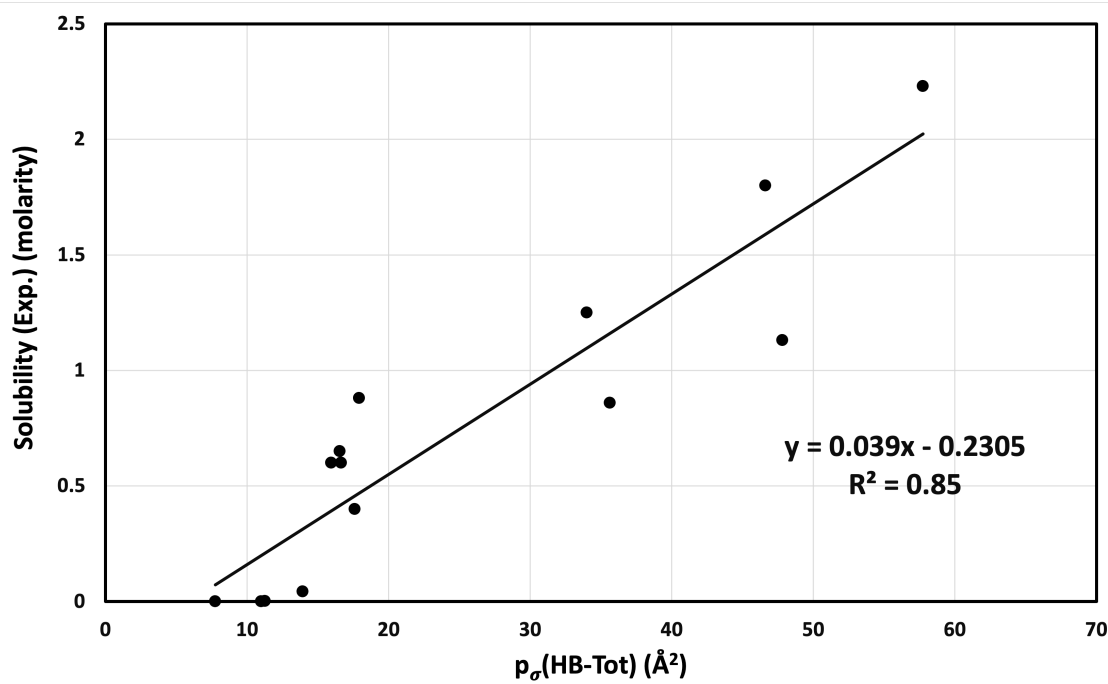
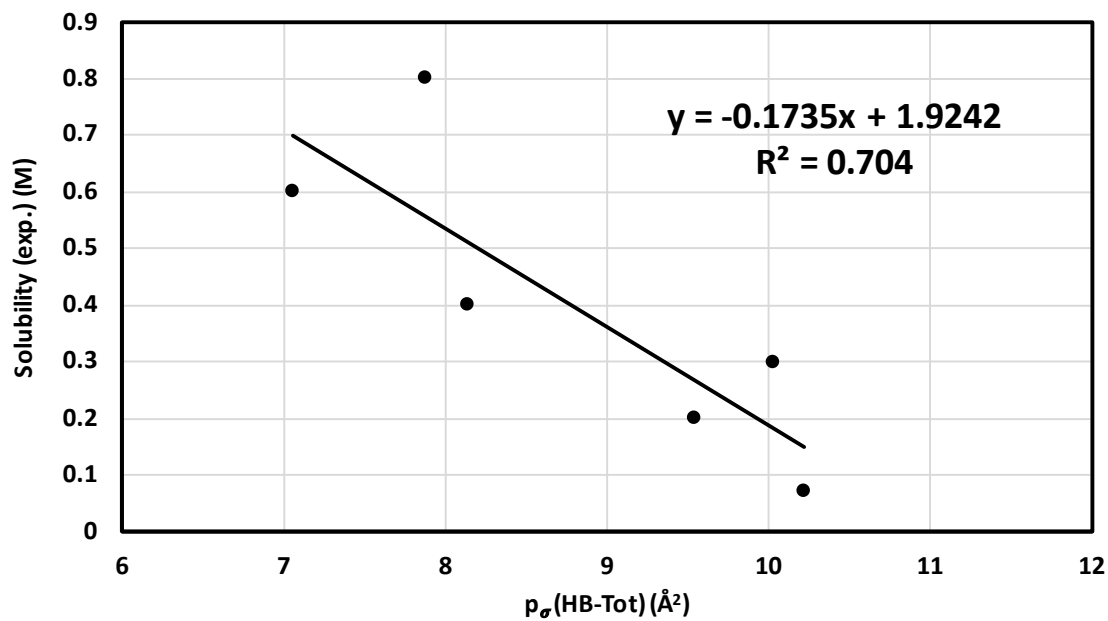


Figure. S 13: The experimental solubility vs $p_{\sigma}(\text{HB})$ for (top) $\text{V}(\text{acac})_3$ in 6 different organic solvents and (bottom) 14 different metal complexes in acetonitrile solvent, respectively. These two plots correspond to the 14×6 (84) screening model.

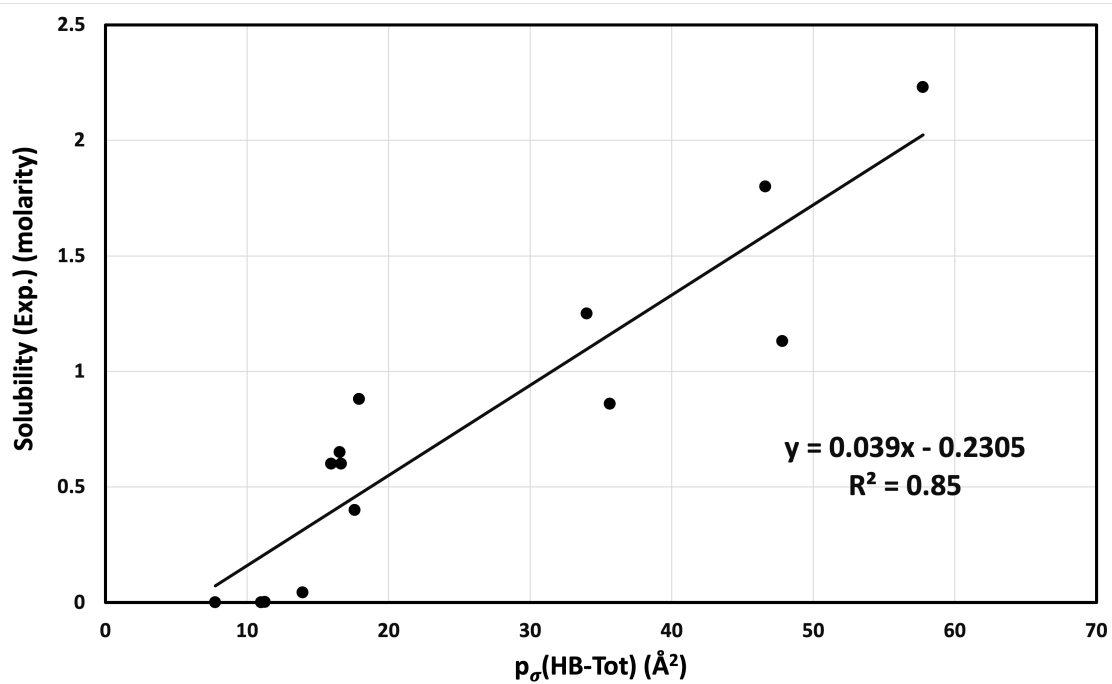
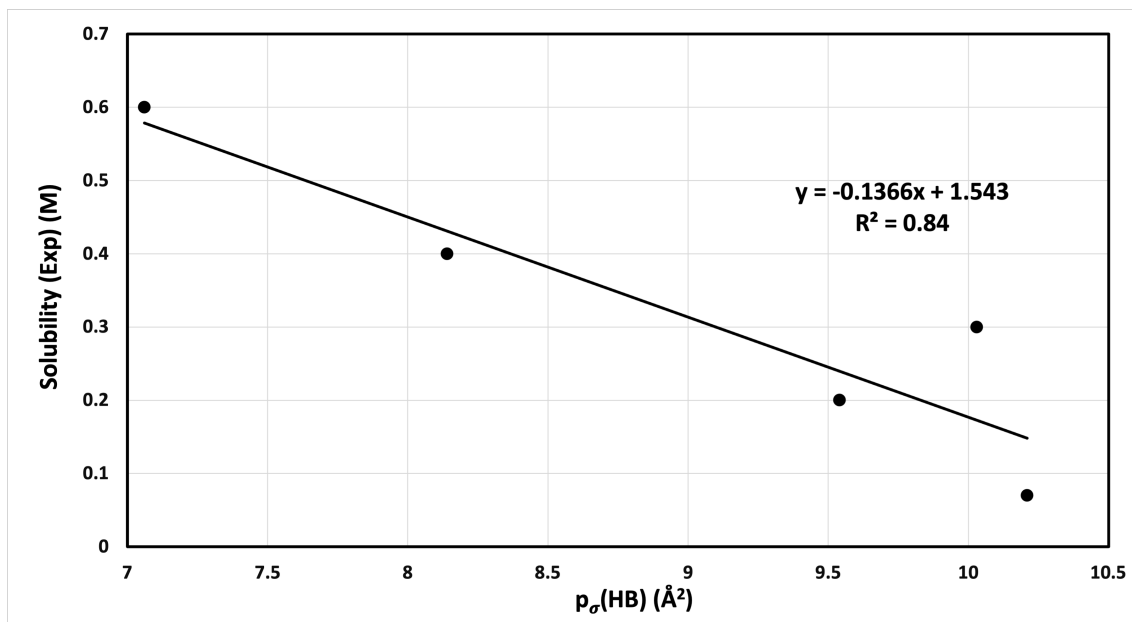


Figure. S 14: The experimental solubility vs $p_{\sigma}(\text{HB})$ for (top) $\text{V}(\text{acac})_3$ in 5 different organic solvents and (bottom) 14 different metal complexes in acetonitrile solvent, respectively. These two plots correspond to the 14×5 (70) screening model.

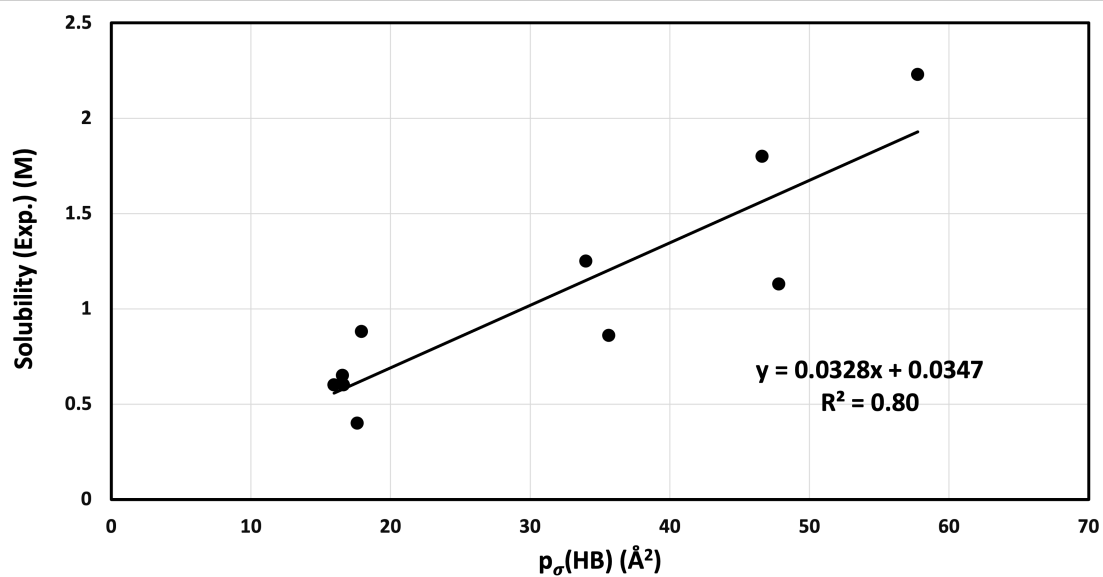
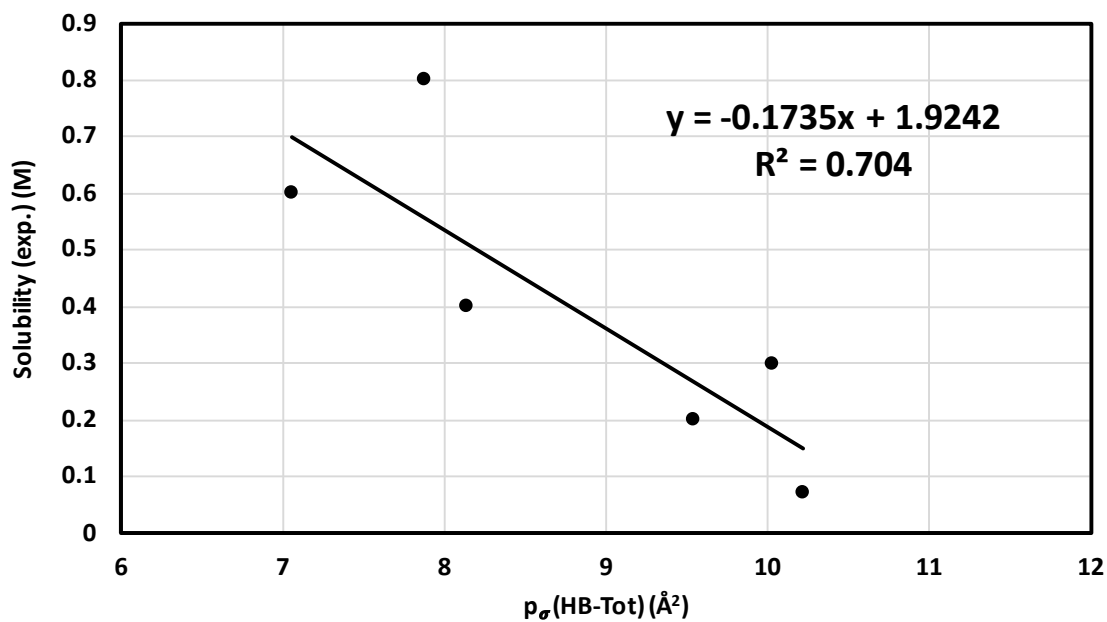


Figure. S 15: The experimental solubility vs $p_{\sigma}(\text{HB})$ for (top) $\text{V}(\text{acac})_3$ in 6 different organic solvents and (bottom) 10 different metal complexes in acetonitrile solvent, respectively. These two plots correspond to the 10×6 (60) screening model.

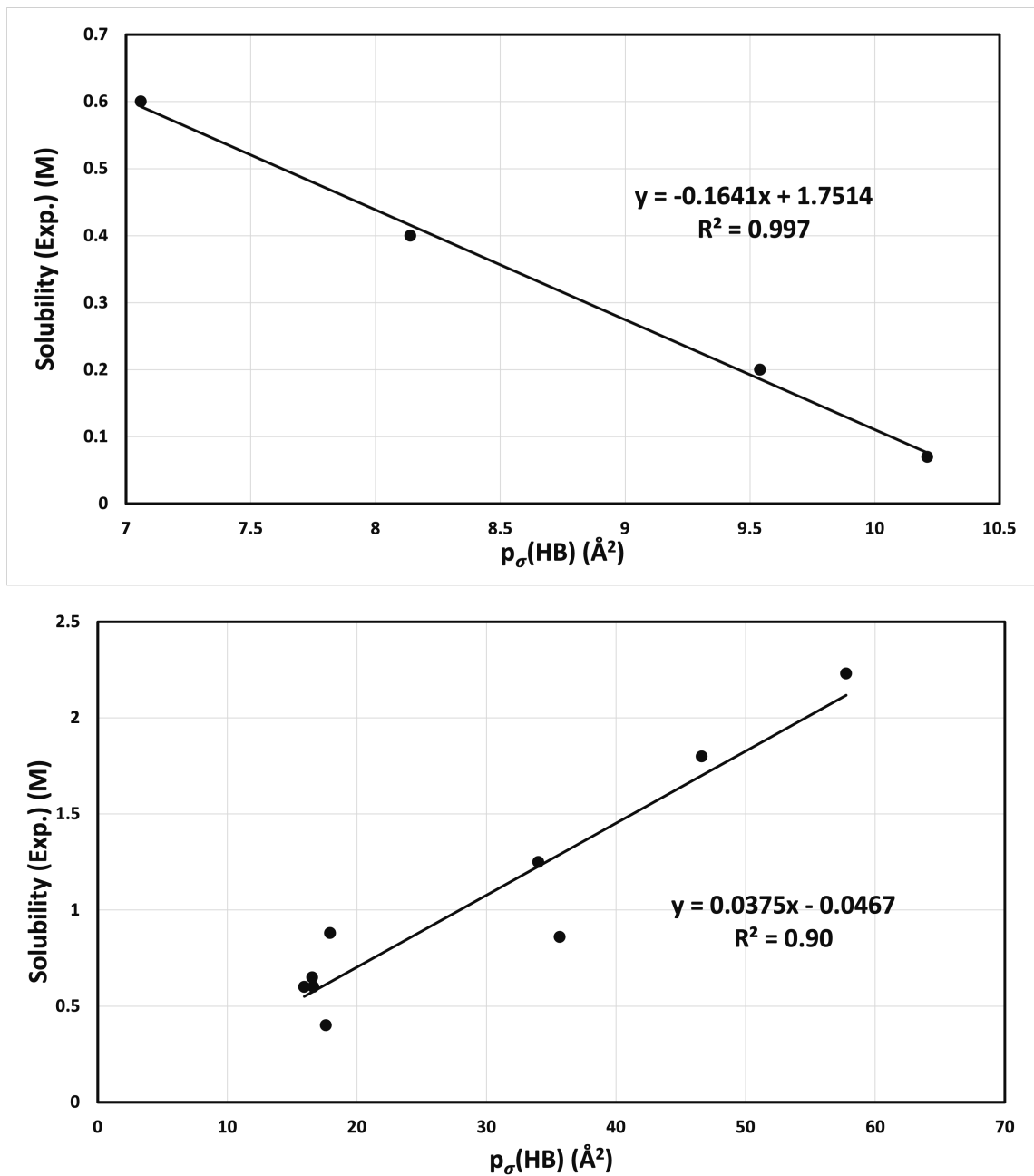


Figure. S 16: The experimental solubility vs $p_{\sigma}(\text{HB})$ for (top) $\text{V}(\text{acac})_3$ in 4 different organic solvents and (bottom) 9 different metal complexes in acetonitrile solvent, respectively. These two plots correspond to the 9×4 (36) screening model.

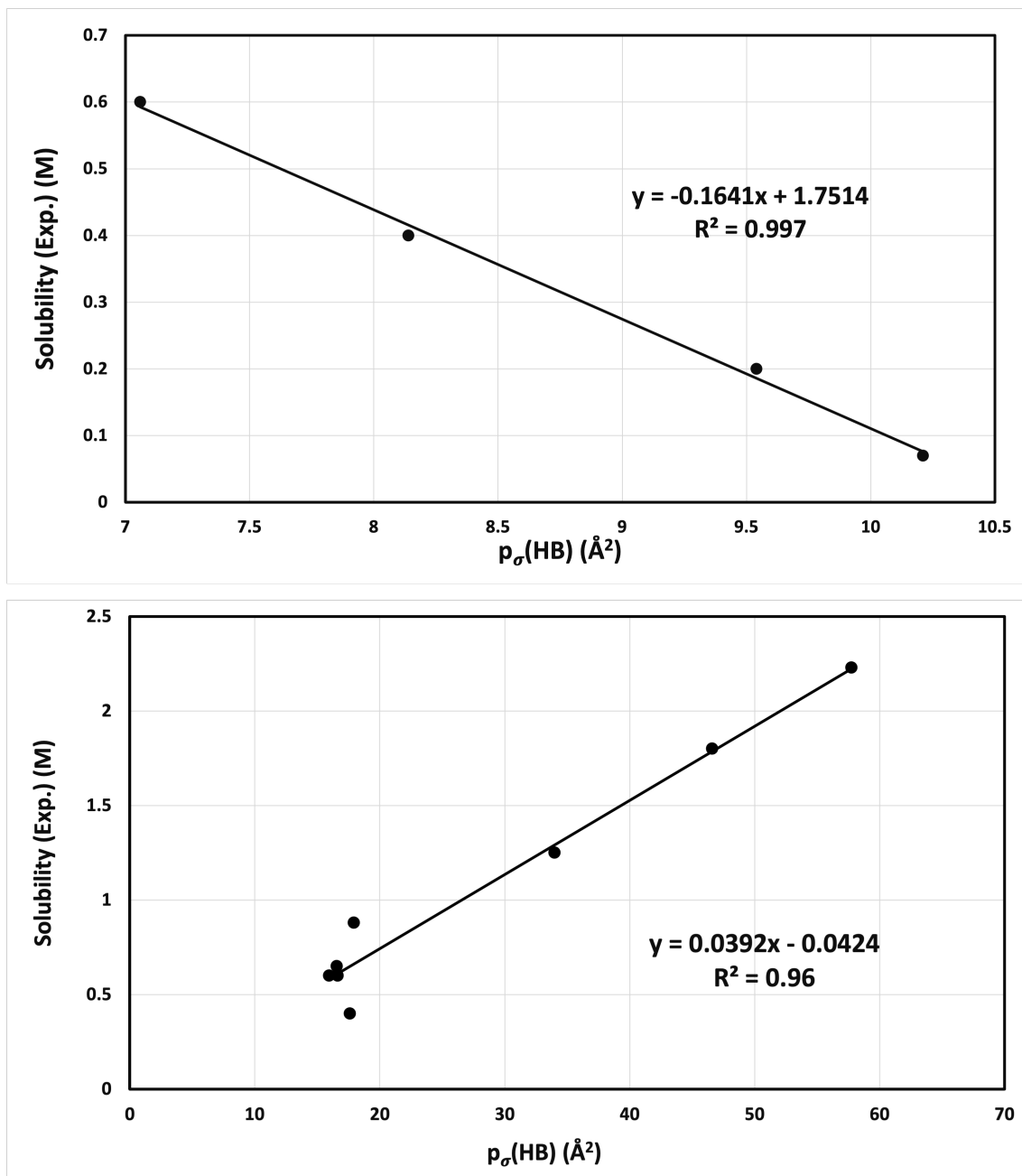


Figure. S 17: The experimental solubility vs $p_{\sigma}(\text{HB})$ for (top) $\text{V}(\text{acac})_3$ in 4 different organic solvents and (bottom) 8 different metal complexes in acetonitrile solvent, respectively. These two plots correspond to the 8×4 (32) screening model.

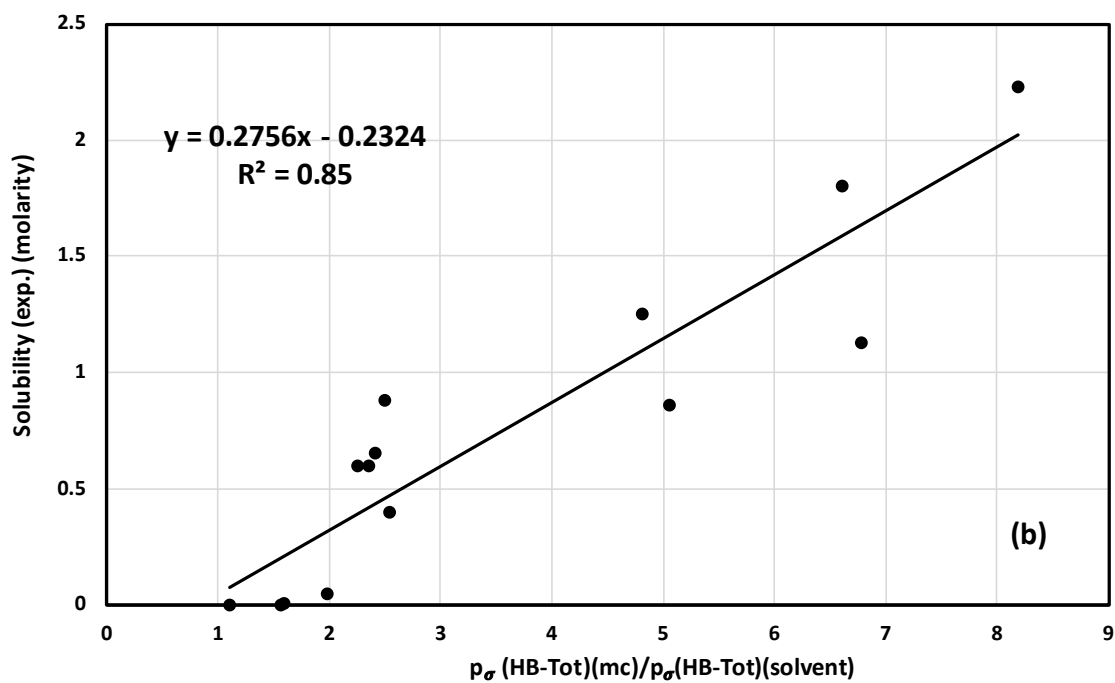
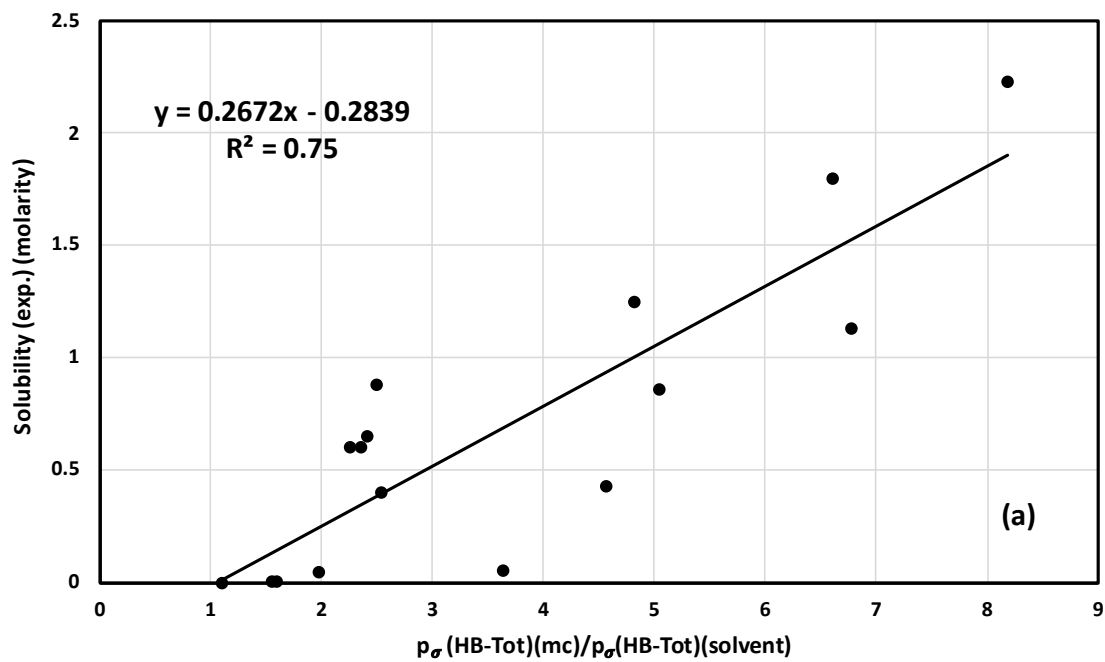


Figure. S 18: The experimental solubility vs χ for (a) 16 different metal complexes and (b) 14 different metal complexes, respectively. The definition of χ has been given in section 6 in the main manuscript.

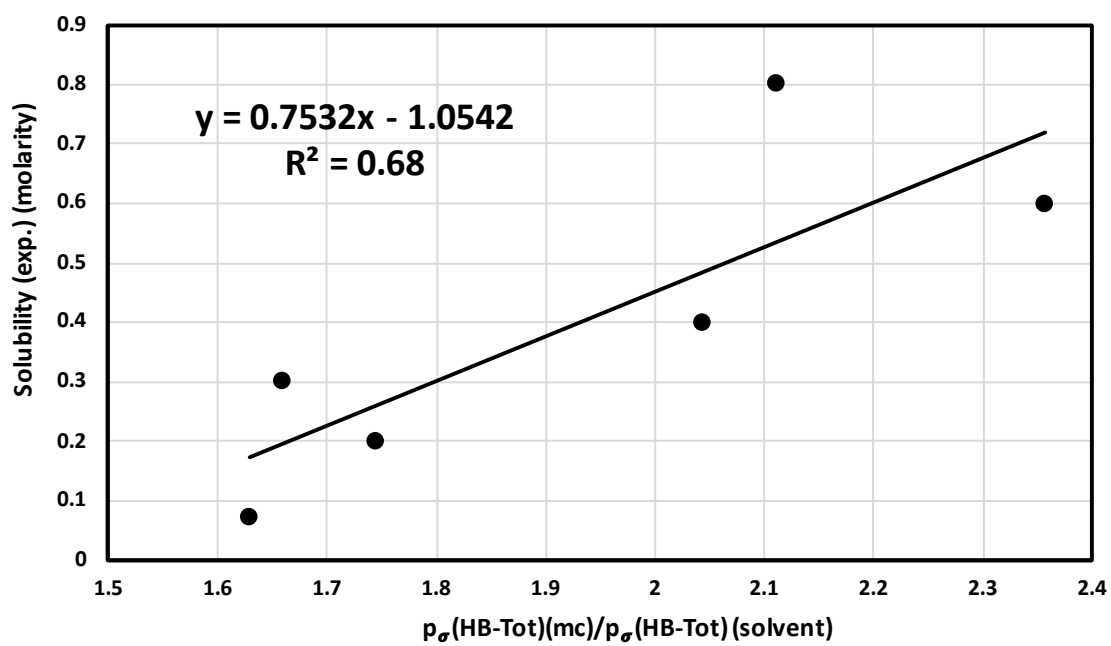


Figure. S 19: The experimental solubility vs χ for $\text{V}(\text{acac})_3$ in 6 different organic solvents. The definition of χ has been given in section 6 in the main manuscript.