

Electronic Supplementary Information for:

Phase Stability of the Tin monochalcogenides SnS and SnSe: a Quasi-Harmonic Lattice-Dynamics Study

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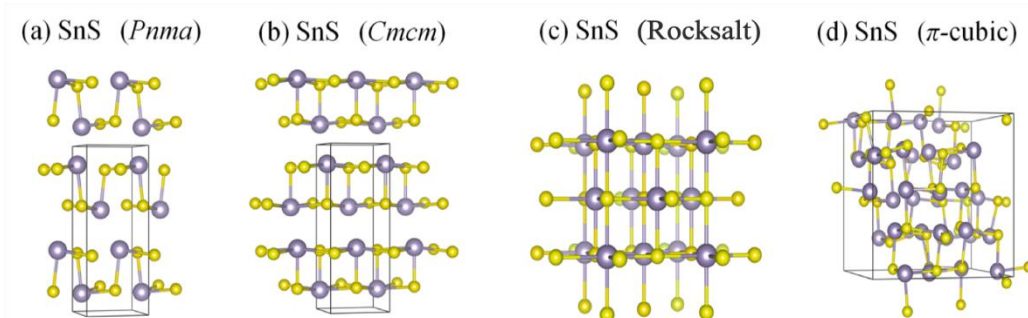


Figure S1. Optimised structures of *Pnma*, *Cmcm*, rocksalt and π -cubic SnS. These images were produced using the VESTA software.¹

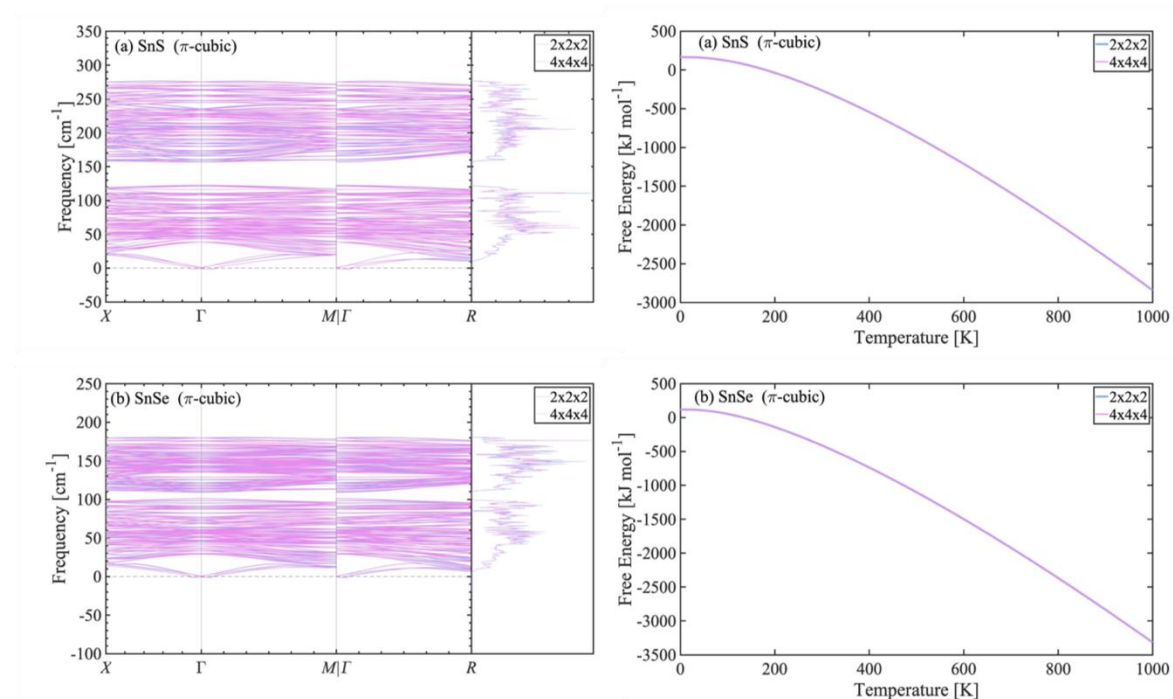


Figure S2. Phonon dispersion and density of states curves and vibrational Helmholtz free energy of the π -cubic phases of SnS (a) and SnSe (b) computed using two k -point meshes with $2 \times 2 \times 2$ and $4 \times 4 \times 4$ subdivisions. Both calculations were performed on the equilibrium structure using the 64-atom unit cell, so the equivalent k -point meshes for the $2 \times 2 \times 2$ supercell used in the production calculations would be meshes with $1 \times 1 \times 1$ (i.e. the Γ point) and $2 \times 2 \times 2$ subdivisions.

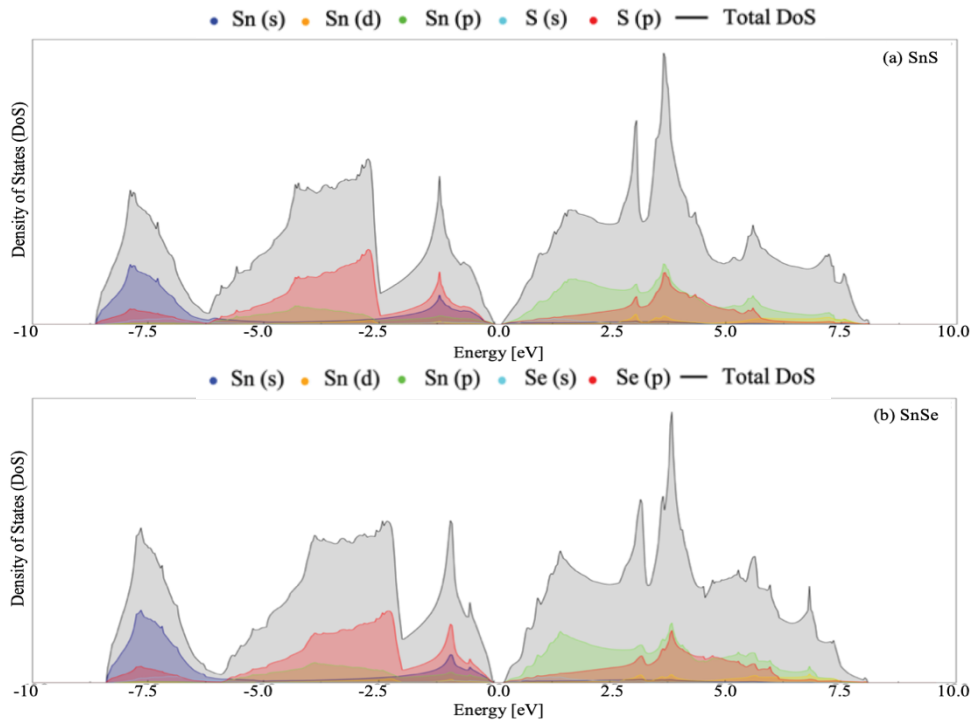


Figure S3. Calculated electronic atom- and orbital-projected density of states (DoS) curves for the rocksalt phases of (a) SnS and (b) SnSe. The states are colored as follows: Sn(s) - blue, Sn(d) - yellow, Sn(p) - green, S/Se(s) - cyan, S/Se(p) - red and total DoS - black.

Table S1. Calculated electronic bandgaps of the four phases of SnS (top) and SnSe (bottom) obtained using the PBEsol + D3 functional, with experimental and theoretical data for comparison where available.

Bandgaps: SnS [eV]			
Phase	PBEsol + D3 (this work)	Experiments	Other DFT studies
Rocksalt	0.15	-	0.52 ²
<i>Pnma</i>	0.579	1.33-1.6 ³	1.352 ⁴ , 1.8 ⁵
<i>Cmcm</i>	0.549	-	1.4 ⁵
π -cubic	1.13 (indirect)	1.53 ⁶	1.74 ⁷
Bandgaps: SnSe [eV]			
Phase	PBEsol + D3 (this work)	Experiments	Other DFT studies
Rocksalt	0.253	-	0.58 ²
<i>Pnma</i>	0.423	0.89 ⁸ , 1.0-1.2 ⁹	0.79 ¹⁰ , 1.18, ⁴ 0.4 ¹¹
<i>Cmcm</i>	0.234	0.39 ⁸	0.05 ¹¹
π -cubic	0.856 (indirect)	1.28 ¹²	0.799/1.011 (LDA/GGA) ¹³

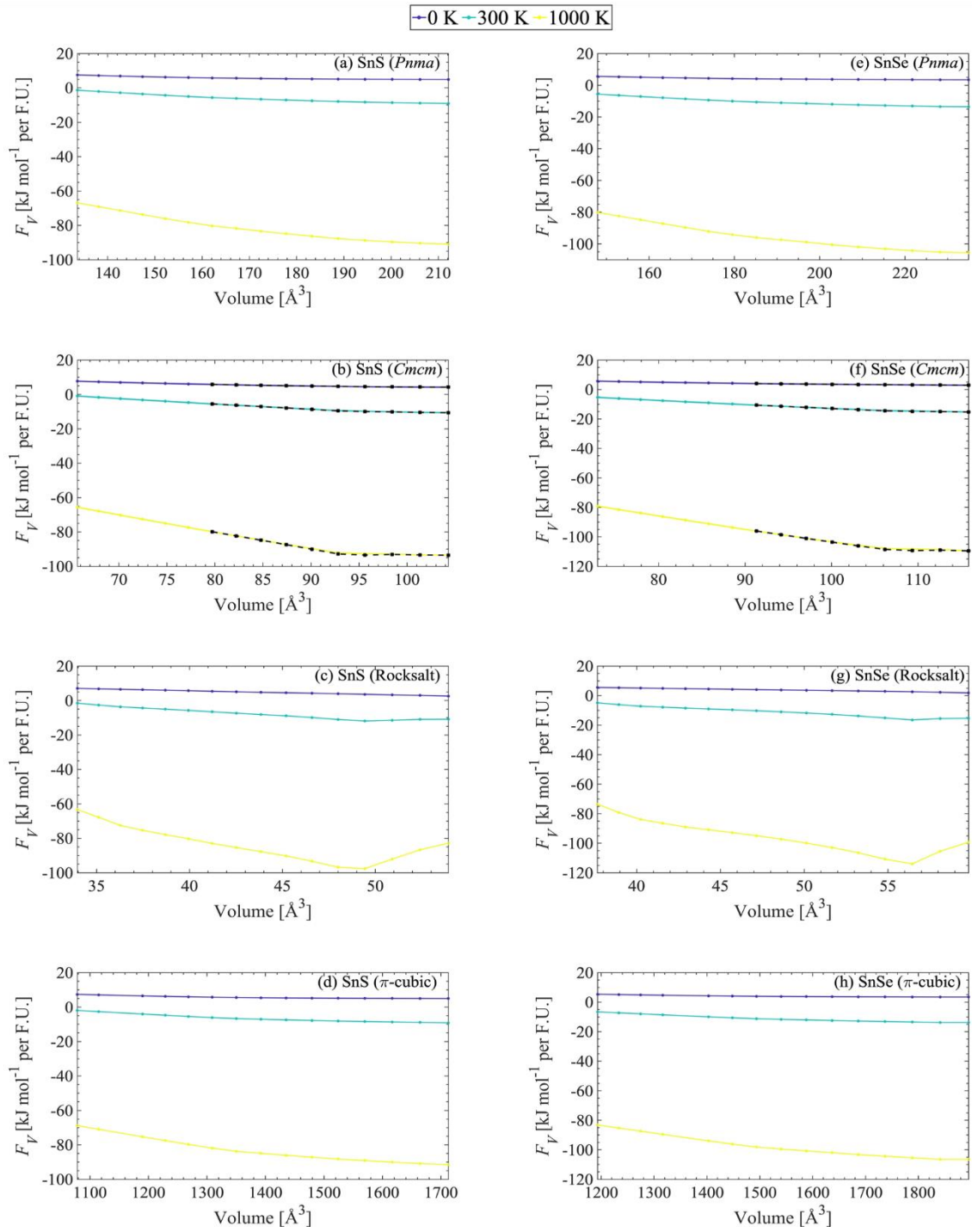


Figure S4 Phonon free energy F_V as a function of volume for the eight tin monochalcogenide phases examined in this work at $T = 0, 300$ and 1000 K. For the $Cmcm$ phases in (b) and (f), the data overlaid in black shows the F_V obtained after renormalisation of the principal imaginary modes at the Γ and Y wavevectors.

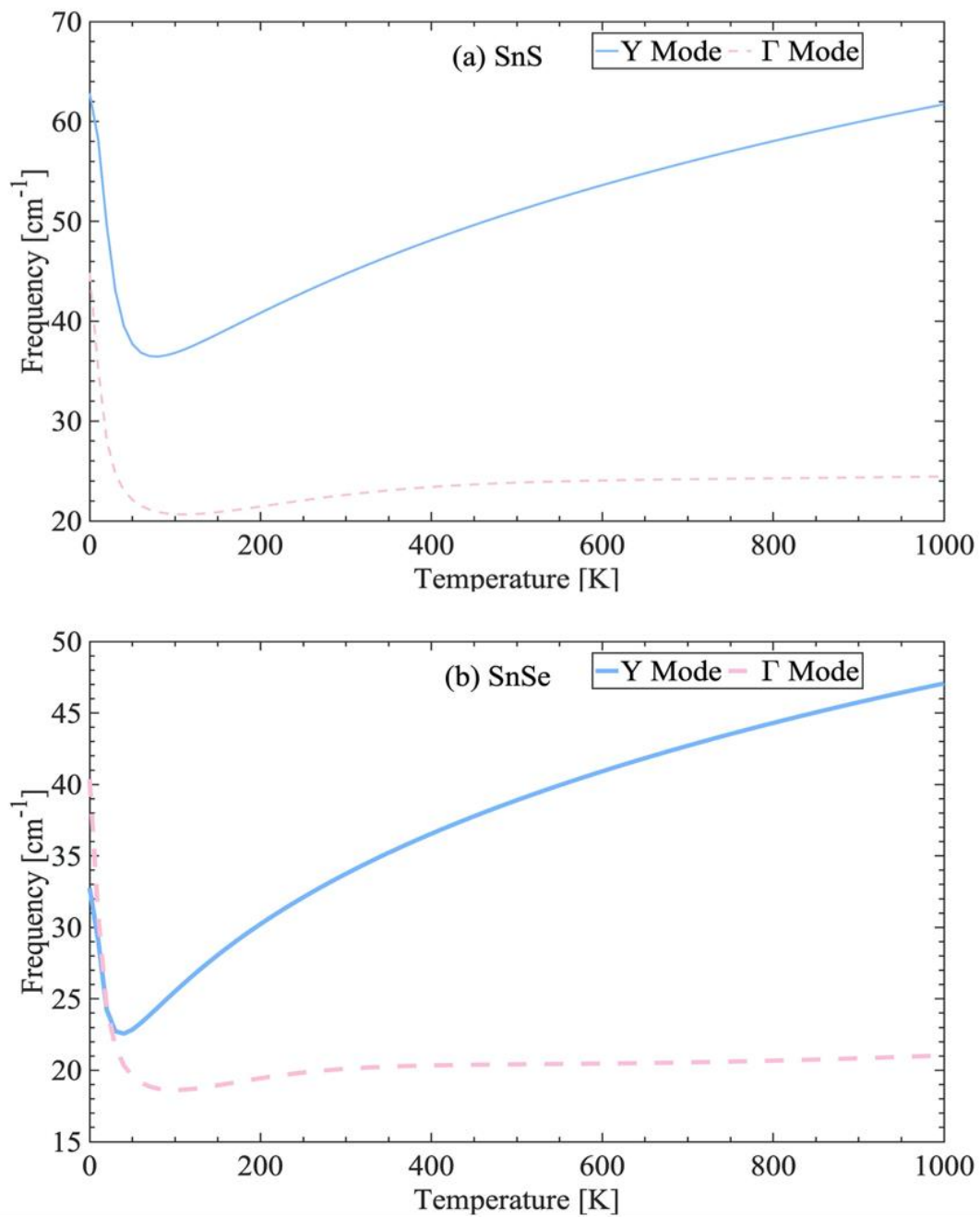


Figure S5. Effective renormalised frequencies of the two imaginary modes of *Cmcm* SnS (a) and SnSe (b) at the equilibrium volume, as a function of temperature, obtained using the method in Ref. 14.

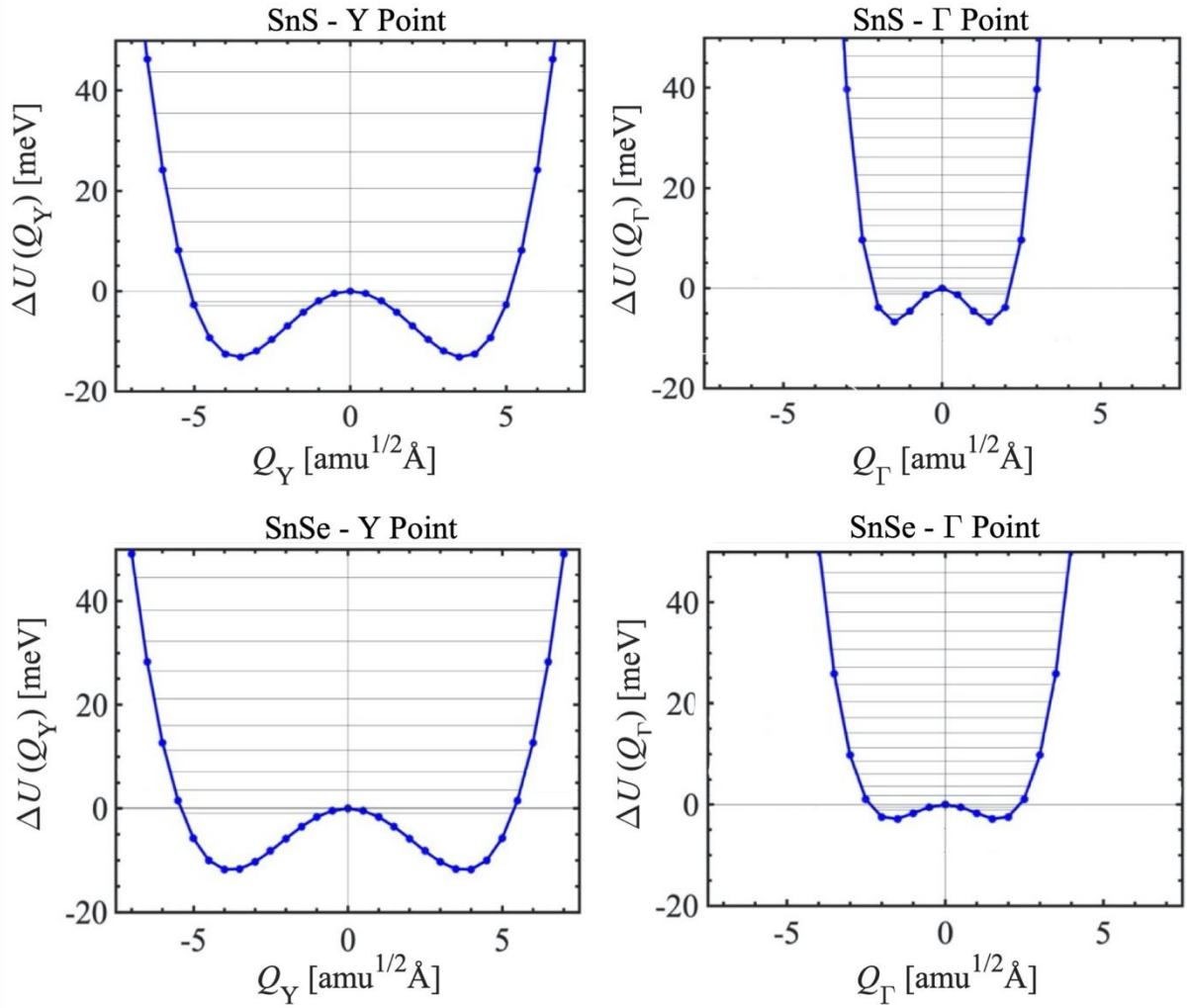


Figure S6. Anharmonic double-well potentials along the two principal imaginary modes at the Y and Γ wavevectors of *Cmcm* SnS (top) and SnSe (bottom) at the equilibrium volume. The black lines inside the potentials show the eigenvalues obtained by solving a 1D Schrödinger equation for the potential.

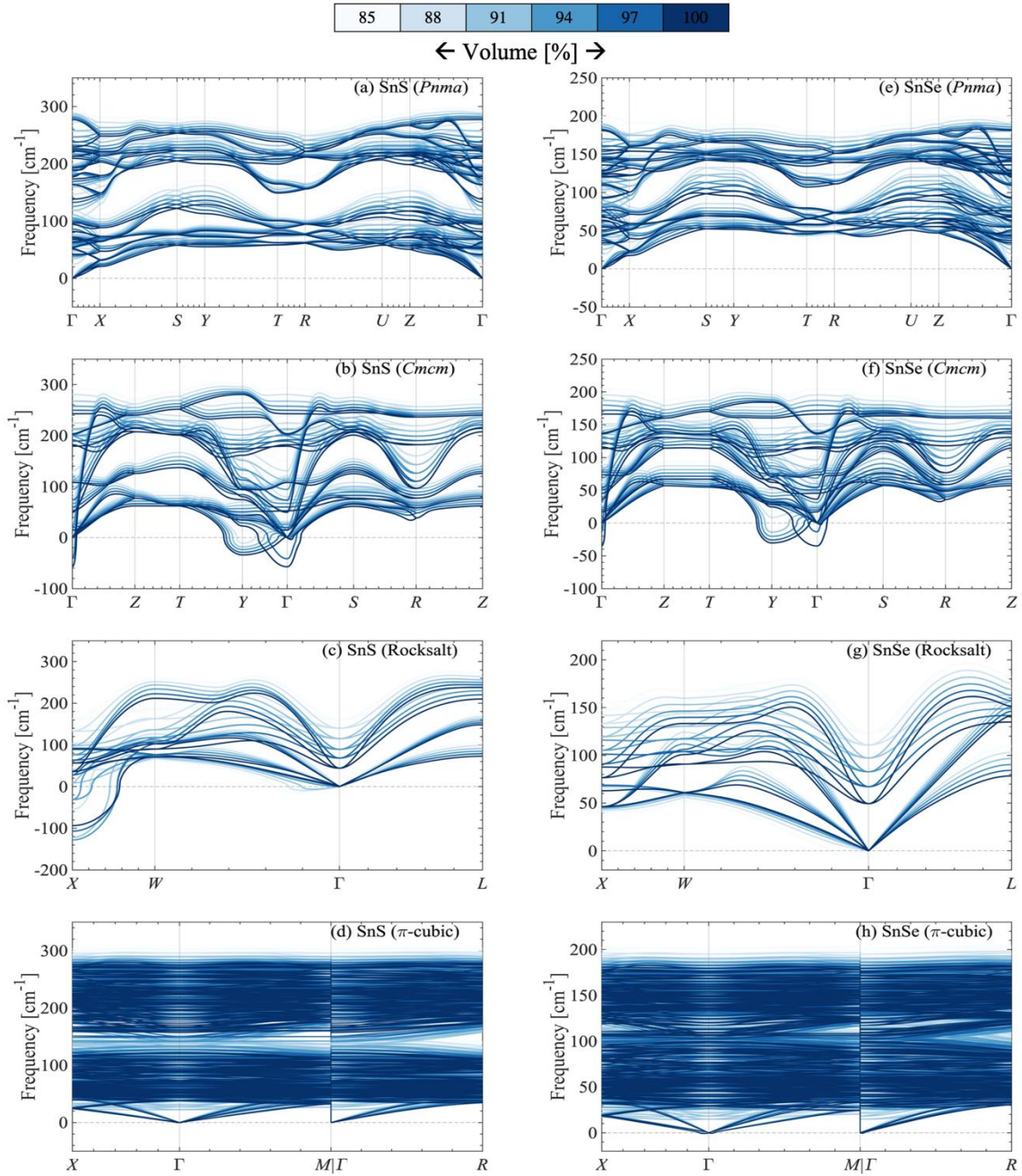


Figure S7. Phonon dispersion and density of states curves for SnS ((a)-(d), left) and SnSe ((e)-(h), right) under up to 15 % volume compression: (a)/(e) *Pnma*, (b)/(f) *Cmcm*, (c)/(g) rocksalt and (d)/(h) π -cubic.

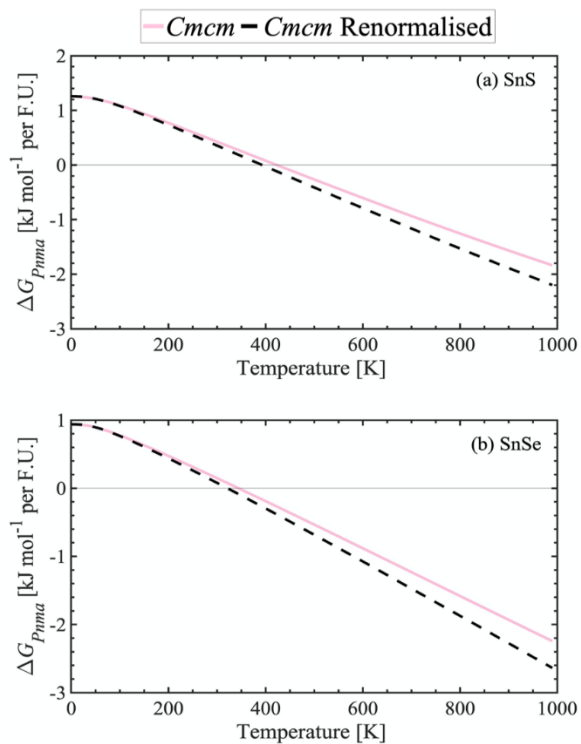


Figure S8. Gibbs energy differences ΔG_{Pnma} between the *Pnma* and *Cmc* phases of (a) SnS and (b) SnSe before (pink) and after renormalization of the imaginary harmonic modes (black).

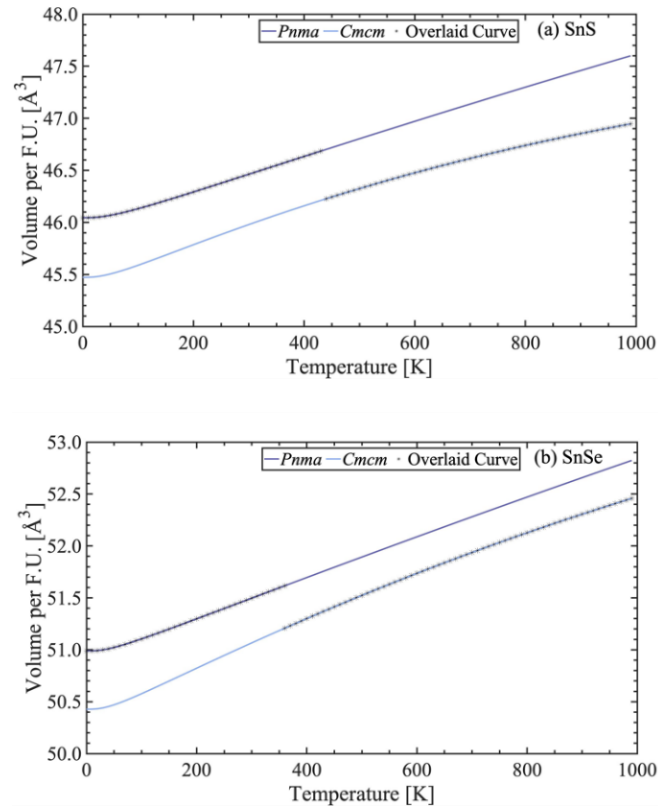


Figure S9. Calculated volume per formula unit as a function of temperature for the *Pnma* (purple) and *CmcM* (light blue) phases of (a) SnS and (b) SnSe. The black stars track the volumes of the phases with the lowest-energy Gibbs free energy to highlight expected discontinuities in the volume at the phase transition.

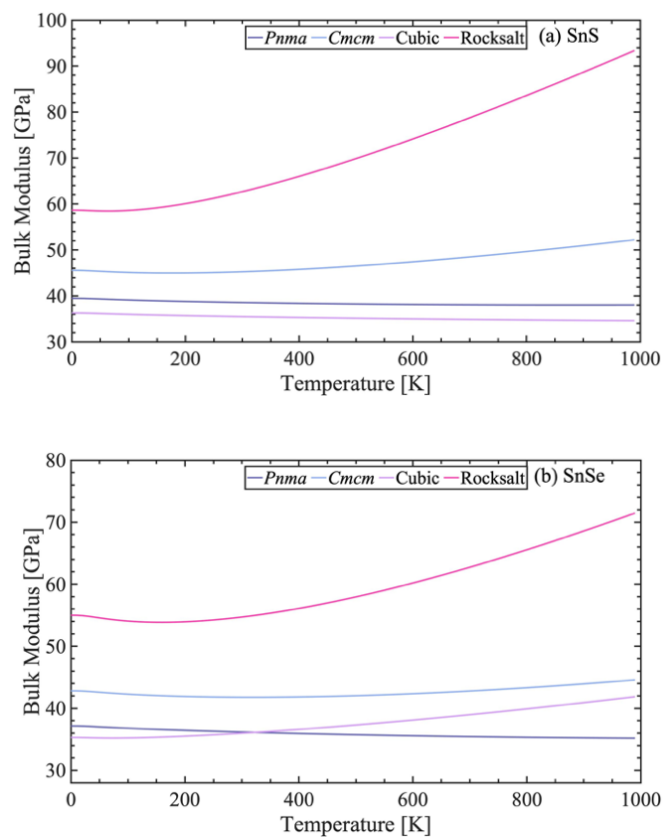


Figure S10. Calculated bulk modulus as a function of temperature for the *Pnma* (purple), *Cmc21* (light blue), π -cubic (purple) and rocksalt (pink) phases (a) SnS and (b) SnSe.

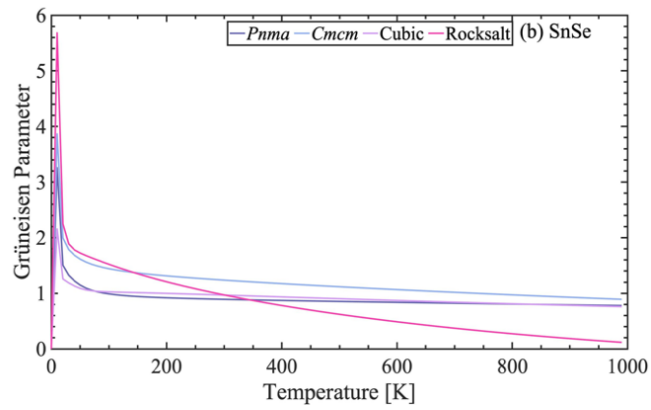
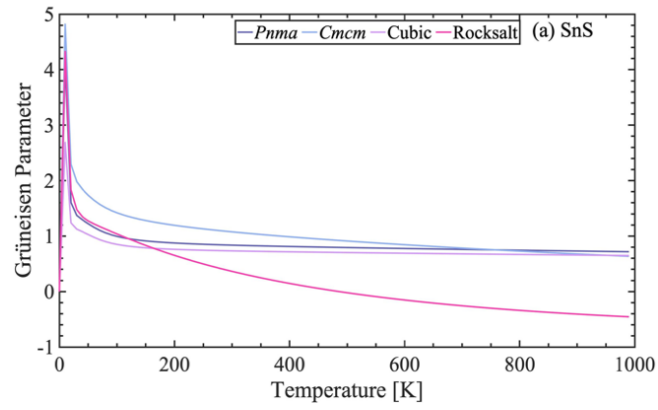


Figure S11. Calculated Grüneisen parameter as a function of temperature for the *Pnma* (purple), *Cmc* (light blue), π -cubic (dark blue) and rocksalt (pink) phases (a) SnS and (b) SnSe.

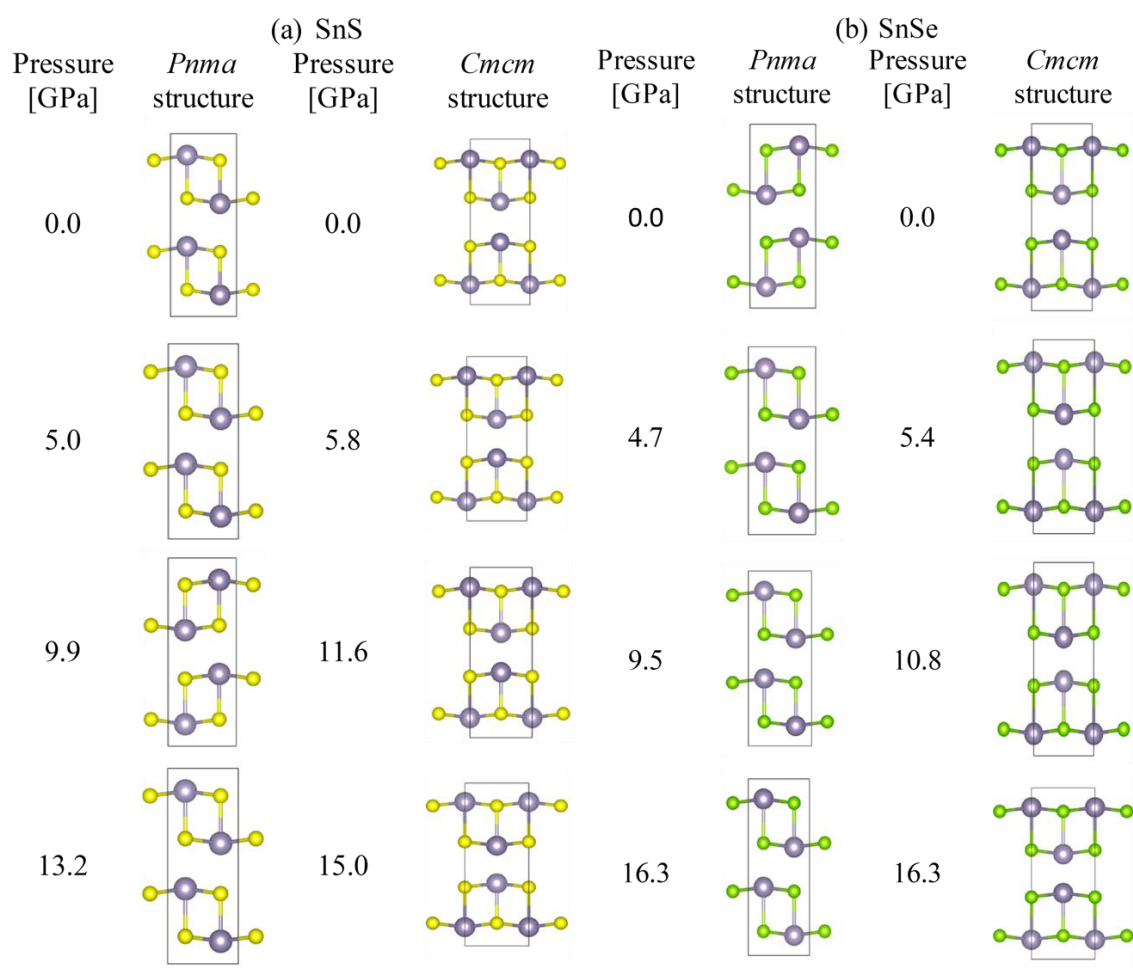


Figure S12. Optimized structures of *Pnma* and *Cmcm* SnS (a) and SnSe (b) at a range of applied pressures. The images were produced using the VESTA software.¹

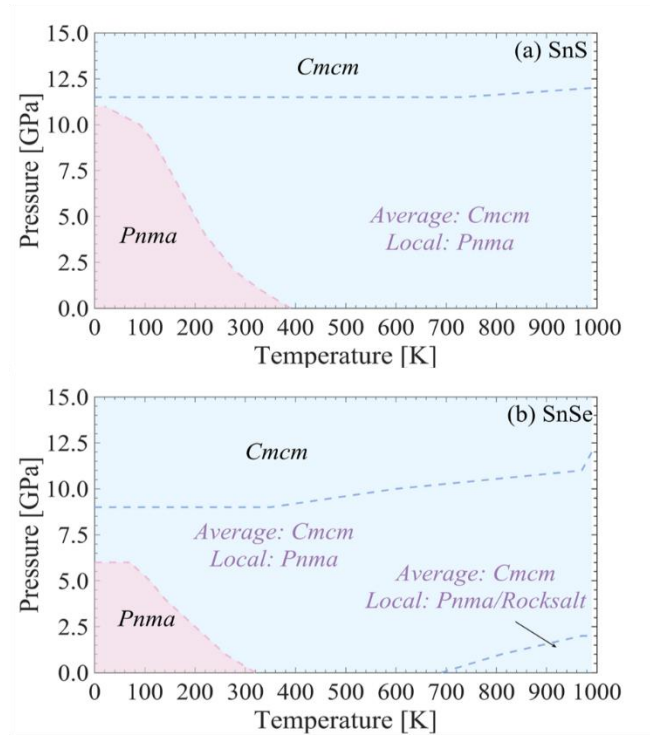


Figure S13 Calculated temperature-pressure phase diagrams of (a) SnS and (b) SnSe, obtained based on the Gibbs energies calculated within the quasi-harmonic after renormalization of the imaginary harmonic modes in the *Cmc* phases. This may be compared with Fig. 9 in the text.

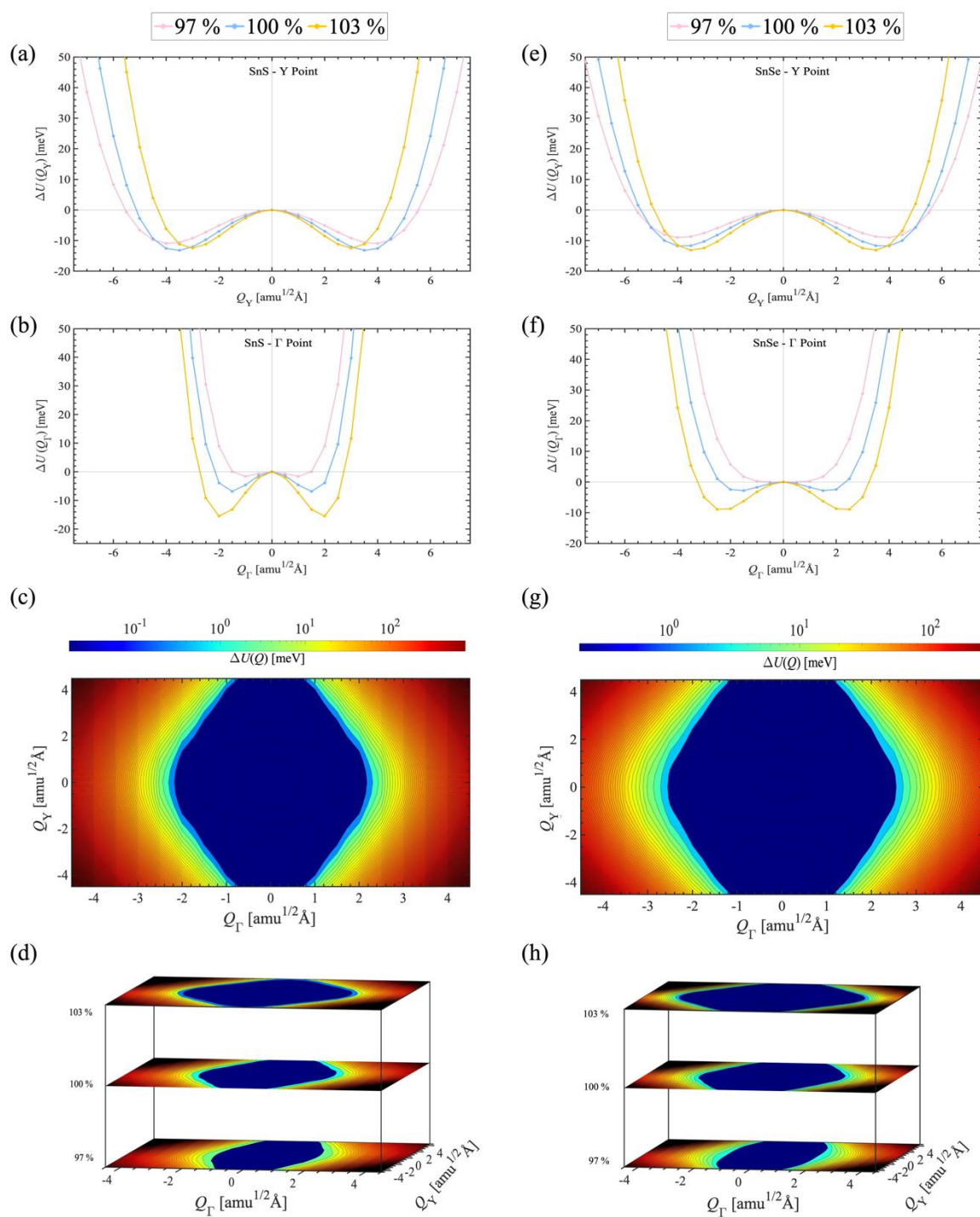


Figure S14. Potential-energy surface (PES) along the two principal imaginary modes at the Y- and Γ wavevectors in *Cmcm* SnS (a)/(b) and SnSe (e)/(f), evaluated at the equilibrium volume and 3 % expansions and compressions. (c)/(g) Two-dimensional PES spanned by both imaginary modes at the equilibrium volumes for (c) SnS and (g) SnSe. (d)/(h) Comparison of the 2D PES for the three volumes shown in (a)/(b) and (e)/(f).

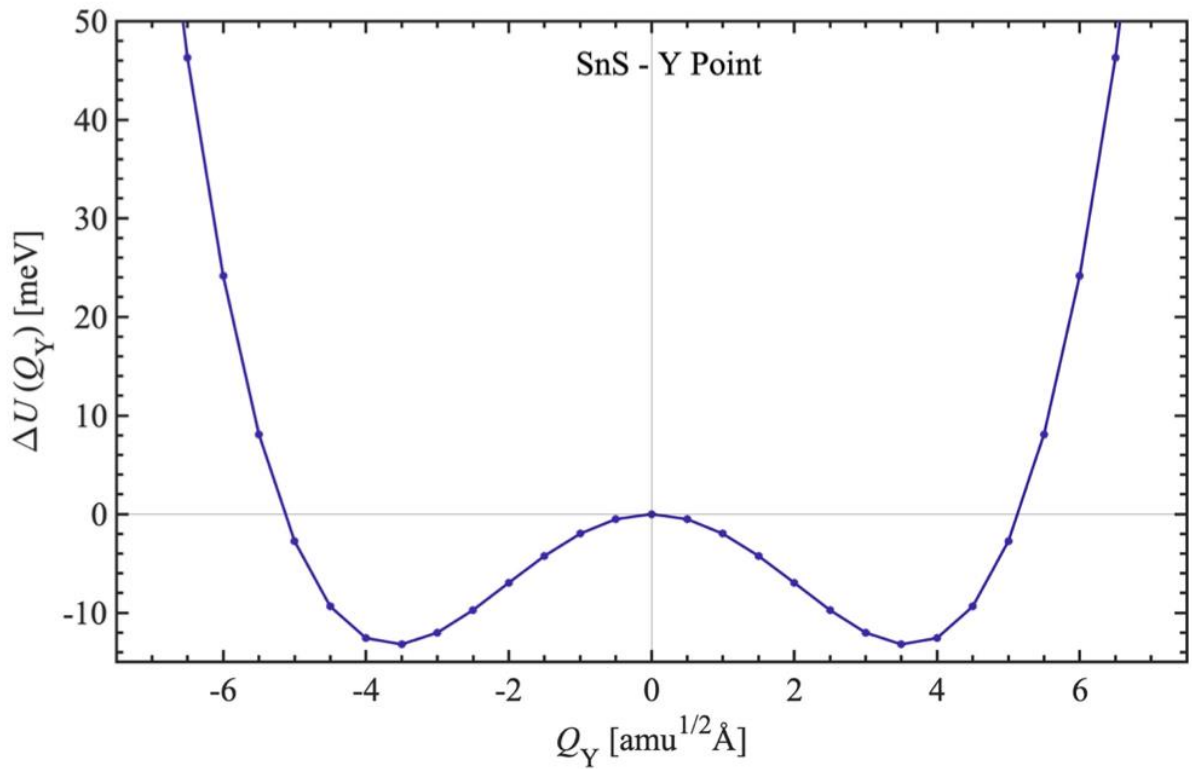
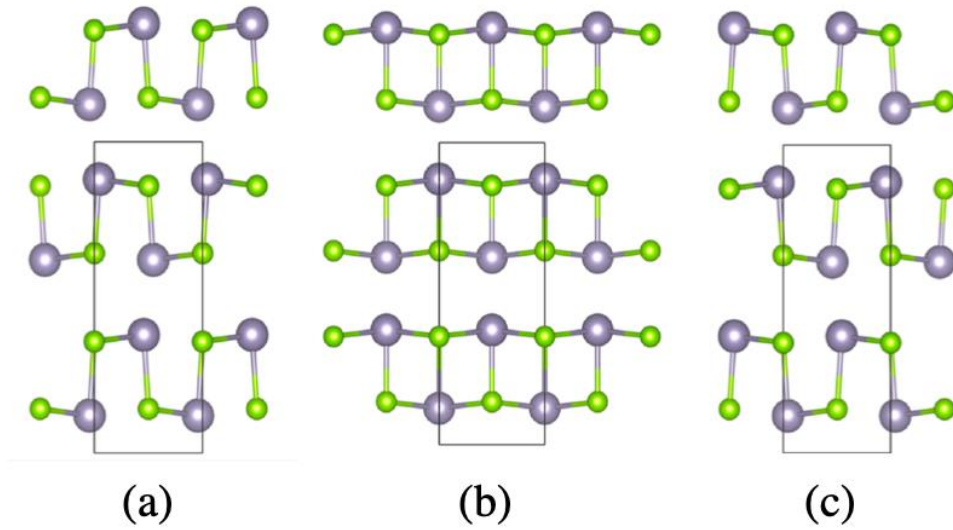


Figure S15. Structures of SnS associated with the minima in the 1D potential-energy surface (PES) obtained by mapping the Y-point imaginary mode in the equilibrium structure. (a) Minimum at $Q = -3.5 \text{ amu}^{1/2} \text{ \AA}$. (b) Maximum at $Q = 0$. (c) Minimum at $Q = +3.5 \text{ amu}^{1/2} \text{ \AA}$. (a) and (c) correspond to the distorted $Pnma$ phase, while (b) corresponds to the $Cmcm$ average structure.

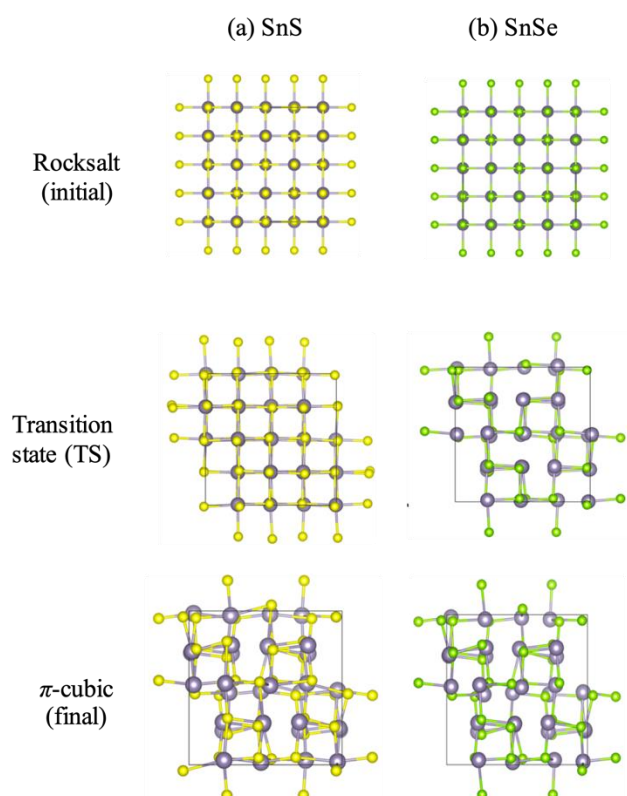


Figure S16. Structures of the initial (rocksalt), transition state (TS), and final (π -cubic) structures of SnS (a) and SnSe (b) obtained from the climbing image nudged elastic band (CI-NEB) calculations. These images were produced by the VESTA software.¹

References

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