

Supplementary Information for

Conservation of the Stokes-Einstein Relation in Supercooled Water

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1. Simulation details for the Jagla model

The initial configuration for the Jagla fluid model¹⁻³ consists of 1728 molecules with a constant box size determined under a constant pressure $P = 153.33$ bar at each temperature. Although the reduced unit is usually adopted when using the Jagla fluid model, we use the SI unit instead by assigning the unit of hardcore diameter $d = 0.3$ nm, that of potential $U_0 = 100k_B$, and that of pressure $P_0 = U_0 / d^3$. All our molecular dynamics (MD) simulations were performed with the GROMACS MD simulation package^{4, 5} and the periodic boundary conditions were applied in all three directions of the Cartesian space. The van der Waals interactions were calculated directly with a truncated spherical cutoff of 1.0 nm. Twenty-four temperatures simulated with the Jagla model are in the range of 30–140 K. The system temperature was kept a constant by the Nosé-Hoover thermostat^{6, 7} and the pressure was controlled by the Parrinello-Rahman barostat.^{8, 9} The simulation time step is 1 fs and the total simulated time for each case ranges from 0.1 to 10 ns depending on the temperature. The k values within 2.5–14.5 nm⁻¹ with an interval of 1 nm⁻¹ for the Jagla fluid model are adopted to investigate the k dependences of $D : \tau^{-1}$ and $D : T/k$. The viscosity $\eta = \Delta p / Vq^2$ of Jagla is evaluated by A/Vl because the box size l is different at different temperatures.

2. Supplementary Figures

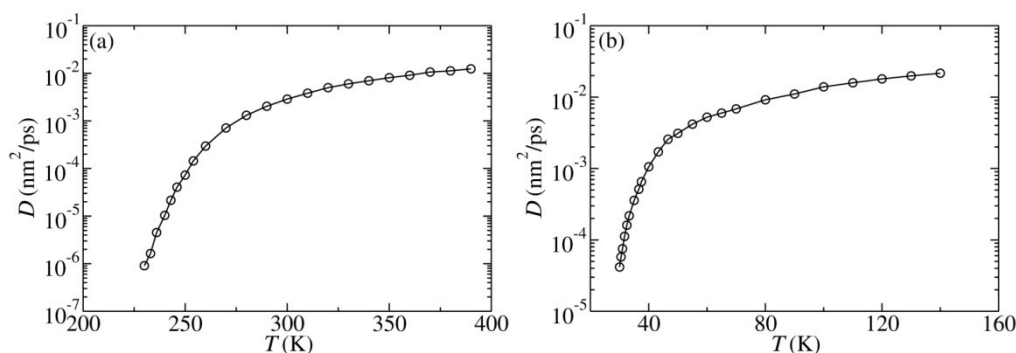


Fig. S1 The diffusion constant D as a function of temperature T within 240–390 K for TIP5P (a) and within 30–140 K for Jagla (b).

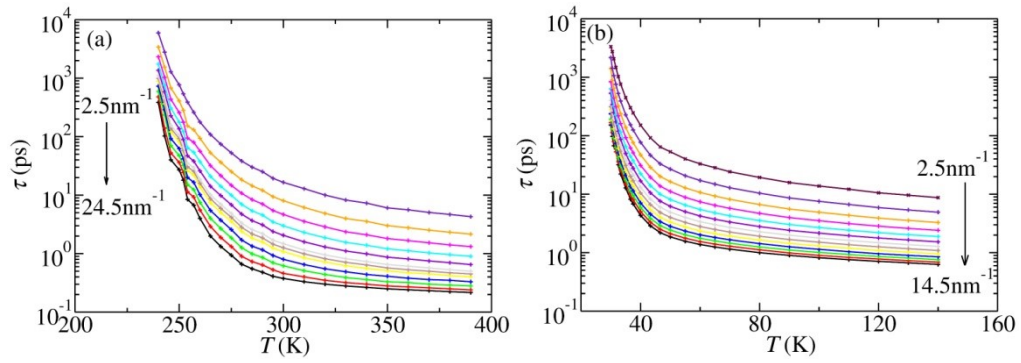


Fig. S2 The structural relaxation time τ for various k values as a function of temperature T for TIP5P (a) and for Jagla (b). The interval between two adjacent k values is 2 nm^{-1} for TIP5P and 1 nm^{-1} for Jagla.

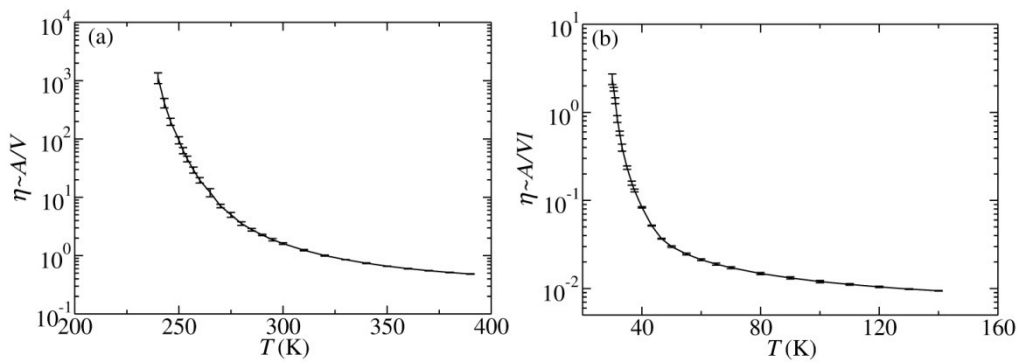


Fig. S3 The viscosity η as a function of temperature T for TIP5P (a) and Jagla (b).

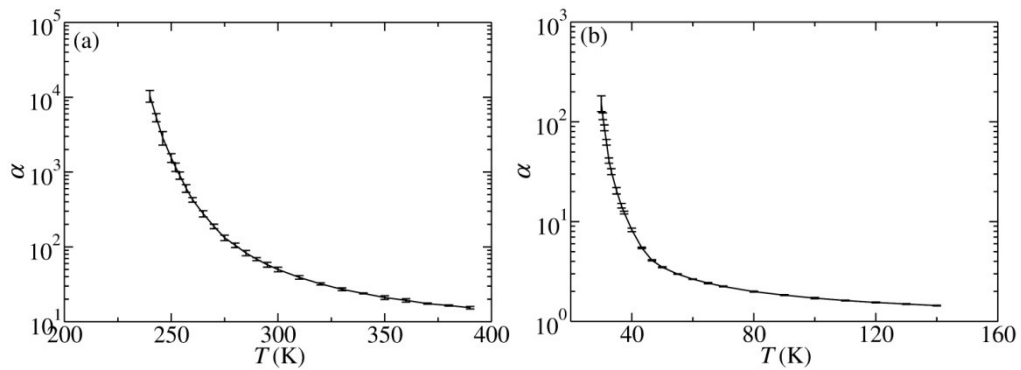


Fig. S4 The frictional coefficient α as a function of temperature T for TIP5P (a) and Jagla (b).

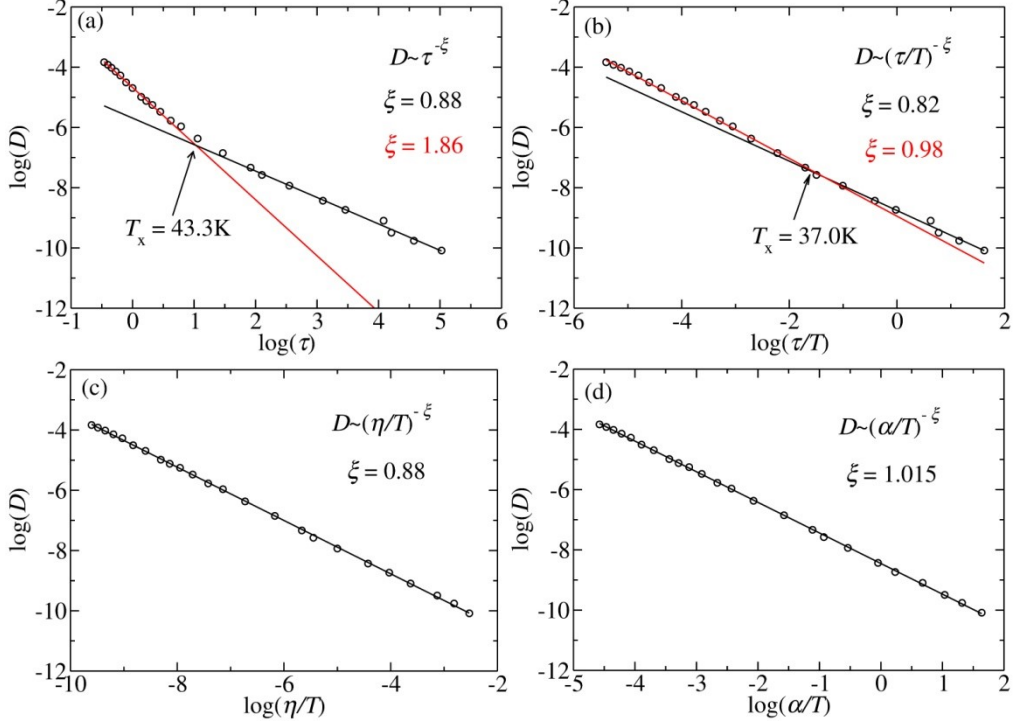


Fig. S5 Verification of the validities of the original SE relation $D : \tau^{-1}$ (a) and its three variants $D : T/\tau$ (b), $D : T/\eta$ (c), and $D : T/\alpha$ (d) for the Jagla fluid model. τ is calculated with the first maximum of static structure factor $k = 12.5 \text{ nm}^{-1}$. The calculated data are represented by circles and fitted by $D : \tau^{-\xi_1}$, $D : (\tau/T)^{-\xi_2}$, $D : (\eta/T)^{-\xi_3}$, and $D : (\alpha/T)^{-\xi_4}$, respectively. The fitted exponent ξ is written in the same color as the corresponding solid fitting line.

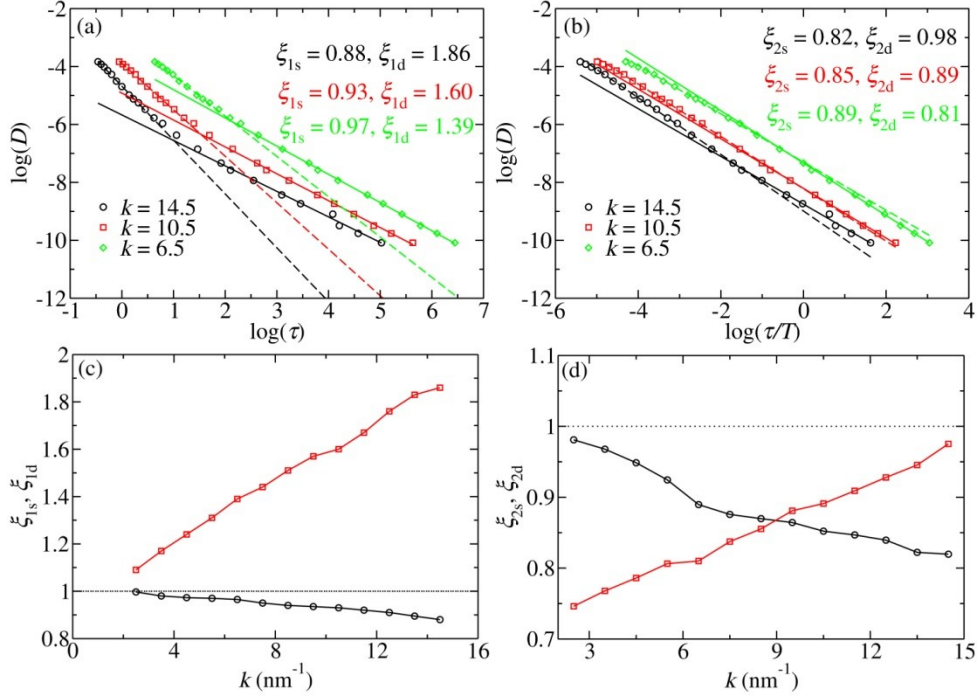


Fig. S6 Fitting of the k -dependent exponent ξ_1 by $D : \tau^{-\xi_1}$ (a) and ξ_2 by $D : (\tau/T)^{-\xi_2}$ for Jagla (b), as well as

ζ_1 vs. k (c) and ζ_2 vs. k (d). In (a) and (b), the calculated data are represented by different symbols and the fitted exponent is written in the same color as the corresponding fitting line; ζ_{1s}, ζ_{2s} values correspond to solid lines and ζ_{1d}, ζ_{2d} values correspond to dotted lines. In (c) and (d), black circles represent ζ_{1s}, ζ_{2s} and red squares are ζ_{1d}, ζ_{2d} .

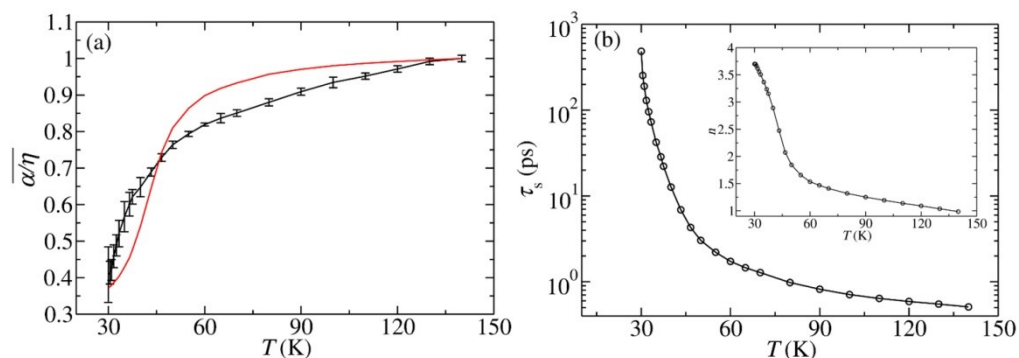


Fig. S7 (a) Effective hydrodynamic radius rescaled by the value at $T = 140$ K $\overline{\alpha/\eta}$ vs. T for the Jagla model. The black line is the simulated result and the red one is the fitted result with $\tau_0 = 19$ ps. (b) Residence correlation time τ_s and coordination number n (inset) of the first solvation shell vs. T for the Jagla fluid model.

References

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