

# Electronic Supplementary Information: Spectroscopic Detection of Gas-Phase HOSO<sub>2</sub>

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Table S-I: Observed line frequencies of HOSO<sub>2</sub> and their assignments.

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
$0^- \leftarrow 0^+$											
1	0	1	1.5	1	0	0	0	0.5	0	14040.362	1
			1.5	2				0.5	1	14041.186	-1
			1.5	1				0.5	1	14047.273	-0
			0.5	0				0.5	1	14068.138	-3
			0.5	1				0.5	0	14071.815	-0
			0.5	1				0.5	1	14078.727	-2
$0^+ \leftarrow 0^-$											
1	0	1	1.5	1	0	0	0	0.5	0	14000.242	2
			1.5	2				0.5	1	14001.116	-0
			1.5	1				0.5	1	14007.153	1
			0.5	0				0.5	1	14032.247	3
			0.5	1				0.5	0	14035.743	1
			0.5	1				0.5	1	14042.654	1
$0^+ \leftarrow 0^+$											
1	1	0	1.5	1	0	0	0	0.5	0	18490.943	-2
			1.5	2				0.5	1	18494.666	-0
			1.5	1				0.5	1	18497.856	-2
			0.5	1				0.5	0	18524.771	1
			0.5	1				0.5	1	18531.688	5
			0.5	0				0.5	1	18533.505	2
$0^- \leftarrow 0^-$											
1	1	0	1.5	1	0	0	0	0.5	0	18490.923	0
			1.5	2				0.5	1	18494.646	-0
			1.5	1				0.5	1	18497.835	-1
			0.5	1				0.5	0	18524.750	-0
			0.5	1				0.5	1	18531.658	-6
			0.5	0				0.5	1	18533.485	2
$0^+ \leftarrow 0^+$											
1	1	1	0.5	1	0	0	0	0.5	0	14294.803 <sup>b</sup>	-4
			1.5	2				0.5	1	14301.727 <sup>c</sup>	-3
			0.5	1				0.5	1	14301.727 <sup>c</sup>	7
			1.5	1				0.5	0	14302.518	2
			0.5	0				0.5	1	14306.723	-1

Table S-I (*continue*)

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
$0^- \leftarrow 0^-$											
1	1	1	0.5	1	0	0	0	0.5	1	14290.696	-1
			1.5	1				0.5	0	14292.530	2
			1.5	2				0.5	1	14293.195	-1
			0.5	0				0.5	1	14294.018	-0
$0^+ \leftarrow 0^+$											
1	1	0	1.5	2	1	0	1	1.5	2	4469.240 <sup>d</sup>	2
			1.5	1				1.5	2	4472.429 <sup>d</sup>	0
			0.5	1				1.5	2	4506.256 <sup>d</sup>	1
$0^- \leftarrow 0^-$											
1	1	0	1.5	2	1	0	1	1.5	2	4477.772 <sup>d</sup>	0
			1.5	1				1.5	2	4480.963 <sup>d</sup>	2
			0.5	1				1.5	2	4514.788 <sup>d</sup>	-0
$0^+ \leftarrow 0^+$											
2	0	2	2.5	3	1	1	1	1.5	2	23838.367	0
			2.5	2				1.5	1	23835.740	2
			2.5	2				1.5	2	23843.456 <sup>c</sup>	18
			2.5	2				0.5	1	23843.456 <sup>c</sup>	8
			1.5	1				0.5	0	23853.588	1
			1.5	2				1.5	1	23856.791	-3
			1.5	1				1.5	2	23858.595 <sup>c</sup>	13
			1.5	1				0.5	1	23858.595 <sup>c</sup>	3
			1.5	2				1.5	2	23864.501 <sup>c</sup>	8
			1.5	2				0.5	1	23864.501 <sup>c</sup>	-2
$0^- \leftarrow 0^-$											
2	0	2	2.5	2	1	1	1	1.5	1	23848.683	-3
			2.5	3				1.5	2	23849.910	-2
			2.5	2				1.5	2	23854.930	0
			2.5	2				0.5	1	23857.430	1
			1.5	1				0.5	0	23868.320	2
			1.5	2				1.5	1	23868.771	-2
			1.5	1				0.5	1	23871.643	3
			1.5	2				1.5	2	23875.015	-2
			1.5	2				0.5	1	23877.519	2
$0^- \leftarrow 0^+$											

Table S-I (*continue*)

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
2	1	2	2.5	2	1	1	1	1.5	1	23860.820	-0
			2.5	3				1.5	2	23863.482	-2
			2.5	2				0.5	1	23868.537	7
			1.5	1				0.5	0	23875.868	-2
			1.5	2				1.5	1	23879.173	-1
$0^+ \leftarrow 0^+$											
2	1	2	1.5	1	1	0	1	0.5	1	24089.312	2
			1.5	2				0.5	1	24095.353	1
			1.5	1				0.5	0	24099.721	-0
			2.5	2				1.5	1	24111.537	-1
			2.5	3				1.5	2	24112.478	-3
			2.5	2				1.5	2	24117.571	-3
			1.5	1				1.5	1	24124.812	-0
			1.5	2				1.5	2	24136.893	3
$0^- \leftarrow 0^-$											
2	1	2	1.5	1	1	0	1	0.5	1	24103.866	1
			1.5	2				0.5	1	24109.875	0
			1.5	1				0.5	0	24114.451	-2
			2.5	2				1.5	1	24122.976	1
			2.5	3				1.5	2	24124.023	-4
			2.5	2				1.5	2	24129.063	1
			1.5	1				1.5	1	24135.323	2
			1.5	2				1.5	2	24147.416	-1
$0^+ \leftarrow 0^-$											
2	0	2	1.5	2	1	0	1	0.5	1	24087.495	1
			2.5	2				1.5	1	24097.895	1
			2.5	3				1.5	2	24098.908	-1
$0^+ \leftarrow 0^+$											
2	1	1	2.5	3	1	0	1	1.5	2	36730.629 <sup>d</sup>	9
			2.5	2				1.5	2	36735.491 <sup>d</sup>	6
			1.5	1				1.5	2	36809.840 <sup>d</sup>	0
			1.5	2				1.5	2	36814.715 <sup>d</sup>	-2
$0^- \leftarrow 0^-$											
2	1	1	2.5	3	1	0	1	1.5	2	36730.254 <sup>d</sup>	-5
			2.5	2				1.5	2	36735.137 <sup>d</sup>	-9

Table S-I (*continue*)

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
			1.5	1				1.5	2	36807.299 <sup>d</sup>	0
			1.5	2				1.5	2	36812.222 <sup>d</sup>	-1
$0^- \leftarrow 0^+$											
2	2	0	2.5	3	1	0	1	1.5	2	41506.713 <sup>d</sup>	5
			2.5	2				1.5	2	41509.260 <sup>d</sup>	5
			1.5	1				0.5	1	41524.184 <sup>d</sup>	3
			1.5	2				0.5	1	41524.308 <sup>d</sup>	1
			1.5	2				1.5	2	41565.848 <sup>d</sup>	3
$0^+ \leftarrow 0^-$											
2	2	0	2.5	3	1	0	1	1.5	2	41466.716 <sup>d</sup>	-3
			2.5	2				1.5	2	41469.264 <sup>d</sup>	-4
			1.5	1				0.5	1	41488.188 <sup>d</sup>	-1
			1.5	2				0.5	1	41488.311 <sup>d</sup>	-3
			1.5	2				1.5	2	41525.849 <sup>d</sup>	-7
$0^+ \leftarrow 0^+$											
2	2	1	2.5	3	1	1	1	1.5	2	37267.319 <sup>e</sup>	35
			2.5	2				1.5	2	37268.240 <sup>d</sup>	-1
			1.5	2				1.5	2	37289.471 <sup>d</sup>	-6
			1.5	1				1.5	2	37290.396 <sup>e</sup>	19
$0^- \leftarrow 0^-$											
2	2	1	2.5	3	1	1	1	1.5	2	37266.958 <sup>d</sup>	-6
			2.5	2				1.5	2	37267.822 <sup>d</sup>	1
			1.5	2				1.5	2	37287.151 <sup>d</sup>	5
			1.5	1				1.5	2	37287.884 <sup>d</sup>	7

<sup>a</sup> Lines without superscript letter were observed by FTMW spectroscopy, and estimated error of 3 kHz are given in the least-squares analysis using the spfit program.

<sup>b</sup> Observed by the FTMW-MW double resonance technique. Estimated error of 20 kHz is given in the least-squares analysis.

<sup>c</sup> Overlapping peak. Not included in the least-squares analysis.

<sup>d</sup> Observed by the FTMW-MW double resonance technique. Estimated error of 6 kHz is given in the least-squares analysis.

<sup>e</sup> Not included in the least-squares analysis.

Table S-II: Observed line frequencies of DOSO<sub>2</sub> and their assignments.

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
$0^+ \leftarrow 0^+$											
1	0	1	1.5	1.5	0	0	0	0.5	0.5	13329.790 <sup>b</sup>	2
			1.5	2.5				0.5	1.5	13330.285	1
			1.5	0.5				0.5	0.5	13330.470 <sup>b</sup>	4
			1.5	1.5				0.5	1.5	13331.519 <sup>c</sup>	1
			1.5	0.5				0.5	1.5	13332.195 <sup>c</sup>	-1
			0.5	0.5				0.5	0.5	13334.197	-3
			0.5	0.5				0.5	1.5	13335.927 <sup>c</sup>	-3
			0.5	1.5				0.5	0.5	13336.382	-1
			0.5	1.5				0.5	1.5	13338.080 <sup>b</sup>	-33
$0^- \leftarrow 0^-$											
1	0	1	1.5	2.5	0	0	0	0.5	1.5	13330.228	-1
			1.5	1.5				0.5	1.5	13331.463 <sup>c</sup>	0
			1.5	0.5				0.5	1.5	13332.138 <sup>c</sup>	-4
			0.5	0.5				0.5	0.5	13334.147	2
			0.5	0.5				0.5	1.5	13335.879 <sup>c</sup>	4
			0.5	1.5				0.5	0.5	13336.332	3
			0.5	1.5				0.5	1.5	13338.080 <sup>b</sup>	22
$0^+ \leftarrow 0^+$											
1	1	0	1.5	2.5	1	1	1	0.5	1.5	3828.473 <sup>d</sup>	1
			1.5	2.5				1.5	1.5	3856.959 <sup>d</sup>	-4
			1.5	2.5				1.5	2.5	3857.794 <sup>d</sup>	-1
$0^- \leftarrow 0^-$											
1	1	0	1.5	2.5	1	1	1	0.5	1.5	3828.519 <sup>d</sup>	-1
			1.5	2.5				1.5	1.5	3857.021 <sup>d</sup>	10
			1.5	2.5				1.5	2.5	3857.845 <sup>d</sup>	2
$0^+ \leftarrow 0^+$											
2	0	2	2.5	2.5	1	0	1	1.5	1.5	23416.465 <sup>c</sup>	-18
			2.5	1.5				1.5	0.5	23416.500 <sup>c</sup>	-4
			2.5	3.5				1.5	2.5	23416.634 <sup>c</sup>	4
			2.5	1.5				1.5	1.5	23417.184 <sup>c</sup>	2
			2.5	2.5				1.5	2.5	23417.719 <sup>c</sup>	2
			1.5	1.5				0.5	1.5	23425.528 <sup>c</sup>	3
			1.5	2.5				0.5	1.5	23426.715 <sup>c</sup>	6

Table S-II (*continue*)

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
			1.5	0.5				0.5	0.5	23426.894 <sup>c</sup>	3
			1.5	1.5				0.5	0.5	23427.709 <sup>c</sup>	1
			1.5	1.5				1.5	1.5	23432.070 <sup>b</sup>	-51
			1.5	2.5				1.5	2.5	23434.500 <sup>b</sup>	-39
$0^- \leftarrow 0^-$											
2	0	2	2.5	2.5	1	0	1	1.5	1.5	23416.390 <sup>c</sup>	-3
			2.5	1.5				1.5	0.5	23416.416 <sup>c</sup>	2
			2.5	3.5				1.5	2.5	23416.541 <sup>c</sup>	1
			2.5	1.5				1.5	1.5	23417.094 <sup>c</sup>	2
			2.5	2.5				1.5	2.5	23417.630 <sup>c</sup>	3
			1.5	1.5				0.5	1.5	23425.435 <sup>c</sup>	0
			1.5	2.5				0.5	1.5	23426.617 <sup>c</sup>	-2
			1.5	0.5				0.5	0.5	23426.801 <sup>f</sup>	-1
			1.5	1.5				0.5	0.5	23427.620 <sup>c</sup>	1
			1.5	1.5				1.5	1.5	23432.070 <sup>b</sup>	39
			1.5	2.5				1.5	2.5	23434.500 <sup>b</sup>	51
$0^+ \leftarrow 0^+$											
2	1	2	1.5	0.5	1	1	1	0.5	0.5	22796.190	1
			1.5	1.5				0.5	1.5	22796.850 <sup>e</sup>	4
			1.5	1.5				0.5	0.5	22796.945	-1
			1.5	2.5				0.5	1.5	22797.949	2
			2.5	3.5				1.5	2.5	22806.675 <sup>c</sup>	1
			2.5	2.5				1.5	1.5	22806.891	0
			2.5	1.5				1.5	0.5	22807.030 <sup>c</sup>	1
			2.5	1.5				1.5	1.5	22807.569	-2
			2.5	2.5				1.5	2.5	22807.724	1
			1.5	2.5				1.5	2.5	22827.256 <sup>f</sup>	-14
$0^- \leftarrow 0^-$											
2	1	2	1.5	0.5	1	1	1	0.5	0.5	22796.095	-1
			1.5	1.5				0.5	1.5	22796.754	0
			1.5	1.5				0.5	0.5	22796.850 <sup>e</sup>	-3
			1.5	2.5				0.5	1.5	22797.855	0
			2.5	3.5				1.5	2.5	22806.581	0
			2.5	2.5				1.5	1.5	22806.799 <sup>c</sup>	0
			2.5	1.5				1.5	0.5	22806.936 <sup>c</sup>	0

Table S-II (*continue*)

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
			2.5	1.5				1.5	1.5	22807.479	0
			2.5	2.5				1.5	2.5	22807.632	1
			1.5	2.5				1.5	2.5	22827.184 <sup>f</sup>	7
$0^+ \leftarrow 0^+$											
2	1	1	1.5	0.5	1	1	0	0.5	0.5	30519.244	1
			1.5	1.5				0.5	0.5	30519.761	0
			1.5	1.5				0.5	1.5	30520.270	-3
			1.5	2.5				0.5	1.5	30521.112	0
			2.5	3.5				1.5	2.5	30524.810	1
			2.5	2.5				1.5	1.5	30525.007	2
			2.5	1.5				1.5	0.5	30525.115 <sup>c</sup>	2
			2.5	2.5				1.5	2.5	30525.716 <sup>g</sup>	2
$0^- \leftarrow 0^-$											
2	1	1	1.5	0.5	1	1	0	0.5	0.5	30519.191	2
			1.5	1.5				0.5	0.5	30519.707	0
			1.5	1.5				0.5	1.5	30520.220	1
			1.5	2.5				0.5	1.5	30521.058	0
			2.5	3.5				1.5	2.5	30524.754	-2
			2.5	2.5				1.5	1.5	30524.953 <sup>c</sup>	3
			2.5	1.5				1.5	0.5	30525.056	-3
			2.5	2.5				1.5	2.5	30525.655 <sup>g</sup>	-5
$0^+ \leftarrow 0^+$											
2	2	1	2.5	1.5	2	0	2	2.5	1.5	13757.533	1
			2.5	2.5				2.5	2.5	13757.821	0
			2.5	1.5				2.5	2.5	13758.229	-2
			2.5	3.5				2.5	3.5	13758.499	-1
			1.5	2.5				1.5	2.5	13808.465	0
			1.5	1.5				1.5	2.5	13808.656	-2
			1.5	2.5				1.5	1.5	13809.649	0
			1.5	1.5				1.5	1.5	13809.844	2
$0^- \leftarrow 0^-$											
2	2	1	2.5	1.5	2	0	2	2.5	1.5	13757.625	-1
			2.5	2.5				2.5	2.5	13757.916	0
			2.5	1.5				2.5	2.5	13758.327	1
			2.5	3.5				2.5	3.5	13758.594	0



Table S-II (*continue*)

$N'$	$K'_a$	$K'_c$	$J'$	$F'$	$N''$	$K''_a$	$K''_c$	$J''$	$F''$	obs. freq. <sup>a</sup> (MHz)	o.-c. (kHz)
			1.5	2.5				1.5	2.5	13808.558	-1
			1.5	1.5				1.5	2.5	13808.753	0
			1.5	2.5				1.5	1.5	13809.744	1
			1.5	1.5				1.5	1.5	13809.937	1
$0^+ \leftarrow 0^+ \text{ \& } 0^- \leftarrow 0^-^h$											
1	1	0	1.5	1.5	0	0	0	0.5	0.5	17883.584 <sup>f</sup>	-1
			1.5	0.5				0.5	0.5	17884.135 <sup>f</sup>	-1
			1.5	2.5				0.5	1.5	17884.606	-1
			1.5	1.5				0.5	1.5	17885.316	1
			1.5	0.5				0.5	1.5	17885.866 <sup>f</sup>	-1
			0.5	1.5				0.5	0.5	17918.854	-1
			0.5	0.5				0.5	0.5	17919.366	-1
			0.5	1.5				0.5	1.5	17920.584 <sup>f</sup>	-1
			0.5	0.5				0.5	1.5	17921.097 <sup>f</sup>	0
$0^+ \leftarrow 0^+ \text{ \& } 0^- \leftarrow 0^-^h$											
2	1	1	2.5	1.5	1	0	1	1.5	0.5	35078.778 <sup>e</sup>	-6
			2.5	2.5				1.5	1.5	35078.804	1
			2.5	3.5				1.5	2.5	35079.132	0
			2.5	2.5				1.5	2.5	35080.039	2
			1.5	0.5				0.5	1.5	35102.228 <sup>i</sup>	1
			1.5	1.5				0.5	1.5	35102.746	2
			1.5	2.5				0.5	1.5	35103.583	-1
			1.5	0.5				0.5	0.5	35104.412	2
			1.5	1.5				0.5	0.5	35104.926	-2
			1.5	2.5				1.5	2.5	35111.414 <sup>i,j</sup>	-2
$0^- \leftarrow 0^+$											
1	1	1	1.5	1.5	0	0	0	0.5	0.5	14025.948 <sup>g</sup>	1
			1.5	2.5				0.5	1.5	14026.847	1
			1.5	1.5				0.5	1.5	14027.672 <sup>g</sup>	-4
$0^+ \leftarrow 0^-$											
1	1	1	1.5	1.5	0	0	0	0.5	0.5	14025.829 <sup>g</sup>	-2
			1.5	2.5				0.5	1.5	14026.731	1
			1.5	1.5				0.5	1.5	14027.562 <sup>g</sup>	1

<sup>a</sup> Lines without superscript letter were observed by FTMW spectroscopy, and estimated error of 3 kHz are given in the least-squares analysis using the spfit program.

- <sup>b</sup> Very broad line. Not included in the least-squares analysis.
- <sup>c</sup> Doppler component(s) of the line is(are) overlapping with other(s). Estimated error of 6 kHz is given in the least-squares analysis.
- <sup>d</sup> Observed by the FTMW-MW double resonance technique. Estimated error of 6 kHz is given in the least-squares analysis.
- <sup>e</sup> The line is overlapping with other. Estimated error of 6 kHz is given in the least-squares analysis.
- <sup>f</sup> Broader line observed. Estimated error of 6 kHz is given in the least-squares analysis.
- <sup>g</sup> Very weak line observed. Estimated error of 6 kHz is given in the least-squares analysis.
- <sup>h</sup> Tunnel splitting is not observed in *c*-type transitions. The observed line frequency is processed as the averaged frequencies for the  $0^+ \leftarrow 0^+$  &  $0^- \leftarrow 0^-$  components in the least squares fit.
- <sup>i</sup> Observed by the FTMW-MW double resonance technique. Estimated error of 20 kHz is given in the least-squares analysis.
- <sup>j</sup> Only the  $0^+ \leftarrow 0^+$  component is observed by monitoring  $1_{01}-0_{00}$  ( $J = 1.5-0.5$ ,  $F = 2.5-1.5$ ,  $0^+ \leftarrow 0^+$ ) line @ 13330.285 MHz.

## A model calculation for the $C$ constant of $\text{HOSO}_2$

For a simplification, we made following assumptions.

- The structure of the  $\text{SO}_3$  frame is invariant during the OH torsional motion.
- The  $c$ -axis is fixed to the  $\text{SO}_3$  frame, perpendicular to the plane involving three O atoms, through the S atom, as illustrated in Fig. S-I.

The inertial moment of the proton with respect to the fixed  $c$ -axis is written as a function of the torsional coordinate  $\alpha$ ,

$$I_{\text{H}}^C(\alpha)/M_{\text{H}} = \left\{ (R_{\text{SO}} + R_{\text{OH}} \cos(\pi - \gamma)) \cdot \cos\left(\beta - \frac{\pi}{2}\right) + R_{\text{OH}} \sin(\pi - \gamma) \sin\left(\beta - \frac{\pi}{2}\right) \cos\alpha \right\}^2 + \{R_{\text{OH}} \sin(\pi - \gamma) \sin\alpha\}^2, \quad (1)$$

where  $M_{\text{H}}$  is the mass of proton. The values of  $R_{\text{SO}}$ ,  $R_{\text{OH}}$ ,  $\beta$ , and  $\gamma$  are fixed to those at the theoretical equilibrium structure in Fig. 1 of the main text, 1.607 Å, 0.968 Å, 102.92°, and 107.69°, respectively. Then, eq. (1) is rewritten as

$$I_{\text{H}}^C(\alpha) = M_{\text{H}} \{ (1.853 + 0.206 \cos\alpha)^2 + (0.922 \sin\alpha)^2 \}. \quad (2)$$

The contribution of the  $\text{SO}_3$  frame,  $I_{\text{SO}_3}^C$ , is constant from the above assumptions, fixed to 98.65 uÅ<sup>2</sup> in the present calculation in order to reproduce the experimental  $C$  constant well.

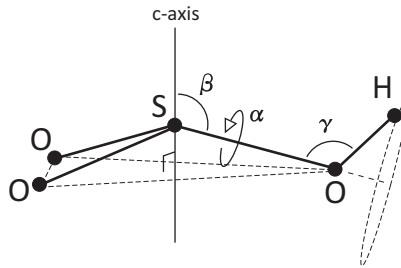


Figure S-I: Structural parameters for a model calculation of the  $C$  constant.  $\alpha$  is the torsional coordinate. The OH bond is parallel to the  $c$ -axis and the proton is above the plane involving three O atoms at  $\alpha = 0$ .  $\beta$  and  $\gamma$  are fixed to 102.92° and 107.69°, respectively.

The total  $I^C(\alpha)$  value is the sum of  $I_{\text{H}}^C(\alpha)$  and  $I_{\text{SO}_3}^C$ . The rotational constant  $C$  is then obtained by calculating the expectation value of the inverse of  $I^C(\alpha)$  using the wavefunction obtained from the tunnel splitting calculation described in the discussion of the main text. The  $C$  constant of HOSO<sub>2</sub> is then calculated to be 4910.69577 and 4910.69558 MHz for the  $0^+$  and  $0^-$  sublevels, respectively, assuming the potential barrier of  $1150 \text{ cm}^{-1}$  ( $V_1=0$  and  $V_2 = 1150 \text{ cm}^{-1}$ ). For DOSO<sub>2</sub>, a similar calculation gives a much smaller difference in the  $C$  constant,  $8 \times 10^{-4} \text{ kHz}$  (the  $C$  constant of  $0^+$  is larger).