Electronic Supplementary Information

Elucidating the effects of individual components in K_xMnO_y/SiO_2 and water on selectivity enhancement in the oxidative coupling of methane

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Mears Criterion for External Diffusion Limitations

To estimate the influence of external diffusion limitations, the Mears criterion was applied:

$$\frac{r_{obs} \cdot \rho_{catalyst} \cdot R \cdot n}{k_c \cdot C} < 0.15$$

 r_{obs} – measured reaction rate, kmol/(kg_{cat}·s)

 $\rho_{catalyst}$ – catalyst density, kg/m³

R – catalyst pellet radius, m

n – reaction order

 k_c – mass transfer coefficient, m/s

C – bulk concentration of reactant, kmol/m³

For the OCM reaction at 800 °C over 10K₂MnO₄/SiO₂ follows for the highest activity:

 $\frac{r_{obs} \cdot \rho_{catalyst} \cdot R \cdot n}{k_c \cdot c} = [5.67 \cdot 10^{-7} \text{ kmol/(kg_{cat} \cdot s)]} \cdot [1.12 \cdot 10^3 \text{ kg/m}^3] \cdot [2 \cdot 10^{-4} \text{ m}] \cdot 2/([1.90 \cdot 10^{-1} \text{ m/s}]) = 2.99 \cdot 10^{-4} << 0.15$

For the OCM reaction at 800 °C over 8KMnO₄/SiO₂ follows for the highest activity:

 $\frac{r_{obs} \cdot \rho_{catalyst} \cdot R \cdot n}{k_c \cdot c} = [8.83 \cdot 10^{-6} \text{ kmol/(kg_{cat} \cdot s)]} \cdot [7.51 \cdot 10^2 \text{ kg/m}^3] \cdot [2 \cdot 10^{-4} \text{ m}] \cdot 2/([1.09 \cdot 10^{-1} \text{ m/s}]) = 5.4 \cdot 10^{-3} << 0.15$

Weisz-Prater criterion for Internal Diffusion Limitations

To estimate the influence of internal diffusion on the reaction rates, the Weisz-Prater criterion was applied:

$$\Psi = \frac{n+1}{2} \cdot \frac{r_{obs} \cdot \rho_{catalyst} \cdot R^2}{D \cdot C}$$
(S1)

If $\Psi < 1$, internal diffusion limitations are negligible.

n – reaction order

 r_{obs} – measured reaction rate, kmol/(kg_{cat}·s)

 $\rho_{catalyst}$ – catalyst density, kg/m³

R – catalyst pellet radius, m

D – diffusion coefficient, m²/s

C – bulk concentration of reactant, kmol/m³

For the OCM reaction at 800 °C over 10K₂MnO₄/SiO₂ follows for the highest activity:

$$\begin{split} \Psi &= [(2 + 1)/2] \quad [5.67 \cdot 10^{-7} \ \text{kmol}/(\text{kg}_{\text{cat}} \cdot \text{s})] \cdot [1.12 \cdot 10^3 \ \text{kg/m}^3] \cdot [(2 \cdot 10^{-4})^2 \ \text{m}^2]/([1.7 \cdot 10^{-4} \ \text{m}^2/\text{s}] \cdot [4.49 \cdot 10^{-3} \ \text{kmol/m}^3]) = \textbf{5.00} \cdot \textbf{10}^{-5} < \textbf{1} \end{split}$$

For the OCM reaction at 800 °C over 8KMnO₄/SiO₂ follows for the highest activity:

$$\begin{split} \Psi &= [(2 + 1)/2] \quad [8.83 \cdot 10^{-6} \quad kmol/(kg_{cat} \cdot s)] \cdot [7.51 \cdot 10^2 \quad kg/m^3] \cdot [(2 \cdot 10^{-4})^2 \quad m^2]/([1.7 \cdot 10^{-4} \ m^2/s]) \cdot [4.49 \cdot 10^{-3} \ kmol/m^3]) = \textbf{5.22 \cdot 10^{-5}} < \textbf{1} \end{split}$$

Mears Criterion for External Heat Transfer Limitations

The external heat transfer limitations were calculated as follows:

$$\frac{r_{obs} \cdot \rho_{catalyst} \cdot R \cdot E_a \cdot \Delta H}{k_g \cdot R_g \cdot T^2} < 0.15$$

 r_{obs} – measured reaction rate, kmol/(kg_{cat}·s)

 $\rho_{catalyst}$ – catalyst density, kg/m³

R – catalyst pellet radius, m

 E_a – activation energy, kJ/kmol

 ΔH – reaction heat, kJ/mol

 k_q – heat transport coefficient, kJ/(m²·s·K)

 R_q – gas constant, kJ/(mol·K)

T – reaction temperature, K

For the OCM reaction at 800 °C over 10K₂MnO₄/SiO₂ follows for the highest activity:

 $\frac{r_{obs} \cdot \rho_{catalyst} \cdot R \cdot E_a \cdot \Delta H}{k_g \cdot R_g \cdot T^2} = [5.67 \cdot 10^{-7} \text{ kmol/(kg_{cat} \cdot s)]} \cdot [1.12 \cdot 10^3 \text{ kg/m}^3] \cdot [2 \cdot 10^{-4} \text{ m}] \cdot [2.1 \cdot 10^5 \text{ kJ/kmol}] \cdot [8.09 \cdot 10^2 \text{ kJ/mol}] / ([1.38 \cdot 10^3 \text{ kJ/(m}^2 \cdot s \cdot K)] \cdot [8.31 \cdot 10^{-3} \text{ kJ/(mol} \cdot K)] \cdot [(1.07 \cdot 10^3)^2 \text{ K}^2]) = 1.63 \cdot 10^{-6} < 0.15$

For the OCM reaction at 800 °C over 10K₂MnO₄/SiO₂ follows for the highest activity:

 $\frac{r_{obs} \cdot \rho_{catalyst} \cdot R \cdot E_{a} \cdot \Delta H}{k_{g} \cdot R_{g} \cdot T^{2}} = [8.83.67 \cdot 10^{-6} \text{ kmol/(kg_{cat} \cdot s)]} \cdot [7.51 \cdot 10^{2} \text{ kg/m}^{3}] \cdot [2 \cdot 10^{-4} \text{ m}] \cdot [1.2 \cdot 10^{5} \text{ kJ/kmol}] \cdot [8.09 \cdot 10^{2} \text{ kJ/mol}] / ([1.38 \cdot 10^{3} \text{ kJ/(m}^{2} \cdot s \cdot K)] \cdot [8.31 \cdot 10^{-3} \text{ kJ/(mol} \cdot K)] \cdot [(1.07 \cdot 10^{3})^{2} \text{ K}^{2}]) = 2.51 \cdot 10^{-5} < 0.15$

	Specific surface area / m²/g				
Catalysts	before OCM reaction	after OCM reaction without H2O	eaction after OCM reaction I2O with H2O		
5K ₂ MnO ₄ /SiO ₂	2.92	1.59	0.36		
$10K_2MnO_4/SiO_2$	0.87	0.09	0.06		
$20K_2MnO_4/SiO_2$	0.19	0.10	0.15		
4KMnO ₄ /SiO ₂	8.95	5.09	0.51		
8KMnO ₄ /SiO ₂	5.34	3.18	0.36		
16KMnO ₄ /SiO ₂	4.22	1.33	0.38		
SiO ₂ (amorphous)	272.3		72.6		
SiO_2 (α -cristobalite)	2.39				
$3Mn/SiO_2$	158.00		34.00		
5K ₂ O/SiO ₂	0.17		0.11		
$3Mn-5K_2O/SiO_2$	0.63	0.47	0.20		

Table S1. BET surface area of K_yMnO_4/SiO_2 (y = 1 or 2) before and after OCM reaction without H_2O (1st dry cycle after 6 h) and with H_2O (in steady state after 120 h).

Table S2. Near-surface composition (wt%) of K_yMnO_4/SiO_2 (y = 1 or 2) with different wt% of K_yMnO_4 (y = 1 or 2) before and after OCM reaction without H_2O (1st dry cycle after 6 h) and with H_2O (in steady state after 120 h) as determined by XPS. The corresponding bulk values determined by ICP-OES are given in the brackets.

Catalysts	Catalyst treatment	K	Mn	Si	0
	Fresh sample	6.9 (1.8)	1.6 (1.4)	43.4	41.7
5K2MnO4/SiO2	After OCM without H ₂ O	6.6	1.7	44.6	42.5
	After OCM with H ₂ O	6.2 (1.8)	1.9 (1.4)	44.8	42.2
20K2MnO4/SiO2	Fresh sample	14.6 (8.1)	3.8 (5.7)	36.6	37.7
	After OCM without H ₂ O	13.2	3.7	35.5	39.6
	After OCM with H ₂ O	13.3 (8.1)	3.9 (5.5)	37.9	38.7
4KMnO ₄ /SiO ₂	Fresh sample	3.4 (1.1)	2.2 (1.5)	46.7	44.3
	After OCM without H ₂ O	5.0	4.0	43.6	43.7
	After OCM with H ₂ O	7.7 (1.0)	6.1 (1.3)	39.1	40.7
16KMnO ₄ /SiO ₂	Fresh sample	5.7 (3.7)	2.6 (4.9)	44.0	44.3
	After OCM without H ₂ O	8.0	5.0	40.3	41.2
	After OCM with H ₂ O	7.7 (3.4)	6.5 (4.6)	38.9	41.8



Figure S1. Determination of the methane conversion rate $r(CH_4)$ from the correlation between the methane conversion $X(CH_4)$ and the contact time τ .



Figure S2. Representative STEM-HAADF images and EDX spectra of $10K_2MnO_4/SiO_2$ (a-d) before and (e-h) after OCM reaction with co-fed H₂O.



Figure S3. Representative STEM-HAADF images of $8KMnO_4/SiO_2$ and EDX spectra (a-d) before and (e-h) after OCM reaction with co-fed H₂O.



Figure S4. XRD patterns of (a) $5K_2MnO_4/SiO_2$, (b) $20K_2MnO_4/SiO_2$, (c) $4KMnO_4/SiO_2$ and (d) $16KMnO_4/SiO_2$ (i, iii, v, vii) before, (ii, iv, vi, viii) after OCM reaction with H₂O. $Mn_7O_8(SiO_4)$ (red bars) (PDF-No. 01-089-5662), Mn_3O_4 (blue bars) (PDF-No. 01-074-6605), tetragonal SiO₂ (black bars) (PDF-No. 01-074-9378) and orthorhombic SiO₂ (PDF-No. 00-042-1401) (green bars).



Figure S5. XRD patterns of (a) SiO₂, (b) $3Mn/SiO_2$ and (c) $5K_2O/SiO_2$ (i, iii, iv, vi) before, (ii, v, vii) after OCM reaction with H₂O. (iii) was calcined at 1600 °C, while all other samples were calcined at 800 °C. Tetragonal SiO₂ (black bars) (PDF-No. 01-074-9378), orthorhombic SiO₂ (PDF-No. 00-042-1401) (green bars), Mn_2O_3 (blue bars) (PDF-No. 00-041-1442), Mn_3O_4 (red bars) (PDF-No. 01-080-0382) and MnO(OH) (purple bars) (PDF-No. 01-088-0649).



Figure S6. (a,b) The overall rate of methane conversion and (c,d) selectivity to C_{2+} hydrocarbons over time on stream over (a,c) $5K_2MnO_4/SiO_2$ and (b,d) $20K_2MnO_4/SiO_2$ without (empty symbols) and with 30 vol% (filled symbols) water; 800 °C, $CH_4/O_2=8$, 40 vol% CH_4 , $X(CH_4) = 0.06, 0.3 \le X(O_2) \le 0.6$.



Figure S7. (a,b) The overall rate of methane conversion and (c,d) selectivity to C_{2+} hydrocarbons over time on stream over (a,c) 4KMnO₄/SiO₂ and (b,d) 16KMnO₄/SiO₂ without (empty symbols) and with 30 vol% (filled symbols) water; 800 °C, CH₄/O₂=8, 40 vol% CH₄, X(CH₄) of 0.06, 0.3 \leq X(O₂) \leq 0.6.



Figure S8. The selectivity to C₂H₆, C₂H₄, CO₂ and CO as function of methane conversion over $5K_2MnO_4/SiO_2$ at 800 °C without and with 30 vol% H₂O. (a-d) Permanent water effect is illustrated by comparison of the data under dry conditions from the 1st cycle (empty symbols) and 6th cycle (crossed symbols, after 114 h). (e-h) Reversible water effect is illustrated by the comparison of the data after 114 h under dry (crossed symbols) and after 120 h under wet (filled symbols) conditions; $0.4 \le X(O_2) \le 1.0$.



Figure S9. The selectivity to C₂H₆, C₂H₄, CO₂ and CO as function of methane conversion over $4KMnO_4/SiO_2$ and $16KMnO_4/SiO_2$ at 800 °C without and with 30 vol% H₂O. (a-d, i-l) Permanent water effect is illustrated by comparison of the data under dry conditions from the 1st cycle (empty symbols) and 6th cycle (crossed symbols, after 114 h). (e-h, m-p) Reversible water effect is illustrated by the comparison of the data after 114 h under dry (crossed symbols) and after 120 h under wet (filled symbols) conditions; $0.1 \le X(O_2) \le 1.0$.



Figure S10. The methane conversion rate into C₂, CO₂ and CO for the OCM reaction without (white bars) and with 30 vol% (black bars) co-fed H₂O over different catalysts at 800 °C in steady state; $0.001 \le X(CH_4) \le 0.003$ for SiO₂ (α -cristobalite), $0.02 \le X(CH_4) \le 0.04$ for all other catalysts.



Figure S11. Height-normalized transient responses of carbon-containing products after pulsing of (a-c) ${}^{18}\text{O}_2$:CH₄:He = 1:8:2 or (d-f) ${}^{18}\text{O}_2$:CH₄:H₂O:He = 1:8:0.85:2 mixtures at 800°C over different catalysts.