

Electronic Supplementary Information:

Distinctive Modulation of Halogen on Optical Anisotropy in α/β - Cd-P-X (X = Cl, Br, I)

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Nonlinear optical properties

The NLO coefficient is crucial for materials to be applied as second harmonic generation (SHG) conversion crystals. Theoretical NLO coefficients of the target compounds were also performed (listed in Table S1). For α -Cd₂P₃X (X= Cl, Br, I), the largest NLO coefficients are $d_{33} = 1.39$, $d_{33} = 1.02$, and $d_{33} = 1.94$ pm/V, respectively. Unfortunately, the relatively weak SHG response is probably associated with the structural arrangement. To analyze the contribution of an ion (or ionic group) to the SHG response, the SHG-density technique is adopted. It was performed by using the effective SHG of each band as a weighting coefficient to sum the probability densities of all states. The SHG-density caused by ion can be clearly viewed through occupied and unoccupied states, however, the states that do not contribute to SHG response will be invisible. SHG-density can be divided into occupied and unoccupied virtual-electron (VE) and virtual-hole (VH), respectively. The contributions of VE and VH of α -Cd₂P₃Cl, α -Cd₂P₃Br, and α -Cd₂P₃I were 40% and 60%, 57% and 43%, 43% and 57%, respectively (Figure S4). Provides a plot of the predominant contribution from X (X = Cl, Br, I) atoms along in occupied states. As for unoccupied states, SHG-density is concentrated on P atoms. What is more remarkable is that all compounds exhibit the increasing tendency of NLO coefficients which is consistent with their incremental hyperpolarizability because the going up halogen atoms size brings more contribution to the SHG effect (Table 1). Similar regularity can be observed in the cesium germanium halide perovskites CsGeX₃ (X = Cl, Br and I).¹

Table S1 Calculated NLO coefficients of NCS α -Cd₂P₃X (X = Cl, Br, I) and the largest first-order hyperpolarizabilities $|\beta_{\max}|$ of [CdP₃X] groups.

Compounds	NLO coefficients (pm/V)	$ \beta_{\max} $ (a.u.)
α -Cd ₂ P ₃ Cl	$d_{11} = -0.96, d_{15} = 0.12, d_{12} = -0.09, d_{13} = 0.78, d_{24} = 0.53, d_{33} = 1.23$	2118.30
α -Cd ₂ P ₃ Br	$d_{11} = -0.58, d_{15} = -0.39, d_{12} = -0.18, d_{13} = -0.82, d_{24} = -0.41, d_{33} = 1.33$	3936.25
α -Cd ₂ P ₃ I	$d_{11} = -0.08, d_{15} = -0.21, d_{12} = -0.42, d_{13} = -0.75, d_{24} = -0.07, d_{33} = 1.93$	4557.03

Table S2 Crystallographic structure data of the title compounds.

Compounds	Space group	Band gap (eV)			Symmetry	Volume (Å ³)	Unit cell dimensions (Å)
		GGA	HSE06	Exp.			
α -Cd ₂ P ₃ Cl ^[2]	<i>Cc</i>	1.28	1.99	/	NCS	531.24	7.969(1), 8.984(2), 7.554(2)
α -Cd ₂ P ₃ Br ^[2]	<i>Cc</i>	1.24	1.93	1.90 ^[2]	NCS	544.11	8.077(1), 9.088(2), 7.534(3)
α -Cd ₂ P ₃ I ^[2]	<i>Cc</i>	1.27	1.85	1.83 ^[2]	NCS	569.84	8.243(1), 9.334(2), 7.516(2)
β -Cd ₂ P ₃ Cl ^[3]	<i>C2/c</i>	1.29	1.98	1.87 ^[3b]	CS	532.62	7.988(1), 8.988(1), 7.555(1)
β -Cd ₂ P ₃ Br ^[3]	<i>C2/c</i>	1.26	1.91	1.86 ^[3b]	CS	544.95	8.089(1), 9.089(1), 7.535(1)
β -Cd ₂ P ₃ I ^[3]	<i>C2/c</i>	1.26	1.89	1.74 ^[3b]	CS	568.93	8.255(1), 9.304(1), 7.514(1)
Hg ₂ P ₃ Cl ^[4]	<i>C2/c</i>	1.12	1.86	/	CS	519.91	7.834(2), 8.844(11), 7.591(1)
Hg ₂ P ₃ Br ^[4]	<i>Pbcn</i>	0.83	1.71	/	CS	558.16	8.014(1), 8.903(1), 7.823(1)

Table S3 Calculated birefringence Δn and optical permittivities $\Delta\epsilon$ ($f \rightarrow \text{infinity}$) of $\alpha/\beta\text{-Cd}_2\text{P}_3\text{X}$ (X = Cl, Br, I).

Compounds	Space group	ϵ_{xx}	ϵ_{yy}	ϵ_{zz}	$\Delta\epsilon$	Δn
$\alpha\text{-Cd}_2\text{P}_3\text{Cl}$	<i>Cc</i>	7.24	7.35	8.87	1.63	0.25
$\alpha\text{-Cd}_2\text{P}_3\text{Br}$	<i>Cc</i>	7.81	7.84	9.08	1.27	0.19
$\alpha\text{-Cd}_2\text{P}_3\text{I}$	<i>Cc</i>	9.18	9.13	9.48	0.35	0.04
$\beta\text{-Cd}_2\text{P}_3\text{Cl}$	<i>C2/c</i>	7.22	7.36	8.86	1.64	0.24
$\beta\text{-Cd}_2\text{P}_3\text{Br}$	<i>C2/c</i>	7.87	7.86	9.09	1.23	0.17
$\beta\text{-Cd}_2\text{P}_3\text{I}$	<i>C2/c</i>	9.25	9.17	9.54	0.37	0.03

Table S4 Birefringence and band gap of a series of excellent halide optical crystals.

Compounds	Space group	Band gap (eV)	Birefringence (@ 1064 nm)
HgBr ₂ ^[5]	<i>Cmc2₁</i>	3.30	0.24
HgI ₂ ^[6]	<i>Cmc2₁</i>	2.37	0.50
Hg ₂ Cl ₂ ^[7]	<i>I4/mmm</i>	2.90	0.54/0.55 (Exp.)
Hg ₂ Br ₂ ^[7]	<i>I4/mmm</i>	2.50	0.70/0.67 (Exp.)
Hg ₂ I ₂ ^[8]	<i>I4/mmm</i>	2.10	1.08/0.95 (Exp.)
CsGeCl ₃ ^[9]	<i>R3m</i>	3.67	0.000
CsGeBr ₃ ^[10]	<i>R3m</i>	2.32	0.001
CsGeI ₃ ^[11]	<i>R3m</i>	1.60	0.002
CsPbCl ₃ ^[12]	<i>Pnma</i>	2.66 (Cal.)	0.104
CsPbBr ₃ ^[12]	<i>Pnma</i>	2.17 (Cal.)	0.179
CsPbI ₃ ^[13]	<i>Pnma</i>	2.13	0.275
(Cu(PS ₃ As ₃) ₄)Cl ^[14]	<i>P31c</i>	2.89 (Cal.)	0.021
(Cu(PS ₃ As ₃) ₄)Br ^[14]	<i>P31c</i>	2.45 (Cal.)	0.024
NaSb ₃ F ₁₀ ^[15]	<i>P6₃</i>	4.97	0.100
NaSb ₃ Cl ₁₀ * ^[16]	<i>P6₃</i>	4.49 (Cal.)	0.170
NaSb ₃ Br ₁₀ * ^[16]	<i>P6₃</i>	3.72 (Cal.)	0.235
NaSb ₃ I ₁₀ * ^[16]	<i>P6₃</i>	2.59 (Cal.)	0.367
SbF ₃ ^[17]	<i>Cmm2</i>	4.29	0.145
SbCl ₃ * ^[16]	<i>Cmm2</i>	4.05 (Cal.)	0.212
SbBr ₃ * ^[16]	<i>Cmm2</i>	3.30 (Cal.)	0.295
SbI ₃ * ^[16]	<i>Cmm2</i>	1.95 (Cal.)	0.924
Sn ₂ B ₅ O ₉ Cl ^[18]	<i>Pnn2</i>	3.53	0.189/0.168 (Exp.) @ 546 nm
Sn ₂ B ₅ O ₉ Br ^[19]	<i>Pnn2</i>	3.11	0.464/0.439 (Exp.) @ 546 nm
Sn ₂ B ₅ O ₉ I* ^[19]	<i>Pnn2</i>	2.99 (Cal.)	0.70 @ 546 nm
Pb ₂ B ₅ O ₉ Cl ^[20]	<i>Pnn2</i>	3.96	0.081/0.067 (Exp.) @ 546 nm
Pb ₂ B ₅ O ₉ Br ^[21]	<i>Pnn2</i>	3.30	0.118/0.130 (Exp.) @ 546 nm
Pb ₂ B ₅ O ₉ I ^[22]	<i>Pnn2</i>	3.10	0.32 @ 546 nm
Pb ₆ Ba ₂ (BO ₃) ₅ Cl ^[23]	<i>C2/m</i>	3.70	0.16 @ 532 nm
Pb ₆ Ba ₂ (BO ₃) ₅ Br ^[23]	<i>C2/m</i>	3.60	0.18 @ 532 nm

* Represents hypothetical crystal.

Table S5 Static polarization and polarization anisotropy of CsPbX₃ (X = Cl, Br, I).

Compound	Space group	Species	$\Delta\alpha$	Static polarization					
				<i>xx</i>	<i>xy</i>	<i>yy</i>	<i>xz</i>	<i>yz</i>	<i>zz</i>
CsPbCl ₃	<i>Pnma</i>	PbCl ₆	1.25	66.40	0.24	66.69	0.11	0.65	66.72
CsPbBr ₃	<i>Pnma</i>	PbBr ₆	2.36	95.29	1.07	95.98	-0.03	0.76	95.88
CsPbI ₃	<i>Pnma</i>	PbI ₆	8.46	146.09	-1.38	144.24	-3.68	-2.49	147.14

Table S6 Cut ionic radius for α/β -Cd₂P₃X (X = Cl, Br, I) and Hg₂P₃Cl.

Compound	Atom	Charge	Cut radius (Å)
α -Cd ₂ P ₃ Cl	Cd	+2	1.27
	P	-1	1.46
	Cl	-1	1.41
α -Cd ₂ P ₃ Br	Cd	+2	1.27
	P	-1	1.43
	Br	-1	1.50
α -Cd ₂ P ₃ I	Cd	+2	1.28
	P	-1	1.46
	I	-1	1.62
β -Cd ₂ P ₃ Cl	Cd	+2	1.27
	P	-1	1.43
	Cl	-1	1.43
β -Cd ₂ P ₃ Br	Cd	+2	1.27
	P	-1	1.45
	Br	-1	1.50
β -Cd ₂ P ₃ I	Cd	+2	1.28
	P	-1	1.47
	I	-1	1.73
Hg ₂ P ₃ Cl	Hg	+2	1.26
	P	-1	1.15
	Cl	-1	1.55

Table S7 Born effective charges of α/β -Cd₂P₃X (X = Cl, Br, I).

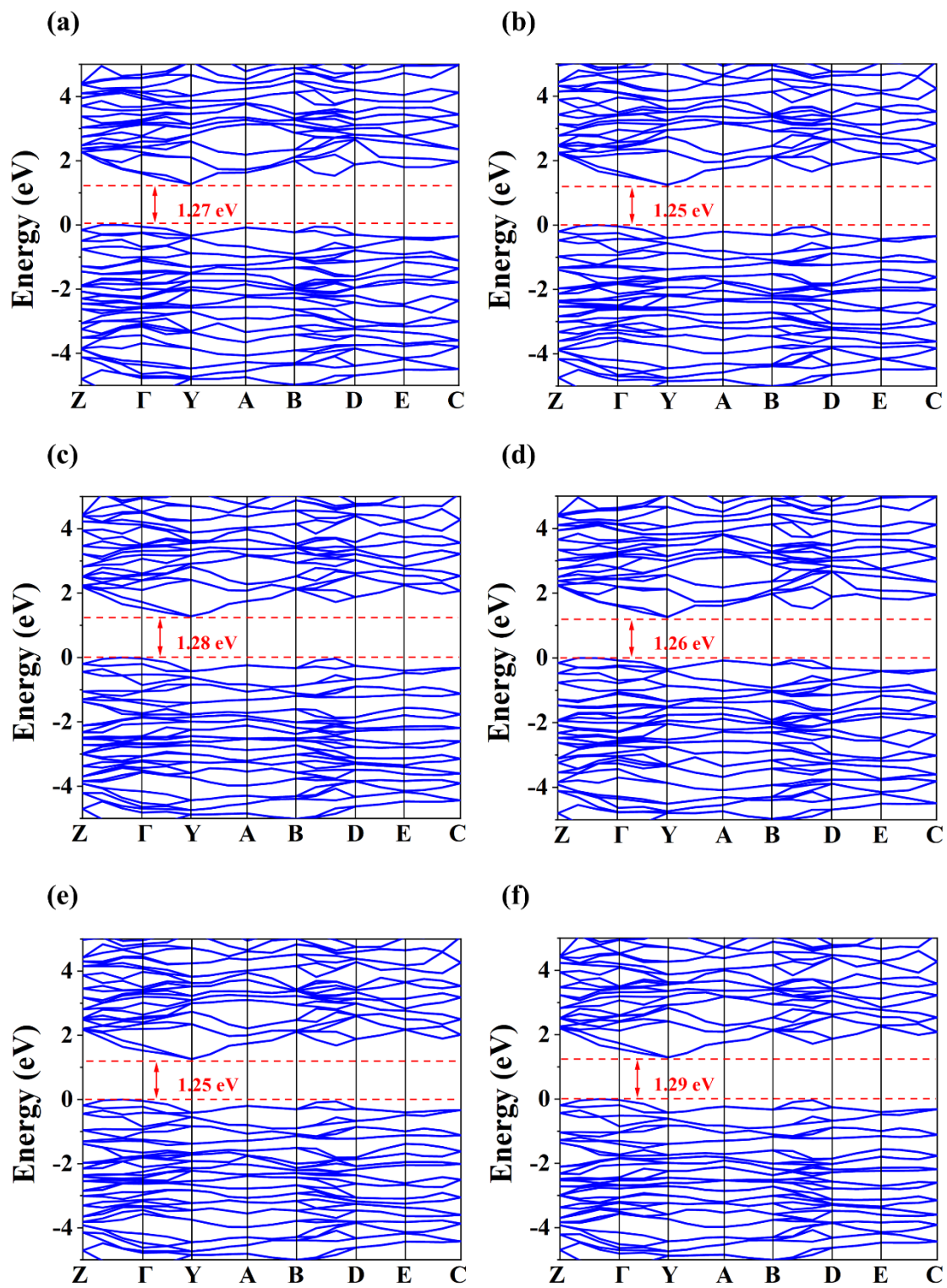
Compound	Atoms	q_{xx}	q_{yy}	q_{zz}	Δq
α -Cd ₂ P ₃ Cl	Cd ₁	2.264	2.178	2.175	-0.002
	Cd ₂	2.285	2.174	2.190	0.016
	Cl	-1.998	-1.879	-1.071	0.808
	P ₁	-0.876	-0.811	-1.418	-0.607
	P ₂	-0.786	-0.831	-0.440	0.391
	P ₃	-0.890	-0.830	-1.437	-0.607
α -Cd ₂ P ₃ Br	Cd ₁	2.41	2.33	2.19	-0.140
	Cd ₂	2.39	2.33	2.17	-0.164
	Br	-2.11	-2.07	-1.06	1.011
	P ₁	-0.91	-0.88	-1.44	-0.565
	P ₂	-0.87	-0.86	-0.44	0.416
	P ₃	-0.92	-0.87	-1.43	-0.558
α -Cd ₂ P ₃ I	Cd ₁	2.69	2.65	2.19	-0.466
	Cd ₂	2.67	2.65	2.17	-0.487
	I	-2.30	-2.34	-1.04	1.302
	P ₁	-0.99	-0.99	-1.42	-0.434
	P ₂	-1.08	-0.99	-0.48	0.511
	P ₃	-0.98	-0.99	-1.42	-0.425
β -Cd ₂ P ₃ Cl	Cd	2.26	2.17	2.18	-0.087
	Cl	-2.00	-1.87	-1.07	0.924
	P ₁	-0.88	-0.81	-1.42	-0.533
	P ₂	-0.76	-0.85	-0.45	0.315
β -Cd ₂ P ₃ Br	Cd	2.40	2.31	2.18	-0.224
	Br	-2.09	-2.03	-1.05	1.035
	P ₁	-0.90	-0.87	-1.43	-0.524
	P ₂	-0.91	-0.84	-0.45	0.462
β -Cd ₂ P ₃ I	Cd	2.68	2.64	2.19	-0.489
	I	-2.32	-2.33	-1.07	1.242
	P ₁	-0.99	-0.98	-1.42	-0.432
	P ₂	-1.42	-0.99	-0.48	0.940

Table S8 Atomic bond-valence for α/β -Cd-P-X (X = Cl, Br, I) [2-3a].

Compound	Atom	X	Y	Z	BVS
α -Cd ₂ P ₃ Cl	Cd(1)	0.000	0.149	0.000	2.081
	Cd(2)	0.494	0.144	0.080	2.161
	P(1)	0.116	0.046	0.318	1.159
	P(2)	-0.258	0.296	0.038	1.342
	P(3)	0.366	0.045	-0.240	1.133
	Cl(1)	0.253	0.345	-0.004	0.690
α -Cd ₂ P ₃ Br	Cd(1)	0.000	0.147	0.000	2.217
	Cd(2)	0.504	0.147	0.080	2.122
	P(1)	0.130	0.038	0.315	1.080
	P(2)	-0.250	0.292	0.005	1.409
	P(3)	0.378	0.040	-0.210	1.198
	Br(1)	0.249	0.374	0.070	0.653
α -Cd ₂ P ₃ I	Cd(1)	0.000	0.141	0.000	1.892
	Cd(2)	0.500	0.145	0.069	2.386
	P(1)	0.147	0.043	0.324	0.897
	P(2)	-0.258	0.290	0.040	1.235
	P(3)	0.388	0.044	-0.239	1.175
	I(1)	0.240	0.374	0.060	0.971
β -Cd ₂ P ₃ Cl	Cd(1)	0.245	0.356	0.290	2.027
	P(1)	0.376	0.047	0.031	1.173
	P(2)	0.000	0.709	0.250	1.319
	Cl(1)	0.000	0.126	0.250	0.518
β -Cd ₂ P ₃ Br	Cd(1)	0.245	0.356	0.290	2.095
	P(1)	0.376	0.047	0.031	1.139
	P(2)	0.000	0.709	0.250	1.226
	Br(1)	0.000	0.126	0.250	0.684
β -Cd ₂ P ₃ I	Cd(1)	0.245	0.356	0.290	2.124
	P(1)	0.376	0.047	0.031	1.069
	P(2)	0.000	0.709	0.250	1.074
	I(1)	0.000	0.126	0.250	1.034

Table S9 Selected bond length for α/β -Cd-P-X (X = Cl, Br, I) [2-3a].

α -Cd ₂ P ₃ Cl		α -Cd ₂ P ₃ Br		α -Cd ₂ P ₃ I	
Cd(1)-P(1)	= 2.508	Cd(1)-P(1)	= 2.529	Cd(1)-P(1)	= 2.591
Cd(1)-P(1)	= 2.579	Cd(1)-P(1)	= 2.612	Cd(1)-P(1)	= 2.689
Cd(1)-P(2)	= 2.505	Cd(1)-P(2)	= 2.417	Cd(1)-P(2)	= 2.601
Cd(1)-Cl(1)	= 2.681	Cd(1)-Br(1)	= 2.863	Cd(1)-I(1)	= 2.923
Cd(1)-Cl(1)	= 3.363	Cd(1)-Br(1)	= 3.305	Cd(1)-I(1)	= 3.367
Cd(2)-P(3)	= 2.508	Cd(2)-P(3)	= 2.441	Cd(2)-P(3)	= 2.451
Cd(2)-P(3)	= 2.598	Cd(2)-P(3)	= 2.646	Cd(2)-P(3)	= 2.524
Cd(2)-P(2)	= 2.471	Cd(2)-P(2)	= 2.531	Cd(2)-P(2)	= 2.550
Cd(2)-Cl(1)	= 2.626	Cd(2)-Br(1)	= 2.907	Cd(2)-I(1)	= 3.019
Cd(2)-Cl(1)	= 3.423	Cd(2)-Br(1)	= 3.183	Cd(2)-I(1)	= 3.219
P(1)-P(2)	= 2.271	P(1)-P(2)	= 2.209	P(1)-P(2)	= 2.290
P(1)-P(3)	= 2.271	P(1)-P(3)	= 2.686	P(1)-P(3)	= 2.269
P(3)-P(2)	= 2.282	P(3)-P(2)	= 2.686	P(3)-P(2)	= 2.435
β -Cd ₂ P ₃ Cl		β -Cd ₂ P ₃ Br		β -Cd ₂ P ₃ I	
Cd(1)-P(1)	= 2.495	Cd(1)-P(1)	= 2.508	Cd(1)-P(1)	= 2.537
Cd(1)-P(1)	= 2.585	Cd(1)-P(1)	= 2.593	Cd(1)-P(1)	= 2.610
Cd(1)-P(2)	= 2.494	Cd(1)-P(2)	= 2.521	Cd(1)-P(2)	= 2.570
Cd(1)-Cl(1)	= 2.819	Cd(1)-Br(1)	= 2.854	Cd(1)-I(1)	= 2.920
Cd(1)-Cl(1)	= 3.224	Cd(1)-Br(1)	= 3.259	Cd(1)-I(1)	= 3.328
P(1)-P(1)	= 2.286	P(1)-P(1)	= 2.308	P(1)-P(1)	= 2.348
P(1)-P(2)	= 2.283	P(1)-P(2)	= 2.301	P(1)-P(2)	= 2.335



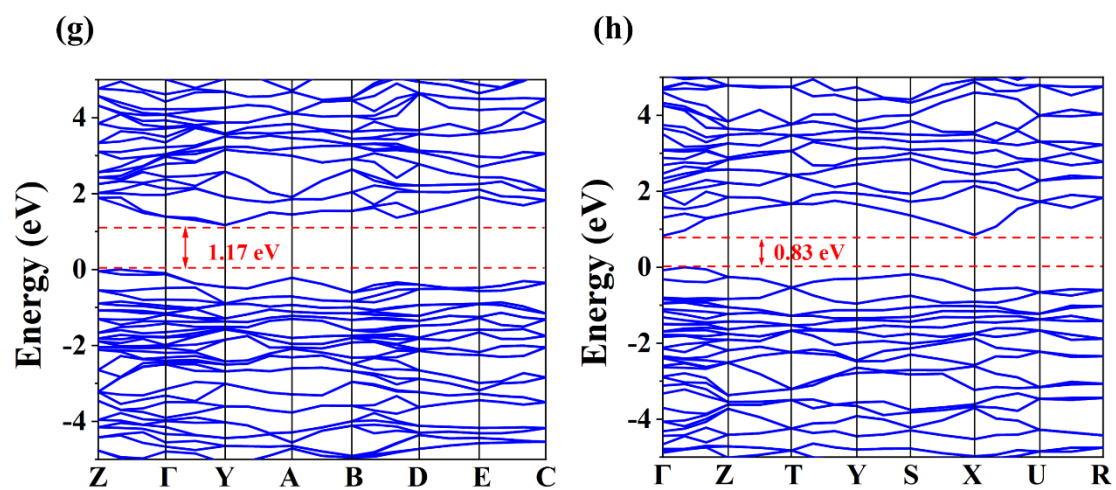
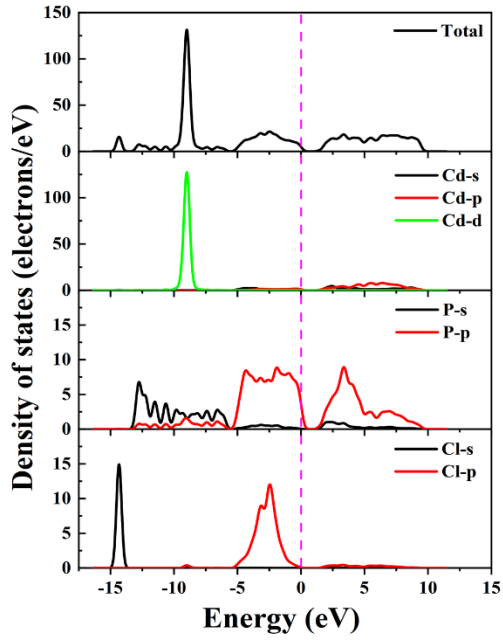
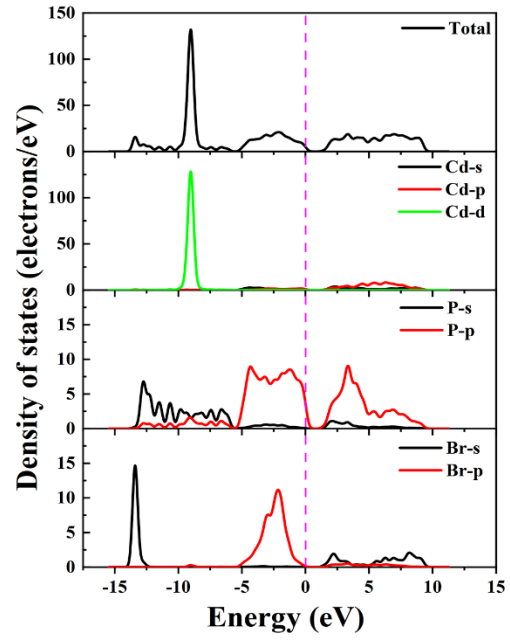
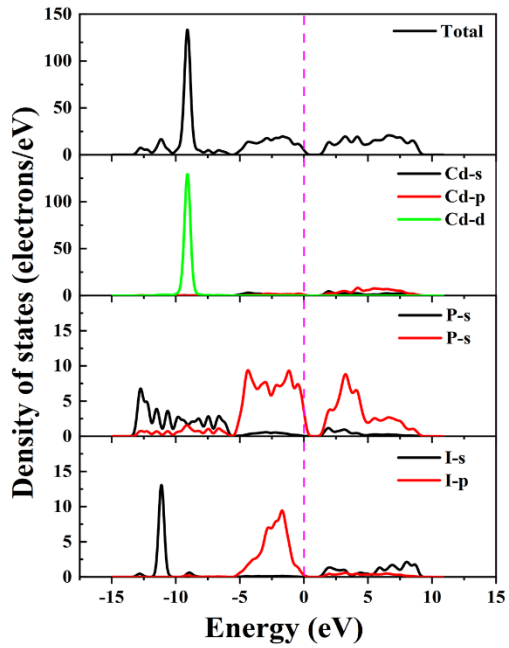
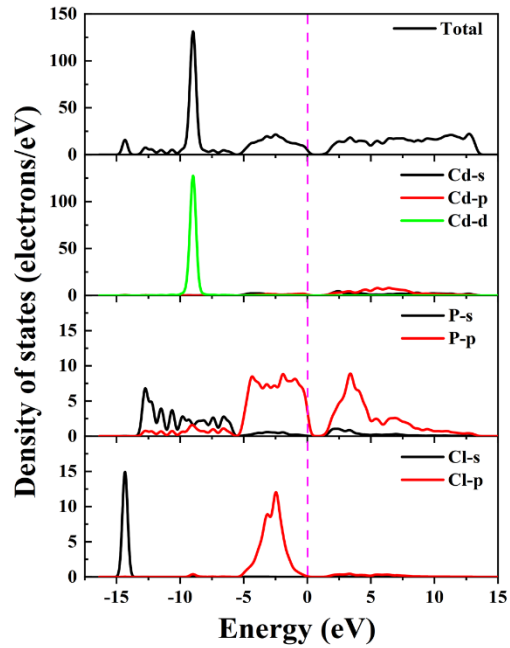


Figure S1 Calculated band gaps of α -Cd₂P₃Cl (a), α -Cd₂P₃Br (b), α -Cd₂P₃I (c), β -Cd₂P₃Cl (d), β -Cd₂P₃Br (e), β -Cd₂P₃I (f), Hg₂P₃Cl (g), and Hg₂P₃Br (h).

(a)**(b)****(c)****(d)**

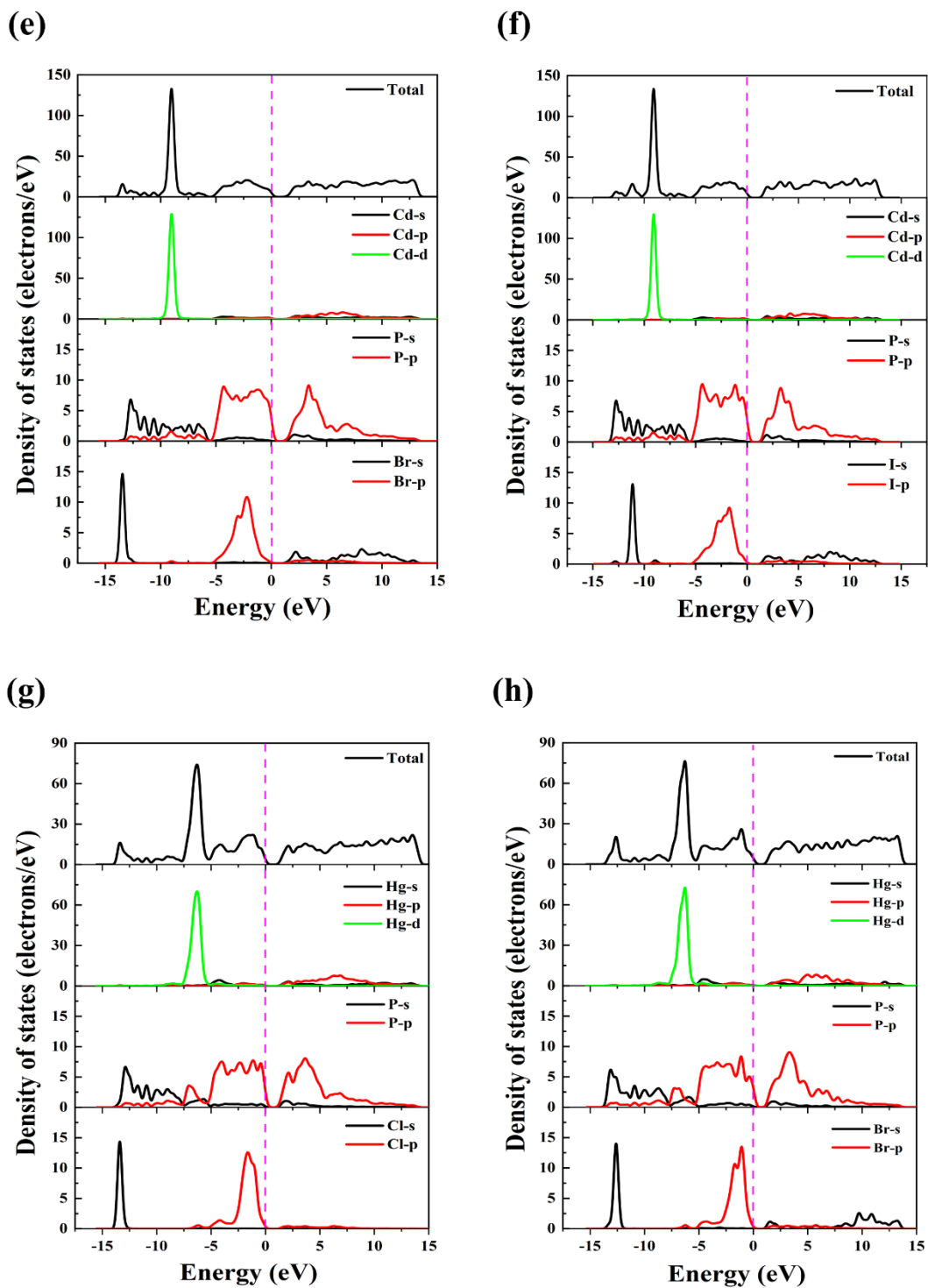


Figure S2 Total and partial density of states (T/PDOS) of α - $\text{Cd}_2\text{P}_3\text{Cl}$ (a), α - $\text{Cd}_2\text{P}_3\text{Br}$ (b), α - $\text{Cd}_2\text{P}_3\text{I}$ (c), β - $\text{Cd}_2\text{P}_3\text{Cl}$ (d), β - $\text{Cd}_2\text{P}_3\text{Br}$ (e), β - $\text{Cd}_2\text{P}_3\text{I}$ (f), $\text{Hg}_2\text{P}_3\text{Cl}$ (g), and $\text{Hg}_2\text{P}_3\text{Br}$ (h).

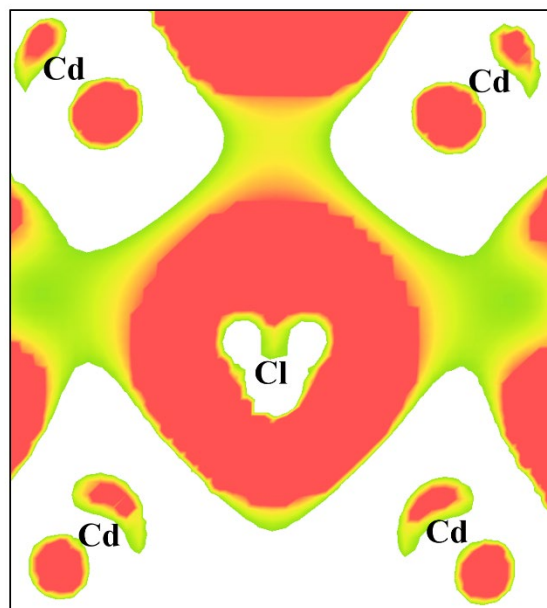


Figure S3 Electron-density difference maps for α - $\text{Cd}_2\text{P}_3\text{Cl}$.

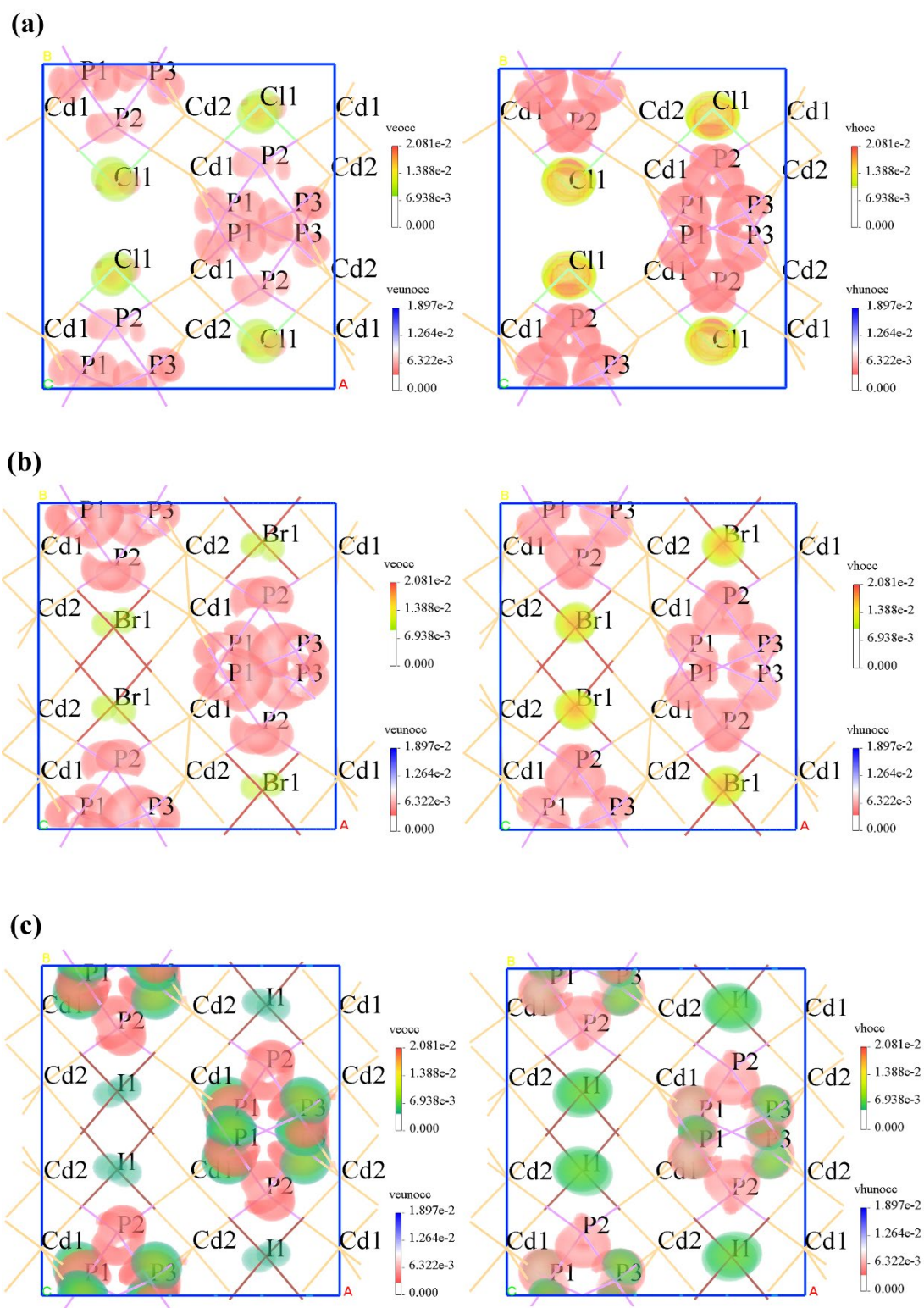


Figure S4 SHG-density of α - $\text{Cd}_2\text{P}_3\text{Cl}$ (a), α - $\text{Cd}_2\text{P}_3\text{Br}$ (b), and α - $\text{Cd}_2\text{P}_3\text{I}$ (c).

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