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Theoretical Prediction of Chiral Actinide Endohedral Borospherenes

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Figure S1. Low-lying isomers of $[Ac@B_{39}]^{2+}$ with the relative energies (eV) at the PBE0/RECP/6-311+G* levels. Light pink and blue spheres represent B and Ac, respectively. All the energies have been corrected for zero-point energies.



Figure S2. Low-lying isomers of $[Th@B_{39}]^{3+}$ with the relative energies (eV) at the PBE0/RECP/6-311+G* levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.



Figure S3. Low-lying isomers of $[Cf@B_{39}]^{2+}$ with the relative energies (eV) at the PBE0/RECP/6-311+G* levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.



Figure S4. Low-lying isomers of Ac@B₃₉ with the relative energies (eV) at the PBE0/RECP/6-311+G* levels. Light pink and blue spheres represent B and Ac, respectively. All the energies have been corrected for zero-point energies.



Figure S5. Low-lying isomers of Th@B₃₉ with the relative energies (eV) at the PBE0/RECP/6-311+G* levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.



Figure S6. Low-lying isomers of Cf@B₃₉ with the relative energies (eV) at the PBE0/RECP/6-311+G* levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.



Figure S7. Bonding pattern of C_2 [Th@B₃₉]³⁺ from AdNDP analysis with the occupation numbers (ONs) indicated at the PBE0/6-311+G*/RECP level of theory.



Figure S8. Bonding pattern of C_2 Ac@B₃₉ from AdNDP analysis with the ONs indicated at the PBE0/6-311+G*/RECP level of theory.



38×3c-2e σ bonds ON=1.77-1.93|e|



2×4c-2e σ bonds ON=1.71|e|



9×5c-2e π bonds ON=1.76-1.79|e|



4×6c-2e π bonds ON=1.84|e|



Figure S9. Bonding pattern of C_2 Th@B₃₉ from AdNDP analysis with the ONs indicated at the PBE0/6-311+G*/RECP level of theory.



Figure S10. QTAIM analysis of C_2 [Th@B₃₉]³⁺ at the PBE0/6-311+G*/RECP level of theory. Red points represent bond critical points, gray lines represent bond paths. Green points represent ring critical points, blue points represent cage critical points.



Figure S11. QTAIM analysis of C_2 Ac@B₃₉ at the PBE0/6-311+G*/RECP level of theory.



Figure S12. QTAIM analysis of C_2 Th@B₃₉ at the PBE0/6-311+G*/RECP level of theory.



Figure S13. The frontier molecular orbitals of $Ac@B_{39}$ and $Th@B_{39}$ at the PBE0/6-311+G*/RECP level of theory.



Figure S14. The composition of MO for $[Ac@B_{39}]^{2+}$ at the PBE0/6-311+G*/RECP level of theory.



Figure S15. The composition of MO for $[Th@B_{39}]^{3+}$ at the PBE0/6-311+G*/RECP level of theory.



Figure S16. The composition of MO for $Ac@B_{39}$ at the PBE0/6-311+G*/RECP level of theory.



Figure S17. The composition of MO for Th@B₃₉ at the PBE0/6-311+G*/RECP level of theory.



Figure S18. The infrared spectra of $C_2 B_{39}$ at the PBE0/6-311+G*/RECP level of theory.



Figure S19. The Raman spectra of $[An@B_{39}]^{n+}$ at the PBE0/6-311+G*/RECP level of theory.



Figure S20. The Raman spectra of $C_2 B_{39}^-$ at the PBE0/6-311+G*/RECP level of theory.

Table S1. Mayer bond orders (MBOs) of the An-B bonds for $[An@B_{39}]^{n+}$ calculated by the PBE0 method.

Species	MBOs	Total MBOs
$C_2 [Ac@B_{39}]^{2+}$	0.022 - 0.119	2.168
$C_2 Ac@B_{39}$	0.048 - 0.115	3.230
$C_2 [Th@B_{39}]^{3+}$	0.146 - 0.304	7.352
C_2 Th@B ₃₉	0.140 - 0.264	6.898

Table S2. The EDA results (kcal/mol) of Th@B₃₉ with Th⁴⁺ and B₃₉⁴⁻ as the two fragments at the PBE/TZP/ZORA level of theory.

Species	ΔE_{Pauli}	ΔE_{elstat}	ΔE_{steric}	ΔE_{orb}	ΔE_{int}
Th@B ₃₉	212.5	-1076.5 (49.9%)	-864.0	-1079.5 (50.1%)	-1943.5

Table S3. In the QTAIM analysis of C_2 [Ac@B₃₉]²⁺, density of electrons ρ , energy density H(r), Laplacian of electron density $\nabla^2 \rho$, and electron localization function ELF at the PBE0/6-311+G*/RECP level.

Name	CP Path	Bond Distances	ρ	H(r)	$ abla^2 ho$	ELF
C ₂ [Ac@B ₃₉] ²⁺	1	2.987	0.02694	-0.00097	0.06686	0.134
	2	2.815	0.03388	-0.00387	0.07179	0.179
	3	3.012	0.02672	-0.00123	0.06130	0.147
	4	2.815	0.03388	-0.00387	0.07179	0.179
	5	3.012	0.02672	-0.00123	0.06130	0.147
	6	2.987	0.02694	-0.00097	0.06685	0.134

Name	CP Path	Bond Distances	ρ	H(r)	$ abla^2 ho$	ELF
C ₂ [Th@B ₃₉] ³⁺	1	2.971	0.03002	-0.00285	0.05971	0.180
	2	2.776	0.03947	-0.00728	0.06586	0.234
	3	2.983	0.03043	-0.00355	0.05351	0.202
	4	2.776	0.03947	-0.00728	0.06586	0.234
	5	2.983	0.03042	-0.00355	0.05351	0.202
	6	2.971	0.03002	-0.00285	0.05971	0.180

Table S4. In the QTAIM analysis of C_2 [Th@B₃₉]³⁺, ρ , H(r), $\nabla^2 \rho$, and ELF at the PBE0/6-311+G*/RECP level.

Table S5. In the QTAIM analysis of C_2 Ac@B₃₉, ρ , H(r), $\nabla^2 \rho$, and ELF at the PBE0/6-311+G*/RECP level.

Name	CP Path	Bond Distances	ρ	H(r)	$ abla^2 ho$	ELF
	1	3.009	0.02621	-0.00061	0.06865	0.122
	2	2.938	0.03032	-0.00235	0.06599	0.168
$C_{\rm r} \Lambda c @ \mathbf{R}_{\rm res}$	3	2.824	0.03376	-0.00369	0.06956	0.187
C_2 AC $((J) D_{39})$	4	2.938	0.03032	-0.00235	0.06599	0.168
	5	2.824	0.03376	-0.00369	0.06956	0.187
	6	3.009	0.02621	-0.00061	0.06865	0.122

Name	CP Path	Bond Distances	ρ	H(r)	$ abla^2 ho$	ELF
	1	2.990	0.02889	-0.00233	0.06539	0.149
C THOD	2	2.772	0.03944	-0.00721	0.06397	0.242
	3	2.908	0.03409	-0.00492	0.05870	0.216
$C_2 \operatorname{III}(\underline{W}\mathbf{D}_{39})$	4	2.772	0.03944	-0.00721	0.06397	0.242
	5	2.908	0.03409	-0.00492	0.05870	0.216
	6	2.990	0.02889	-0.00233	0.06539	0.149

Table S6. In the QTAIM analysis of C_2 Th@B₃₉, ρ , H(r), $\nabla^2 \rho$, and ELF at the PBE0/6-311+G*/RECP level.

Table S7. The formation energy (kcal/mol) of $[An@B_{39}]^{n+}$ at the PBE0/6-311+G*/RECP level.

Reactions	Formation Energy
$Ac^{3+} + B_{39}^{-} = [Ac@B_{39}]^{2+}$	-529.1
$\mathbf{A}\mathbf{c}^{+}+\mathbf{B}_{39}^{-}=\mathbf{A}\mathbf{c}@\mathbf{B}_{39}$	-212.5
$Th^{4+} + B_{39}^{-} = [Th@B_{39}]^{3+}$	-1009.2
$\mathrm{Th}^{+} + \mathrm{B}_{39}^{-} = \mathrm{Th}@\mathrm{B}_{39}$	-296.8