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## Theoretical Prediction of Chiral Actinide Endohedral Borospherenes

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Figure S1. Low-lying isomers of $\left[\mathrm{Ac} @ \mathrm{~B}_{39}\right]^{2+}$ with the relative energies $(\mathrm{eV})$ at the PBE0/RECP/6-311+G* levels. Light pink and blue spheres represent B and Ac, respectively. All the energies have been corrected for zero-point energies.


Figure S2. Low-lying isomers of $\left[\mathrm{Th} @ \mathrm{~B}_{39}\right]^{3+}$ with the relative energies $(\mathrm{eV})$ at the PBE0/RECP/6-311+G* levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.


Figure S3. Low-lying isomers of $\left[\mathrm{Cf} @ \mathrm{~B}_{39}\right]^{2+}$ with the relative energies $(\mathrm{eV})$ at the PBE0/RECP/6-311+G* levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.


Figure S4. Low-lying isomers of $\mathrm{Ac} @ \mathrm{~B}_{39}$ with the relative energies $(\mathrm{eV})$ at the PBE0/RECP/6$311+G^{*}$ levels. Light pink and blue spheres represent B and Ac, respectively. All the energies have been corrected for zero-point energies.


Figure S5. Low-lying isomers of $\operatorname{Th} @ \mathrm{~B}_{39}$ with the relative energies $(\mathrm{eV})$ at the PBE0/RECP/6$311+G^{*}$ levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.


Figure S6. Low-lying isomers of $\mathrm{Cf} @ \mathrm{~B}_{39}$ with the relative energies $(\mathrm{eV})$ at the PBE0/RECP/6$311+G^{*}$ levels. Light pink and yellow spheres represent B and Th, respectively. All the energies have been corrected for zero-point energies.


Figure S7. Bonding pattern of $C_{2}\left[\operatorname{Th} @ \mathrm{~B}_{39}\right]^{3+}$ from AdNDP analysis with the occupation numbers (ONs) indicated at the PBE0/6-311+G*/RECP level of theory.


Figure S8. Bonding pattern of $C_{2} \mathrm{Ac} @ \mathrm{~B}_{39}$ from AdNDP analysis with the ONs indicated at the PBE0/6-311+G*/RECP level of theory.


Figure S9. Bonding pattern of $C_{2} \mathrm{Th} @ \mathrm{~B}_{39}$ from AdNDP analysis with the ONs indicated at the PBE0/6-311+G*/RECP level of theory.


Figure S10. QTAIM analysis of $C_{2}\left[{\left.\mathrm{Th} @ \mathrm{~B}_{39}\right]^{3+} \text { at the PBE0/6-311+G*/RECP level of theory. }}_{\text {P }}\right.$. Red points represent bond critical points, gray lines represent bond paths. Green points represent ring critical points, blue points represent cage critical points.


Figure S11. QTAIM analysis of $C_{2} \mathrm{Ac} @ \mathrm{~B}_{39}$ at the PBE0/6-311+G*/RECP level of theory.


Figure S12. QTAIM analysis of $C_{2} \operatorname{Th} @ \mathrm{~B}_{39}$ at the PBE $0 / 6-311+\mathrm{G}^{*} /$ RECP level of theory.


Figure S13. The frontier molecular orbitals of $A c @ B_{39}$ and $T h @ B_{39}$ at the PBE0/6$311+\mathrm{G}^{*} / \mathrm{RECP}$ level of theory.


Figure S14. The composition of MO for $\left[\mathrm{Ac} @ \mathrm{~B}_{39}\right]^{2+}$ at the PBE0/6-311+G*/RECP level of theory.


HOMO(a)
d 2\%
f 10\%



HOMO-1(b)
p 1\%
d 1\%



HOMO-3(b) f 17\%

Figure S15. The composition of MO for $\left[\mathrm{Th} @ \mathrm{~B}_{39}\right]^{3+}$ at the PBE0/6-311+G*/RECP level of theory.


Figure S16. The composition of MO for $\mathrm{Ac} @ \mathrm{~B}_{39}$ at the PBE0/6-311+G*/RECP level of theory.


Figure S17. The composition of MO for $\operatorname{Th} @ \mathrm{~B}_{39}$ at the PBE0/6-311+G*/RECP level of theory.


Figure S18. The infrared spectra of $C_{2} \mathrm{~B}_{39}{ }^{-}$at the PBE0/6-311+G*/RECP level of theory.


Figure S19. The Raman spectra of $\left[\mathrm{An} @ \mathrm{~B}_{39}\right]^{n+}$ at the PBE0/6-311+G*/RECP level of theory.


Figure S20. The Raman spectra of $C_{2} \mathrm{~B}_{39}{ }^{-}$at the $\mathrm{PBE} 0 / 6-311+\mathrm{G}^{*} / \mathrm{RECP}$ level of theory.

Table S1. Mayer bond orders (MBOs) of the An-B bonds for $\left[\mathrm{An} @ \mathrm{~B}_{39}\right]^{n+}$ calculated by the PBE0 method.

| Species | MBOs | Total MBOs |
| :---: | :---: | :---: |
| $\mathrm{C}_{2}\left[\mathrm{Ac} @ \mathrm{~B}_{39}\right]^{2+}$ | $0.022-0.119$ | 2.168 |
| $\mathrm{C}_{2} \mathrm{Ac} @ \mathrm{~B}_{39}$ | $0.048-0.115$ | 3.230 |
| $\mathrm{C}_{2}\left[\mathrm{Th} @ \mathrm{~B}_{39}\right]^{3+}$ | $0.146-0.304$ | 7.352 |
| $\mathrm{C}_{2} \mathrm{Th} @ \mathrm{~B}_{39}$ | $0.140-0.264$ | 6.898 |

Table S2. The EDA results ( $\mathrm{kcal} / \mathrm{mol}$ ) of $\mathrm{Th} @ \mathrm{~B}_{39}$ with $\mathrm{Th}^{4+}$ and $\mathrm{B}_{39}{ }^{4-}$ as the two fragments at the PBE/TZP/ZORA level of theory.

| Species | $\Delta \mathrm{E}_{\text {Pauli }}$ | $\Delta \mathrm{E}_{\text {elstat }}$ | $\Delta \mathrm{E}_{\text {steric }}$ | $\Delta \mathrm{E}_{\text {orb }}$ | $\Delta \mathrm{E}_{\text {int }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Th} @ \mathrm{~B}_{39}$ | 212.5 | -1076.5 |  | -1079.5 |  |

Table S3. In the QTAIM analysis of $C_{2}\left[\operatorname{Ac} @ \mathrm{~B}_{39}\right]^{2+}$, density of electrons $\rho$, energy density $H(r)$, Laplacian of electron density $\nabla^{2} \rho$, and electron localization function ELF at the PBE0/6$311+G^{*} /$ RECP level.

| Name | CP Path | Bond Distances | $\rho$ | $H(r)$ | $\nabla^{2} \rho$ | ELF |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.987 | 0.02694 | -0.00097 | 0.06686 | 0.134 |  |
| $C_{2}\left[\mathrm{Ac} @ \mathrm{~B}_{39}\right]^{2+}$ | 2 | 2.815 | 0.03388 | -0.00387 | 0.07179 | 0.179 |
|  | 4 | 3.012 | 0.02672 | -0.00123 | 0.06130 | 0.147 |
|  | 5 | 2.815 | 0.03388 | -0.00387 | 0.07179 | 0.179 |
|  | 6 | 3.012 | 0.02672 | -0.00123 | 0.06130 | 0.147 |

Table S4. In the QTAIM analysis of $C_{2}\left[\operatorname{Th} @ \mathrm{~B}_{39}\right]^{3+}, \rho, \mathrm{H}(\mathrm{r}), \nabla^{2} \rho$, and ELF at the PBE0/6$311+G * / R E C P$ level.

| Name | CP Path | Bond Distances | $\rho$ | $H(r)$ | $\nabla^{2} \rho$ | ELF |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2.971 | 0.03002 | -0.00285 | 0.05971 | 0.180 |
| $C_{2}\left[{\left.\mathrm{Th} @ \mathrm{~B}_{39}\right]^{3+}}^{2}\right.$ | 3 | 2.776 | 0.03947 | -0.00728 | 0.06586 | 0.234 |
|  | 4 | 2.983 | 0.03043 | -0.00355 | 0.05351 | 0.202 |
|  | 5 | 2.983 | 0.03947 | -0.00728 | 0.06586 | 0.234 |
|  | 6 | 2.971 | 0.03002 | -0.00285 | 0.05971 | 0.180 |

Table S5. In the QTAIM analysis of $C_{2} \operatorname{Ac} @ \mathrm{~B}_{39}, \rho, \mathrm{H}(\mathrm{r}), \nabla^{2} \rho$, and ELF at the PBE0/6$311+G^{*} /$ RECP level.

| Name | CP Path | Bond Distances | $\rho$ | $H(\mathrm{r})$ | $\nabla^{2} \rho$ | ELF |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 3.009 | 0.02621 | -0.00061 | 0.06865 | 0.122 |
| $C_{2} \mathrm{Ac} @ \mathrm{~B}_{39}$ | 2 | 2.938 | 0.03032 | -0.00235 | 0.06599 | 0.168 |
|  | 4 | 2.824 | 0.03376 | -0.00369 | 0.06956 | 0.187 |
|  | 5 | 2.938 | 0.03032 | -0.00235 | 0.06599 | 0.168 |
|  | 6 | 3.009 | 0.026 | 0.03376 | -0.00369 | 0.06956 |
|  |  | 0.00061 | 0.06865 | 0.127 |  |  |

Table S6. In the QTAIM analysis of $C_{2} \operatorname{Th} @ \mathrm{~B}_{39}, \rho, \mathrm{H}(\mathrm{r}), \nabla^{2} \rho$, and ELF at the PBE0/6$311+G * / R E C P$ level.

| Name | CP Path | Bond Distances | $\rho$ | $H(r)$ | $\nabla^{2} \rho$ | ELF |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.990 | 0.02889 | -0.00233 | 0.06539 | 0.149 |  |
| $C_{2} \mathrm{Th} @ \mathrm{~B}_{39}$ | 2 | 2.772 | 0.03944 | -0.00721 | 0.06397 | 0.242 |
|  | 4 | 2.908 | 0.03409 | -0.00492 | 0.05870 | 0.216 |
|  | 5 | 2.772 | 0.03944 | -0.00721 | 0.06397 | 0.242 |
|  | 6 | 2.908 | 0.03409 | -0.00492 | 0.05870 | 0.216 |
|  |  |  | 0.990 |  |  |  |

Table S7. The formation energy ( $\mathrm{kcal} / \mathrm{mol}$ ) of $\left[\mathrm{An} @ \mathrm{~B}_{39}\right]^{n+}$ at the PBE0/6-311+G*/RECP level.

| Reactions | Formation Energy |
| :---: | :---: |
| $\mathrm{Ac}^{3+}+\mathrm{B}_{39^{-}}=\left[\mathrm{Ac} @ \mathrm{~B}_{39}\right]^{2+}$ | -529.1 |
| $\mathrm{Ac}^{+}+\mathrm{B}_{39^{-}}=\mathrm{Ac} @ \mathrm{~B}_{39}$ | -212.5 |
| $\mathrm{Th}^{4+}+\mathrm{B}_{39}=\left[\mathrm{Th} @ \mathrm{~B}_{39}\right]^{3+}$ | -1009.2 |
| $\mathrm{Th}^{+}+\mathrm{B}_{39^{-}}=\mathrm{Th} @ \mathrm{~B}_{39}$ | -296.8 |


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