

## Supporting Information

### Third-Order Nonlinear Optical Property Contrast as Self- Assembly Recognition for Nanorings $\supset C_{60}$

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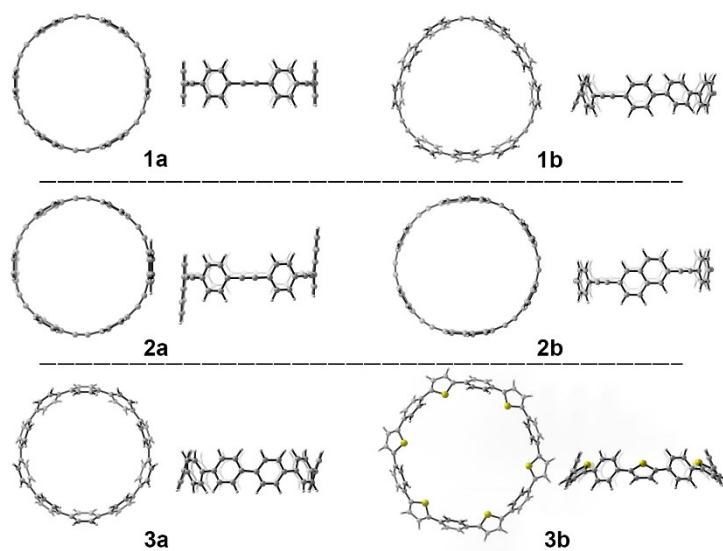


Fig. S1. The optimized structures of nanorings in top view and side view.

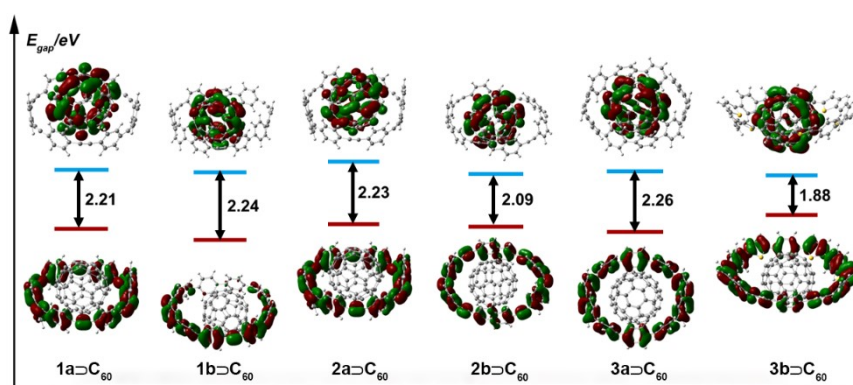
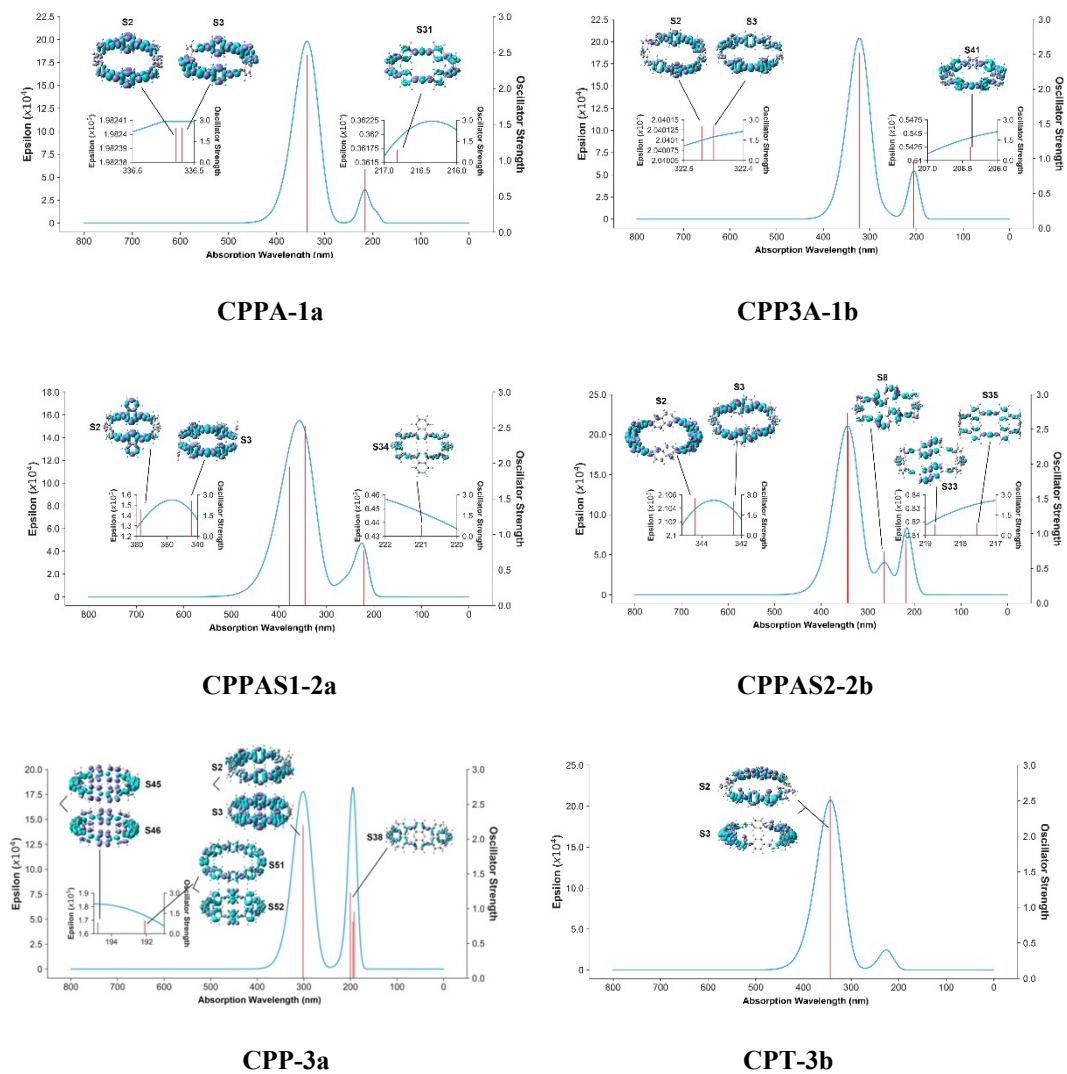
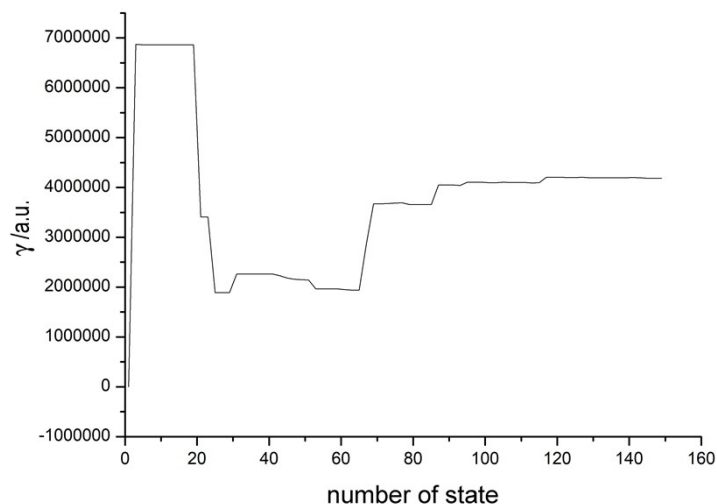


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**Table S1.** The TDDFT results calculated at  $\omega$ B97XD/6-31+G(d) level (absorption wavelength ( $\lambda$ /nm), transition energy ( $\Delta E$ /eV), and oscillator strength ( $f$ ) of major molecular orbital transitions) for nanorings.

nanoring	Transition State	$\Delta E$ /eV	$\lambda$ /nm	$f$
<b>1a</b>	S0-S2	3.6842	336.53	2.4387
	S0-S3	3.6843	336.52	2.4560
	S0-S31	5.7183	216.82	0.8775
<b>1b</b>	S0-S2	3.8449	322.47	2.5150
	S0-S3	3.8451	322.45	2.5131
	S0-S41	6.0073	206.39	0.9747
<b>2a</b>	S0-S2	3.2835	377.59	1.9473
	S0-S3	3.6043	343.99	2.5293
	S0-S34	5.6103	220.99	0.7706
<b>2b</b>	S0-S2	3.6007	344.34	2.7280
	S0-S3	3.6209	342.41	2.4717
	S0-S8	4.6695	265.52	0.7442
	S0-S33	5.6685	218.73	0.7710
	S0-S35	5.6998	217.53	0.9009
<b>3a</b>	S0-S2	4.1088	301.75	2.1955
	S0-S3	4.1088	301.75	2.1956
	S0-S38	6.1909	200.27	1.2291
	S0-S45	6.3658	194.77	0.8072
	S0-S46	6.3658	194.77	0.8068
	S0-S51	6.4543	192.10	0.9486
	S0-S52	6.4543	192.09	0.9487
<b>3b</b>	S0-S2	3.6128	343.18	2.5611
	S0-S3	3.6128	343.18	2.5610

**Table S2.** The first hyperpolarizabilities of nanorings and nanorings  $\supset C_{60}$ .

	a.u.				esu ( $\times 10^{-30}$ )
	$\beta_x$	$\beta_y$	$\beta_z$	$\beta^a$	$\beta$
<b>1a</b>	0	0	0	0	0
<b>1b</b>	156	-399	750	864	7
<b>2a</b>	10	-14	-10	20	0.2
<b>2b</b>	0	0	0	0	0
<b>3a</b>	0	0	0	0	0
<b>3b</b>	0	0	-9034	9034	78
<b>C<sub>60</sub></b>	0	0	0	0	1
<b>1a <math>\supset C_{60}</math></b>	-4353	-1973	4481	6551	57
<b>1b <math>\supset C_{60}</math></b>	1936	-342	-1269	2340	20
<b>2a <math>\supset C_{60}</math></b>	1018	2304	-636	2598	22
<b>2b <math>\supset C_{60}</math></b>	9097	4145	-1414	10096	87
<b>3a <math>\supset C_{60}</math></b>	16	14	14	25	0.2
<b>3b <math>\supset C_{60}</math></b>	-68	-11	3476	3476	30

<sup>a</sup>the  $\beta$  were calculated by software Multiwfn in the sum-overstates (SOS) method, the total magnitude of  $\beta$  can be measured by eqs.

$$\beta_{ABC}(-\omega_\sigma; \omega_1, \omega_2) = \hat{P}[A(-\omega_\sigma); B(\omega_1), C(\omega_2)] \sum_{i \neq 0} \sum_{j \neq 0} \frac{\mu_{0i}^A \overline{\mu_{ij}^B} \mu_{j0}^C}{(\Delta_i - \omega_\sigma)(\Delta_i - \omega_2)};$$

$$\mu_{ij}^A = \langle i | \hat{\mu}^A | j \rangle; \quad \overline{\mu_{ij}^A} = \mu_{ij}^A - \mu_{00}^A \delta_{ij}; \quad \omega_\sigma = \sum_i \omega_i$$

**Table S3.** The frequency-dependent second hyperpolarizabilities  $\gamma(-\omega; \omega, 0, 0)$  of nanorings and nanorings  $\supset C_{60}$ .

	esu ( $\times 10^{-36}$ )		
	$\gamma(\omega=0.06 \text{ a.u., } 760 \text{ nm})$	$\gamma(\omega=0.07 \text{ a.u., } 650 \text{ nm})$	$\gamma(\omega=0.08 \text{ a.u., } 570 \text{ nm})$
<b>1a</b>	1151	1214	1280
<b>1b</b>	320	379	521
<b>2a</b>	1400	1457	1480
<b>2b</b>	649	662	778
<b>3a</b>	656	780	967
<b>3b</b>	350	550	919
<b>1a <math>\supset C_{60}</math></b>	4297	4928	5853
<b>1b <math>\supset C_{60}</math></b>	1506	1683	1906
<b>2a <math>\supset C_{60}</math></b>	4170	5093	6677
<b>2b <math>\supset C_{60}</math></b>	3417	3866	4473
<b>3a <math>\supset C_{60}</math></b>	3504	3896	4408
<b>3b <math>\supset C_{60}</math></b>	5531	6406	7720

**Table S4.** The third-order NLO coefficients of nanorings and nanorings  $\supset C_{60}$  in dichloroethane.

	a.u.			esu ( $\times 10^{-36}$ )		$R^a$
	$\gamma_x$	$\gamma_y$	$\gamma_z$	$\gamma$	$\gamma$	
<b>1a</b>	-2.64	-2.57	-0.66	3.74	1886	1.92
<b>1b</b>	-0.83	-0.83	-0.49	1.27	638	2.20
<b>2a</b>	-2.66	-2.06	-1.07	3.53	1780	1.48
<b>2b</b>	-0.97	-2.66	-1.19	3.07	1547	2.34
<b>3a</b>	-1.48	-1.48	-0.81	2.25	1131	2.63
<b>3b</b>	-0.06	-0.10	-0.49	0.50	251	1.48
<b>C<sub>60</sub></b>	-2.57	-2.45	-2.53	4.36	2198	1.54
<b>1a <math>\supset C_{60}</math></b>	-5.13	-4.93	-1.36	7.24	3647	1.18
<b>1b <math>\supset C_{60}</math></b>	-2.16	-1.41	-0.67	2.66	1342	1.19
<b>2a <math>\supset C_{60}</math></b>	-2.53	-5.06	-0.75	5.70	2871	1.07
<b>2b <math>\supset C_{60}</math></b>	-2.67	-3.85	-0.94	4.78	2408	0.96
<b>3a <math>\supset C_{60}</math></b>	-4.78	-4.85	-1.42	6.95	3501	1.31
<b>3b <math>\supset C_{60}</math></b>	-5.23	-5.19	-1.96	7.62	3840	0.98

<sup>a</sup>the magnification of  $\gamma$  value in solution divided by  $\gamma$  value in gas phase.