

**Supporting Information (SI)**

**Two-Dimensional Transition Metal Borides as High Activity and Selectivity  
Catalysts for Ammonia Synthesis**

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## COMPUTATIONAL METHODS

All the geometry optimization and electronic property calculations were performed by means of the spin-polarized density functional theory (DFT), using Vienna *ab initio* simulation package (VASP).<sup>1,2</sup> The generalized gradient approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE)<sup>3,4</sup> formalism was applied to describe the exchange correlation functional. In addition, the projector-augmented wave (PAW) method<sup>5,6</sup> was used to treat the core–valence interactions with a kinetic cutoff energy of 550 eV for the plane wave basis set. Considering the van der Waals interactions (vdW), the DFT–D2 by Grimme was carried out in this work.<sup>7</sup> The coverage tolerances for total energy and force were set to  $10^{-5}$  eV and  $0.01$  eV/Å, respectively. The Monkhorst–Pack  $k$ -point meshes of  $3 \times 3 \times 1$  and  $5 \times 5 \times 1$  were implemented in geometry optimization and electronic self-consistence for a  $2 \times 3$  supercell of TMB<sub>2</sub> system, respectively. In order to avoid the interactions between periodic images, a vacuum space of 20 Å was applied along the  $z$  axis. The thermal stability of the TMB<sub>2</sub> was evaluated by *ab initio* molecular dynamics (AIMD) simulations at 700 K for 5 ps with a time step of 1 fs. The transition states and kinetic energy barriers were calculated by the climbing-image nudged elastic band (CI-NEB) method.<sup>8</sup>

The computational hydrogen electrode (CHE) model<sup>9,10</sup> was applied to compute the Gibbs free energy change ( $\Delta G$ ) for each elemental step in the NRR process, which can be obtained from the following equation

$$\Delta G = \Delta E + \Delta E_{\text{ZPE}} - T\Delta S + eU + \Delta G_{\text{pH}}$$

where  $\Delta E$  is the electronic energy difference between the product and reactant of each

elemental step in NRR process,  $\Delta E_{\text{ZPE}}$  and  $\Delta S$  are the corresponding changes in zero-point energy and entropy, respectively, obtained from frequency calculations at  $T = 298.15$  K. The entropy of gas molecules ( $\text{N}_2$  and  $\text{NH}_3$ ) was taken from standard values.  $e$  is the number of transferred electrons and  $U$  stands for the applied electrode potential.  $\Delta G_{\text{pH}}$  is the correction of pH, which can be expressed by

$$\Delta G_{\text{pH}} = \ln 10 \times k_{\text{B}} T \times \text{pH}$$

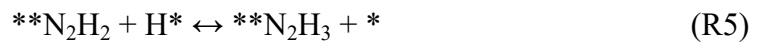
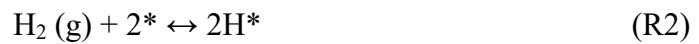
where  $k_{\text{B}}$  is the Boltzmann constant and the value of pH is set to zero in this work.

To ensure every protonation step exothermic, an additional voltage should be applied, which is defined as the limiting potential ( $U_{\text{L}}$ ) that can be obtained from the free energy change in the potential-determining step (PDS)

$$U_{\text{L}} = -\Delta G_{\text{max}}/e$$

## MICROKINETIC MODELING

The elementary reactions of ammonia synthesis on the  $\text{ReB}_2$  are considered



where \* represents a metal active site. Considering that N<sub>2</sub> adsorption on ReB<sub>2</sub> in side-on pattern occupies two reaction sites, and thus is denoted as \*\*N<sub>2</sub>. The rate of each

elementary step can be written as

$$r_1 = k_1 p_{N_2} \theta_*^2 - k_{-1} \theta_{**N_2} \quad \#(1)$$

$$r_2 = k_2 p_{H_2} \theta_*^2 - k_{-2} \theta_{*H}^2 \quad \#(2)$$

$$r_3 = k_3 \theta_{**N_2} \theta_{*H} - k_{-3} \theta_{**N_2H} \theta_* \quad \#(3)$$

$$r_4 = k_4 \theta_{**N_2H} \theta_{*H} - k_{-4} \theta_{**N_2H_2} \theta_* \quad \#(4)$$

$$r_5 = k_5 \theta_{**N_2H_2} \theta_{*H} - k_{-5} \theta_{**N_2H_3} \theta_* \quad \#(5)$$

$$r_6 = k_6 \theta_{**N_2H_3} \theta_{*H} - k_{-6} \theta_{*NH_2}^2 \theta_* \quad \#(6)$$

$$r_7 = k_7 \theta_{*NH_2} \theta_{*H} - k_{-7} \theta_{*NH_3} \theta_* \quad \#(7)$$

$$r_8 = k_8 \theta_{*NH_3} - k_{-8} p_{NH_3} \theta_* \quad \#(8)$$

where  $k_i$  is the rate constant for step  $i$ ,  $p$  denotes the partial pressure of gas N<sub>2</sub> and NH<sub>3</sub>,  $\theta$  denotes the coverage of the adsorbed species (N<sub>x</sub>H<sub>y</sub>). Our kinetic barrier calculation

shows that the step R<sub>4</sub> is the rate-determining step (RDS), therefore, under the quasi-equilibrium approximation (QEA),<sup>11-13</sup> the rates of all the other steps equal to zero ( $r_1 = r_2 = r_3 = r_5 = r_6 = r_7 = 0$ ). Hence, the coverage of reaction species can be

obtained

$$\theta_{**N_2} = K_1 p_{N_2} \theta_*^2 \quad \#(9)$$

$$\theta_{*H} = \sqrt{K_2 p_{H_2} \theta_*^2} \quad \#(10)$$

$$\theta_{**N_2H} = K_3 K_1 \sqrt{K_2 p_{H_2} p_{N_2}} \theta_*^2 \quad \#(11)$$

$$\theta_{**N_2H_2} = \frac{p_{NH_3}^2 \theta_*^2}{K_8^2 K_7^2 K_6 K_5 K_2^2 p_{H_2}^2} \quad \#(12)$$

$$\theta_{**N_2H_3} = \frac{p_{NH_3}^2 \theta_*^2}{K_8^2 K_7^2 K_6 \sqrt{K_2 p_{H_2}^3}} \#(13)$$

$$\theta_{*NH_2} = \frac{p_{NH_3} \theta_*}{K_8 K_7 \sqrt{K_2 p_{H_2}}} \#(14)$$

$$\theta_{*NH_3} = \frac{p_{NH_3} \theta_*}{K_8} \#(15)$$

where  $K_i = k_i/k_{-i}$  is the equilibrium constant for step  $i$ , which can be expressed by

$$K_i = e^{\frac{-\Delta G_i}{k_B T}} \#(16)$$

$$k_i = \frac{k_B T}{h} e^{\frac{-\Delta G_{TS}}{k_B T}} \#(17)$$

where  $\Delta G_i$  and  $\Delta G_{TS}$  are free energies of reaction and activation, respectively.  $k_B$  is Boltzmann constant;  $h$  is Planck constant. The sum of coverage of all the reaction species equals to one

$$\sum_i \theta_i = 1 \#(18)$$

Combining Equations (9)–(18), a quadratic equation on  $\theta_*$  can be solved analytically with the conversion ratio of  $NH_3$  fixed at 10%.<sup>13</sup> Then, the rate of slow step  $R_3$  can be obtained.

**Table S1.** Structure parameters ( $a$  and  $b$ ), area of the optimized unit cell ( $S_0$ ), and  $\partial^2 E_{\text{total}}/\partial \varepsilon^2$  of  $\text{TMB}_2$ .

	$a$ (Å)	$b$ (Å)	$S_0$ (Å <sup>2</sup> )	$\partial^2 E_{\text{total}}/\partial \varepsilon^2$
TiB <sub>2</sub>	4.55	2.99	13.62	85.22
VB <sub>2</sub>	4.54	2.86	12.99	94.65
CrB <sub>2</sub>	4.48	2.82	12.62	82.71
MnB <sub>2</sub>	4.52	2.69	12.18	100.81
FeB <sub>2</sub>	4.51	2.64	11.89	122.72
CoB <sub>2</sub>	4.68	2.51	11.76	146.96
NbB <sub>2</sub>	4.58	2.93	13.43	97.05
MoB <sub>2</sub>	4.65	2.84	13.22	109.05
TcB <sub>2</sub>	4.51	2.87	12.94	106.64
RuB <sub>2</sub>	4.50	2.84	12.77	131.97
WB <sub>2</sub>	4.64	2.82	13.06	124.86
ReB <sub>2</sub>	4.65	2.77	12.89	136.47
OsB <sub>2</sub>	4.56	2.81	12.78	145.58

**Table S2.** Total energy of  $\text{TMB}_2$  ( $E_{\text{TMB}_2}$ ), energy of single TM atom ( $E_{\text{TM}}$ ) and cohesive energy ( $E_{\text{coh}}$ ).

	$E_{\text{TMB}_2}$ (eV)	$E_{\text{TM}}$ (eV)	$E_{\text{coh}}$ (eV)
TiB <sub>2</sub>	-40.95	-2.30	5.84
VB <sub>2</sub>	-42.67	-3.58	5.70
CrB <sub>2</sub>	-43.05	-5.44	5.14
MnB <sub>2</sub>	-42.82	-5.11	5.21
FeB <sub>2</sub>	-41.50	-3.30	5.60
CoB <sub>2</sub>	-39.10	-1.72	5.72
NbB <sub>2</sub>	-45.46	-3.21	6.29
MoB <sub>2</sub>	-46.52	-4.59	6.00
TcB <sub>2</sub>	-45.92	-3.39	6.30
RuB <sub>2</sub>	-43.91	-2.47	6.27
WB <sub>2</sub>	-51.06	-4.54	6.78
ReB <sub>2</sub>	-50.40	-4.61	6.64
OsB <sub>2</sub>	-48.37	-2.93	6.86

**Table S3.** Total energy of  $\text{TMB}_2$  with ( $E$ ) and without  $\text{N}_2$  adsorption ( $E_{*\text{N}_2}$ ); zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) for NRR on  $\text{TMB}_2$  monolayer with  $\text{N}_2$  end-on adsorption.

	$E$	$E_{*\text{N}_2}$	$E_{\text{ZPE}}$	$TS$	$\Delta G_{*\text{N}_2}$
$\text{VB}_2$	-256.04	-274.20	0.19	0.19	-1.08
$\text{CrB}_2$	-258.27	-276.23	0.19	0.25	-0.93
$\text{MnB}_2$	-256.93	-274.66	0.20	0.18	-0.62
$\text{FeB}_2$	-248.92	-266.62	0.20	0.19	-0.61
$\text{CoB}_2$	-234.49	-252.23	0.22	0.14	-0.59
$\text{NbB}_2$	-272.67	-290.27	0.19	0.20	-0.54
$\text{MoB}_2$	-278.99	-296.69	0.19	0.20	-0.61
$\text{TcB}_2$	-275.40	-293.15	0.19	0.23	-0.72
$\text{RuB}_2$	-263.30	-280.87	0.21	0.16	-0.45
$\text{WB}_2$	-306.33	-324.54	0.20	0.20	-1.13
$\text{ReB}_2$	-302.03	-319.96	0.20	0.16	-0.80
$\text{OsB}_2$	-289.98	-307.77	0.21	0.15	-0.64



**Table S4.** Total energy of  $\text{TMB}_2$  with ( $E$ ) and without  $\text{N}_2$  adsorption ( $E_{*\text{N}_2}$ ); zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) for NRR on  $\text{TMB}_2$  monolayer with  $\text{N}_2$  side-on adsorption.

	$E$	$E_{*\text{N}_2}$	$E_{\text{ZPE}}$	$TS$	$\Delta G_{*\text{N}_2}$
$\text{TiB}_2$	-245.65	-263.99	0.20	0.11	-1.17
$\text{VB}_2$	-256.04	-274.81	0.20	0.11	-1.60
$\text{CrB}_2$	-258.27	-277.02	0.19	0.13	-1.61
$\text{MnB}_2$	-256.93	-274.62	0.19	0.13	-0.55
$\text{FeB}_2$	-248.92	-266.36	0.18	0.16	-0.34
$\text{NbB}_2$	-272.67	-290.92	0.19	0.13	-1.11
$\text{MoB}_2$	-278.99	-296.96	0.19	0.13	-0.82
$\text{TcB}_2$	-275.40	-293.11	0.18	0.16	-0.62
$\text{RuB}_2$	-263.30	-280.50	0.16	0.23	-0.18
$\text{WB}_2$	-306.33	-324.91	0.19	0.12	-1.42
$\text{ReB}_2$	-302.03	-319.80	0.18	0.13	-0.64
$\text{OsB}_2$	-289.98	-307.27	0.17	0.16	-0.20

**Table S5.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on  $\text{CrB}_2$  along mix pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-276.23	0.19	0.25	-276.29
*N-NH	-279.83	0.47	0.14	-279.50
*NH-NH	-283.37	0.76	0.19	-282.80
*NH-NH <sub>2</sub>	-287.27	1.12	0.25	-286.40
*NH <sub>2</sub> -NH <sub>2</sub>	-293.94	1.40	0.16	-292.70
*NH <sub>2</sub> -NH <sub>3</sub>	-296.44	1.71	0.25	-294.98
*NH <sub>2</sub>	-275.68	0.47	0.14	-275.35
*NH <sub>3</sub>	-279.20	1.00	0.19	-278.39

**Table S6.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on  $\text{ReB}_2$  along distal pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-319.96	0.20	0.16	-319.92
*N-NH	-323.33	0.47	0.17	-323.03
*N-NH <sub>2</sub>	-327.26	0.79	0.21	-326.68
*N-NH <sub>3</sub>	-332.43	1.11	0.19	-331.51
*N	-310.27	0.07	0.09	-310.29
*NH	-315.55	0.34	0.11	-315.32
*NH <sub>2</sub>	-319.91	0.66	0.12	-319.37
*NH <sub>3</sub>	-323.77	1.03	0.17	-322.91

**Table S7.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on  $\text{ReB}_2$  along mix pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-319.96	0.20	0.16	-319.92
*N-NH	-323.33	0.47	0.17	-323.03
*NH-NH	-327.05	0.83	0.17	-326.39
*NH-NH <sub>2</sub>	-332.04	1.15	0.15	-331.04
*NH <sub>2</sub> -NH <sub>2</sub>	-337.19	1.35	0.21	-336.05
*NH <sub>2</sub> -NH <sub>3</sub>	-341.26	1.71	0.22	-339.77
*NH <sub>2</sub>	-319.91	0.66	0.12	-319.37
*NH <sub>3</sub>	-323.77	1.03	0.17	-322.91

**Table S8.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on OsB<sub>2</sub> along distal pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-307.77	0.21	0.15	-307.71
*N-NH	-310.60	0.49	0.15	-310.26
*N-NH <sub>2</sub>	-314.26	0.80	0.21	-313.67
*N-NH <sub>3</sub>	-319.74	1.12	0.17	-318.79
*N	-298.44	0.08	0.04	-298.40
*NH	-302.67	0.35	0.08	-302.40
*NH <sub>2</sub>	-307.24	0.68	0.11	-306.67
*NH <sub>3</sub>	-311.20	1.03	0.13	-310.30

**Table S9.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on CrB<sub>2</sub> along enzymatic pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-277.02	0.19	0.13	-276.96
*N-NH	-279.83	0.47	0.14	-279.50
*NH-NH	-283.37	0.76	0.19	-282.80
*NH-NH <sub>2</sub>	-287.27	1.12	0.25	-286.40
*NH <sub>2</sub> -NH <sub>2</sub>	-293.94	1.40	0.16	-292.70
*NH <sub>2</sub> -NH <sub>3</sub>	-296.44	1.71	0.25	-294.98
*NH <sub>2</sub>	-275.68	0.47	0.14	-275.35
*NH <sub>3</sub>	-279.20	1.00	0.19	-278.39

**Table S10.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on  $\text{MnB}_2$  along enzymatic pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-274.62	0.19	0.13	-274.56
*N-NH	-277.80	0.48	0.12	-277.44
*NH-NH	-281.71	0.80	0.14	-281.05
*NH-NH <sub>2</sub>	-285.64	1.13	0.16	-284.67
*NH <sub>2</sub> -NH <sub>2</sub>	-291.52	1.42	1.52	-291.62
*NH <sub>2</sub> -NH <sub>3</sub>	-295.22	1.72	0.26	-293.76
*NH <sub>2</sub>	-274.28	0.70	0.08	-273.66
*NH <sub>3</sub>	-277.71	1.02	0.17	-276.86

**Table S11.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on FeB<sub>2</sub> along enzymatic pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-266.36	0.18	0.16	-266.34
*N-NH	-269.56	0.48	0.13	-269.21
*NH-NH	-273.62	0.81	0.12	-272.93
*NH-NH <sub>2</sub>	-277.45	1.14	0.17	-276.48
*NH <sub>2</sub> -NH <sub>2</sub>	-282.02	1.36	0.20	-280.86
*NH <sub>2</sub> -NH <sub>3</sub>	-286.91	1.71	0.28	-285.48
*NH <sub>2</sub>	-265.96	0.70	0.09	-265.35
*NH <sub>3</sub>	-269.80	1.02	0.18	-268.96



**Table S12.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on TcB<sub>2</sub> along enzymatic pathway.

	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-293.11	0.18	0.16	-293.09
*N-NH	-296.26	0.47	0.13	-295.92
*NH-NH	-300.21	0.79	0.15	-299.57
*NH-NH <sub>2</sub>	-304.20	1.13	0.17	-303.24
*NH <sub>2</sub> -NH <sub>2</sub>	-309.72	1.34	0.21	-308.59
*NH <sub>2</sub> -NH <sub>3</sub>	-313.79	1.71	0.27	-312.35
*NH <sub>2</sub>	-292.94	0.70	0.08	-292.32
*NH <sub>3</sub>	-296.17	1.01	0.18	-295.34

**Table S13.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on RuB<sub>2</sub> along enzymatic pathway.

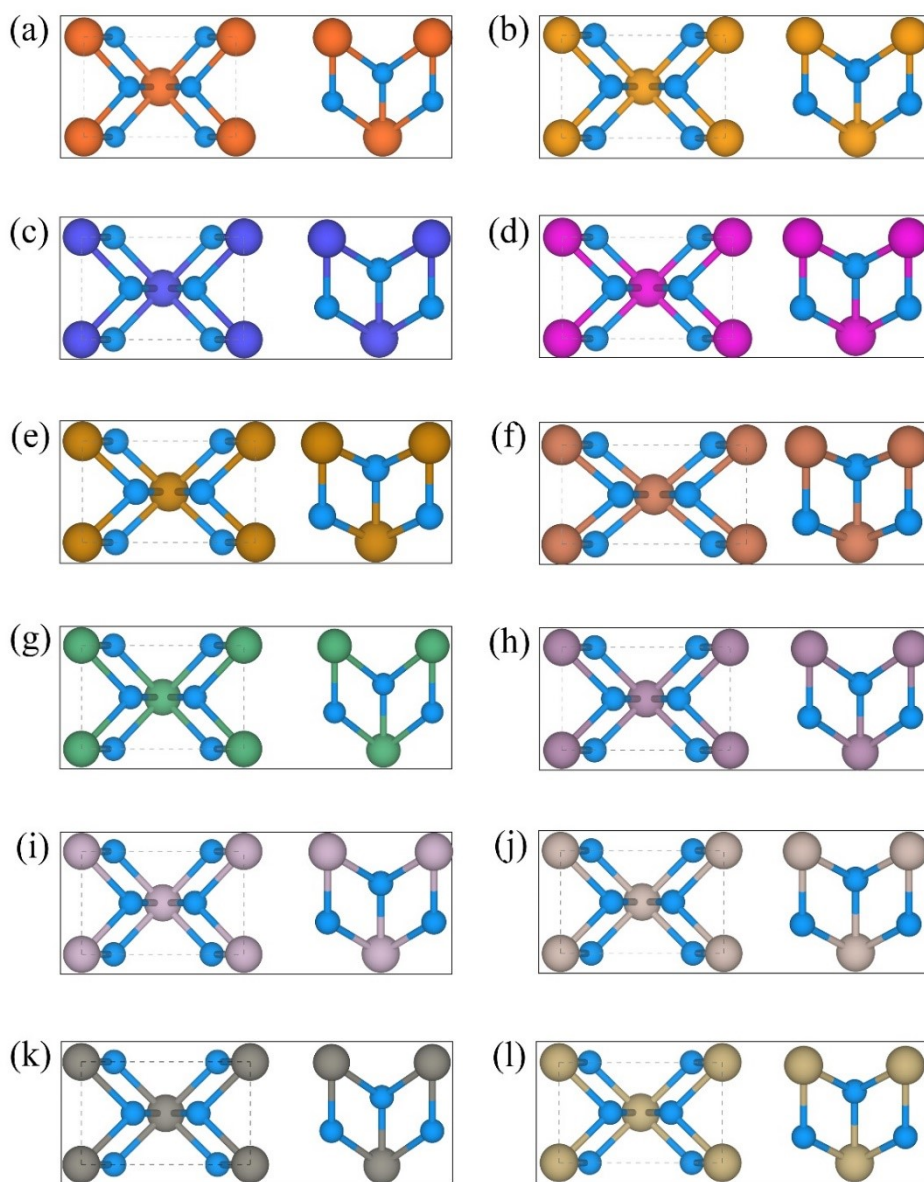
	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-280.50	0.16	0.23	-280.57
*N-NH	-283.61	0.48	0.12	-283.25
*NH-NH	-287.65	0.80	0.14	-286.99
*NH-NH <sub>2</sub>	-291.72	1.15	0.14	-290.71
*NH <sub>2</sub> -NH <sub>2</sub>	-296.25	1.31	0.24	-295.18
*NH <sub>2</sub> -NH <sub>3</sub>	-300.88	1.68	0.23	-299.43
*NH <sub>2</sub>	-279.89	0.66	0.12	-279.35
*NH <sub>3</sub>	-283.97	1.02	0.18	-283.13

**Table S14.** Total energy ( $E_{\text{tot}}$ ), zero-point energy ( $E_{\text{ZPE}}$ ) and entropy ( $TS$ ) of intermediates for NRR on OsB<sub>2</sub> along enzymatic pathway.

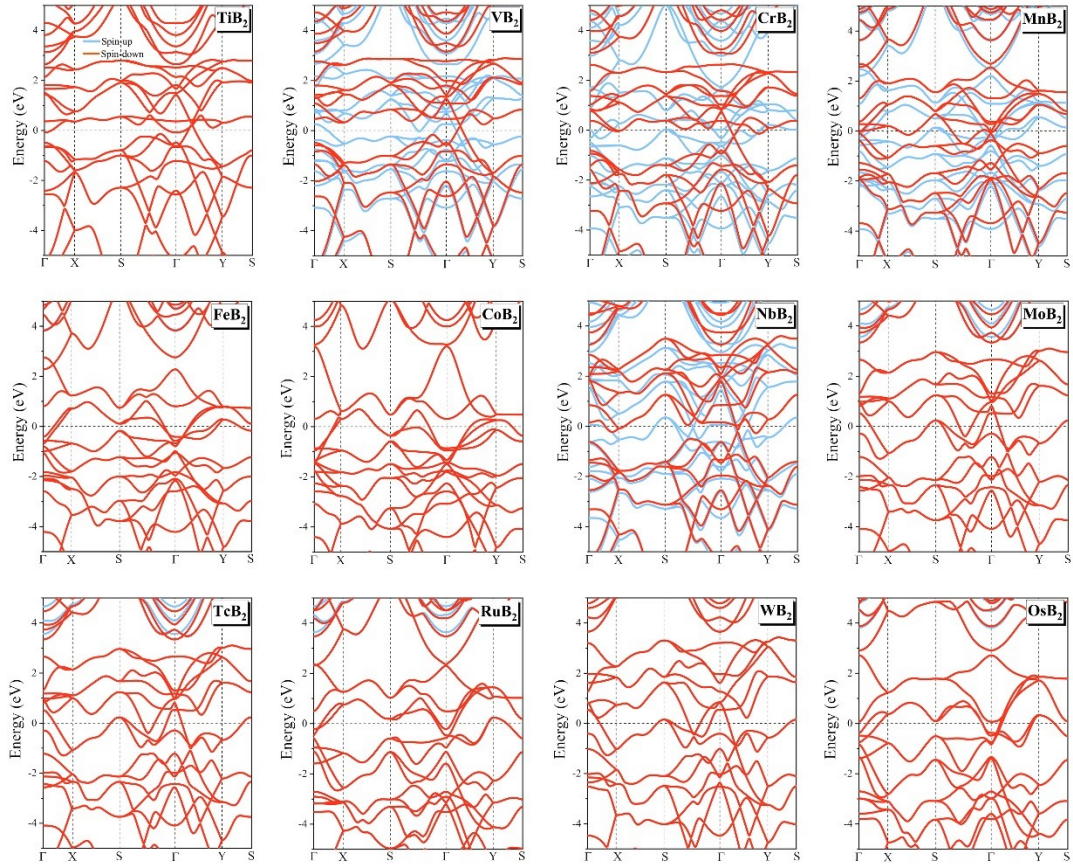
	$E_{\text{tot}}$	$E_{\text{ZPE}}$	$TS$	$G$
*N <sub>2</sub>	-307.27	0.17	0.16	-307.26
*N-NH	-310.92	0.49	0.11	-310.54
*NH-NH	-315.26	0.82	0.12	-314.56
*NH-NH <sub>2</sub>	-319.01	1.16	0.15	-318.00
*NH <sub>2</sub> -NH <sub>2</sub>	-324.17	1.38	0.18	-322.97
*NH <sub>2</sub> -NH <sub>3</sub>	-328.37	1.72	0.21	-326.86
*NH <sub>2</sub>	-307.10	0.71	0.09	-306.48
*NH <sub>3</sub>	-311.20	1.03	0.13	-310.30

**Table S15.** Gibbs free energy change of \*H at possible adsorption sites for 13 TMB<sub>2</sub>.

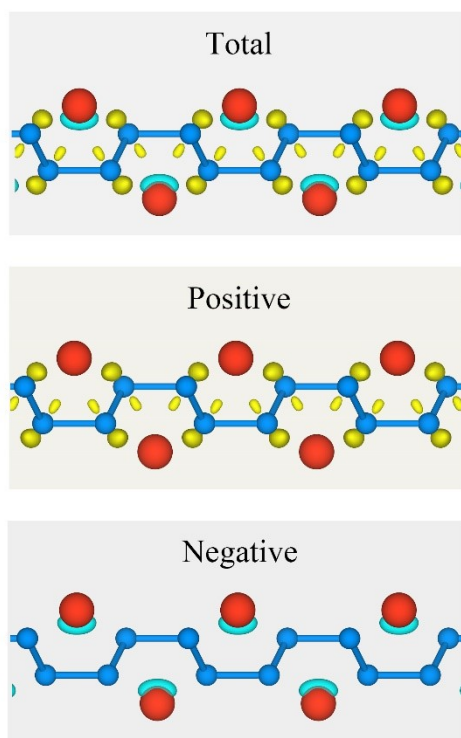
	$\Delta G_{*H} (S1)$	$\Delta G_{*H} (S2)$	$\Delta G_{*H} (S3)$	$\Delta G_{*H} (S4)$
TiB <sub>2</sub>	-0.23	0.27	/	/
VB <sub>2</sub>	-0.72	/	-0.15	/
CrB <sub>2</sub>	-0.60	-0.33	-0.26	/
MnB <sub>2</sub>	-0.16	-0.17	-0.24	0.17
FeB <sub>2</sub>	-0.09	-0.08	-0.07	/
CoB <sub>2</sub>	-0.08	-0.24	-0.23	/
NbB <sub>2</sub>	-1.03	-0.16	-0.21	/
MoB <sub>2</sub>	-0.83	-0.27	-0.07	/
TcB <sub>2</sub>	-0.39	0.09	-0.12	-0.16
RuB <sub>2</sub>	-0.71	-0.33	-0.51	-0.56
WB <sub>2</sub>	-0.99	/	-0.06	-0.06
ReB <sub>2</sub>	-0.63	/	-0.03	-0.62
OsB <sub>2</sub>	-0.33	/	0.05	-0.31



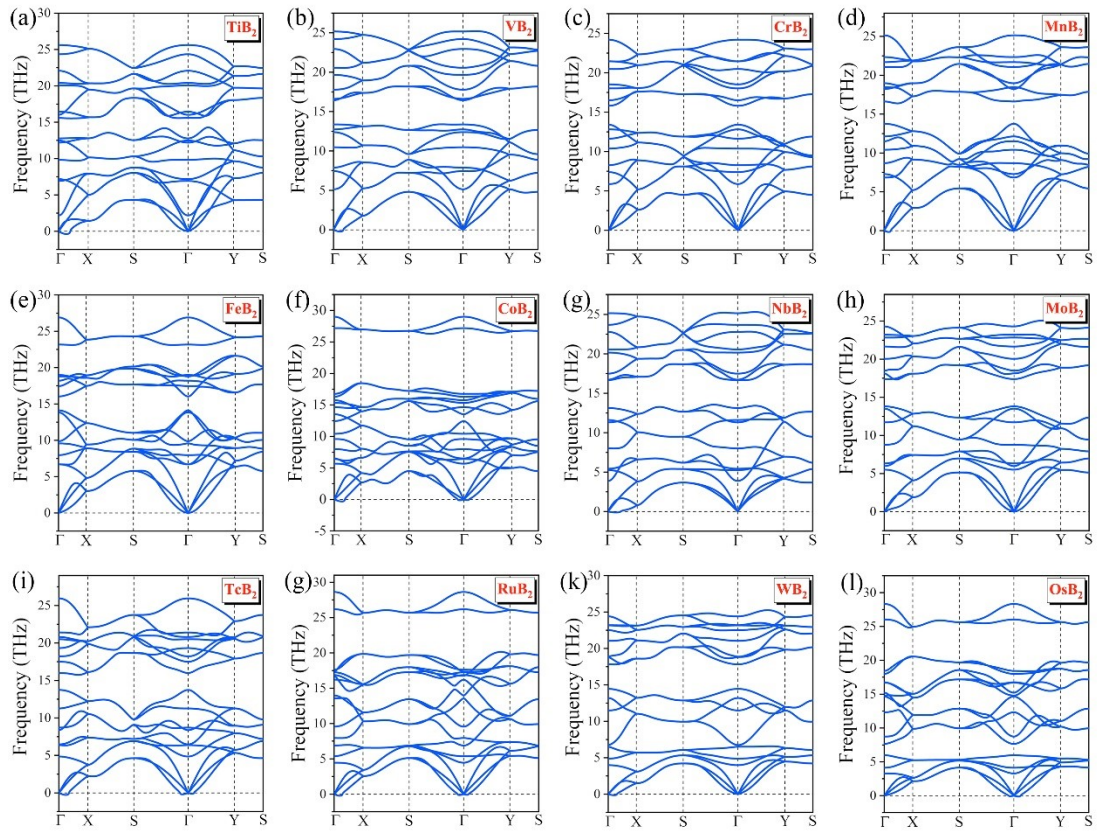
**Fig. S1** Structure of (a) TiB<sub>2</sub>, (b) VB<sub>2</sub>, (c) CrB<sub>2</sub>, (d) MnB<sub>2</sub>, (e) FeB<sub>2</sub>, (f) CoB<sub>2</sub>, (g) NbB<sub>2</sub>, (h) MoB<sub>2</sub>, (i) TcB<sub>2</sub>, (j) RuB<sub>2</sub>, (k) WB<sub>2</sub>, and (l) OsB<sub>2</sub>, with rectangle marking the unit cell.



**Fig. S2** Band structures of  $TMB_2$ . The Fermi level is set to zero.



**Fig. S3** Charge density difference with Re adsorption on borophene; yellow and cyan regions represent electron accumulation and depletion, respectively. The isosurface value is set to  $0.03 \text{ e}/\text{\AA}^3$ .



**Fig. S4** Phonon spectrum of (a)  $\text{TiB}_2$ , (b)  $\text{VB}_2$ , (c)  $\text{CrB}_2$ , (d)  $\text{MnB}_2$ , (e)  $\text{FeB}_2$ , (f)  $\text{CoB}_2$ , (g)  $\text{NbB}_2$ , (h)  $\text{MoB}_2$ , (i)  $\text{TcB}_2$ , (j)  $\text{RuB}_2$ , (k)  $\text{WB}_2$ , and (l)  $\text{OsB}_2$ .



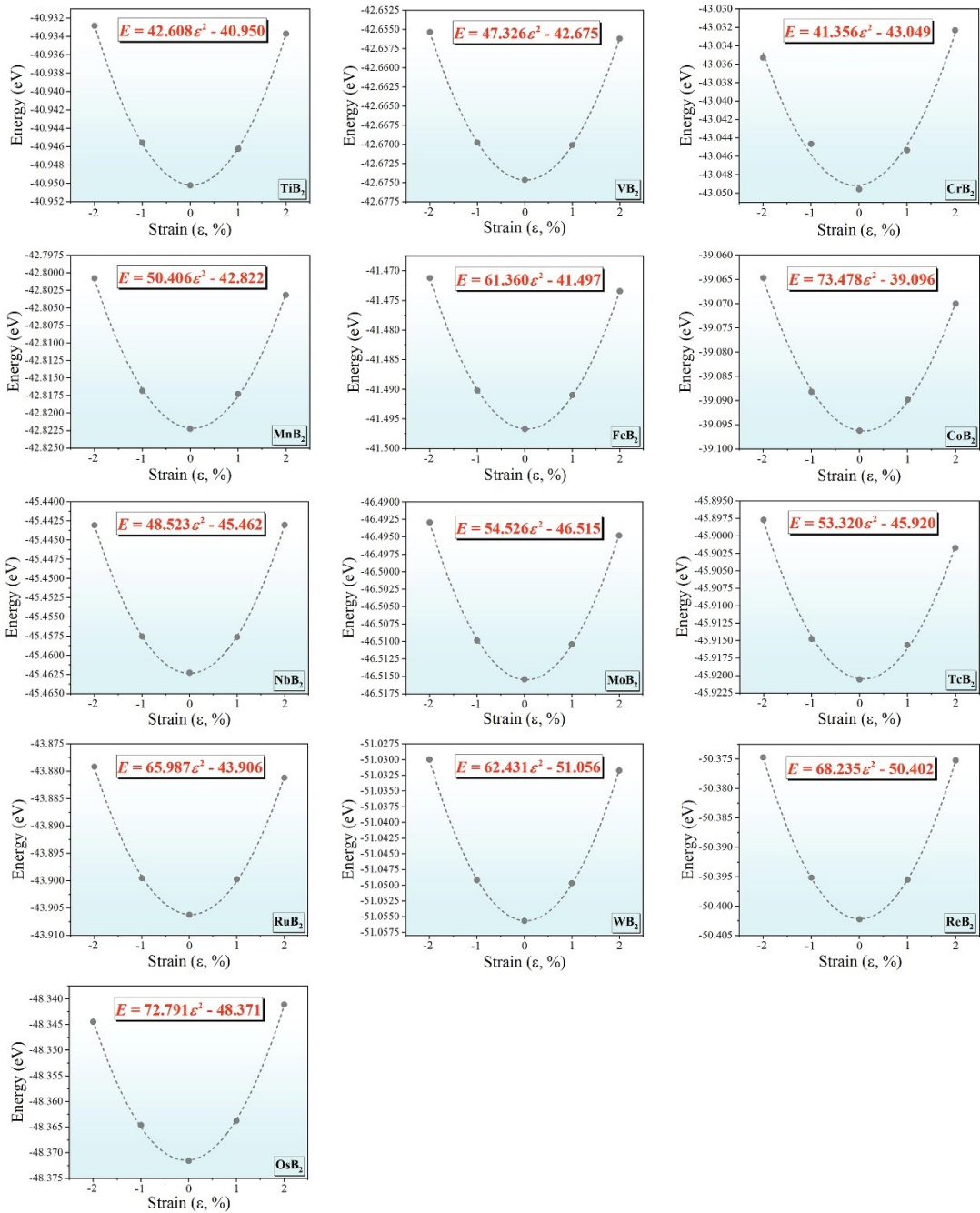
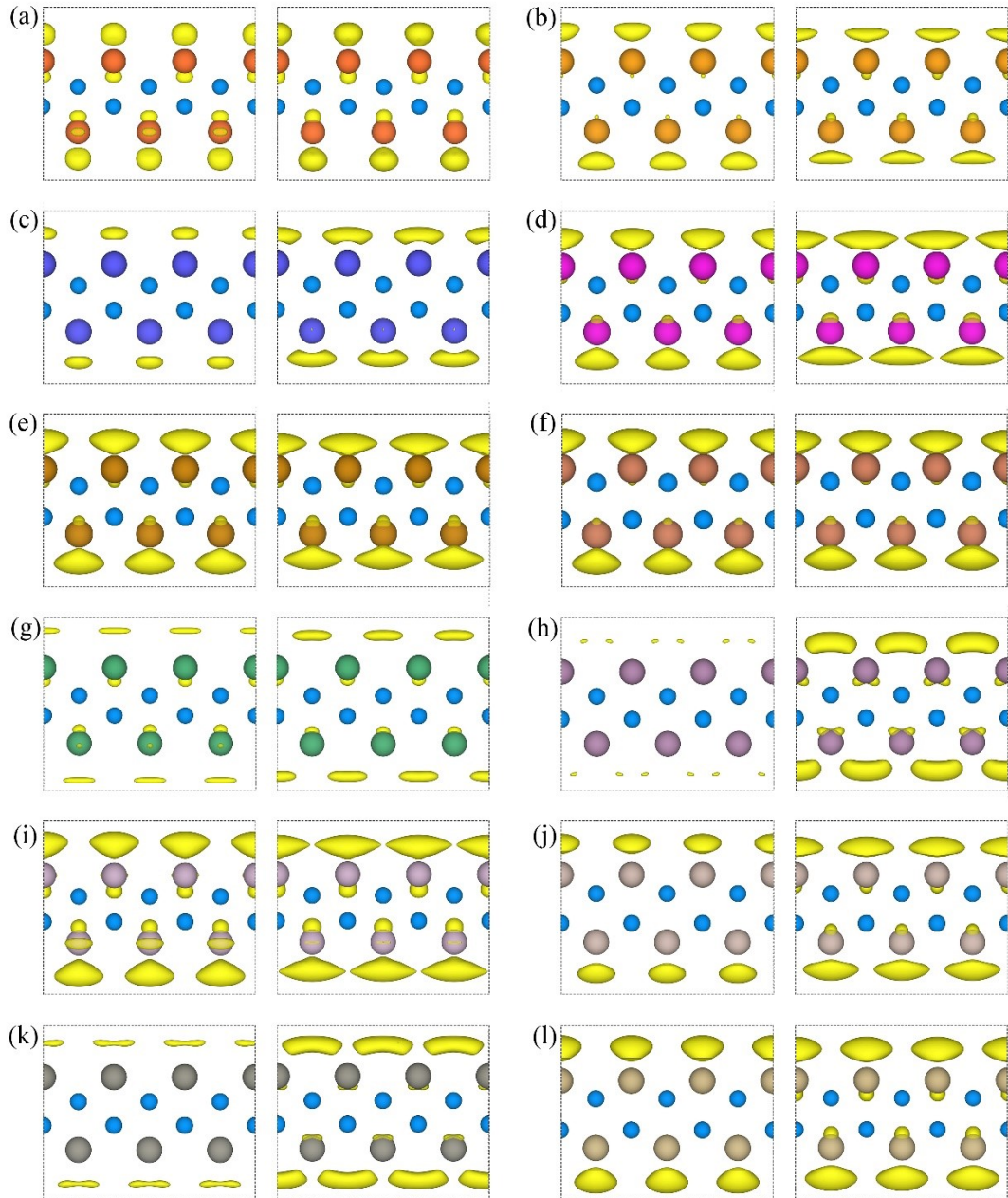
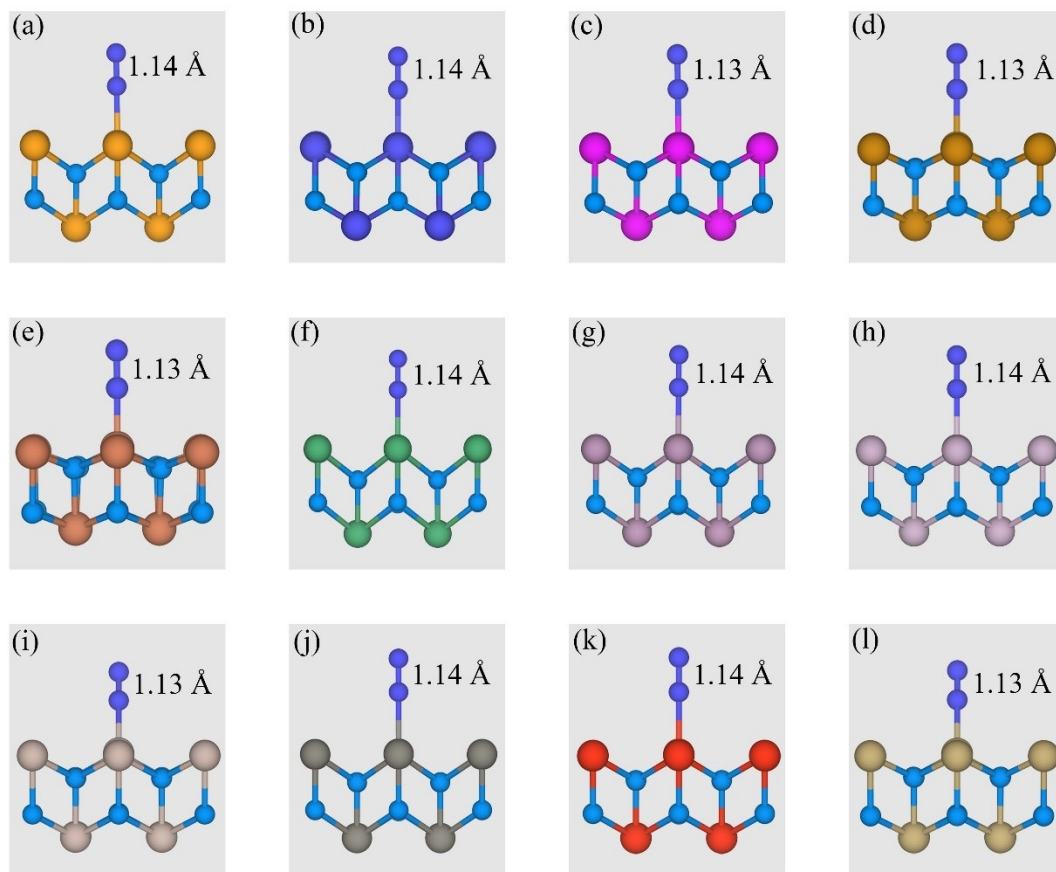


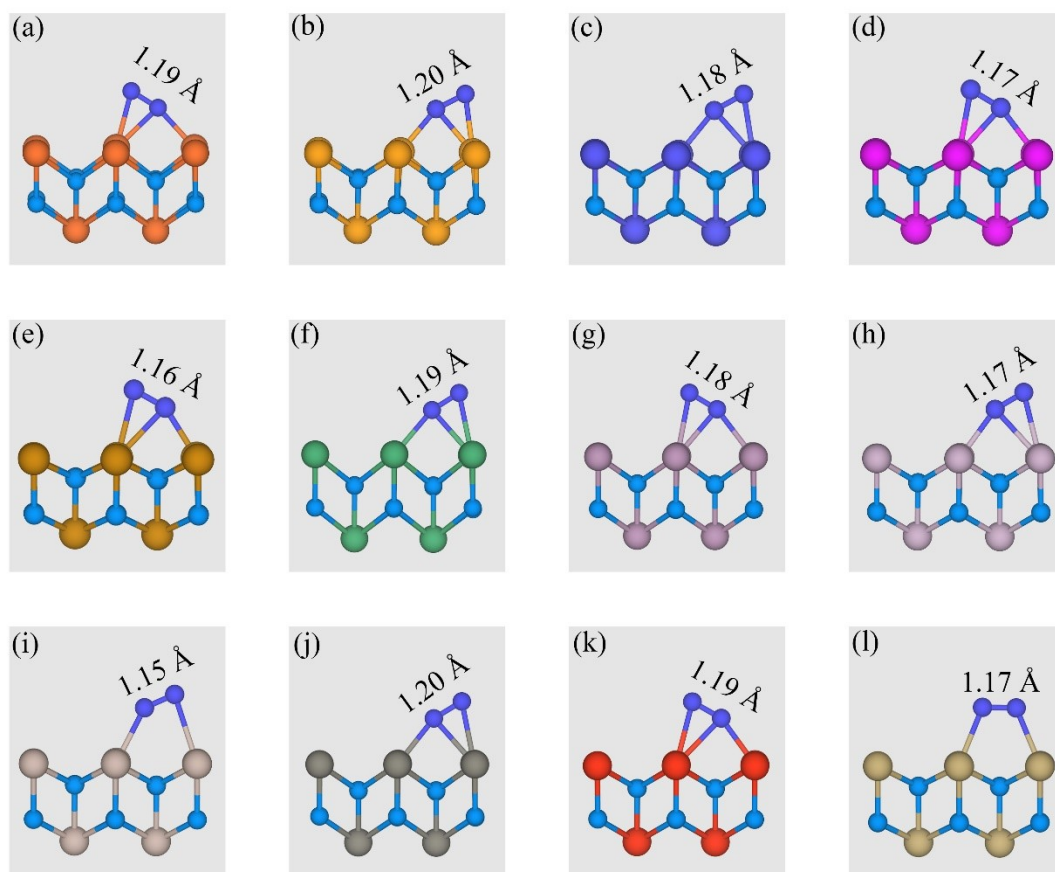
Fig. S5 Relationship between energy and strain along armchair directions.



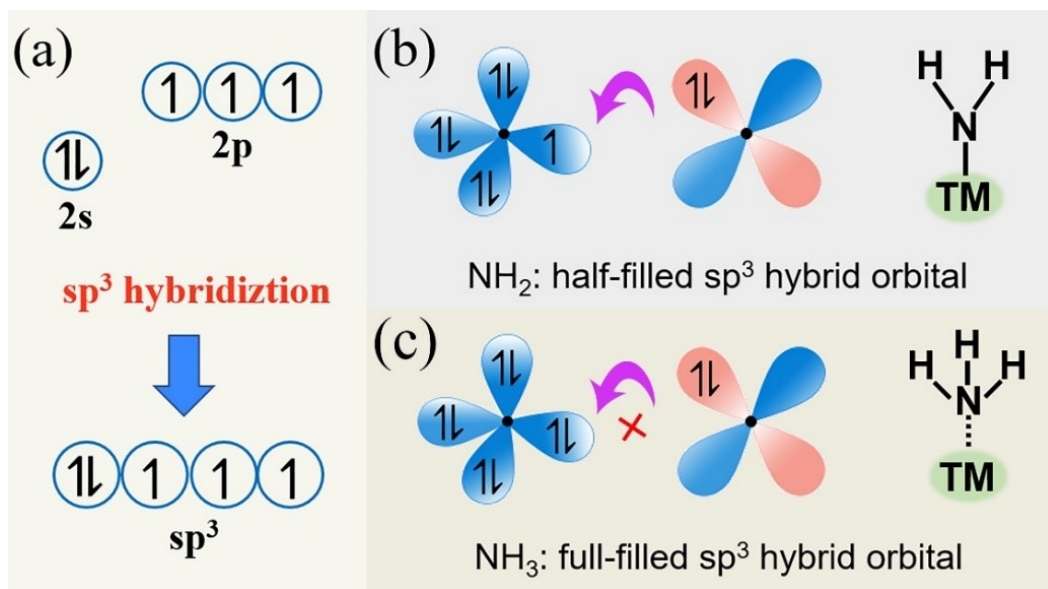
**Fig. S6** Fukui functions of  $F^+(r)$  (left) and  $F^-(r)$  (right) of (a)  $\text{TiB}_2$ , (b)  $\text{VB}_2$ , (c)  $\text{CrB}_2$ , (d)  $\text{MnB}_2$ , (e)  $\text{FeB}_2$ , (f)  $\text{CoB}_2$ , (g)  $\text{NbB}_2$ , (h)  $\text{MoB}_2$ , (i)  $\text{TcB}_2$ , (j)  $\text{RuB}_2$ , (k)  $\text{WB}_2$  and (l)  $\text{OsB}_2$ . The isosurface value is  $0.001 \text{ e}/\text{\AA}^3$ .



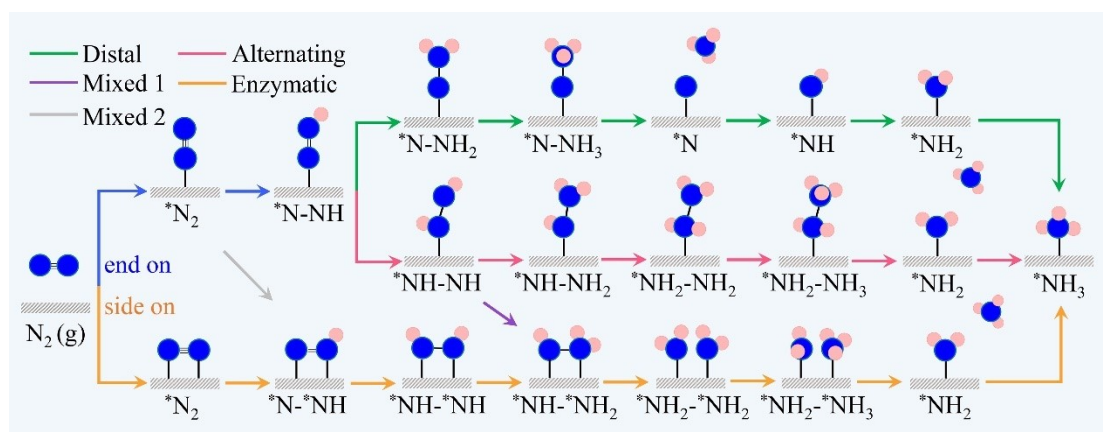
**Fig. S7** Structures of  $N_2$  end-on adsorption on (a)  $VB_2$ , (b)  $CrB_2$ , (c)  $MnB_2$ , (d)  $FeB_2$ , (e)  $CoB_2$ , (f)  $NbB_2$ , (g)  $MoB_2$ , (h)  $TcB_2$ , (i)  $RuB_2$ , (j)  $WB_2$ , (k)  $ReB_2$  and (l)  $OsB_2$ .



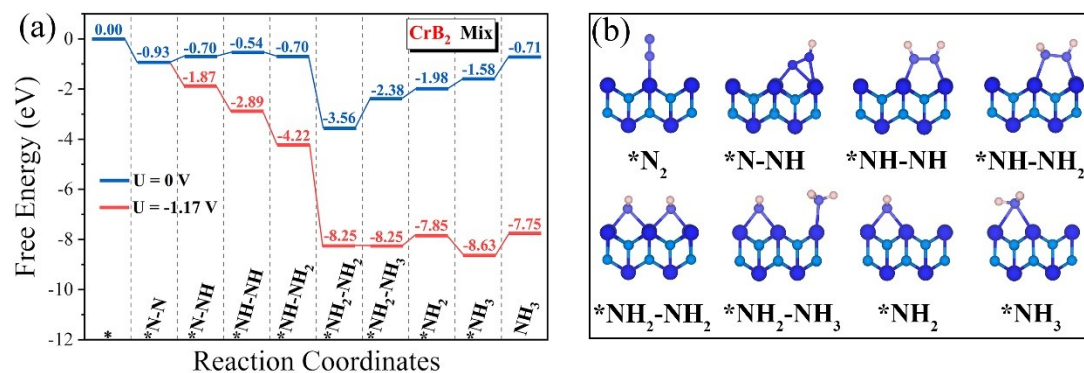
**Fig. S8** Structures of  $N_2$  side-on adsorption on (a)  $TiB_2$ , (b)  $VB_2$ , (c)  $CrB_2$ , (d)  $MnB_2$ , (e)  $FeB_2$ , (f)  $NbB_2$ , (g)  $MoB_2$ , (h)  $TcB_2$ , (i)  $RuB_2$ , (j)  $WB_2$ , (k)  $ReB_2$  and (l)  $OsB_2$ .



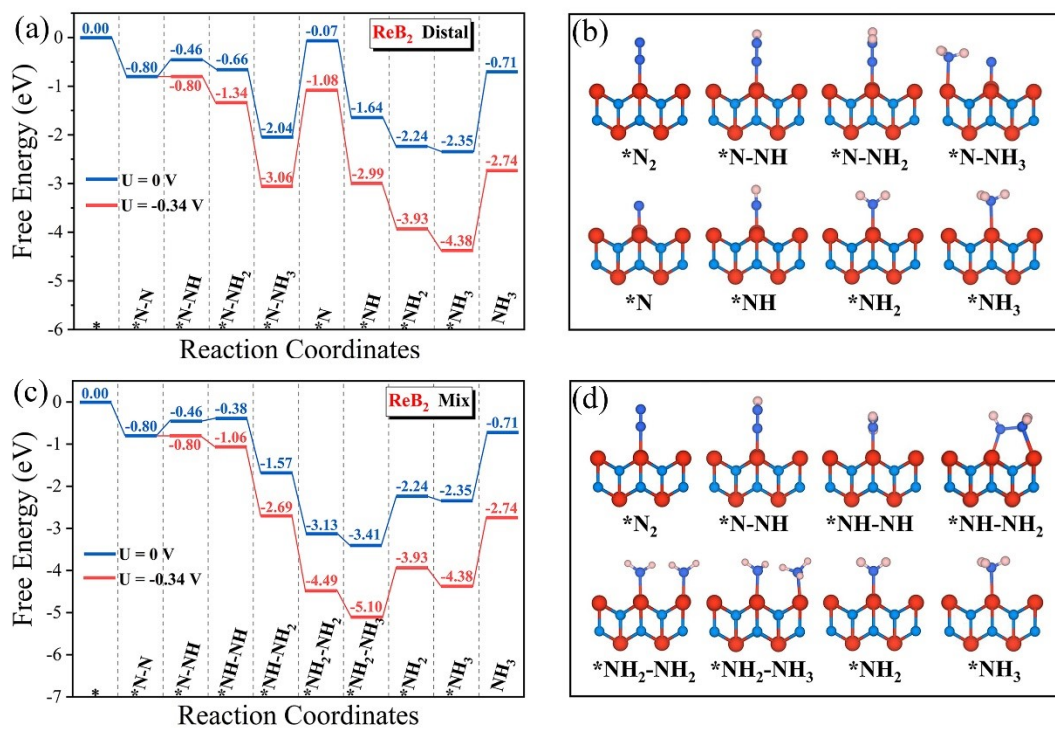
**Fig. S9** Electronic configuration of (a) N with  $sp^3$  hybridization, (b)  $^*NH_2$  and (c)  $^*NH_3$ .



**Fig. S10** Schematic of distal, alternating, enzymatic, and mixed mechanisms for  $N_2$  reduction to  $NH_3$ . Blue and pink spheres represent N and H atoms, respectively.

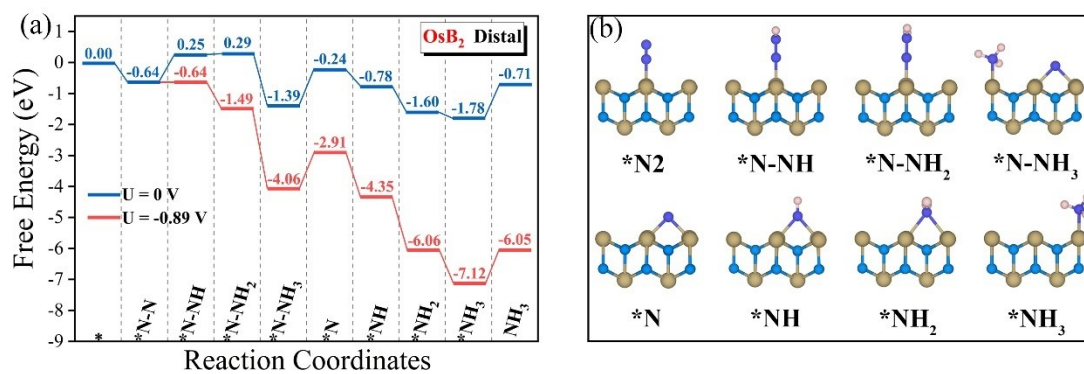


**Fig. S11** (a) Gibbs free energy diagram for the NRR on CrB<sub>2</sub> at zero (blue line) and applied potential (red line) through mix mechanism. (b) Corresponding adsorption configurations of reaction intermediates.

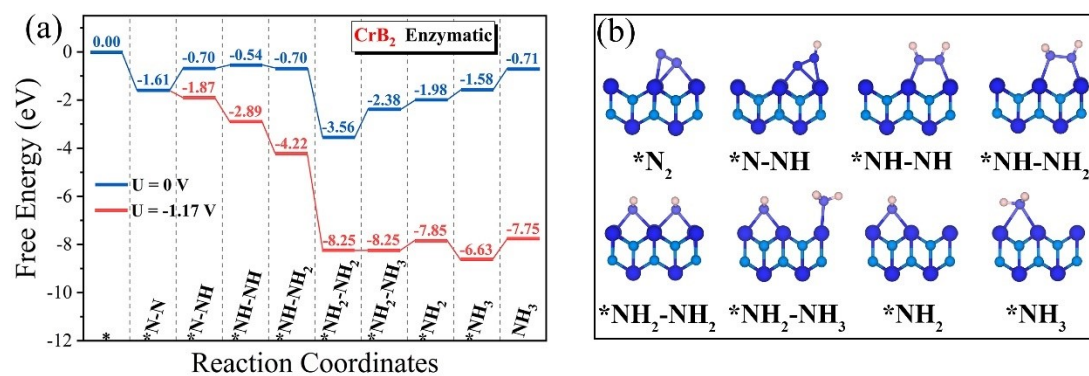


**Fig. S12** Gibbs free energy diagram for NRR on ReB<sub>2</sub> at zero (blue line) and applied potential (red line) along (a) distal and (c) mix mechanisms. The corresponding adsorption configurations are displayed in (b) and (d).

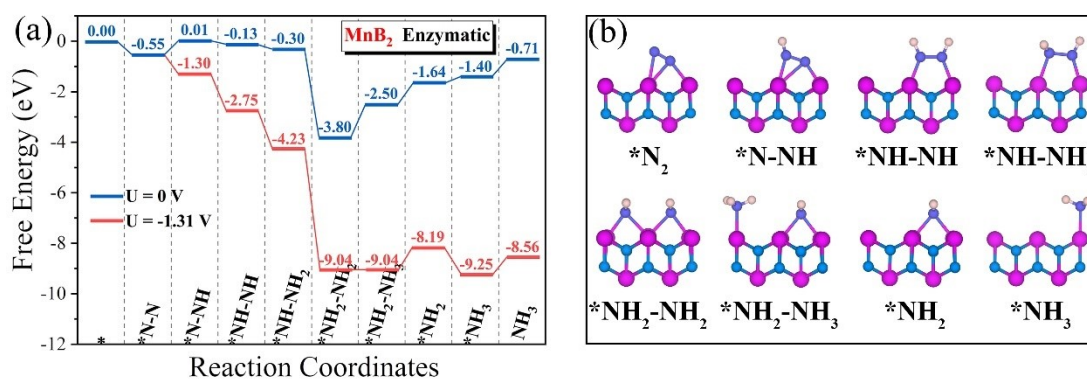




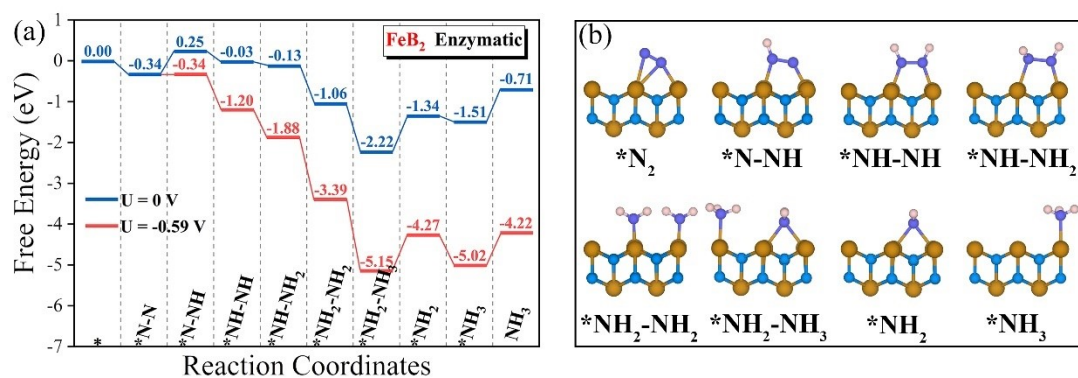
**Fig. S13** (a) Gibbs free energy diagram for NRR on OsB<sub>2</sub> at zero (blue line) and applied potential (red line) through distal mechanism. (b) Corresponding adsorption configurations of reaction intermediates.



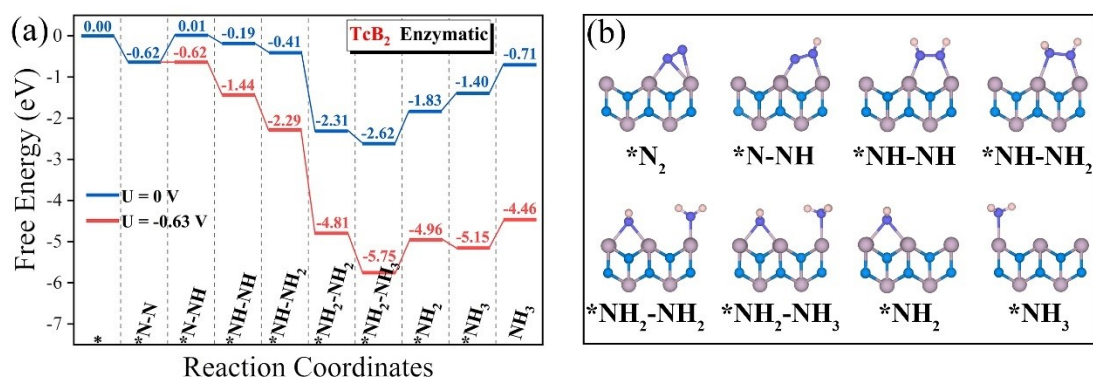
**Fig. S14** (a) Gibbs free energy diagram for NRR on CrB<sub>2</sub> at zero (blue line) and applied potential (red line) through enzymatic mechanism. (b) Corresponding adsorption configurations of reaction intermediates.



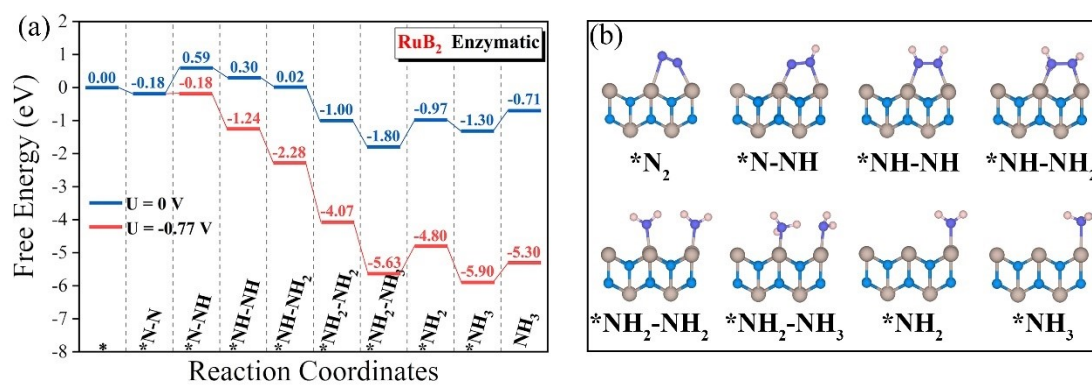
**Fig. S15** (a) Gibbs free energy diagram for NRR on MnB<sub>2</sub> at zero (blue line) and applied potential (red line) through enzymatic mechanism. (b) Corresponding adsorption configurations of reaction intermediates.



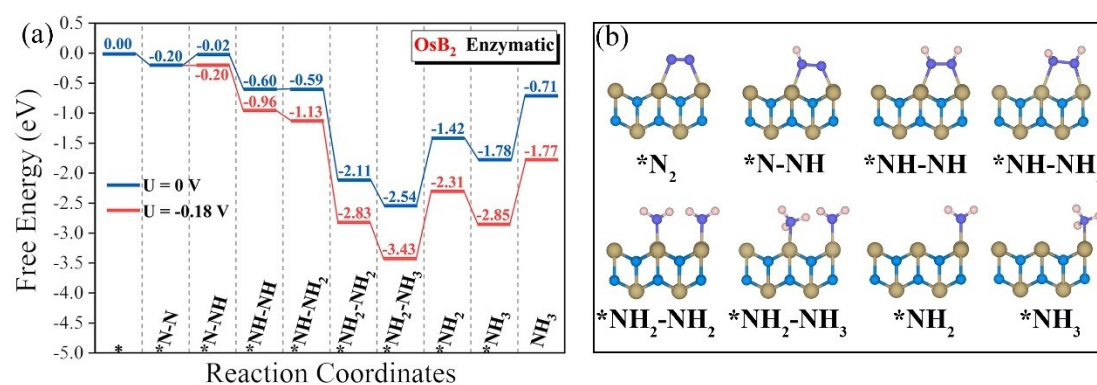
**Fig. S16** (a) Gibbs free energy diagram for NRR on FeB<sub>2</sub> at zero (blue line) and applied potential (red line) through enzymatic mechanism. (b) Corresponding adsorption configurations of reaction intermediates.



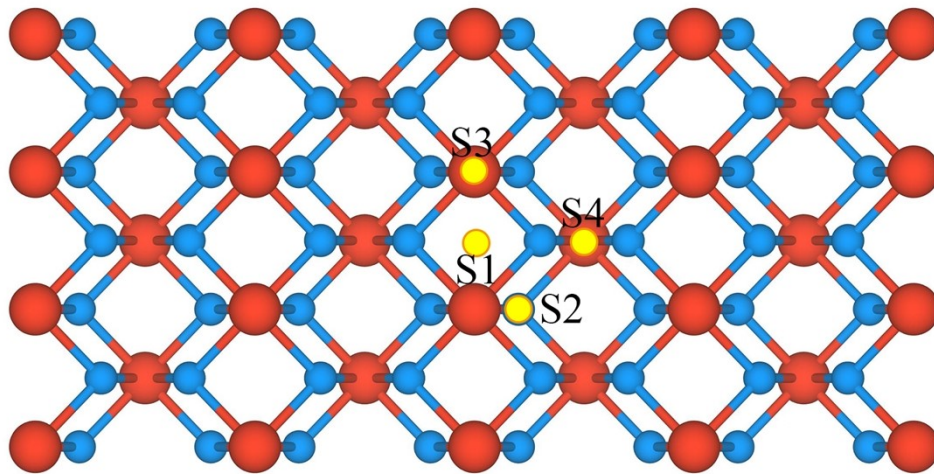
**Fig. S17** (a) Gibbs free energy diagram for NRR on TcB<sub>2</sub> at zero (blue line) and applied potential (red line) through enzymatic mechanism. (b) Corresponding adsorption configurations of reaction intermediates.



**Fig. S18** (a) Gibbs free energy diagram for NRR on RuB<sub>2</sub> at zero (blue line) and applied potential (red line) through enzymatic mechanism. (b) Corresponding adsorption configurations of reaction intermediates.

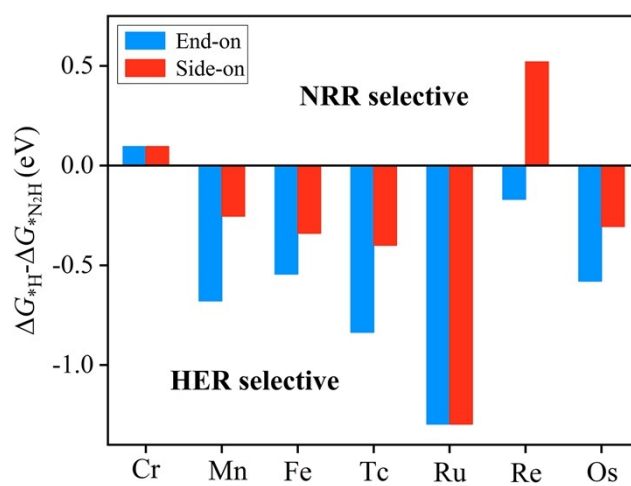


**Fig. S19** (a) Gibbs free energy diagram for NRR on OsB<sub>2</sub> at zero (blue line) and applied potential (red line) through enzymatic mechanism. (b) Corresponding adsorption configurations of reaction intermediates.

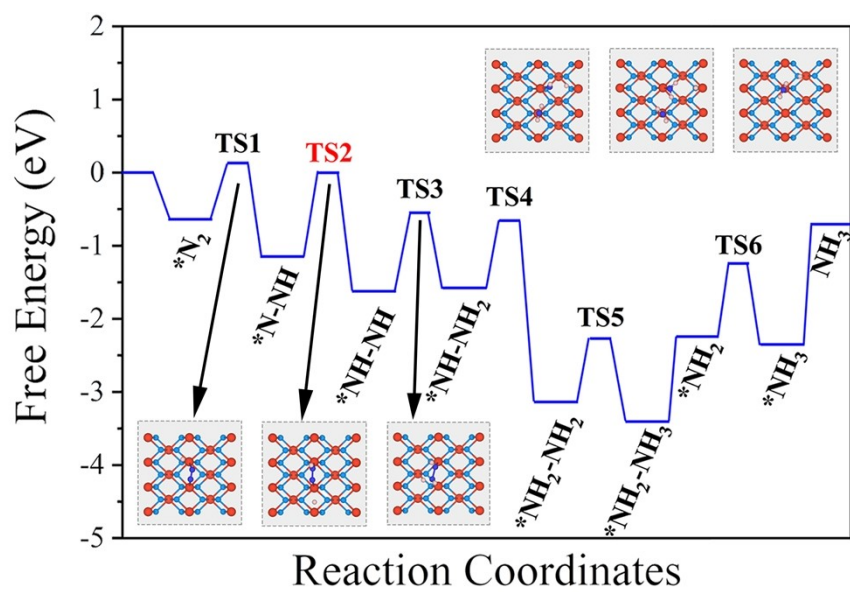


**Fig. S20** Possible active sites for hydrogen adsorption.

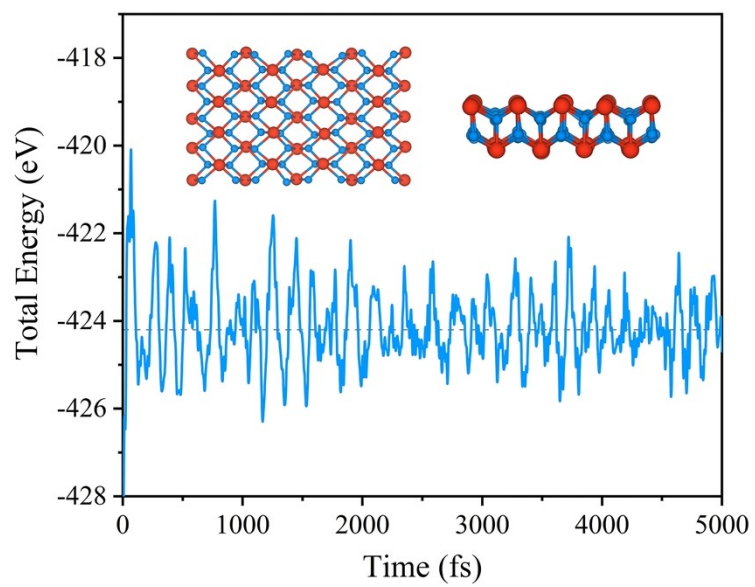




**Fig. S21** Gibbs free energy difference of  $*H$  and  $*N_2H$  ( $\Delta G_{*H} - \Delta G_{*N_2H}$ ) on  $TMB_2$  (TM = Cr, Mn, Fe, Tc, Ru, Re, Os).



**Fig. S22** Kinetic barriers for  $\text{N}_2$  conversion to  $\text{NH}_3$  on  $\text{ReB}_2$ , insets show the transition states. The H, B, N, and Re atoms are shown in pink, blue, cyan, and red colors, respectively.



**Fig. S23** AIMD simulations of ReB<sub>2</sub> at 700 K for 5 ps with a time step of 1 fs.

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