# **Supplemental Material**

## Spatial Correlation of Cell Stiffness and Traction Forces in Cancer Cells Measured with Combined SICM and TFM

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#### **Cell Morphology and Stiffness on Rigid Substrates**



**Supplementary Figure S-1 | Cell morphology and stiffness on rigid substrates. (a)** SICM topography image (left) and stiffness map (right) of a normal MCF10A and **(b)** of a cancerous MCF7 human breast epithelial cell on rigid cell culture dishes. On rigid substrates, the cells are more spread, but show a similar morphology compared to cells on elastic TFM substrates (see Figure 4).

#### Theoretical Modell and Effect of Finite Cell Thickness

The apparent cell stiffness  $E_{app}$  was measured as described previously.<sup>1</sup> Briefly, a constant pressure  $p_0$  was applied to the upper end of the capillary and *IZ*-curves were recorded. The sample stiffness in terms of the apparent Young's modulus  $E_{app}$  was then obtained from the slope *s* of the *IZ*-curve between 98 and 99% relative ion current as

$$E_{\rm app} = p_0 A \left(\frac{s_{\infty}}{s} - 1\right)^{-1},\tag{S1}$$

where  $s_{\infty}$  is the slope measured on the substrate and A = 0.26 is a pipette-dependent geometrical parameter.

As demonstrated for the cell shown in Figure 2b, flat extensions of the cells sometimes appear comparably stiff (also see, e.g., Supplementary Figure S-2a and b). The presence of large traction forces in the extensions might induce an artificial correlation between apparent stiffness and traction force density (Supplementary Figure S-2c,  $\rho = 0.12 \pm 0.02$ ). To avoid this possible artifact, the effect of the finite cell thickness was corrected by<sup>2</sup>

$$E = E_{\text{app}} \cdot \left\{ \exp\left(a\frac{r_{\text{i}}}{h}\right) + b\frac{r_{\text{i}}}{h} \left[1 - \exp\left(-c\frac{r_{\text{i}}}{h}\right)\right] \right\}^{-1}$$
(S2)

with cell thickness h (here equivalent to the cell height  $z_0$ ) and pipette inner opening radius  $r_i$  and using a = 1.462, b = 3.30, and c = 0.66, assuming a Poisson's ratio v = 0.499 and the cell sticking to an infinitely stiff underlying substrate. The corrected cell stiffness (Supplementary Figure S-2d) is generally lower than the apparent cell stiffness (Supplementary Figure S-2b), for example by a factor of 1.7 for a thickness of 1  $\mu$ m, but still shows a similar subcellular distribution with a soft cell body and stiffer extensions. The correlation between cell stiffness and traction force density is even stronger for the corrected cell stiffness (Supplementary Figure S-1e,  $\rho = 0.29 \pm 0.02$ ). Both the apparent and the corrected cell stiffness (median stiffness here 4.9 kPa and 1.6 kPa, respectively) are significantly softer than the substrate ( $E \cong 15$  kPa), indicating that the assumption of an infinitely stiff underlying substrate was valid.



**Supplementary Figure S-2 | Effect of cell thickness on measured cell stiffness. (a)** SICM topography image, **(b)** map of apparent stiffness, and **(c)** apparent local cell stiffness as a function of local traction force density for the cell shown in Figure 2b and 3a. **(d)** Map of corrected stiffness calculated using Equation (S2) (with  $r_i = 300 \text{ nm}$ ) and **(e)** corrected local cell stiffness as a function of local traction force density. The red lines are fits of Equation (1). The scatter plot grayscale level indicates point density.

### References

- 1. J. Rheinlaender and T. E. Schäffer, *Soft Matter*, 2013, **9**, 3230-3236.
- 2. J. Rheinlaender and T. E. Schäffer, *Appl. Phys. Lett.*, 2020, **117**, 113701.