

## SUPPLEMENTARY INFORMATION

### “ZIF-95 as a Filler for Enhanced Gas Separation Performance of Polysulfone Membrane”

Sanaullah Shafiq <sup>a</sup>, Bassem A. Al-Maythalony <sup>b,c</sup>, Muhammad Usman <sup>d</sup>, Mohammad Saleh Ba-Shammakh <sup>a</sup>, Abdallah A. Al-Shammari <sup>a,\*</sup>

<sup>a</sup> Chemical Engineering Department, King Fahad University of Petroleum and Minerals, Dhahran 31261, Saudi Arabia.

<sup>b</sup> King Abdulaziz City for Science and Technology—Technology Innovation Centre on Carbon Capture and Sequestration (KACST-TIC on CCS) at King Fahd University of Petroleum and Minerals, Dhahran 31261, Saudi Arabia.

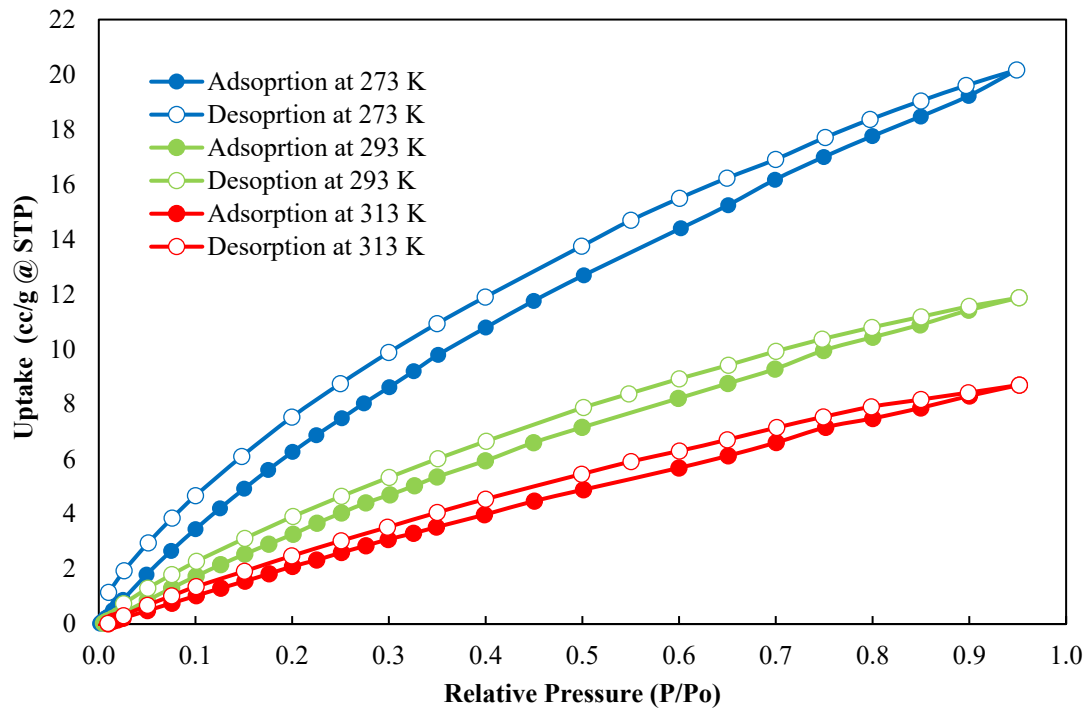
<sup>c</sup> Material Discovery Unit-Research and Development, Royal Scientific Society (RSS), Amman 11941, Jordan.

<sup>d</sup> Center of Research Excellence in Nanotechnology, King Fahd University of Petroleum and Minerals, Dhahran 31261, Saudi Arabia.

\*Correspondence should be addressed at: [alshammari@kfupm.edu.sa](mailto:alshammari@kfupm.edu.sa)

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**S1. CO<sub>2</sub> Adsorption Isotherm of ZIF-95:**



**Fig. S1.** Adsorption and desorption isotherms of CO<sub>2</sub> at 273 K (blue), 293 K (green), and 313 K (red) for synthesized ZIF-95.

**Clausius-Clapeyron equation:**

$$Q_{st} = -R \frac{\partial \ln p}{\partial \left(\frac{1}{T}\right)} \dots \dots \dots (eq. S1)$$

Where,  $Q_{st}$  is the isosteric heat of adsorption in kJ/mol,  $R$  is the general gas constant (kJ/mol.K),  $p$  is the relative pressure, and  $T$  is the temperature (Kelvin).

**S2. Activation Procedure:**

Acetone was used to solvent exchange the DMF from ZIF-95 crystals. As-synthesized sample was immersed in acetone for 5 days during which acetone was refreshed 2 to 3 times in a day. Afterward, the crystals of ZIF-95 were partially dried overnight in the fume hood. The degassing of the partially dried sample was done using a vacuum degassing option on Autosorb iQ equipment. The sample was first heated to 50 °C for 10 hours and then to 110 °C for 12 hours under vacuum.

**S3. Permeability calculations:**

$$P_i = \frac{Flux_i \cdot L}{\Delta p} \dots \dots \dots (eq. S2)$$

Where,  $P_i$  is the permeability of gas “ $i$ ” in “Barrer”,  $L$  is the thickness of membrane in “ $cm$ ”,  $\Delta p$  is the pressure difference across the membrane in “ $cmHg$ ”, and  $F_i$  is the flux of gas “ $i$ ”. The flux of gas “ $i$ ” was calculated using the following equation:

$$F_i = 10^{10} \left( \frac{dp_d^{SS}}{dt} - \frac{dp_d^{LR}}{dt} \right) \cdot V_d \cdot ART \dots \dots \dots (eq.S3)$$

where,

$A$  = Area of membrane ( $cm^2$ )

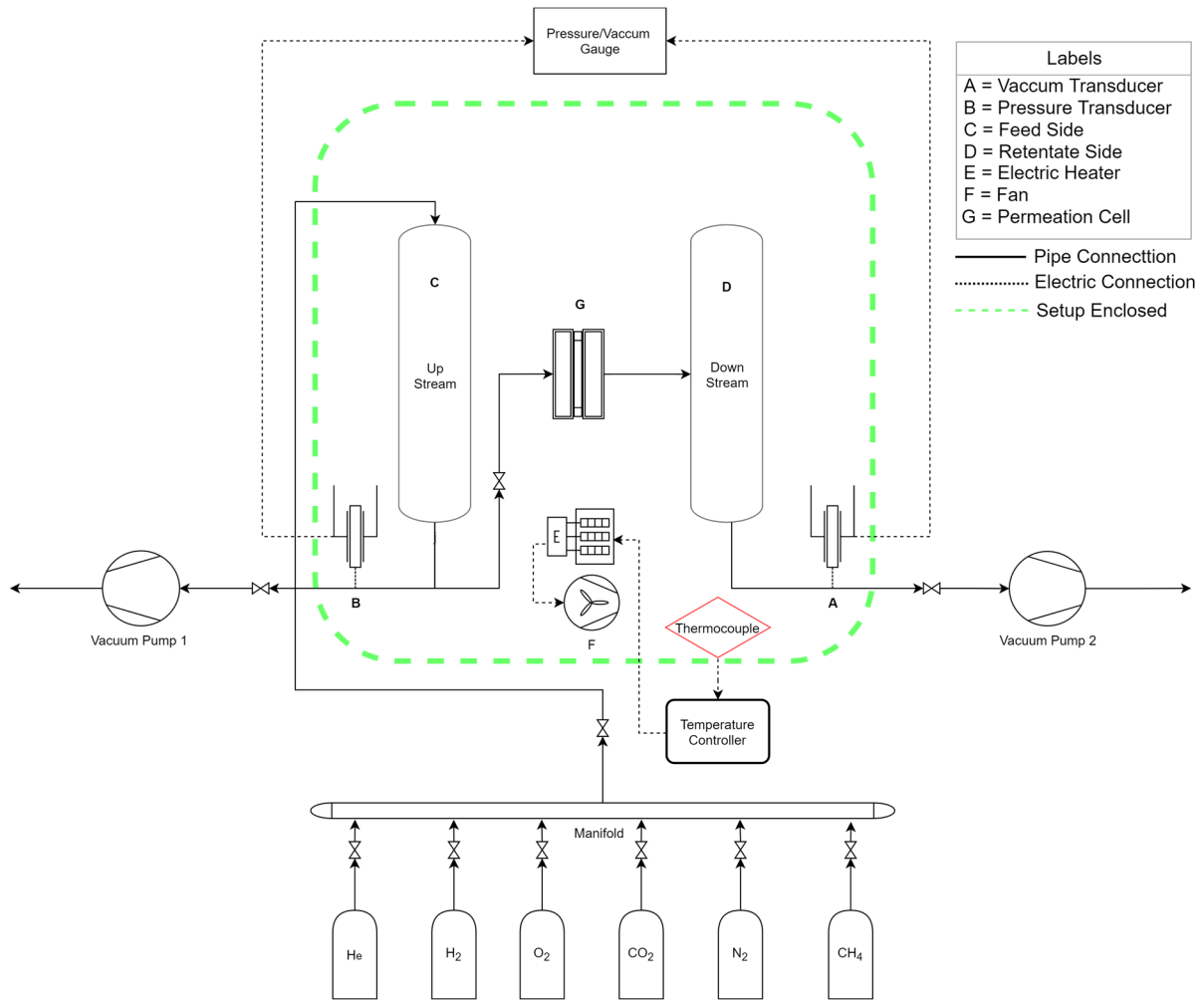
$V_d$  = Volume of down stream ( $cm^3$ )

$R$  = General gas constant [  $0.278 \text{ cm}^3 \text{ cmHg}/(\text{cm}^3(\text{STP})K$  ]

$T$  = Temperature (Kelvin)

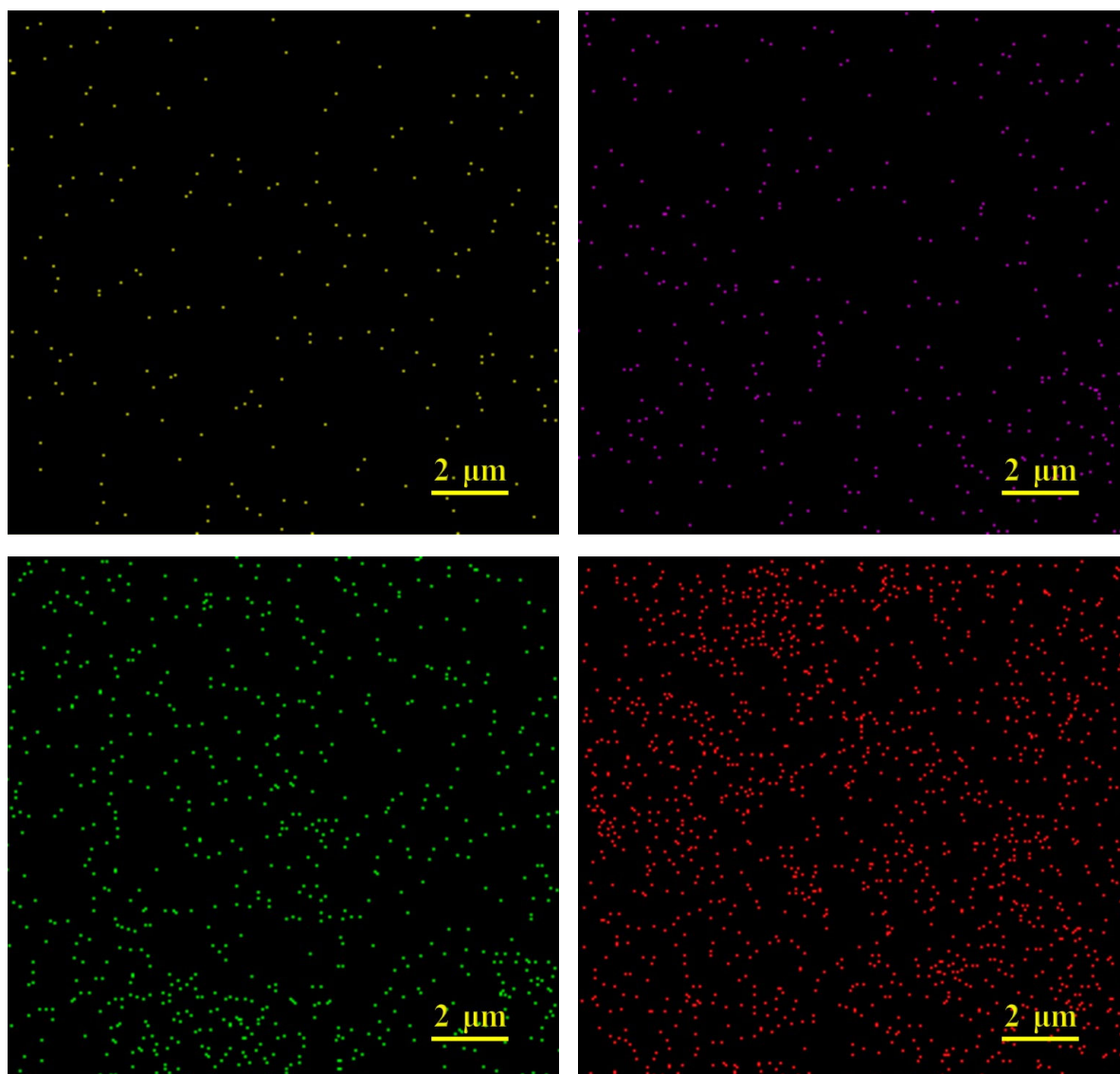
$\frac{dp_d^{SS}}{dt}$  = Pressure rise in down stream at steady state ( $cmHg/s$ )

$\frac{dp_d^{LR}}{dt}$  = Leak rate on the down stream ( $cmHg/s$ )



**Fig. S2.** The schematic diagram of permeation setup.

#### S4. EDS Mapping of Cross-Section:



**Fig. S3.** EDS mapping (Zinc) of PSF-ZIF-95-8% loaded membrane (yellow), PSF-ZIF-95-16% loaded membrane (purple), PSF-ZIF-95-24% loaded membrane (green), and PSF-ZIF-95-32% loaded membrane (red).

### S5. DSC Data of Membranes:

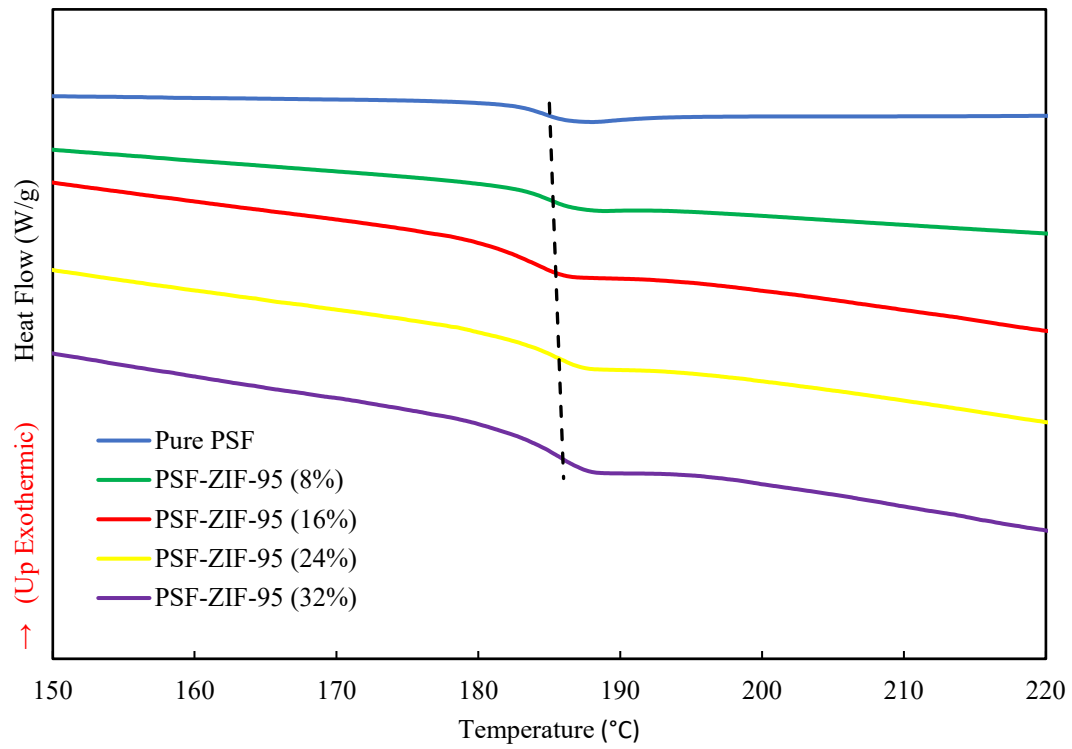


Fig. S4. DSC thermograms of pure and loaded mixed matrix membranes

## S6. Permeabilities & Selectivity:

**Note: In all the tables, permeabilities and permeances are provided Barrer and GPU units, respectively.**

**Table S1.** Permeability of synthesized membranes.

MEMBRANE	Permeability (Barrer)					
	Helium	Hydrogen	Oxygen	Carbon dioxide	Nitrogen	Methane
Polysulfone Pure	9.34	9.60	0.91	4.88	0.160	0.160
Polysufone-ZIF-95 (8%)	10.2	11.28	1.03	5.50	0.160	0.160
Polysufone-ZIF-95 (16%)	12.04	13.14	1.23	6.47	0.195	0.186
Polysufone-ZIF-95 (24%)	15.21	17.30	1.62	8.16	0.256	0.250
Polysufone-ZIF-95 (32%)	17.68	21.14	2.19	11.11	0.399	0.390

**Table S2.** Selectivity of synthesized membranes.

MEMBRANE	Ideal Selectivity												
	He/H <sub>2</sub>	He/O <sub>2</sub>	He/CO <sub>2</sub>	He/N <sub>2</sub>	He/CH <sub>4</sub>	H <sub>2</sub> /O <sub>2</sub>	H <sub>2</sub> /CO <sub>2</sub>	H <sub>2</sub> /N <sub>2</sub>	H <sub>2</sub> /CH <sub>4</sub>	CO <sub>2</sub> /N <sub>2</sub>	CO <sub>2</sub> /CH <sub>4</sub>	O <sub>2</sub> /N <sub>2</sub>	N <sub>2</sub> /CH <sub>4</sub>
Polysulfone Pure (0 %)	0.972	10.263	1.913	58.375	58.375	10.549	1.967	60.000	60.000	30.500	30.500	5.687	1.000
Polysufone-ZIF-95 (8 %)	0.904	9.902	1.854	63.750	63.750	10.951	2.050	70.500	70.500	34.375	34.375	6.437	1.000
Polysufone-ZIF-95 (16 %)	0.916	9.788	1.860	61.743	64.731	10.682	2.030	67.384	70.645	33.179	34.784	6.307	1.048
Polysufone-ZIF-95 (24 %)	0.879	9.388	1.864	59.414	60.840	10.679	2.120	67.578	69.200	31.875	32.640	6.328	1.024
Polysufone-ZIF-95 (32 %)	0.836	8.073	1.5632	44.310	45.333	9.652	1.902	52.982	54.205	27.844	28.487	5.488	1.023

## S7. Diffusivity and Solubility

**Table S3.** Diffusivity coefficients (cm<sup>2</sup>/s) of Pure and loaded mixed matrix membranes.

Membrane	D_He	D_H <sub>2</sub>	D_O <sub>2</sub>	D_CO <sub>2</sub>	D_N <sub>2</sub>	D_CH <sub>4</sub>
Pure PSF	1.08×10 <sup>-7</sup>	5.6×10 <sup>-8</sup>	1.53×10 <sup>-8</sup>	6.61×10 <sup>-9</sup>	2.39×10 <sup>-9</sup>	1.98×10 <sup>-9</sup>
PSF-ZIF-95-8%	1.46×10 <sup>-7</sup>	1.09×10 <sup>-8</sup>	1.80×10 <sup>-8</sup>	7.78×10 <sup>-9</sup>	2.89×10 <sup>-9</sup>	1.95×10 <sup>-9</sup>
PSF-ZIF-95-16%	2.05×10 <sup>-7</sup>	2.29×10 <sup>-7</sup>	2.25×10 <sup>-8</sup>	1.13×10 <sup>-8</sup>	4.43×10 <sup>-9</sup>	2.07×10 <sup>-9</sup>
PSF-ZIF-95-24%	3.17×10 <sup>-7</sup>	3.70×10 <sup>-7</sup>	2.93×10 <sup>-8</sup>	1.41×10 <sup>-8</sup>	6.27×10 <sup>-9</sup>	2.41×10 <sup>-9</sup>
PSF-ZIF-95-32%	4.01×10 <sup>-7</sup>	5.77×10 <sup>-7</sup>	3.94×10 <sup>-8</sup>	2.15×10 <sup>-8</sup>	9.8×10 <sup>-9</sup>	3.10×10 <sup>-9</sup>

MEMBRANE Table S3 (continued)	Diffusivity Selectivity												
	He/H <sub>2</sub>	He/O <sub>2</sub>	He/CO <sub>2</sub>	He/N <sub>2</sub>	He/CH <sub>4</sub>	H <sub>2</sub> /O <sub>2</sub>	H <sub>2</sub> /CO <sub>2</sub>	H <sub>2</sub> /N <sub>2</sub>	H <sub>2</sub> /CH <sub>4</sub>	CO <sub>2</sub> /N <sub>2</sub>	CO <sub>2</sub> /CH <sub>4</sub>	O <sub>2</sub> /N <sub>2</sub>	N <sub>2</sub> /CH <sub>4</sub>
Polysulfone Pure (0 %)	1.926	7.051	16.320	45.038	54.486	3.660	8.472	23.378	28.283	2.760	3.339	6.387	1.210
Polysulfone-ZIF-95 (8 %)	1.338	8.114	18.763	50.614	74.900	6.063	14.021	37.821	55.968	2.698	3.992	6.238	1.480
Polysulfone-ZIF-95 (16 %)	0.892	9.107	18.202	46.244	98.934	10.204	20.395	51.815	110.853	2.541	5.435	5.078	2.139
Polysulfone-ZIF-95 (24 %)	0.857	10.823	22.427	50.615	131.748	12.622	26.155	59.027	153.646	2.257	5.874	4.676	2.603
Polysulfone-ZIF-95 (32 %)	0.695	10.163	18.673	40.839	129.311	14.620	26.862	58.750	186.022	2.187	6.925	4.018	3.166

**Table S4.** Solubility coefficients [Unit = cm<sup>3</sup> (gas) cm<sup>-3</sup> (ZIF) cmHg ] of bare and loaded mixed matrix membrane.

Membrane	S_He	S_H <sub>2</sub>	S_O <sub>2</sub>	S_CO <sub>2</sub>	S_N <sub>2</sub>	S_CH <sub>4</sub>
Pure PSF	8.67×10 <sup>7</sup>	1.74 ×10 <sup>8</sup>	5.73×10 <sup>7</sup>	7.36×10 <sup>8</sup>	7.18×10 <sup>7</sup>	8.43×10 <sup>7</sup>
PSF-ZIF-95-8%	7.05×10 <sup>7</sup>	1.03×10 <sup>8</sup>	5.87×10 <sup>7</sup>	7.10×10 <sup>8</sup>	6.32 ×10 <sup>7</sup>	8.67 ×10 <sup>7</sup>
PSF-ZIF-95-16%	5.85×10 <sup>7</sup>	5.63×10 <sup>7</sup>	5.32×10 <sup>7</sup>	5.59×10 <sup>8</sup>	5.56×10 <sup>7</sup>	9.38×10 <sup>7</sup>
PSF-ZIF-95-24%	4.79×10 <sup>7</sup>	4.67×10 <sup>7</sup>	5.60×10 <sup>7</sup>	5.75×10 <sup>8</sup>	4.46×10 <sup>7</sup>	1.08×10 <sup>8</sup>
PSF-ZIF-95-32%	4.44×10 <sup>7</sup>	3.64×10 <sup>7</sup>	5.36×10 <sup>7</sup>	5.14×10 <sup>8</sup>	4.04×10 <sup>7</sup>	1.10×10 <sup>8</sup>

MEMBRANE Table S4(Continued)	Solubility Selectivity												
	He/H <sub>2</sub>	He/O <sub>2</sub>	He/CO <sub>2</sub>	He/N <sub>2</sub>	He/CH <sub>4</sub>	H <sub>2</sub> /O <sub>2</sub>	H <sub>2</sub> /CO <sub>2</sub>	H <sub>2</sub> /N <sub>2</sub>	H <sub>2</sub> /CH <sub>4</sub>	CO <sub>2</sub> /N <sub>2</sub>	CO <sub>2</sub> /CH <sub>4</sub>	O <sub>2</sub> /N <sub>2</sub>	N <sub>2</sub> /CH <sub>4</sub>
Polysulfone Pure (0 %)	0.498	1.513	0.117	1.207	1.028	3.036	0.236	2.422	2.064	10.249	8.732	0.797	0.852
Polysulfone-ZIF-95 (8 %)	0.681	1.201	0.099	1.115	0.813	1.762	0.145	1.635	1.193	11.222	8.184	0.928	0.729
Polysulfone-ZIF-95 (16 %)	1.038	1.098	0.104	1.052	0.623	1.057	0.100	1.013	0.600	10.061	5.959	0.957	0.592
Polysulfone-ZIF-95 (24 %)	1.025	0.856	0.083	1.074	0.443	0.834	0.081	1.047	0.432	12.907	5.322	1.255	0.412
Polysulfone-ZIF-95 (32 %)	1.220	0.829	0.086	1.099	0.400	0.679	0.070	0.901	0.327	12.727	4.631	1.325	0.363



**S8. Literature of Mixed Matrix Membranes** (Reporting permeabilities except where permanence is mentioned)

**Table S5.** Literature review of MMMs reported for He, H<sub>2</sub>, O<sub>2</sub>, CO<sub>2</sub>, N<sub>2</sub>, and CH<sub>4</sub> gases separation.

MEMBRANE	YEAR	Temperature	Helium	Hydrogen	Oxygen	Carbon dioxide	Nitrogen	Methane	Ref
PSF	2006	35 C (4 Bar)	8.02		0.89	4.46	0.18	0.17	<sup>1</sup>
PSF/MCM-48 (20%)			32.1		4.14	18.21	0.77	0.77	
Matrimid 5218	2011	35 C (3 Bar)	8.75		1.29	4.3	0.22	0.21	<sup>2</sup>
Matrimid/TiO <sub>2</sub> (20 %)			19		2.45	10.54	0.92	0.77	
Matrimid 5218	2012	22 C (4 Bar)		32.68	2.62	8.07	0.36	0.23	<sup>3</sup>
Matrimid/ZIF-8 (20%)				63.53	5.63	16.63	0.88	0.46	
PEI	2014	25 C (6 Bar)		10.07		1.68	0.1	0.09	<sup>4</sup>
PEI/MOF-5 (25%)				28.32		5.39	0.19	0.23	
PIM-1	2016	25 C (5 Bar)	1170	2710	875	4770	219	286	<sup>5</sup>
PIM-1/UiO-66-NH <sub>2</sub> (16.6 %)			1340	3130	1090	6340	303	425	
PIM-1	2016	25 C (2 Bar)		32.68	2.62	8.07	0.36	0.23	<sup>6</sup>
PIM/Mg-MOF-74 (20 %)				63.53	5.63	16.63	0.88	0.46	
PEI	2017	35 C (2 Bar)		856	119.9	82.5	21.8	18.9	<sup>7</sup>
PEI/nZIF-7-PSM (5%)				2020	272.9	245.9	182.6	107.9	
Akram PI spongy	2019	35 C (2 Bar)		128.7 (Permeance)	16.8 (Permeance)	69.1 (Permeance)	4.3 (Permeance)	4.1 (Permeance)	<sup>8</sup>
Akram PI/ZIF-302 (5%)				156.4 (Permeance)	14.1 (Permeance)	62 (Permeance)	2.5 (Permeance)	3.7 (Permeance)	

Table S5 Continued	Ideal Selectivity												
Membrane	He/H <sub>2</sub>	He/O <sub>2</sub>	He/CO <sub>2</sub>	He/N <sub>2</sub>	He/CH <sub>4</sub>	H <sub>2</sub> /O <sub>2</sub>	H <sub>2</sub> /CO <sub>2</sub>	H <sub>2</sub> /N <sub>2</sub>	H <sub>2</sub> /CH <sub>4</sub>	CO <sub>2</sub> /N <sub>2</sub>	CO <sub>2</sub> /CH <sub>4</sub>	O <sub>2</sub> /N <sub>2</sub>	N <sub>2</sub> /CH <sub>4</sub>
PSF		8.183	1.798	44.555	47.176					24.777	26.235	5.444	1.058
PSF/MCM-48 (20%)		7.753	1.762	41.688	41.688					23.649	23.649	5.376	1.000
Matrimid 5218		6.782	2.034	39.772	41.666					19.545	20.476	5.863	1.047
Matrimid/TiO <sub>2</sub> (20 %)		7.755	1.802	20.652	24.675					11.456	13.688	2.663	1.194
Matrimid 5218						12.473	4.049	90.777	142.087	22.416	35.087	7.277	1.565
Matrimid/ZIF-8 (20%)						11.284	3.820	72.193	138.108	18.897	36.152	6.397	1.913
PEI							5.994	100.700	111.888	16.800	18.666		1.111
PEI/MOF-5 (25%)							5.254	149.052	123.130	28.368	23.434		0.826
PIM-1	0.431	1.337	0.245	5.342	4.090	3.097	0.568	12.374	9.475	21.780	16.678	3.995	0.765
PIM-1/UiO-66-NH <sub>2</sub> (16.6 %)	0.428	1.229	0.211	4.422	3.152	2.871	0.493	10.330	7.364	20.924	14.917	3.597	0.712
PIM-1						3.299	0.537	10.076	6.598	18.73	12.268	3.054	0.654
PIM/Mg-MOF-74 (20 %)						5.095	0.539	15.456	10.295	28.664	19.092	3.033	0.666
PEI						7.139	10.375	39.266	45.291	3.784	4.365	5.500	1.153
PEI/nZIF-7-PSM (5%)						7.405	8.218	11.067	18.729	1.346	2.279	1.494	1.692
PI						7.660	1.862	29.930	31.390	16.069	16.853	3.907	1.048
PI/ZIF-302 (5%)						11.092	2.522	62.560	42.270	24.800	16.756	5.640	0.675

**Table S6.** Literature review of MMMs reported for O<sub>2</sub>, CO<sub>2</sub>, N<sub>2</sub>, and CH<sub>4</sub> gases separation.

MEMBRANE	YEAR	Temperature	Oxygen	Carbon dioxide	Nitrogen	Methane	CO <sub>2</sub> /N <sub>2</sub>	CO <sub>2</sub> /CH <sub>4</sub>	O <sub>2</sub> /N <sub>2</sub>	N <sub>2</sub> /CH <sub>4</sub>	Ref.
PSF	1996	35 C (10 Bar)	1.29	5.5	0.22	0.24	25.000	22.916	5.863	0.916	<sup>9</sup>
PSF-HN <sub>2</sub> -16%			0.69	2.7	0.11	0.11	24.545	24.545	6.272	1.000	
PSF	2001	35 C (3 Bar)	1.5	7.53	0.257	0.389	29.299	19.357	5.836	0.660	<sup>10</sup>
PSF/MCM-41 (30%)			3.83	20.5	0.753	1.05	27.224	19.523	5.086	0.717	
PSF	2011	25 C (4 Bar)	2.75	16	0.47	0.45	34.042	35.555	5.851	1.044	<sup>11</sup>
PSF/MCM41-APTMS-Modified (20 %)			4.04	23	0.52	0.52	44.230	44.230	7.769	1.000	
PSF	2011	35 C (3.5Bar)	1.107	2	0.402	0.484	4.975	4.125	2.753	0.829	<sup>12</sup>
PI			0.727	1.595	0.2403	0.361	6.641	4.413	3.027	0.664	
PSF-PI/ZSM-5 (20%)			0.876	1.528	0.2943	0.349	5.194	4.379	2.978	0.843	
PSF	2012	30 C (3 Bar)	1.47		0.25				5.88		<sup>13</sup>
PSF/MIL-101(Cr) (8%)			2.53		0.47				5.383		
PSF/MIL-101(Fe) (8%)			2.03		0.35				5.80		
PSF	2016	35 C (3 Bar)		5.6	0.19	0.21					<sup>14</sup>
PSF/NH <sub>2</sub> -UiO-66 (50%)				43	1.65	1.8					
PSF	2017	35 C (3 Bar)		5.6 (Permeance)	0.91 (Permeance)	1.73 (Permeance)	6.153	3.237			<sup>15</sup>
PSF/SAPO-34-IL6 (5%)				7.24 (Permeance)	0.38 (Permeance)	0.36 (Permeance)	19.052	20.111			

<b>Table S6 Continued</b>	<b>Year</b>	<b>Temperature</b>	<b>Oxygen</b>	<b>Carbon</b>	<b>Nitrogen</b>	<b>Methane</b>	<b>CO<sub>2</sub>/N<sub>2</sub></b>	<b>CO<sub>2</sub>/CH<sub>4</sub></b>	<b>O<sub>2</sub>/N<sub>2</sub></b>	<b>N<sub>2</sub>/CH<sub>4</sub></b>	<b>Ref.</b>
<b>PSF</b>	2011	35 C (2.75 Bar)	1.6		0.28				5.7143		<sup>16</sup>
<b>PSF/ZIF-8 (16%)</b>			2.6		0.31				8.3871		
<b>PES/MWCNT(Purified) (1%)</b>	2011	27 C (3 Bar)	2.319	7.742	0.91	0.396	8.507	19.550	2.5484	2.2980	<sup>17</sup>
<b>PES/MWCNT (Aptes Modified 1%)</b>			3.178	2.794	0.511	0.09	5.467	31.044	6.2192	5.6778	
<b>PSF</b>	2019	25 C (10 Bar)		6.18	0.21	0.22	29.428	28.090		0.9545	<sup>18</sup>
<b>PSF/Bio-MOF-1 (30%)</b>				16.57	0.36	0.39	46.027	42.487		0.9231	
<b>PI</b>	2018	25 C (1 Bar)	27.8	125.4	5.49	3.12	22.841	40.192	5.0638	1.7596	<sup>19</sup>
<b>PI/ZIF-L (20%)</b>			30.9	19.4	6.29	4.23	3.084	4.586	4.9126	1.4870	
<b>Matrimid 5218</b>	2015	35 C (10 Bar)		4.44	0.131	0.126	33.893	35.238		1.0397	<sup>20</sup>
<b>Matrimid /MIL-101(Cr) (10 %)</b>				6.95	0.12	0.12	57.916	57.916		1.0000	
<b>6FDA-DAM</b>	2018	24 C (4 Bar)		770	32.08		24.00				<sup>21</sup>
<b>6FDA-DAM/ ZIF-94 (40%)</b>				2310	105		22.00				
<b>PEBAX</b>	2017	0 C (1 Bar)		53.7	1.79	3.00	30.00	17.900		0.5967	<sup>22</sup>
<b>PEBAX/ ZIF-8 (15%) IL-(80%)</b>				231.4	8.57	19.6	27.001	11.806		0.4372	
<b>Matrimid-PBI (3:1)</b>	2021	22 C (10 Bar)	1.6	8.0	0.24		33.00				<sup>23</sup>
<b>Matrimid-PBI (3:1)/ZIF-95X (20%)</b>			0.78	3.1	0.16		19.38				

**Table S7.** Literature review of MMMs reported for CO<sub>2</sub>, N<sub>2</sub>, and CH<sub>4</sub> gases separation.

MEMBRANE	YEAR	Temperature	Carbon dioxide	Nitrogen	Methane	CO <sub>2</sub> /N <sub>2</sub>	CO <sub>2</sub> /CH <sub>4</sub>	N <sub>2</sub> /CH <sub>4</sub>	Ref.
PSF	2011	35 C (2.75 Bar)	5.95	0.24		24.791			16
PSF/Silicate-1-HKUST-(16%)			8.9	0.22		40.454			
PSF	2011	35 C (2.75 Bar)	4.6		0.19		24.210		16
PSF/Silicate-1-HKUST-(16%)			8.9		0.39		22.820		
PSF	2016	35 C (2 Bar)	4.7		0.21		22.38		24
PSF/ MIL-101(Cr)-ZIF-8 (16%)			14.2		0.35		40.57		
PSF	2016	25 C (2 Bar)	6.32	0.24		26.333			25
PSF/ZIF-301 (30%)			17.12	0.62		27.612			
PSF	2016	25 C (2 Bar)	6.32	0.24		26.333			26
PSF/GO-ZIF-301 (1%) (30%)			25	0.4		62.500			
PSF	2016	25 C (2 Bar)	6.32	0.24		26.333			27
PSFZIF-302-CNT-(12%) (8%)			18	0.514		35.019			
PSF	2016	25 C (2 Bar)	6.32	0.24		26.333			28
PSF/ZIF-302-GO (30%) (1%)			13.21	0.26		50.807			
PSF	2020	25 C (3 Bar)	10.75		0.354		30.367		29
PSF/ ZIF-11 (24%)			22.14		0.519		42.659		

**Table S8.** Literature review of MMMs reported for H<sub>2</sub>, CO<sub>2</sub>, N<sub>2</sub>, and CH<sub>4</sub> gases separation.

MEMBRANE	YEA R	Temperature	Hydrogen	Carbon dioxide	Methane	H <sub>2</sub> /CO <sub>2</sub>	H <sub>2</sub> /CH <sub>4</sub>	Ref.
PSF-acrylate	2010	25 C (12 Bar)	12.7 (Permeance)	8.19 (Permeance)		1.550		<sup>30</sup>
PSF/ APTMS- Zeolite-3A (30%)			14.78 (Permeance)	5.53 (Permeance)		2.672		
PSF	2011	35C (2.75 Bar)	11		0.19		57.89	<sup>16</sup>
PSF/ ZIF-8-(16%)			39.8		0.34		117.05	
PSF	2013	35 C (3 Bar)	8.2	3	0.27	2.733	30.37	<sup>31</sup>
PSF/SiO <sub>2</sub> -silanol modified (25%)			25	10.2	1.126	2.451	22.05	
PMP	2014	30 C (2 Bar)	11.14	98.74		0.112		<sup>32</sup>
PMP/ MIL-53(Al) (30%)			13.11	217.65		0.060		
PBI	2015	35 C (10 Bar)	3.62	0.4		9.05		<sup>33</sup>
PBI/[Cu <sub>2</sub> (ndc) <sub>2</sub> (d abco)] <sub>n</sub> (20%)			6.14	0.39		15.743		
PBI	2016	150 C (5 Bar)	30	7.89		3.802		<sup>34</sup>
PBI/ ZIF-8(10 %)			40	8.89		4.499		
Matrimid 5218	2018	35 C (7 Bar)		7.33	0.21		CO <sub>2</sub> /CH <sub>4</sub> 34.904	<sup>35</sup>
PI-PVDF/ MIL- 101 (Cr) (10%)				14.87	0.24		CO <sub>2</sub> /CH <sub>4</sub> 61.958	
Matrimid	2021	35 C (7 Bar)	22.30	5.70	0.17		131.18	<sup>36</sup>
Matrimid/ZIF-95 (30%)			76.60	23.20	0.40		191.50	

### S9. Upper Bounds:

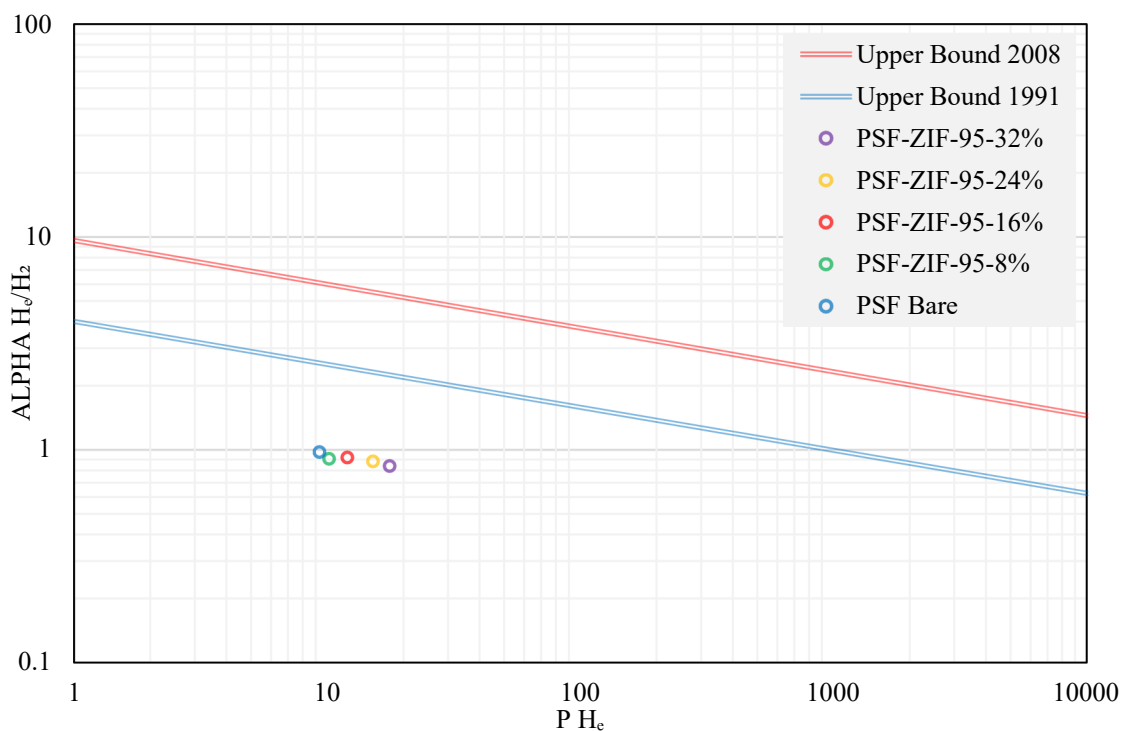


Fig. S5. He/H<sub>2</sub> selectivity vs He permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).

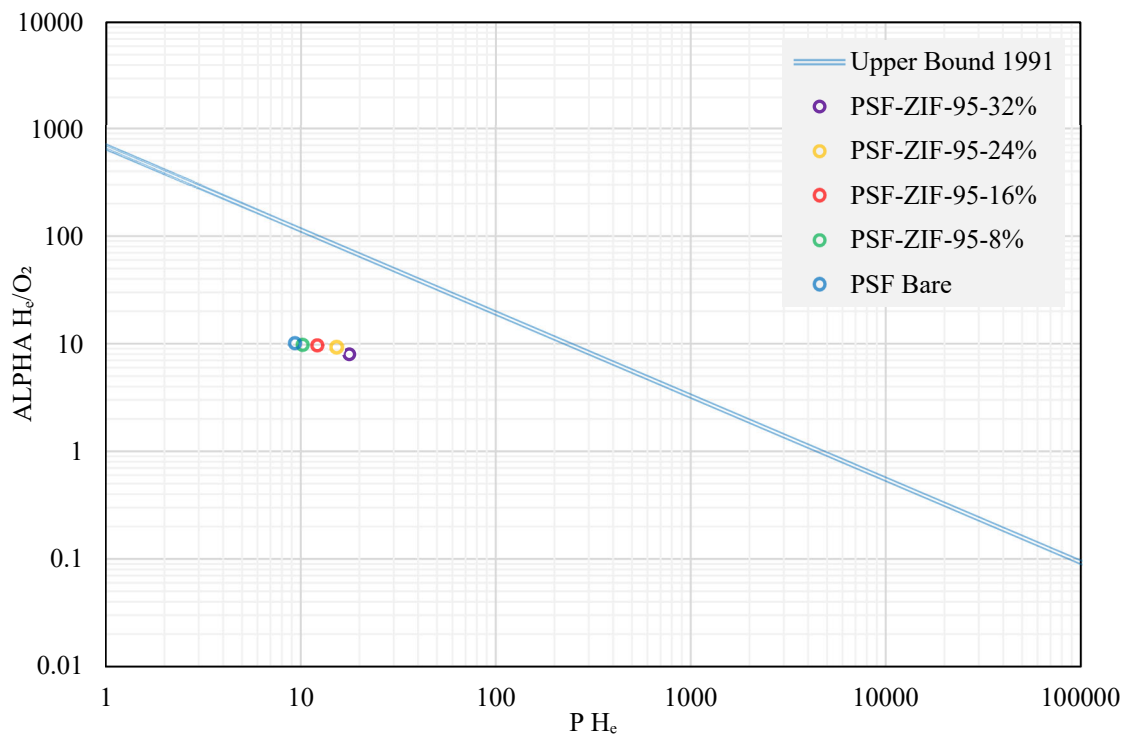


Fig. S6. He/O<sub>2</sub> selectivity vs He permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).

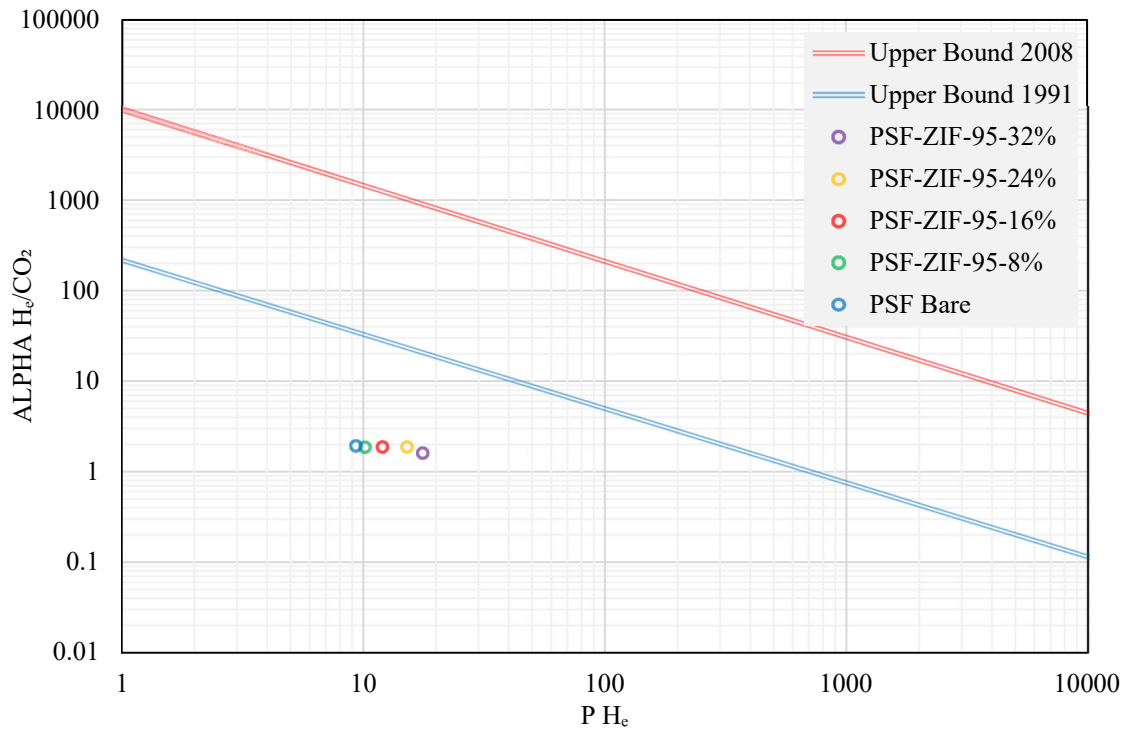


Fig. S7. He/CO<sub>2</sub> selectivity vs He permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).

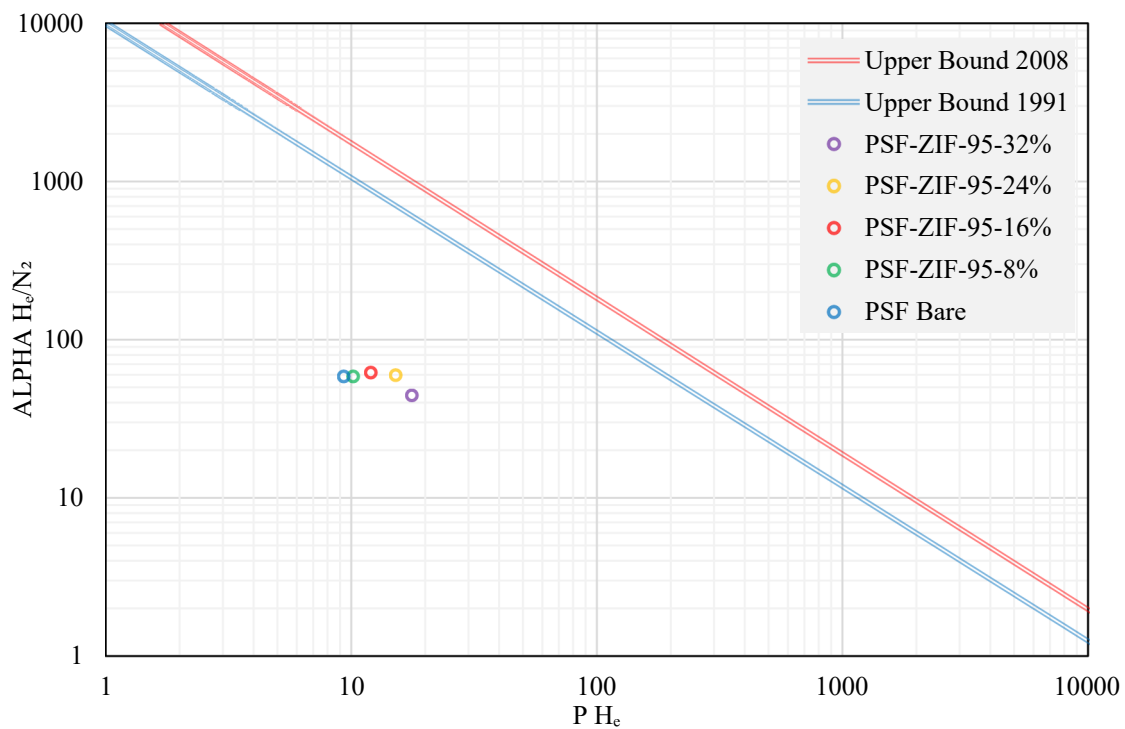
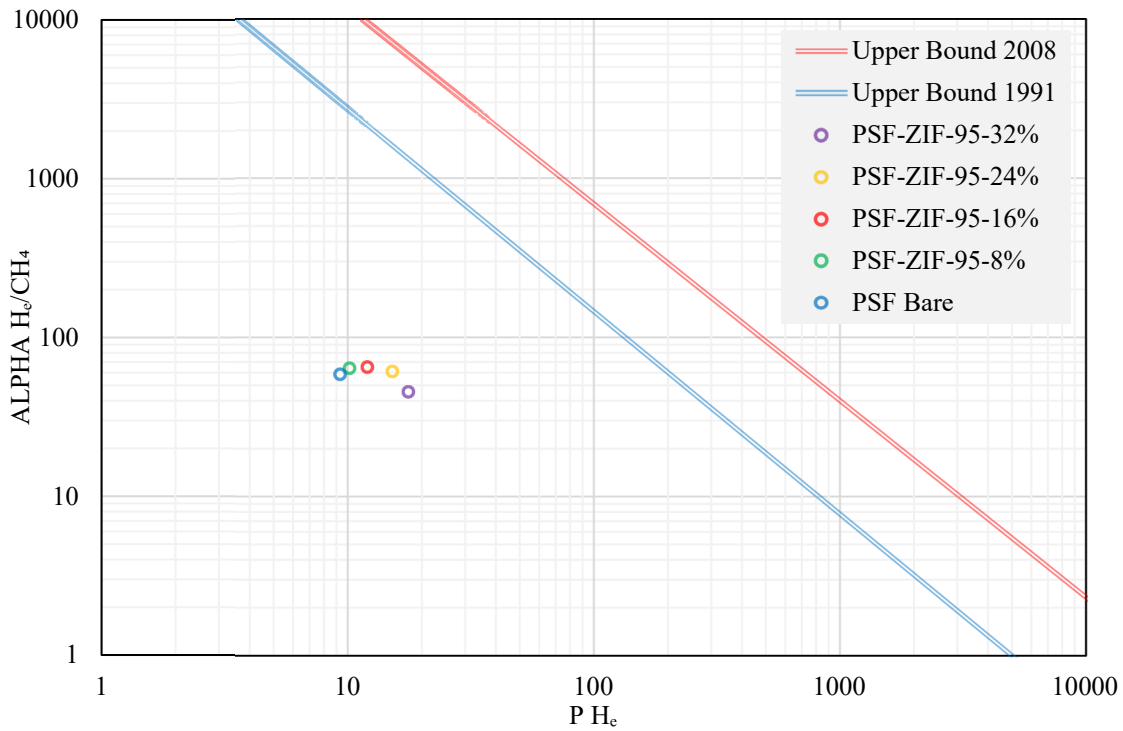
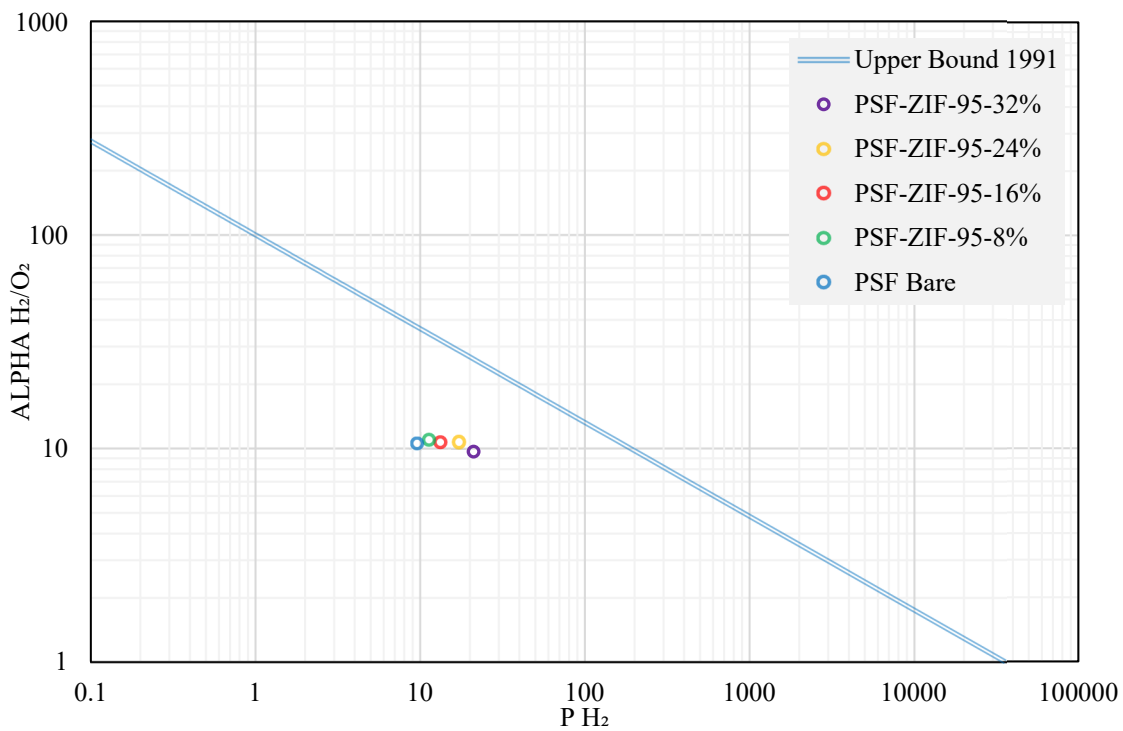


Fig. S8. He/N<sub>2</sub> selectivity vs He permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).

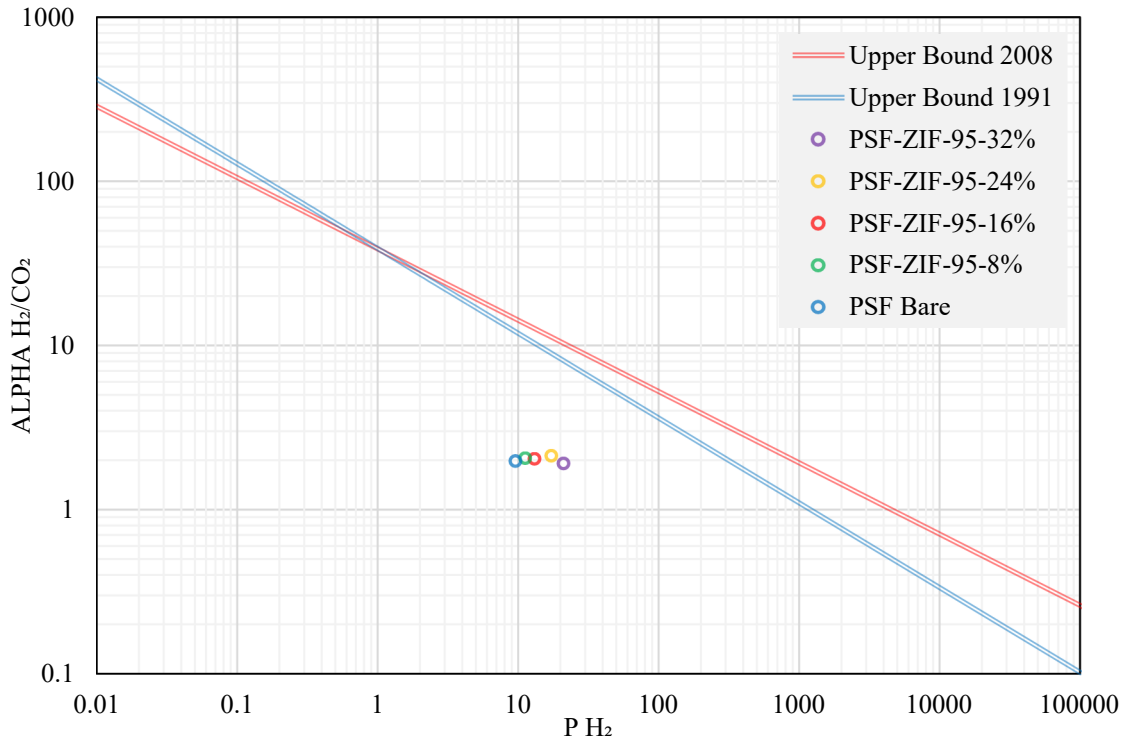




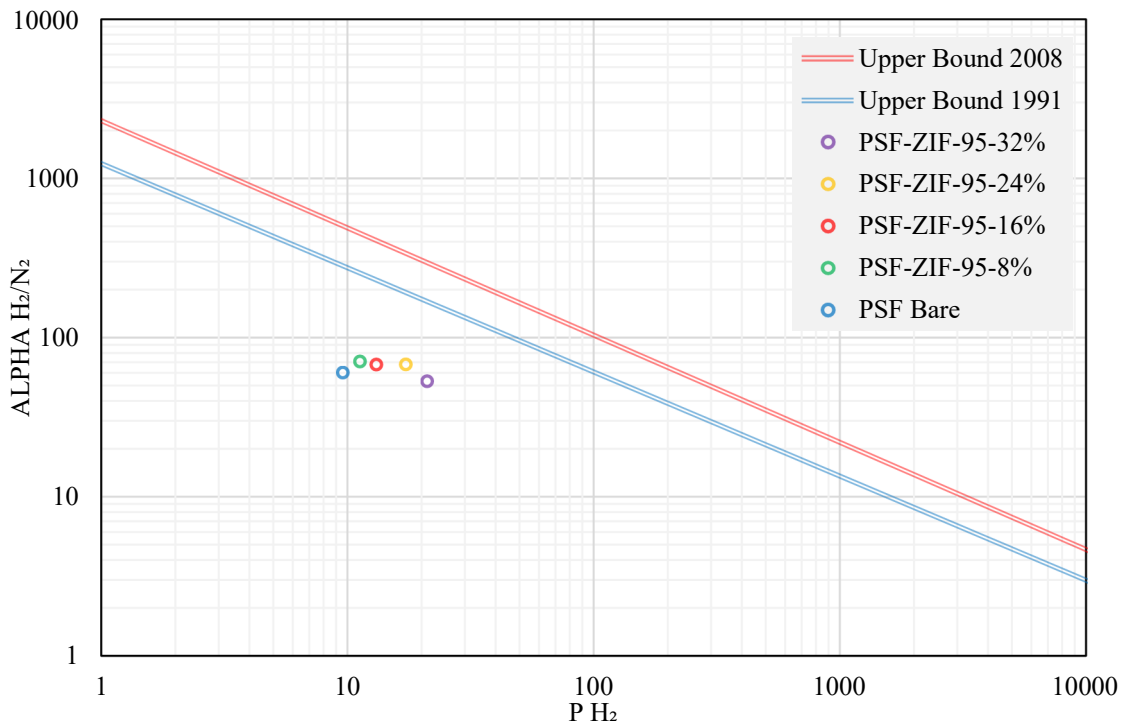
**Fig. S9.** He/CH<sub>4</sub> selectivity vs He permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



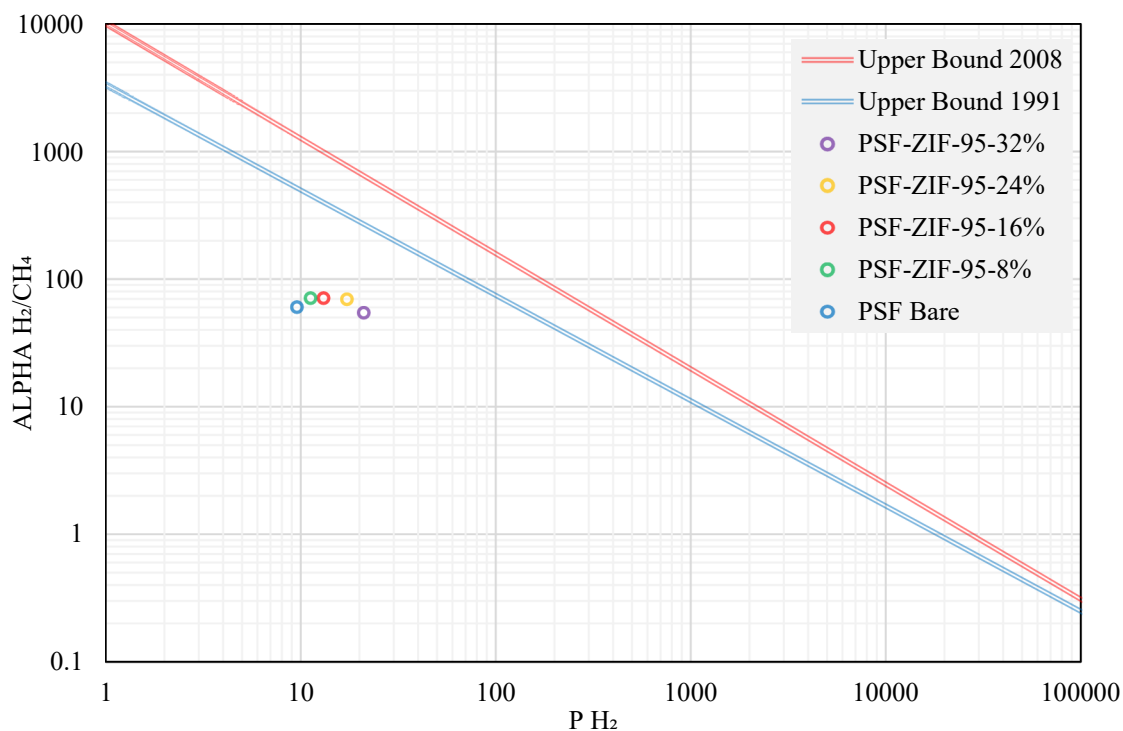
**Fig. S10.** H<sub>2</sub>/O<sub>2</sub> selectivity vs H<sub>2</sub> permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



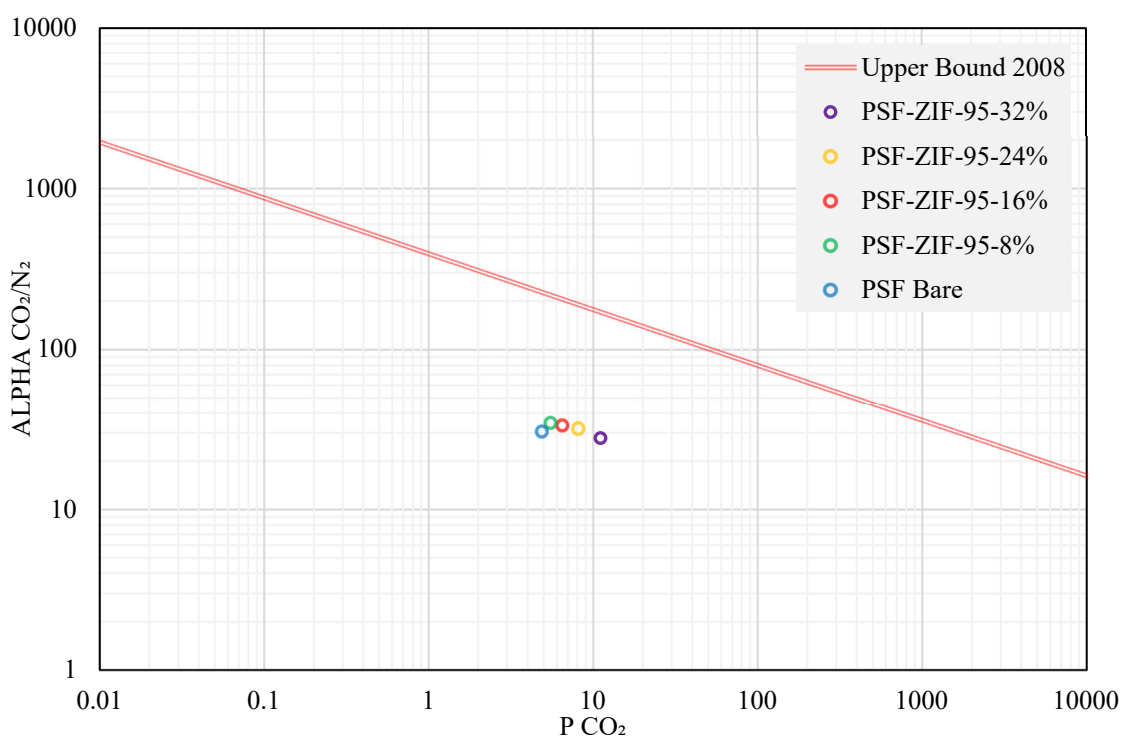
**Fig. S11.**  $H_2/CO_2$  selectivity vs  $H_2$  permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



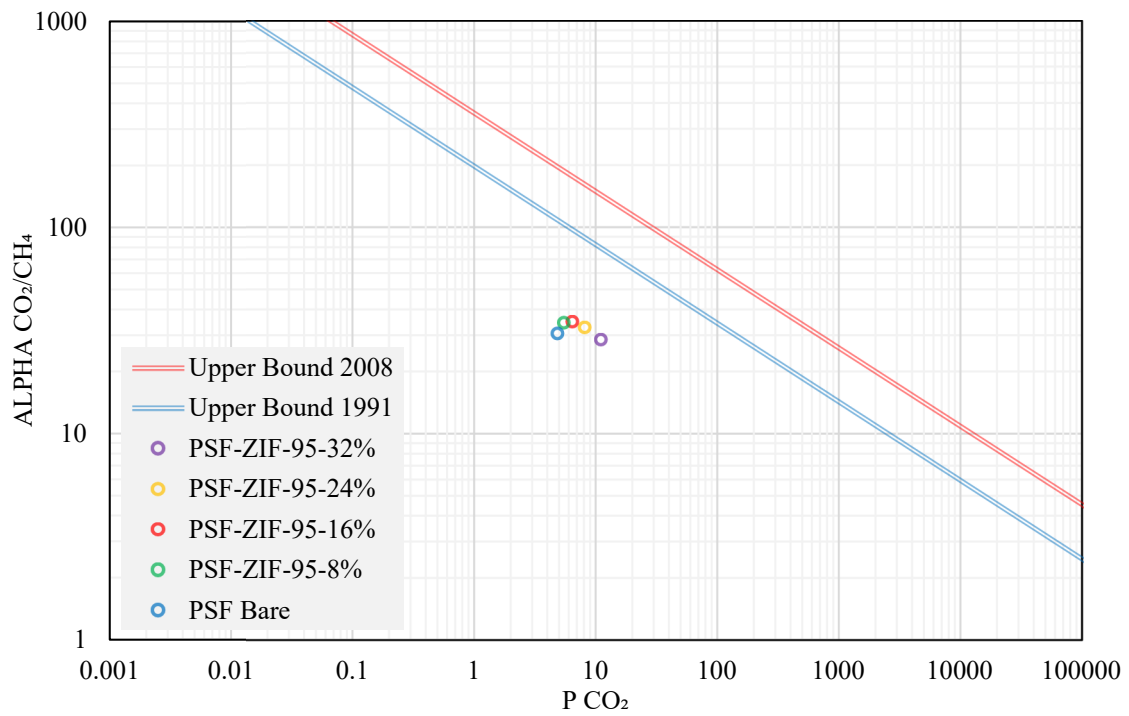
**Fig. S12.**  $H_2/N_2$  selectivity vs  $H_2$  permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



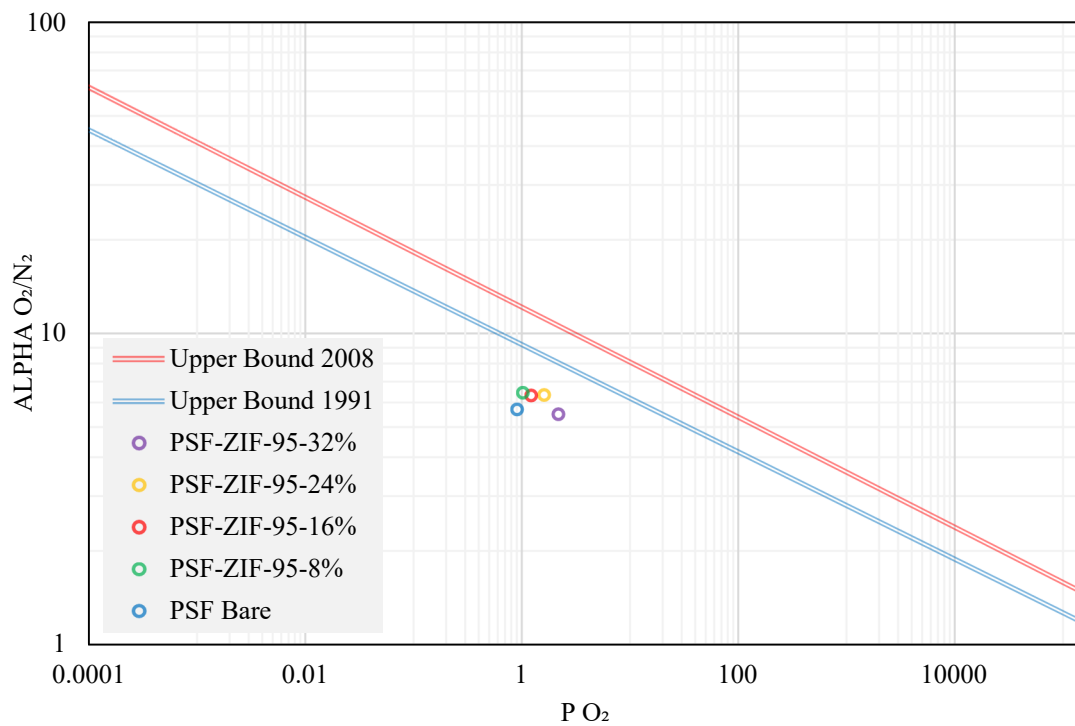
**Fig. S13.** H<sub>2</sub>/CH<sub>4</sub> selectivity vs H<sub>2</sub> permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



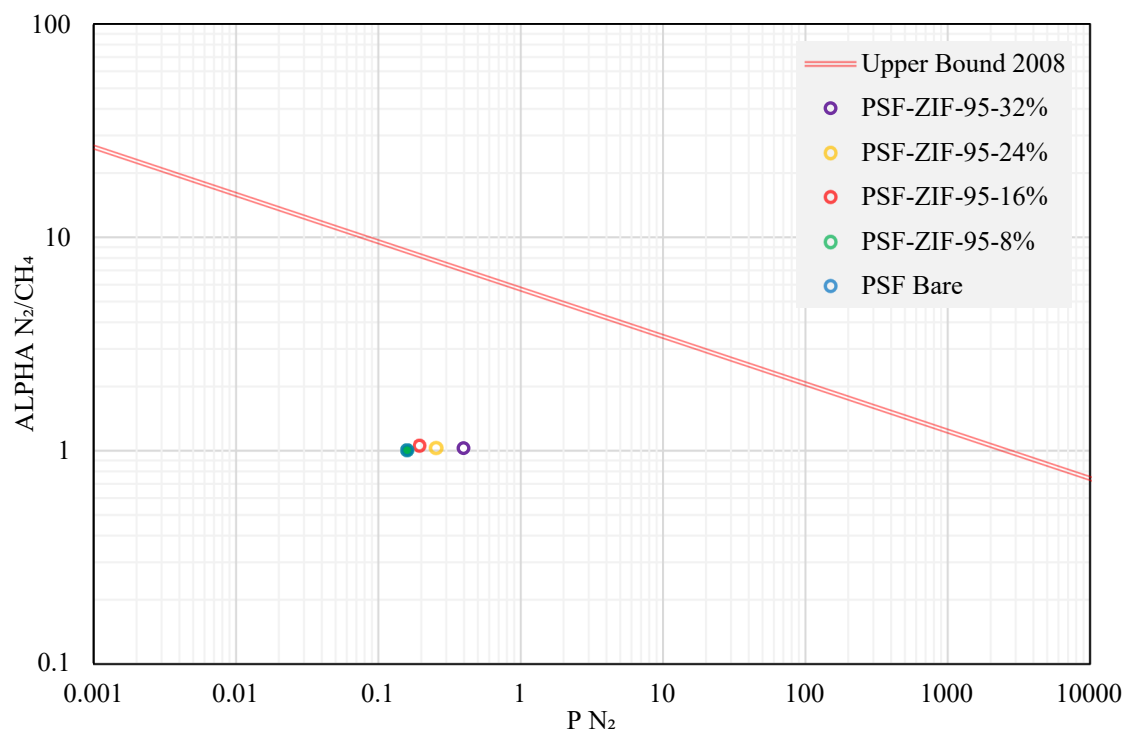
**Fig. S14.** CO<sub>2</sub>/N<sub>2</sub> selectivity vs CO<sub>2</sub> permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



**Fig. S15.** CO<sub>2</sub>/CH<sub>4</sub> selectivity vs CO<sub>2</sub> permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



**Fig. S16.** O<sub>2</sub>/N<sub>2</sub> selectivity vs O<sub>2</sub> permeability of Pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).



**Fig. S17.**  $N_2/CH_4$  selectivity vs  $N_2$  permeability of pure membrane (blue), 8% loaded membrane (green), 16% loaded membrane (red), 24% loaded membrane (yellow), and 32% loaded membrane (purple).

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