## **Supplementary information:**

## Insights into the thermal conductivity of MOF-5 from first principles

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The phonon lifetime  $\tau_{\lambda}$  is calculated based on a perturbation to the non-interacting harmonic modes  $\lambda = (q,s)$ . We focus our attention on the three-phonon processes whose scattering rate  $1/\tau_{\lambda}$  in the single-mode relaxation time approximation can be computed via

$$\frac{1}{\tau_{\lambda}} = \pi \sum_{\substack{q,s,s' \\ q,s,s'}} |V_{3}(s, -q; s', q'; s'', q'')|^{2} \times \left[ \left(1 + n_{s'q'} + n_{s'q''} \right) \delta(\omega_{s'q'} + \omega_{s'q''} - \omega_{s, -q}) + 2\left(n_{s'q''} - n_{s'q'} \right) \delta(\omega_{s'q'} - \omega_{s'q''} - \omega_{s, -q}) \right]$$

where  $V_3(s, -q; s', q'; s'', q'')$  are the three-phonon coupling matrix elements.



Fig. S1 The optimized crystal structure of MOF-5 in consist of organic linkers and ZnO<sub>4</sub> metal clusters.

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Fig. S2. (I). The phonon dispersion curves and phonon PDOS of MOF-5 with different metals (a) Zn, (b) Mg, and (c) Cd. (II). The phonon dispersion curves and phonon PDOS of MOF-5 under  $\varepsilon$  of (e) 2%, (f) 4%, and (g) 6%. For clarity, only the low-frequency phonon bands are shown, since phonon dispersion curves above 8 THz are rather flat.