

## Novel Metal Oxides with Promising High-Temperature Thermoelectric Performance

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### Detailed computations: method of verification

In the detailed calculations of  $ATa_2O_6$  ( $A = Mg, Ca$ ) and  $SrTiO_3$ , the PBEsol exchange-correlation functional<sup>1</sup> was used better to describe the structural properties. The LDA +  $U$  method of Dudarev *et al.*<sup>2</sup> with  $U - J = 5^3$  and of Liechtenstein *et al.*<sup>4</sup> with  $U = 5$  eV and  $J = 0.64$  eV<sup>5</sup> were used for the Ta  $5d$  states of  $ATa_2O_6$  ( $A = Mg, Ca$ ) and the Ti  $3d$  states of  $SrTiO_3$ , respectively. Considering the underestimation of the size of the bandgap in GGA-based calculations, the Heyd-Scuseria-Ernzerhof (HSE06) hybrid functional<sup>6</sup>, with accurate exchange and correlation energy, was applied to calculate the band gaps of  $ATa_2O_6$  ( $A = Mg, Ca$ ), as shown in Fig. S1a and Fig. S1c. Our results coincide with the results of other theoretical calculations<sup>3</sup> and experimental results.<sup>7, 8</sup> Moreover, the spin-orbit coupling (SOC) effects on the electronic structure of  $ATa_2O_6$  ( $A = Mg, Ca$ ) and  $SrTiO_3$  were also studied (see Fig. S1b, Fig. S1d and Fig. S2a) but there are no obvious changes. Therefore, SOC effects are not considered in the following calculations. To accurately estimate the electronic-transport properties, fine  $k$ -point meshes of  $18 \times 18 \times 12$  for  $MgTa_2O_6$ ,  $20 \times 20 \times 20$  for  $CaTa_2O_6$  and  $27 \times 27 \times 27$  for  $SrTiO_3$  were used. Meanwhile, the scissor operator was also applied to correct the bandgap but leave the band dispersion unchanged. For  $CaTa_2O_6$ , the phonon dispersion was calculated with a  $2 \times 2 \times 2$  supercell and a  $2 \times 2 \times 2$   $k$ -point mesh. For the thermal-conductivity calculation of  $MgTa_2O_6$ , the linearized phonon version of the

Boltzmann transport equation was solved, considering only two- and three-phonon scattering processes, using the ShengBTE code.<sup>9</sup> The second-order interatomic force constants (IFCs) were obtained via a  $2 \times 2 \times 2$  supercell with a  $2 \times 2 \times 2$   $k$ -point mesh using density-functional perturbation theory (DFPT), as implemented in Phonopy.<sup>10</sup> The third-order IFCs were calculated using a  $2 \times 2 \times 2$  supercell and a  $1 \times 1 \times 1$   $k$ -point mesh with only the gamma point, where interactions further than third neighbors in the supercell were neglected.

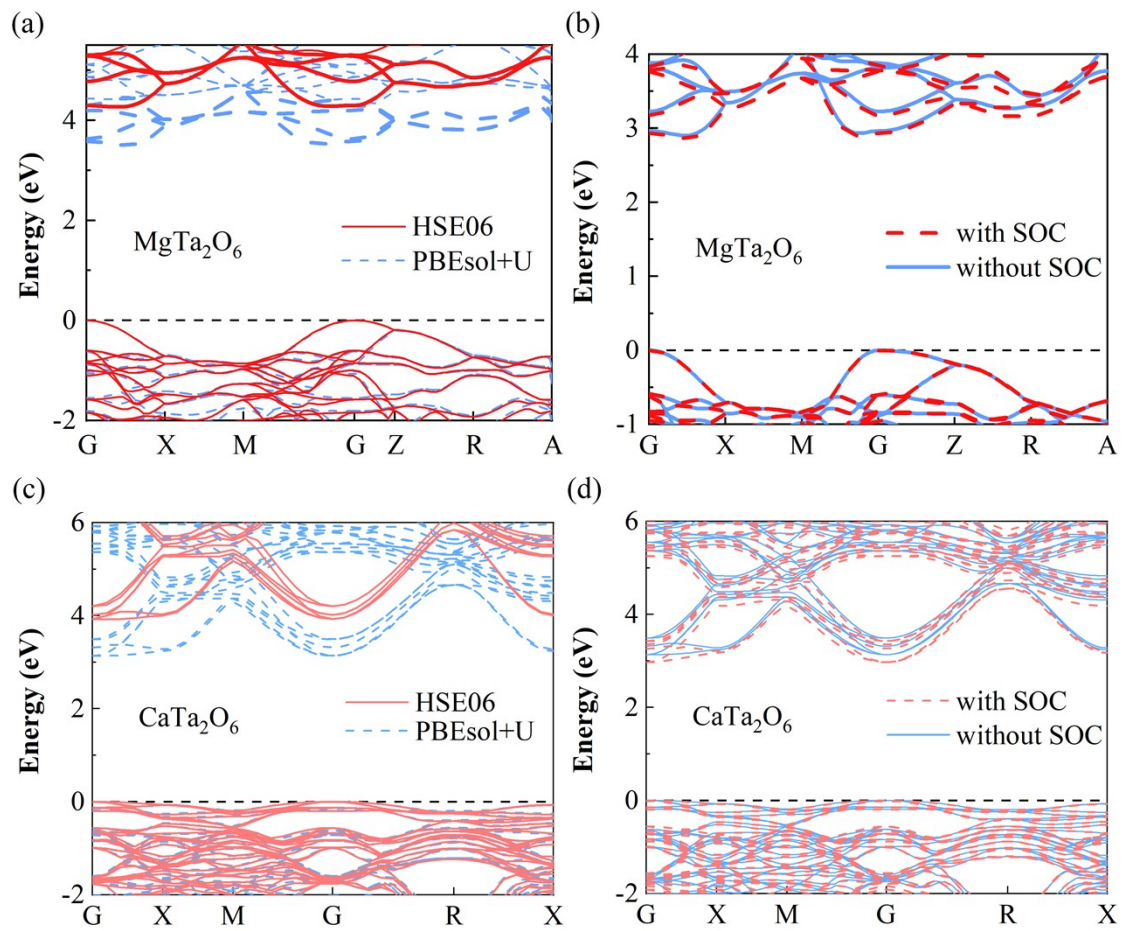


Fig S1. The effects of: (a) exchange-correlation functional; (b) spin-orbit coupling (SOC), on the electronic band structure of  $\text{MgTa}_2\text{O}_6$  calculated with the PBEsol exchange-correlation functional and without using the LDA + $U$  correction.

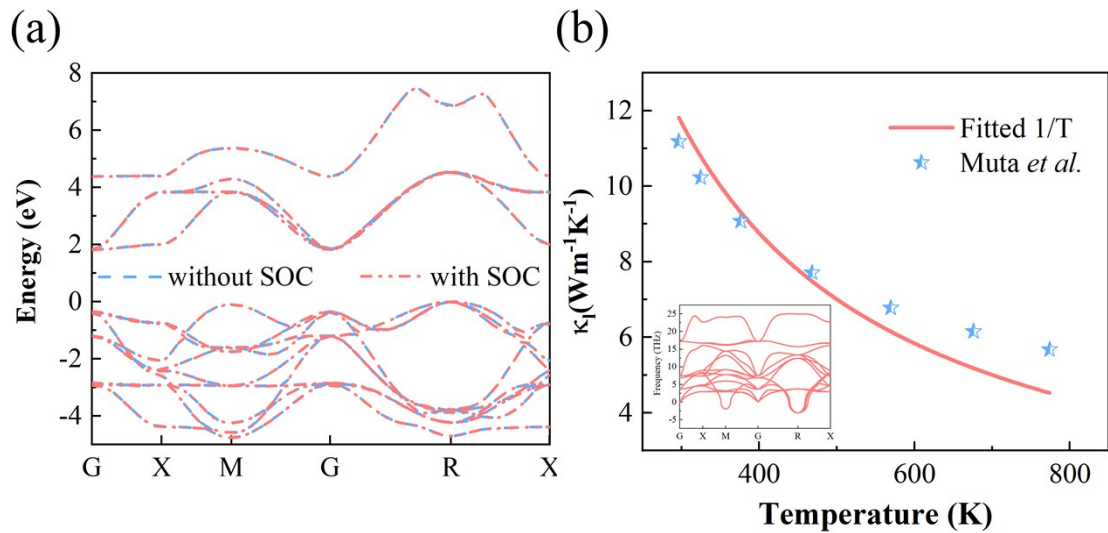


Fig S2 (a) The effects of spin-orbit coupling (SOC) on the electronic band structure of SrTiO<sub>3</sub> calculated with the PBEsol exchange-correlation functional. (b) The fitting curve plotting for SrTiO<sub>3</sub> with the  $\kappa_l \sim 1/T$  relation in which the data points for the temperature dependence of the lattice thermal conductivity are extracted from the experimental results of Muta *et al.*<sup>11</sup> The inset shows the phonon-dispersion curves for SrTiO<sub>3</sub> calculated at 0 K.

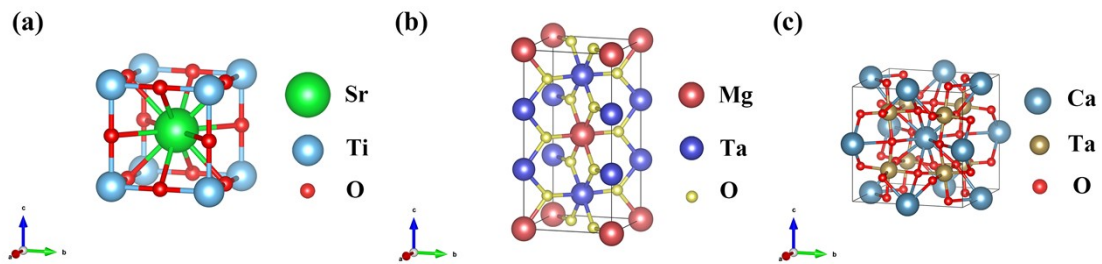


Fig S3 Crystal structure of: (a) SrTiO<sub>3</sub>; (b) MgTa<sub>2</sub>O<sub>6</sub>; (c) CaTa<sub>2</sub>O<sub>6</sub>.

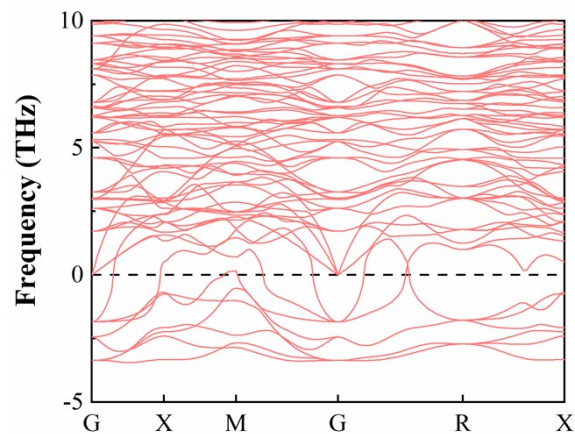


Fig S4 The phonon-dispersion curves for CaTa<sub>2</sub>O<sub>6</sub>.

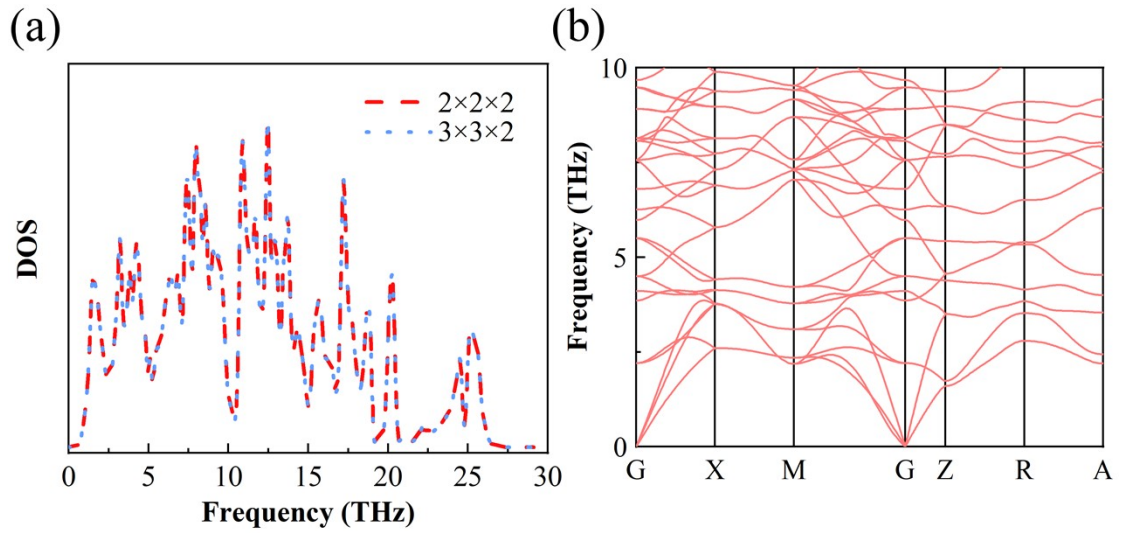


Fig. S5. (a) The phonon density of states of  $\text{MgTa}_2\text{O}_6$  computed from supercell expansions of  $2 \times 2 \times 2$  and  $3 \times 3 \times 2$ . (b) The phonon-dispersion curves for  $\text{MgTa}_2\text{O}_6$ .

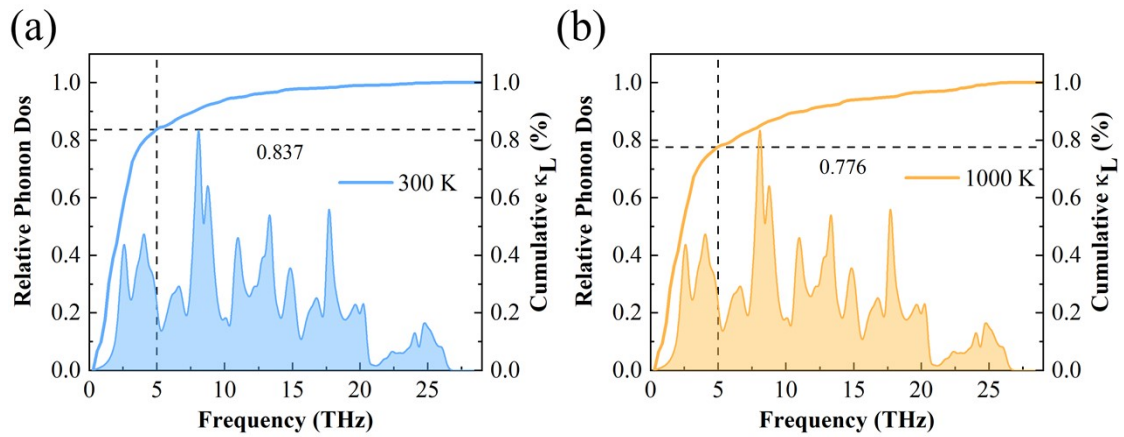


Fig. S6. The normalized phonon DOS and cumulative lattice thermal conductivity of  $\text{MgTa}_2\text{O}_6$  at: (a) 300 K; (b) 1000 K.

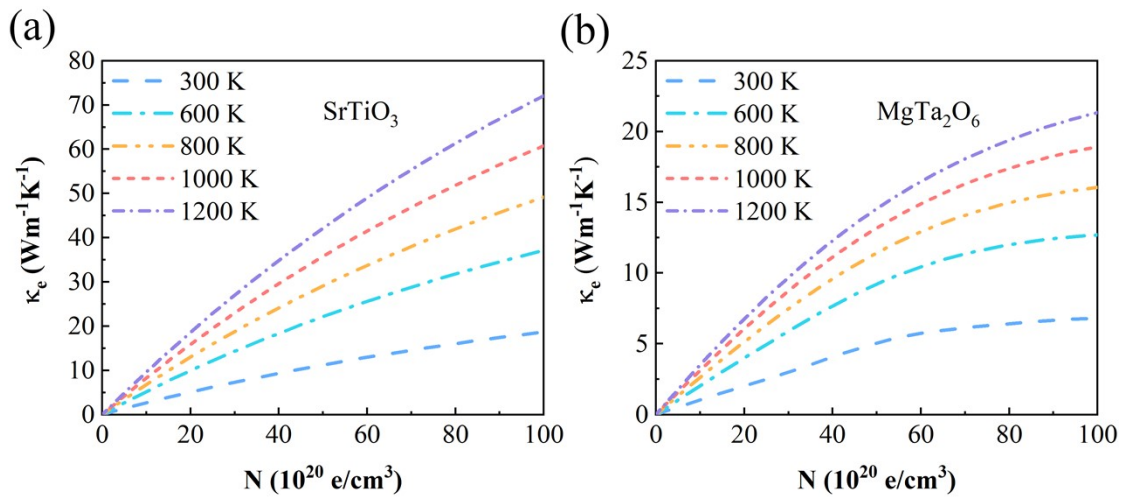


Fig. S7. Temperature-dependent electronic thermal conductivity of: (a) SrTiO<sub>3</sub>; and (b) MgTa<sub>2</sub>O<sub>6</sub>, as a function of carrier concentration.

Table S1 The formula, space-group symbols (SG), space-group numbers (SN), bandgap ( $E_g$ ), semiconductor type (n-type or p-type), and the corresponding carrier concentration ( $n_{max}$ ,  $p_{max}$ ), effective conductivity mass ( $m_c$ ) and Seebeck mass ( $m_s$ ), Fermi-surface complexity factors ( $N_v^*K^*$ ) calculated at the maximum  $PF$  of the binary and ternary oxides at 1000 K. The table of electrical-transport properties from  $KCoO_2$  onwards are left blank as their bandgaps are less than 0.1 eV (the bandgap screening criterion).

formula	SG	SN	$E_g$	type	$n_{max}, p_{max}$ ( $10^{20} \text{ cm}^{-3}$ )	$m_s$ ( $PF_{max}$ )	$m_c$ ( $PF_{max}$ )	$N_v^*K^*$ ( $PF_{max}$ )	$PF_{max}$ ( $\mu\text{W}/(\text{cmK}^2)$ )
$Al_2O_3$	$R\bar{3}c$	167	5.868	p	50.000	6.387	6.266	1.029	65.655
$As_2O_3$	$Fd\bar{3}m$	227	4.026	n	10.000	2.566	2.419	1.093	40.648
$As_2O_5$	$P4_12_12$	92	1.357	n	100.000	5.139	12.894	0.252	22.852
$B_2O_3$	$P3_121$	152	6.347	n	25.000	3.133	4.030	0.686	43.850
$Ba_2ZrO_4$	$I4/mmm$	139	3.156	p	25.000	5.503	6.700	0.744	55.952
$Ba_3Mn_2O_8$	$R\bar{3}m$	166	1.592	n	10.000	2.531	7.825	0.184	15.272
$Ba_3Y_4O_9$	$R32$	155	3.214	n	100.000	6.864	17.465	0.246	31.175
$Ba_4Nb_2O_9$	$P6_3/m$	176	3.518	n	10.000	2.668	5.681	0.322	18.188
$Ba_5Ta_4O_{15}$	$P\bar{3}m1$	164	3.083	n	10.000	1.708	85.310	0.003	44.049
$Ba_8V_7O_{22}$	$R\bar{3}m$	166	0.438	p	10.000	2.480	43460.5 45	0.000	6.200
$BaCoO_2$	$P3_121$	152	1.129	n	7.500	1.449	2.123	0.564	23.531
$BaHgO_2$	$R\bar{3}m$	166	2.301	p	25.000	5.325	4.317	1.370	71.597
$BaMnO_3$	$P6_3/mmc$	194	1.932	p	25.000	4.494	5.488	0.741	44.279
$BaMoO_4$	$I4_1/a$	88	4.375	p	25.000	6.377	13.730	0.317	26.510
$BaO_2$	$I4/mmm$	139	2.218	n	50.000	2.410	1.054	3.458	238.158

BaTa <sub>2</sub> O <sub>6</sub>	$P6/mmm$	191	2.079	n	10.000	1.283	19.220	0.017	34.519
BaTiO <sub>3</sub>	$Pm\bar{3}m$	221	1.676	p	50.000	5.436	2.284	3.671	141.781
BaV <sub>6</sub> O <sub>11</sub>	$P6_3mc$	186	0.603	p	10.000	2.838	14.050	0.091	9.105
BaWO <sub>4</sub>	$I4_1/a$	88	0.970	p	25.000	5.892	23.310	0.127	13.606
BaZnO <sub>2</sub>	$P3_121$	152	2.246	p	25.000	5.305	13.006	0.261	22.059
BaZrO <sub>3</sub>	$Pm\bar{3}m$	221	3.121	p	50.000	5.298	2.362	3.358	132.278
Ca <sub>2</sub> Hf <sub>7</sub> O <sub>16</sub>	$R\bar{3}$	148	4.303	p	7.500	3.443	29.249	0.040	11.757
Ca <sub>2</sub> MnO <sub>4</sub>	$I4_1/acd$	142	0.395	n	100.000	2.179	14.500	0.058	26.745
Ca <sub>2</sub> Nb <sub>2</sub> O <sub>7</sub>	$Fd\bar{3}m$	227	1.434	n	5.000	1.489	3.069	0.338	14.466
Ca <sub>2</sub> Ta <sub>2</sub> O <sub>7</sub>	$Fd\bar{3}m$	227	2.317	n	5.000	1.742	3.898	0.299	13.788
CaCrO <sub>4</sub>	$I4_1/amd$	141	2.429	p	50.000	6.235	9.109	0.566	44.297
CaMoO <sub>4</sub>	$I4_1/a$	88	3.769	p	25.000	6.180	13.213	0.320	37.637
CaO	$Fm\bar{3}m$	225	3.641	p	100.000	5.725	2.222	4.135	157.859
CaO <sub>2</sub>	$I4/mmm$	139	2.784	n	75.000	4.278	5.283	0.729	201.574
CaTa <sub>2</sub> O <sub>6</sub>	$Pm\bar{3}$	200	2.455	n	10.000	1.876	0.651	4.889	100.692
CaTa <sub>4</sub> O <sub>11</sub>	$P6_322$	182	3.573	n	25.000	3.765	17.276	0.102	30.429
CaV <sub>4</sub> O <sub>9</sub>	$P4/n$	85	2.447	n	25.000	5.405	43.869	0.043	7.783
CdIn <sub>2</sub> O <sub>4</sub>	$Fd\bar{3}m$	227	0.880	p	75.000	8.541	20.114	0.277	30.753
CdO <sub>2</sub>	$Pa\bar{3}$	205	1.241	p	50.000	4.330	1.707	4.041	136.635
CoO <sub>2</sub>	$P\bar{3}m1$	164	0.982	p	50.000	5.465	2.385	3.468	141.242
Cr <sub>2</sub> O <sub>3</sub>	$R\bar{3}c$	167	2.401	n	10.000	2.755	4.805	0.434	22.446

$\text{Cs}_2\text{V}_5\text{O}_{13}$	$I4mm$	107	1.551	p	50.000	8.620	217.699	0.008	45.311
$\text{Fe}_2\text{O}_3$	$R\bar{3}c$	167	1.565	p	25.000	4.548	9.615	0.325	24.718
$\text{Ga}_2\text{O}_3$	$R\bar{3}c$	167	2.329	p	100.000	7.829	16.793	0.318	34.658
$\text{GeO}_2$	$P\bar{3}_121$	152	3.215	n	100.000	3.247	3.378	0.942	40.151
$\text{HfO}_2$	$Fm\bar{3}m$	225	3.804	p	25.000	2.798	0.824	6.252	146.918
$\text{In}_2\text{O}_3$	$Ia\bar{3}$	206	0.893	p	25.000	5.877	14.361	0.262	22.017
$\text{K}_2\text{V}_3\text{O}_8$	$P4bm$	100	2.000	p	50.000	16.569	355.152	0.010	15.828
$\text{K}_2\text{Zn}_6\text{O}_7$	$P4_2nm$	102	0.868	p	5.000	2.688	121.366	0.003	16.647
$\text{K}_4\text{Zr}_5\text{O}_{12}$	$P\bar{3}m1$	164	3.247	p	25.000	4.101	36.005	0.038	43.634
$\text{K}_5\text{V}_3\text{O}_{10}$	$P4_12_12$	92	3.058	p	10.000	3.138	108480. 705	0.000	0.502
$\text{K}_6\text{CdO}_4$	$P6_3mc$	186	1.599	n	1.000	0.430	0.472	0.868	15.113
$\text{KO}_3$	$I4/mcm$	140	0.617	n	5.000	1.351	14.420	0.029	4.627
$\text{KReO}_4$	$I4_1/a$	88	3.969	p	25.000	6.732	35.779	0.082	10.417
$\text{Li}_3\text{CuO}_3$	$P4_2/mnm$	136	1.175	p	100.000	9.545	41.065	0.112	21.358
$\text{Mg}(\text{RhO}_2)_2$	$Fd\bar{3}m$	227	1.177	n	10.000	2.197	0.915	3.719	88.450
$\text{Mg}_2\text{Mo}_3\text{O}_8$	$P6_3mc$	186	1.641	p	10.000	2.863	25.763	0.037	16.388
$\text{Mg}_3\text{Nb}_6\text{O}_{11}$	$P\bar{3}m1$	164	0.237	p	25.000	2.484	7.398	0.195	35.124
$\text{Mg}_4\text{Nb}_2\text{O}_9$	$P\bar{3}c1$	165	3.419	p	25.000	4.197	16.616	0.127	23.757
$\text{Mg}_6\text{MnO}_8$	$Fm\bar{3}m$	225	2.312	p	25.000	5.365	12.657	0.276	22.543
$\text{MgCr}_2\text{O}_4$	$Fd\bar{3}m$	227	2.814	n	7.500	1.741	1.357	1.453	42.422
$\text{MgO}_2$	$Pa\bar{3}$	205	3.716	n	25.000	6.446	3.908	2.118	89.446



MgTa <sub>2</sub> O <sub>6</sub>	$P4_2/mnm$	136	2.857	n	10.000	2.541	2.361	1.116	48.630
MgTiO <sub>3</sub>	$R\bar{3}$	148	3.519	p	50.000	6.681	11.957	0.418	39.771
Mn <sub>3</sub> O <sub>4</sub>	$I4_1/amd$	141	0.655	n	10.000	1.982	7.082	0.148	42.392
MnO	$Fm\bar{3}m$	225	0.120	p	25.000	3.937	1.138	6.436	171.612
Na <sub>14</sub> Cd <sub>2</sub> O <sub>9</sub>	$P\bar{3}$	147	1.372	n	50.000	0.890	2.071	0.282	15.577
Na <sub>2</sub> O <sub>2</sub>	$P\bar{6}2m$	189	1.717	n	50.000	1.066	5.199	0.093	58.822
Na <sub>2</sub> Ta <sub>4</sub> O <sub>11</sub>	$R\bar{3}c$	167	3.494	p	25.000	5.457	$\frac{1850.25}{5}$	0.000	22.424
Na <sub>3</sub> CoO <sub>2</sub>	$P4_2/mnm$	136	1.366	n	2.500	0.842	1.666	0.359	11.668
Na <sub>4</sub> Ti <sub>5</sub> O <sub>12</sub>	$P\bar{3}$	147	2.502	n	25.000	4.057	29.237	0.052	60.598
NaNbO <sub>2</sub>	$P6_3/mmc$	194	1.389	n	75.000	3.956	3.833	1.049	105.347
NaNbO <sub>3</sub>	$R\bar{3}$	148	3.843	n	25.000	4.153	16.742	0.124	39.818
Nb <sub>2</sub> O <sub>5</sub>	$I4/mmm$	139	1.493	p	10.000	2.837	$\frac{82826.3}{58}$	0.000	13.573
NbO <sub>2</sub>	$I4_1/a$	88	0.406	n	25.000	2.800	6.705	0.270	19.321
Pb <sub>3</sub> O <sub>4</sub>	$P4_2/mbc$	135	1.113	p	7.500	2.323	3.022	0.674	27.230
PoO <sub>2</sub>	$Fm\bar{3}m$	225	1.916	n	7.500	1.388	0.365	7.406	115.424
Rb <sub>3</sub> TaO <sub>8</sub>	$I\bar{4}2m$	121	3.083	n	10.000	2.343	5.910	0.250	21.906
Rb <sub>3</sub> V <sub>5</sub> O <sub>14</sub>	$P31m$	157	2.262	n	7.500	2.417	282.709	0.001	22.279
RbScO <sub>2</sub>	$P6_3/mmc$	194	3.464	p	50.000	5.671	8.352	0.560	82.163
Rh <sub>2</sub> O <sub>3</sub>	$R\bar{3}c$	167	0.669	n	25.000	4.487	3.880	1.243	60.565

Sb <sub>2</sub> O <sub>3</sub>	$Fd\bar{3}m$	227	3.290	n	25.000	2.239	1.153	2.707	74.308
Sc <sub>2</sub> O <sub>3</sub>	$Ia\bar{3}$	206	3.826	p	10.000	3.800	6.207	0.479	24.558
SeO <sub>2</sub>	$P4_2/mbc$	135	3.235	n	5.000	1.363	2.179	0.495	36.767
SiO <sub>2</sub>	$P3_221$	154	5.727	p	25.000	6.469	9.033	0.606	51.325
SnO <sub>2</sub>	$P4_2/mnm$	136	0.619	p	25.000	2.538	2.906	0.817	36.058
Sr <sub>3</sub> V <sub>2</sub> O <sub>7</sub>	$I4/mmm$	139	0.534	p	25.000	1.689	1718.13 0	0.000	24.709
Sr <sub>6</sub> (CoO <sub>3</sub> ) <sub>5</sub>	$R32$	155	0.373	p	10.000	2.886	87.441	0.006	1.639
SrMoO <sub>4</sub>	$I4_1/a$	88	4.061	p	25.000	6.151	13.779	0.298	30.262
SrO <sub>2</sub>	$I4/mmm$	139	2.817	n	50.000	5.110	8.245	0.488	252.999
SrTa <sub>4</sub> O <sub>11</sub>	$P6_322$	182	3.550	n	25.000	3.678	13.727	0.139	27.717
SrTiO <sub>3</sub>	$Pm\bar{3}m$	221	1.791	n	10.000	2.430	0.842	4.903	109.233
SrV <sub>13</sub> O <sub>18</sub>	$R\bar{3}$	148	0.108	n	50.000	1.503	61.895	0.004	1.033
SrWO <sub>4</sub>	$I4_1/a$	88	0.687	p	25.000	5.429	7158.35 5	0.000	17.470
SrZrO <sub>3</sub>	$Pm\bar{3}m$	221	3.307	p	100.000	5.604	2.138	4.244	158.530
Te <sub>4</sub> O <sub>9</sub>	$R\bar{3}$	148	2.211	p	10.000	3.751	8.141	0.313	19.040
TeO <sub>3</sub>	$R\bar{3}c$	167	1.132	p	25.000	5.689	5.301	1.112	61.132
TiO <sub>2</sub>	$P4_2/mnm$	136	1.789	n	50.000	5.375	1.772	5.282	182.470
V <sub>2</sub> O <sub>3</sub>	$Ia\bar{3}$	206	0.890	n	5.000	1.285	3.394	0.233	10.817
VO <sub>2</sub>	$P4_2/mnm$	136	0.882	p	25.000	4.251	2.646	2.036	90.812

Y <sub>2</sub> O <sub>3</sub>	$Ia\bar{3}$	206	4.119	p	25.000	4.309	10.732	0.254	20.425
ZnO <sub>2</sub>	$Pa\bar{3}$	205	2.113	p	50.000	4.169	1.662	3.974	132.473
ZrO <sub>2</sub>	$P4_2/nmc$	137	4.045	p	50.000	7.532	3.302	3.446	167.613
KCoO <sub>2</sub>	$I\bar{4}2d$	122	0.092						
BaV <sub>13</sub> O <sub>18</sub>	$R\bar{3}$	148	0.075						
Sr <sub>5</sub> (CoO <sub>3</sub> ) <sub>4</sub>	$P\bar{3}c1$	165	0.057						
Ca <sub>3</sub> (CoO <sub>3</sub> ) <sub>2</sub>	$R\bar{3}c$	167	0.039						
Ba <sub>3</sub> W <sub>2</sub> O <sub>9</sub>	$R\bar{3}c$	167	0.018						
PbO <sub>2</sub>	$P4_2/mnm$	136	0.015						
Mg <sub>2</sub> VO <sub>4</sub>	$Fd\bar{3}m$	227	0.008						
Ba <sub>2</sub> Co <sub>9</sub> O <sub>14</sub>	$R\bar{3}m$	166	0.000						
Ba <sub>2</sub> Nb <sub>15</sub> O <sub>32</sub>	$R\bar{3}$	148	0.000						
Ba <sub>2</sub> Nb <sub>5</sub> O <sub>9</sub>	$P4/mmm$	123	0.000						
Ba <sub>3</sub> Cr <sub>2</sub> O <sub>8</sub>	$R\bar{3}m$	166	0.000						
Ba <sub>3</sub> Ta <sub>5</sub> O <sub>15</sub>	$P4/mbm$	127	0.000						
Ba <sub>5</sub> Co <sub>5</sub> O <sub>14</sub>	$P\bar{3}m1$	164	0.000						
BaCoO <sub>3</sub>	$P6_3/mmc$	194	0.000						
BaIrO <sub>3</sub>	$Pm\bar{3}m$	221	0.000						
BaMoO <sub>3</sub>	$Pm\bar{3}m$	221	0.000						
BaNb <sub>4</sub> O <sub>6</sub>	$P4/mmm$	123	0.000						

BaRhO <sub>3</sub>	$P6_3/mmc$	194	0.000	
Bi <sub>2</sub> O <sub>3</sub>	$Pn\bar{3}m$	224	0.000	
BiO <sub>2</sub>	$Fm\bar{3}m$	225	0.000	
Ca <sub>2</sub> IrO <sub>4</sub>	$P\bar{6}2m$	189	0.000	
CaMn <sub>7</sub> O <sub>12</sub>	$Im\bar{3}$	204	0.000	
CdO	$Fm\bar{3}m$	225	0.000	
Co <sub>3</sub> O <sub>4</sub>	$Fd\bar{3}m$	227	0.000	
Cr <sub>3</sub> O	$Pm\bar{3}n$	223	0.000	
CrO <sub>2</sub>	$P4_2/mnm$	136	0.000	
Cu <sub>3</sub> TeO <sub>6</sub>	$Ia\bar{3}$	206	0.000	
FeO	$Fm\bar{3}m$	225	0.000	
IrO <sub>2</sub>	$Pa\bar{3}$	205	0.000	
K(IrO <sub>2</sub> ) <sub>4</sub>	$I4/m$	87	0.000	
K(Mo <sub>2</sub> O <sub>3</sub> ) <sub>2</sub>	$P4/mbm$	127	0.000	
K <sub>2</sub> Ta <sub>15</sub> O <sub>32</sub>	$R\bar{3}$	148	0.000	
K <sub>4</sub> (CoO <sub>2</sub> ) <sub>7</sub>	$P6_3/m$	176	0.000	
KCr <sub>4</sub> O <sub>8</sub>	$I4/m$	87	0.000	
KIrO <sub>3</sub>	$Pn\bar{3}$	201	0.000	
KO <sub>2</sub>	$I4/mmm$	139	0.000	

$\text{KV}_4\text{O}_8$	$I4/m$	87	0.000
$\text{MgTi}_2\text{O}_4$	$Fd\bar{3}m$	227	0.000
$\text{MgV}_2\text{O}_4$	$Fd\bar{3}m$	227	0.000
$\text{Mn}_2\text{O}_3$	$Ia\bar{3}$	206	0.000
$\text{MnO}_2$	$P4_2/mnm$	136	0.000
$\text{MoO}_2$	$P4_2/mnm$	136	0.000
$\text{Na}(\text{Mo}_2\text{O}_3)_2$	$P4/mbm$	127	0.000
$\text{NaMn}_7\text{O}_{12}$	$Im\bar{3}$	204	0.000
$\text{NaO}_2$	$Pa\bar{3}$	205	0.000
$\text{NaTi}_8\text{O}_{13}$	$R\bar{3}$	148	0.000
$\text{NaV}_6\text{O}_{11}$	$P6_3mc$	186	0.000
$\text{NaWO}_3$	$Pm\bar{3}m$	221	0.000
$\text{Nb}_4\text{O}_5$	$P4_2/nmc$	137	0.000
$\text{Rb}_2\text{Ta}_{15}\text{O}_{32}$	$R\bar{3}$	148	0.000
$\text{Rb}_4\text{Nb}_{11}\text{O}_{30}$	$R\bar{3}m$	166	0.000
$\text{ReO}_2$	$P4_2/mnm$	136	0.000
$\text{ReO}_3$	$Im\bar{3}$	204	0.000
$\text{RhO}_2$	$P4_2/mnm$	136	0.000
$\text{Sb}_2\text{O}_5$	$Fd\bar{3}m$	227	0.000

SbO <sub>2</sub>	$Fd\bar{3}m$	227	0.000
Sr <sub>2</sub> IrO <sub>4</sub>	$I4_1/acd$	142	0.000
Sr <sub>2</sub> Nb <sub>5</sub> O <sub>9</sub>	$P4/mmm$	123	0.000
Sr <sub>2</sub> TcO <sub>4</sub>	$I4/mmm$	139	0.000
Sr <sub>2</sub> VO <sub>4</sub>	$I4/mmm$	139	0.000
Sr <sub>3</sub> (CoO <sub>3</sub> ) <sub>2</sub>	$R\bar{3}c$	167	0.000
Sr <sub>4</sub> Cr <sub>3</sub> O <sub>9</sub>	$P\bar{3}$	143	0.000
Sr <sub>4</sub> IrO <sub>6</sub>	$R\bar{3}c$	167	0.000
Sr <sub>4</sub> RhO <sub>6</sub>	$R\bar{3}c$	167	0.000
Sr <sub>4</sub> V <sub>3</sub> O <sub>10</sub>	$I4/mmm$	139	0.000
Sr <sub>7</sub> Nb <sub>6</sub> O <sub>21</sub>	$R\bar{3}$	148	0.000
SrCo <sub>12</sub> O <sub>19</sub>	$P6_3/mmc$	194	0.000
SrCo <sub>6</sub> O <sub>11</sub>	$P6_3/mmc$	194	0.000
SrMoO <sub>3</sub>	$Pm\bar{3}m$	221	0.000
SrNbO <sub>3</sub>	$Pm\bar{3}m$	221	0.000
SrV <sub>6</sub> O <sub>11</sub>	$P6_3/mmc$	194	0.000
TaO <sub>2</sub>	$P4_2/mnm$	136	0.000
TeO <sub>2</sub>	$P4_2/mnm$	136	0.000
Ti <sub>2</sub> O <sub>3</sub>	$R\bar{3}c$	167	0.000

$\text{Ti}_4\text{O}_5$	$I4/m$	87	0.000
$\text{Ti}_6\text{O}$	$P\bar{3}1m$	162	0.000
$\text{Tl}_2\text{O}_3$	$Ia\bar{3}$	206	0.000
$\text{Tl}_2\text{TeO}_6$	$P321$	150	0.000
$\text{V}_{13}\text{O}_{16}$	$I4_1/amd$	141	0.000
$\text{V}_{16}\text{O}_3$	$I4/mmm$	139	0.000
$\text{WO}_2$	$P4_2/mnm$	136	0.000
$\text{Yb}_2\text{O}_3$	$Ia\bar{3}$	206	0.000

Table S2 Bulk modulus,  $B_{vrh}$ , and shear modulus,  $G_{vrh}$ , calculated using the Voigt-Reuss-Hill approximation, the Grüneisen constant,  $\gamma$ , the Clarke thermal conductivity,  $\kappa_{Clarke}$ , the Cahill thermal conductivity,  $\kappa_{Cahill}$ , the Slack thermal conductivity,  $\kappa_{Slack}$ , and the maximum thermal conductivity,  $\kappa_{max}$ , between  $\kappa_{Clarke}$  and  $\kappa_{Slack}$  for the binary and ternary oxides at 1000 K.

formula	$B_{vrh}$ (GPa)	$G_{vrh}$ (GPa)	$\gamma$	$\kappa_{Clarke}$ (Wm <sup>-1</sup> K <sup>-1</sup> )	$\kappa_{Cahill}$ (Wm <sup>-1</sup> K <sup>-1</sup> )	$\kappa_{Slack}$ (Wm <sup>-1</sup> K <sup>-1</sup> )	$\kappa_{max}$ (Wm <sup>-1</sup> K <sup>-1</sup> )
Al <sub>2</sub> O <sub>3</sub>	234.343	144.074	1.476	2.737	2.991	5.864	5.864
As <sub>2</sub> O <sub>3</sub>	9.938	5.724	1.541	0.345	0.379	0.077	0.345
As <sub>2</sub> O <sub>5</sub>	93.753	51.418	1.591	1.213	1.333	1.248	1.248
B <sub>2</sub> O <sub>3</sub>	45.957	44.602	1.063	1.740	1.895	4.011	4.011
Ba <sub>2</sub> ZrO <sub>4</sub>	104.762	55.270	1.631	0.878	0.967	3.125	3.125
Ba <sub>3</sub> Mn <sub>2</sub> O <sub>8</sub>	62.924	28.780	1.782	0.722	0.804	0.313	0.722
Ba <sub>3</sub> Y <sub>4</sub> O <sub>9</sub>	99.925	47.869	1.733	0.857	0.951	0.626	0.857
Ba <sub>4</sub> Nb <sub>2</sub> O <sub>9</sub>	72.579	30.955	1.858	0.700	0.784	0.341	0.700
Ba <sub>5</sub> Ta <sub>4</sub> O <sub>15</sub>	113.227	60.231	1.623	0.888	0.978	1.313	1.313
Ba <sub>8</sub> V <sub>7</sub> O <sub>22</sub>	45.029	27.719	1.474	0.706	0.772	0.214	0.706
BaCoO <sub>2</sub>	77.419	27.762	2.050	0.666	0.760	0.483	0.666
BaHgO <sub>2</sub>	45.633	8.740	2.747	0.284	0.358	0.049	0.284
BaMnO <sub>3</sub>	72.401	12.480	2.858	0.519	0.667	0.076	0.519
BaMoO <sub>4</sub>	52.397	24.352	1.765	0.659	0.733	0.367	0.659
BaO <sub>2</sub>	70.113	35.462	1.675	0.742	0.820	1.682	1.682
BaTa <sub>2</sub> O <sub>6</sub>	160.878	84.962	1.630	1.086	1.197	0.776	1.086
BaTiO <sub>3</sub>	163.849	107.202	1.415	1.444	1.574	12.889	12.889
BaV <sub>6</sub> O <sub>11</sub>	166.546	51.414	2.218	1.268	1.474	0.441	1.268
BaWO <sub>4</sub>	49.562	22.915	1.771	0.556	0.618	0.489	0.556



BaZnO <sub>2</sub>	79.781	32.948	1.893	0.707	0.795	0.740	0.740
BaZrO <sub>3</sub>	148.340	93.162	1.455	1.211	1.322	10.226	10.226
Ca <sub>2</sub> Hf <sub>7</sub> O <sub>16</sub>	188.244	91.240	1.720	1.184	1.312	0.895	1.184
Ca <sub>2</sub> MnO <sub>4</sub>	120.441	68.360	1.556	1.517	1.665	2.026	2.026
Ca <sub>2</sub> Nb <sub>2</sub> O <sub>7</sub>	140.721	88.295	1.456	1.526	1.666	4.023	4.023
Ca <sub>2</sub> Ta <sub>2</sub> O <sub>7</sub>	155.654	97.299	1.459	1.327	1.449	3.778	3.778
CaCrO <sub>4</sub>	17.264	27.497	0.713	0.862	0.970	5.062	5.062
CaMoO <sub>4</sub>	67.730	33.595	1.696	0.972	1.076	1.051	1.051
CaO	105.983	75.109	1.338	1.528	1.662	21.468	21.468
CaO <sub>2</sub>	70.875	47.407	1.393	1.346	1.466	7.369	7.369
CaTa <sub>2</sub> O <sub>6</sub>	160.749	35.484	2.592	0.809	0.992	0.176	0.809
CaTa <sub>4</sub> O <sub>11</sub>	165.369	33.330	2.692	0.770	0.959	0.149	0.770
CaV <sub>4</sub> O <sub>9</sub>	42.214	37.634	1.133	1.077	1.171	1.728	1.728
CdIn <sub>2</sub> O <sub>4</sub>	122.470	45.614	2.008	0.864	0.982	0.850	0.864
CdO <sub>2</sub>	107.251	36.554	2.107	0.868	0.997	0.617	0.868
CoO <sub>2</sub>	43.671	6.573	2.997	0.502	0.664	0.056	0.502
Cr <sub>2</sub> O <sub>3</sub>	206.172	114.571	1.578	1.974	2.168	3.286	3.286
Cs <sub>2</sub> V <sub>5</sub> O <sub>13</sub>	25.348	8.231	2.161	0.447	0.517	0.069	0.447
Fe <sub>2</sub> O <sub>3</sub>	191.441	85.539	1.808	1.678	1.872	1.619	1.678
Ga <sub>2</sub> O <sub>3</sub>	199.308	87.752	1.824	1.581	1.767	1.470	1.581
GeO <sub>2</sub>	52.015	26.520	1.667	0.843	0.931	0.902	0.902
HfO <sub>2</sub>	254.816	115.216	1.795	1.296	1.444	8.581	8.581
In <sub>2</sub> O <sub>3</sub>	118.390	55.450	1.757	0.979	1.088	0.692	0.979
K <sub>2</sub> V <sub>3</sub> O <sub>8</sub>	40.422	19.441	1.729	0.787	0.872	0.347	0.787

$K_2Zn_6O_7$	70.566	27.503	1.957	0.827	0.935	0.292	0.827
$K_4Zr_5O_{12}$	128.410	54.349	1.867	1.152	1.291	1.211	1.211
$K_5V_3O_{10}$	5.491	1.795	2.153	0.238	0.274	0.003	0.238
$K_6CdO_4$	32.155	15.079	1.756	0.580	0.645	0.254	0.580
$KO_3$	21.848	6.988	2.178	0.539	0.623	0.076	0.539
$KReO_4$	29.160	7.627	2.404	0.381	0.454	0.058	0.381
$Li_3CuO_3$	50.888	36.284	1.333	1.370	1.490	1.138	1.370
$Mg(RhO_2)_2$	174.460	53.906	2.217	1.160	1.348	0.857	1.160
$Mg_2Mo_3O_8$	129.549	55.769	1.848	1.266	1.417	0.908	1.266
$Mg_3Nb_6O_{11}$	180.711	89.631	1.696	1.478	1.635	2.640	2.640
$Mg_4Nb_2O_9$	142.786	68.198	1.736	1.561	1.732	2.814	2.814
$Mg_6MnO_8$	131.662	100.013	1.274	2.093	2.275	8.164	8.164
$MgCr_2O_4$	159.369	77.780	1.713	1.692	1.874	3.008	3.008
$MgO_2$	122.826	82.654	1.388	2.093	2.280	6.261	6.261
$MgTa_2O_6$	182.312	94.648	1.648	1.314	1.450	2.817	2.817
$MgTiO_3$	159.352	81.970	1.658	1.869	2.062	2.131	2.131
$Mn_3O_4$	130.113	44.306	2.108	1.179	1.354	0.827	1.179
$MnO$	146.459	64.486	1.824	1.353	1.511	6.726	6.726
$Na_{14}Cd_2O_9$	44.199	27.897	1.450	0.940	1.026	0.802	0.940
$Na_2O_2$	52.683	29.695	1.563	1.201	1.318	1.259	1.259
$Na_2Ta_4O_{11}$	160.990	55.703	2.090	1.012	1.160	0.347	1.012
$Na_3CoO_2$	13.838	17.041	0.881	0.676	0.744	1.239	1.239
$Na_4Ti_5O_{12}$	128.665	61.167	1.741	1.572	1.745	1.656	1.656
$NaNbO_2$	125.719	97.398	1.256	1.567	1.703	10.082	10.082

NaNbO <sub>3</sub>	79.316	35.171	1.816	1.020	1.139	0.511	1.020
Nb <sub>2</sub> O <sub>5</sub>	151.015	64.298	1.860	1.254	1.405	0.833	1.254
NbO <sub>2</sub>	212.585	80.208	1.993	1.402	1.591	0.871	1.402
Pb <sub>3</sub> O <sub>4</sub>	37.066	10.815	2.281	0.312	0.365	0.047	0.312
PoO <sub>2</sub>	163.502	73.207	1.805	0.927	1.034	4.868	4.868
Rb <sub>3</sub> TaO <sub>8</sub>	32.511	11.901	2.027	0.474	0.540	0.162	0.474
Rb <sub>3</sub> V <sub>5</sub> O <sub>14</sub>	46.249	21.216	1.779	0.756	0.842	1.205	1.205
RbScO <sub>2</sub>	94.065	57.446	1.482	1.119	1.223	3.934	3.934
Rh <sub>2</sub> O <sub>3</sub>	225.174	99.901	1.815	1.428	1.595	1.666	1.666
Sb <sub>2</sub> O <sub>3</sub>	13.380	9.099	1.377	0.354	0.385	0.160	0.354
Sc <sub>2</sub> O <sub>3</sub>	163.170	80.545	1.701	1.684	1.864	1.755	1.755
SeO <sub>2</sub>	23.003	10.615	1.773	0.507	0.564	0.117	0.507
SiO <sub>2</sub>	4.466	25.179	0.227	0.690	1.012	12.546	12.546
SnO <sub>2</sub>	172.945	85.281	1.702	1.278	1.414	5.139	5.139
Sr <sub>3</sub> V <sub>2</sub> O <sub>7</sub>	136.461	72.258	1.627	1.307	1.440	3.222	3.222
Sr <sub>6</sub> (CoO <sub>3</sub> ) <sub>5</sub>	42.500	47.417	0.954	0.977	1.069	3.453	3.453
SrMoO <sub>4</sub>	63.350	31.011	1.710	0.825	0.913	0.906	0.906
SrO <sub>2</sub>	74.651	40.367	1.606	0.958	1.053	3.780	3.780
SrTa <sub>4</sub> O <sub>11</sub>	173.097	24.156	3.071	0.643	0.866	0.070	0.643
SrTiO <sub>3</sub>	169.469	109.170	1.430	1.674	1.826	5.317	5.317
SrV <sub>13</sub> O <sub>18</sub>	139.227	110.175	1.237	1.806	1.962	2.347	2.347
SrWO <sub>4</sub>	53.623	28.202	1.635	0.670	0.739	0.750	0.750
SrZrO <sub>3</sub>	148.877	81.159	1.597	1.271	1.398	7.293	7.293
Te <sub>4</sub> O <sub>9</sub>	37.347	18.330	1.707	0.582	0.644	0.347	0.582

TeO <sub>3</sub>	99.154	97.622	1.051	1.395	1.520	13.642	13.642
TiO <sub>2</sub>	213.729	111.104	1.647	2.051	2.262	9.814	9.814
V <sub>2</sub> O <sub>3</sub>	193.063	64.784	2.124	1.524	1.753	0.667	1.524
VO <sub>2</sub>	234.644	117.597	1.685	2.089	2.309	9.701	9.701
Y <sub>2</sub> O <sub>3</sub>	137.879	64.126	1.765	1.141	1.269	1.064	1.141
ZnO <sub>2</sub>	144.282	62.406	1.843	1.422	1.591	1.784	1.784
ZrO <sub>2</sub>	165.676	52.087	2.197	1.150	1.335	1.485	1.485

## References

1. J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou and K. Burke, *Phys. Rev. Lett.*, 2008, **100**, 136406.
2. S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys and A. P. Sutton, *Phys. Rev. B*, 1998, **57**, 1505–1509.
3. T. Liu, M. Dupuis and C. Li, *J. Phys. Chem. C*, 2016, **120**, 6930–6937.
4. A. I. Liechtenstein, V. I. Anisimov and J. Zaanen, *Phys. Rev. B*, 1995, **52**, R5467–R5470.
5. S. Okamoto, A. J. Millis and N. A. Spaldin, *Phys. Rev. Lett.*, 2006, **97**, 056802.
6. J. Heyd, G. E. Scuseria and M. Ernzerhof, *J. Chem. Phys.*, 2003, **118**, 8207–8215.
7. S. Chen, Y. Qi, G. Liu, J. Yang, F. Zhang and C. Li, *Chem. Commun.*, 2014, **50**, 14415–14417.
8. F. Subhan, S. Azam, G. Khan, M. Irfan, S. Muhammad, A. G. Al-Sehemi, S. H. Naqib, R. Khenata, S. Khan, I. V. Kityk and B. Amin, *J. Alloys Compd.*, 2019, **785**, 232-239.
9. W. Li, J. Carrete, N. A. Katcho and N. Mingo, *Comput. Phys. Commun.*, 2014, **185**, 1747–1758.
10. A. Togo, F. Oba and I. Tanaka, *Phys. Rev. B*, 2008, **78**, 134106.
11. H. Muta, K. Kurosaki and S. Yamanaka, *J. Alloys Compd.*, 2005, **392**, 306-309.