

## Supplementary materials

The Raman spectroscopy was used to analyze the relationship between dielectric properties and crystal structure of BNT-AGx ceramics in this work. As shown in Table S1, for all 8d and 4c wyckoff positions with one 4a position, BNT-AGx structure belonged to the space group Pbnm and had 8 types vibration modes in lattice:  $A_g$ ,  $A_u$ ,  $B_{1g}$ ,  $B_{1u}$ ,  $B_{2g}$ ,  $B_{2u}$ ,  $B_{3g}$  and  $B_{3u}$  based on the group theory and  $D_{2h}$  point group. The irreducible representations for the structure were obtained by the following equation<sup>[1]</sup>:

$$n_m = \frac{1}{h} \sum_R \chi(R) U(R) (\pm 1 + 2\cos\theta_R)$$

Here,  $n_m$  was the number of vibrational modes with a symmetry presented by the  $m$ th irreducible representation, the  $h=8$  was derived from the order of vector group that made up of all symmetry elements  $R$ ,  $\chi(R)$  was the reducible representation of  $R$ ,  $U(R)$  was the number of atoms under the symmetry operations of space group, and  $(\pm 1 + 2\cos\theta_R)$  was the trace of the matrix  $R$ .

Table 1 Data used for irreducible representation analysis

$D_{2h}$	R								Functions	Number of vibration modes
	E	$C_2^z$	$C_2^y$	$C_2^x$	I	$\sigma_{xy}$	$\sigma_{xz}$	$\sigma_{yz}$		
$A_g$	1	1	1	1	1	1	1	1	$x^2, y^2, z^2$	71
$B_{1g}$	1	1	-1	-1	1	1	-1	-1	$xy, J_z$	55
$B_{2g}$	1	-1	1	-1	1	-1	1	-1	$xz, J_y$	71
$B_{3g}$	1	-1	-1	1	1	-1	-1	1	$yz, J_x$	55
$A_u$	1	1	1	1	-1	-1	-1	-1	-	58
$B_{1u}$	1	1	-1	-1	-1	-1	1	1	$z$	74
$B_{2u}$	1	-1	1	-1	-1	1	-1	1	$y$	58
$B_{3u}$	1	-1	-1	1	-1	1	1	-1	$x$	74
U(R)	172	0	0	0	4	64	0	0		
$\pm 1 + 2\cos\theta_R$	3	-1	-1	-1	-3	1	1	1		

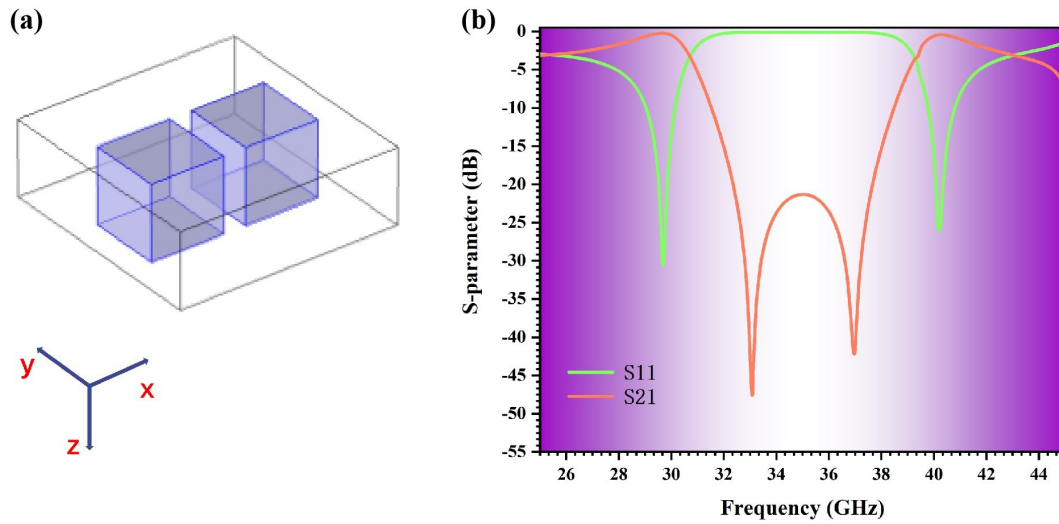


Fig. S1 Simulated results of (a) the BNT-AGx reflective filter unit cell structure and (b) the S-parameter.

Here, we utilized a dimer structure ( $1 \times 1 \times 1 \text{ mm}^3$ , in Fig. S1(a)) embedded in FR4 ( $p=3 \text{ mm}$ , the distance between two blocks was  $1 \text{ mm}$ ) to achieve the mode coupling between BNT-AGx blocks, forming a broadband reflective filter. The transmission stop-band was about  $7 \text{ GHz}$  (@  $10 \text{ dB}$ ) with low insertion loss about  $0.5 \text{ dB}$ , as shown in Fig. S1(b).

## Reference

- [1] S. R. Zhang, Z. X. Fang, Z. Xiong, B. Tang, C. T. Yang, *J. Alloys Compd.* **2017**, 723, 580.