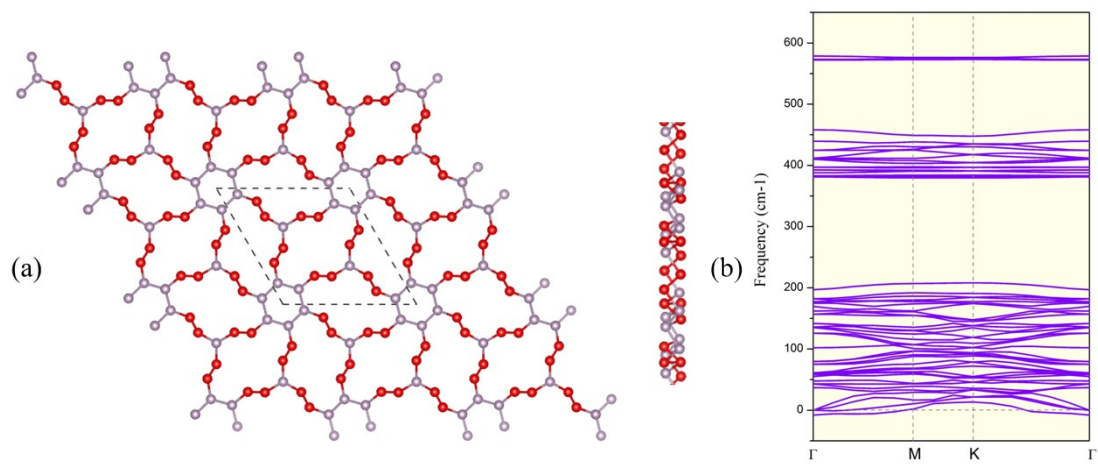
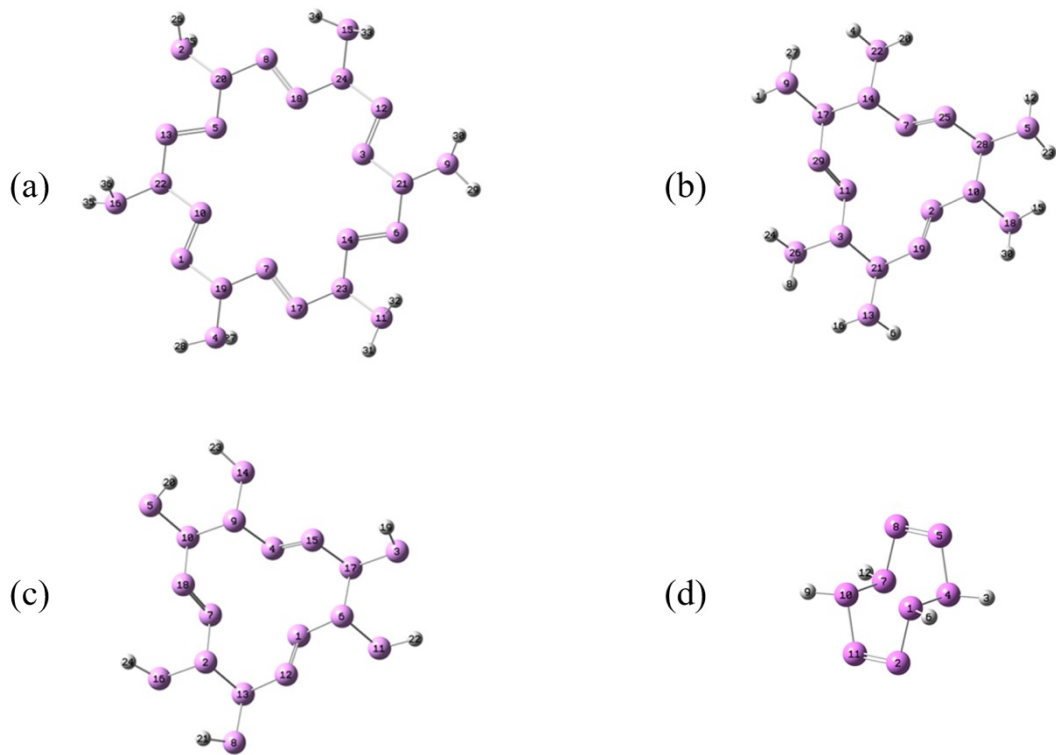


## Supplemental information

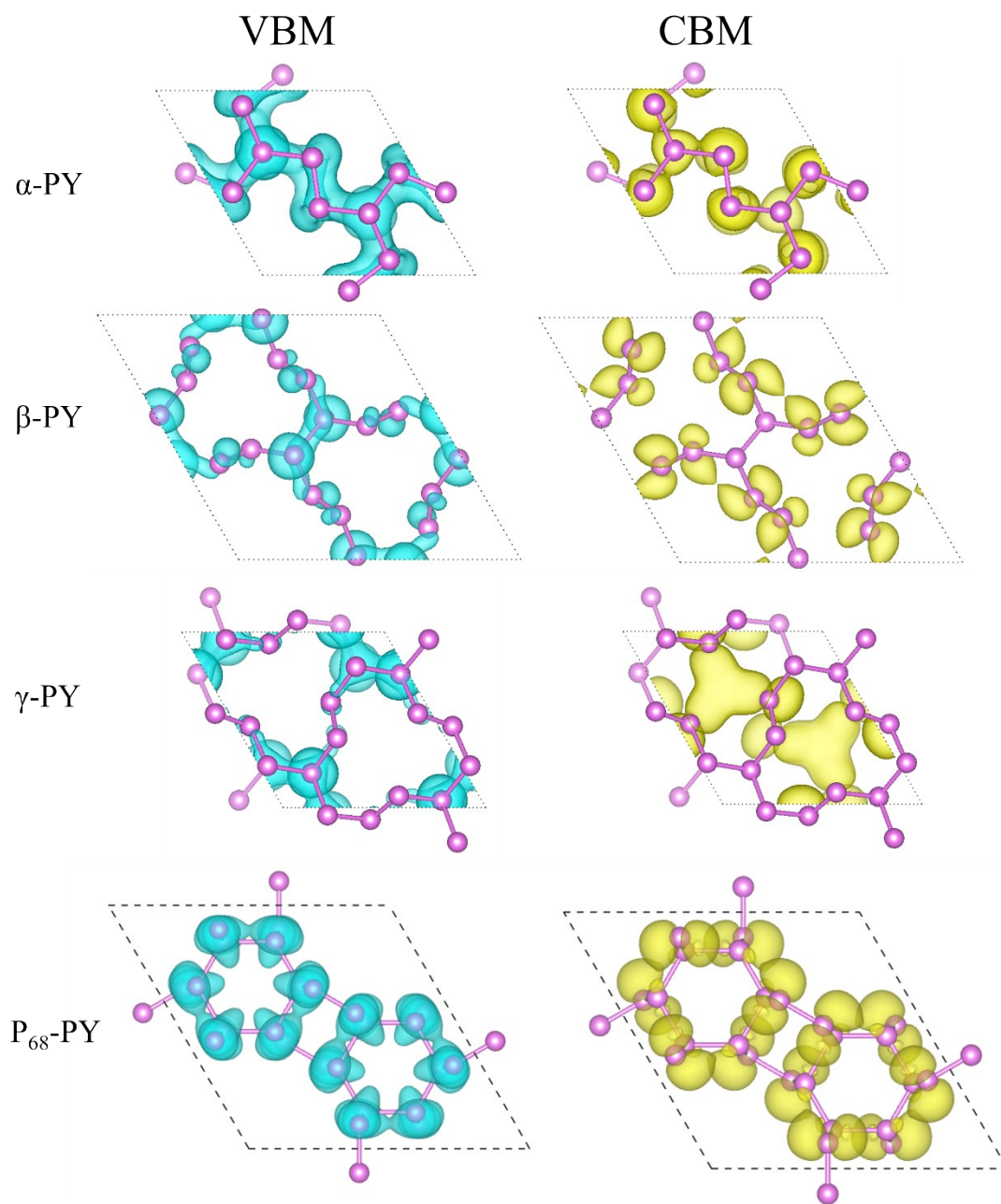
Excavate the missing piece of unsaturated two-dimensional  
phosphorous: a theoretical approach



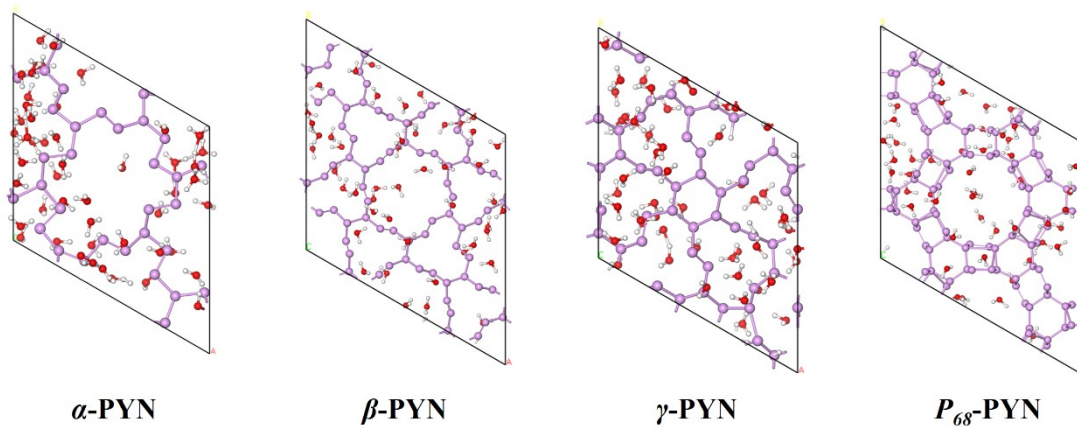
**Figure S1.** (a) optimized structure of  $\delta$ -PY and (b) its phonon dispersion. The existence of inescapable soft modes illustrates its unstable nature, dynamically.



**Figure S2.** Smallest unit of (a)  $\alpha$ -, (b)  $\beta$ -, (c)  $\gamma$ - and (d)  $P_{68}$ -PY used in NBO analysis



**Figure S3.** Density profile of the electron at valence band maximum and conduction band minimum for PY monolayers



**Figure S4.** Snapshot of 5 ps AIMD simulations of PY in wet surroundings; water molecules are more favorable to approach  $sp^2$  phosphorous atoms, and some H atoms are dissociated from water molecules and bind to PY surface or even forming  $H_2$ .

**Table S1** Structural parameters of phosphoryne allotropes

	Angle (°)			
	$sp^2-sp^2-sp^3$	$sp^2-sp^3-sp^2$	$sp^2-sp^3-sp^3$	$sp^3-sp^3-sp^3$
$\alpha$ -PY	99.26	104.71	/	/
$\beta$ -PY	94.32	94.63	94.49	/
$\gamma$ -PY	93.66	/	89.90	94.45
$P_{68}$ -PY	103.12	/	94.45/100.12	109.99

**Table S2** Second-Order Perturbation Theory Analysis of Fock Matrix in the NBO Basis corresponding to the intramolecular bonds of the unit of  $\beta$ -,  $\gamma$ - and  $P_{68}$ -PY at M062x/6-311G+(d, p) theoretical level

	donor(i)	acceptor (j)	E <sup>(2)</sup> Kcal/mol
$\beta$ -PY	$\sigma(\text{P}_3\text{-P}_{26})$	$\pi^*(\text{P}_{11}\text{-P}_{29})$	3.71
	$\sigma(\text{P}_3\text{-P}_{21})$	$\pi^*(\text{P}_2\text{-P}_{19})$	3.54
	$\sigma(\text{P}_{10}\text{-P}_{18})$	$\pi^*(\text{P}_2\text{-P}_{19})$	4.03
	$\sigma(\text{P}_{10}\text{-P}_{28})$	$\pi^*(\text{P}_7\text{-P}_{25})$	3.52
	$\sigma(\text{P}_{14}\text{-P}_{17})$	$\pi^*(\text{P}_{11}\text{-P}_{29})$	3.57
	$\sigma(\text{P}_{14}\text{-P}_{22})$	$\pi^*(\text{P}_7\text{-P}_{25})$	3.70
$\gamma$ -PY	$\sigma(\text{P}_2\text{-P}_{13})$	$\pi^*(\text{P}_1\text{-P}_{12})$	3.36
	$\sigma(\text{P}_2\text{-P}_{16})$	$\pi^*(\text{P}_7\text{-P}_{18})$	3.82
	$\sigma(\text{P}_6\text{-P}_{11})$	$\pi^*(\text{P}_1\text{-P}_{12})$	3.24
	$\sigma(\text{P}_6\text{-P}_{17})$	$\pi^*(\text{P}_4\text{-P}_{15})$	3.49
	$\sigma(\text{P}_9\text{-P}_{10})$	$\pi^*(\text{P}_7\text{-P}_{18})$	3.42
	$\sigma(\text{P}_9\text{-P}_{14})$	$\pi^*(\text{P}_4\text{-P}_{15})$	2.87
$P_{68}$ -PY	$\sigma(\text{P}_1\text{-P}_4)$	$\pi^*(\text{P}_2\text{-P}_{11})$	2.54
	$\sigma(\text{P}_1\text{-P}_4)$	$\pi^*(\text{P}_5\text{-P}_8)$	2.54
	$\sigma(\text{P}_7\text{-P}_{10})$	$\pi^*(\text{P}_2\text{-P}_{11})$	2.54
	$\sigma(\text{P}_7\text{-P}_{10})$	$\pi^*(\text{P}_5\text{-P}_8)$	2.54

POSCAR of  $\alpha$ -PY

1PY

1.000000000000000		
8.5156002045000001	0.0000000000000000	0.0000000000000000
-4.2578001022000000	7.3747261054999997	0.0000000000000000
0.0000000000000000	0.0000000000000000	17.0466995238999992

P

8

Direct

0.4480800259999995	0.3641400200000007	0.9908799889999997
0.5519200430000026	0.635860060000015	0.0091199880000019
0.6358599280000021	0.0839400030000022	0.9908799889999997
0.3641400129999965	0.9160599909999974	0.0091199880000019
0.9160599630000021	0.5519200359999985	0.9908799889999997
0.0839400099999992	0.4480800230000028	0.0091199880000019
0.6666666759999984	0.3333333530000004	0.0429999999999993
0.3333333200000013	0.6666666409999991	0.9570000379999968



POSCAR of  $\beta$ -PY

2PY

1.000000000000000		
11.8448657177374006	-0.0000001601842046	-0.0000000000000006
-5.9224327200895379	10.2579546960665411	0.0000000000000002
-0.0000000000000004	-0.0000000000000007	24.5453769430127586

P

18

Direct

0.7289198818701266	0.5481343437515349	0.5300306911785526
0.2710800761298771	0.4518655732484618	0.4699692708214442
0.4518655792484623	0.1807855431185956	0.5300306911785455
0.5481343317515339	0.8192144468814035	0.4699692708214442
0.8192144798814098	0.2710800791298666	0.5300306911785526
0.1807855571185897	0.7289199108701325	0.4699692708214442
0.1298144457666268	0.3929831234498806	0.5289430131141586
0.8701855592333700	0.6070168665501186	0.4710569488858383
0.6070168625501182	0.7368312933167473	0.5289430131141586
0.3929831204498839	0.2631686726832569	0.4710569488858383
0.2631686796832540	0.8701855382333719	0.5289430131141586
0.7368313093167416	0.1298144387666227	0.4710569488858383
0.5897847122136355	0.5738607996109977	0.4769332743992862
0.4102152707863667	0.4261391653890030	0.5230667256007138
0.4261391903890015	0.0159238776026385	0.4769332743992862
0.5738608096109985	0.9840761213973650	0.5230667256007138
0.9840760313973647	0.4102152727863668	0.4769332743992862
0.0159238676026376	0.5897846932136375	0.5230667256007138

POSCAR of  $\gamma$ -PY

3PY

1.0000000000000000		
8.6417581362278817	0.0000000630528554	0.0000000000000000
-4.3208791227193153	7.4839820478088788	0.0000000000000000
0.0000000000000000	0.0000000000000000	21.4264348866011964

P

12

Direct

0.0420249493563531	0.2392527660574473	0.0281467971946938
0.9579751056436407	0.7607472149425476	0.9718531728053037
0.7607472699425486	0.8027721682989082	0.0281467971946938
0.2392527560574464	0.1972278577010940	0.9718531728053037
0.1972278457010930	0.9579751176436417	0.0281467971946938
0.8027721072989067	0.0420249463563565	0.9718531728053037
0.5359889135362366	0.6037096993834297	0.9689993870638460
0.4640111074637687	0.3962903416165702	0.0310006609361579
0.3962903386165735	0.9322792831527948	0.9689993870638460
0.6037096963834330	0.0677207358472032	0.0310006609361579
0.0677207208472055	0.4640110704637692	0.9689993870638460
0.9322792581527963	0.5359889405362352	0.0310006609361579

POSCAR of  $P_{68}$ -PY

4PY

1.000000000000000		
12.0612790545750475	-0.0000000136799655	-0.0000000000000002
-6.0306395154145083	10.4453740701894056	0.0000000000000002
-0.00000000000000013	0.0000000000000000	30.3466732144643103

P

24

Direct

0.4821721763218463	0.3323719812229982	0.0008853167870484
0.5178278476781557	0.6676280027770005	0.9991147172129544
0.6676280397770071	0.1498001650988670	0.0008853167870484
0.3323719652229897	0.8501997809011357	0.9991147172129544
0.8501998069011449	0.5178278376781336	0.0008853167870484
0.1498001520988552	0.4821721453218615	0.9991147172129544
0.9012994880273126	0.5577917159673120	0.9301272773173466
0.0987005359726894	0.4422082670326830	0.0698726966826513
0.4422082410326809	0.3435077160600102	0.9301272773173466
0.5577916839673165	0.6564922299399925	0.0698726966826513
0.6564922969400087	0.0987005239726741	0.9301272773173466
0.3435077310599937	0.9012994690273288	0.0698726966826513
0.8500266994207379	0.3322302865493114	0.9992710999610139
0.1499732895792647	0.6677696594506912	0.0007289340389889
0.6677696754506854	0.5177964018714007	0.9992710999610139
0.3322303005493197	0.4822035811285943	0.0007289340389889
0.4822035841285839	0.1499732945792829	0.9992710999610139
0.5177964068714189	0.8500266884207122	0.0007289340389889
0.9015605493449002	0.3437575464078577	0.0699927931147784
0.0984394236550941	0.6562423995921449	0.9300072228852230
0.6562424295921332	0.5578029819370514	0.0699927931147784
0.3437575614078625	0.4421970010629508	0.9300072228852230
0.4421970080629620	0.0984394446550922	0.0699927931147784
0.5578029789370405	0.9015605293449127	0.9300072228852230