

# Encoding hexanitrobenzene (HNB) and 1,3,5-triamino-2,4,6-trinitrobenzene (TATB) as two distinctive energetic nitrobenzene compounds by machine learning

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## Supplementary information

### Table of contents

**S1: HOF calculations for a solid.**

**S2: BDE calculations.**

**S3:  $v_D$  calculations.**

**S4: Oxygen balance (OB%) definition**

**S5: ML results of BDE**

**S6: Top molecules by  $\rho_{ML}$  and  $v_{DML}$ .**

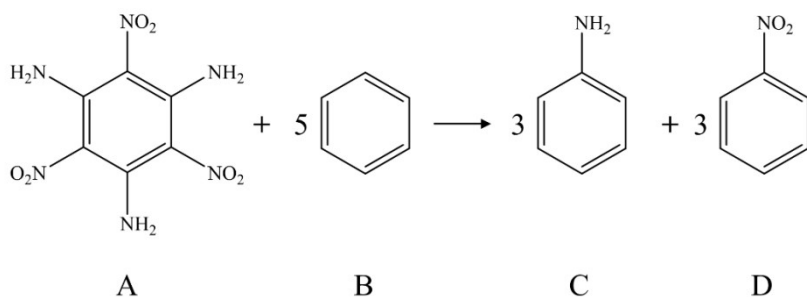
**S7: Performance of ML in predicting BDE of C-NO<sub>2</sub> and N-NO<sub>2</sub>.**

**S8: References**

## S1: HOF calculations for a solid.

### (A) HOF calculations of gaseous molecules

As for the isodesmic reaction, one example of the isodesmic reaction for TATB (compound A) is illustrated in Figure S1. The heat of reaction  $\Delta H_{298}$  at 298 K was calculated on the level of B3LYP method/6-31g(d) with following eq 1:



**Figure S1.** Isodesmic reaction designed for calculating HOF of TATB.

$$\Delta H_{298} = \Delta H_{f, P} - \Delta H_{f, R} \quad (1)$$

where  $\Delta H_{f, R}$  and  $\Delta H_{f, P}$  represent the HOFs of reactants and products at 298 K, respectively. For compounds in the isodesmic reactions with available data, they were directly adopted, as shown in Table S1.

**Table S1.** The HOFs of references compounds from CRC handbook. The unit of  $\Delta H_{f, \text{Exp}}^g$  is kJ/mol.

Name	Molecular structural formula	$\Delta H_{f, \text{Exp}}^g$
Benzene	PhH	82.9
Nitrobenzene	PhNO <sub>2</sub>	68.5
Phenol	PhOH	-96.4
Toluene	PhCH <sub>3</sub>	50.5
Benzoic acid	PhCOOH	-294.0
Anisole	PhOCH <sub>3</sub>	-67.9
Aniline	PhNH <sub>2</sub>	87.5
Acetophenone	PhCOCH <sub>3</sub>	-86.7
Benzaldehyde	PhCHO	-36.7
Benzonitrile	PhCN	215.7
Benzamide	PhCONH <sub>2</sub>	-100.9
Ethoxybenzene	PhOCH <sub>2</sub> CH <sub>3</sub>	-101.6
Ethylbenzene	PhCH <sub>2</sub> CH <sub>3</sub>	29.9

For the compounds in the isodesmic reactions without available experimental HOFs, the atomization scheme was employed with calculations on the G3 level to predict their HOFs, as shown in Table S2. By means of the atomization scheme, the standard HOF of a molecule ( $\Delta H_f^g$ ) can be calculated by eq 2.

$$\Delta H_f^g = \Delta E_{298} + \Delta(PV) = \Delta E_0 + \Delta E_{ZPE} + \Delta E_T + \Delta nRT \quad (2)$$

where  $\Delta E_0$  means the change in total energy between the products and reactants at 0 K;  $\Delta E_{ZPE}$  is the value of difference between the zero-point energies of the products and reactants at 0 K;  $\Delta E_T$  is the thermal correction from 0 to 298 K. The  $\Delta(PV)$  value means the PV work term and equals  $\Delta nRT$  for the reactions of an ideal gas. For the isodesmic reaction in this work,  $\Delta n = 0$ , so  $\Delta(PV) = 0$ . From Table S2, we can confirmed that the largest error is only 6.9 kJ/mol, showing the high reliability of the G3 method.

**Table S2.**  $\Delta H_f^g$  of mono-substituted benzene molecules used for designing isodesmic reactions.  $\Delta H_{fExp}^g$  and  $\Delta H_{fG3}^g$  denote the  $\Delta H_f^g$  derived from experimental measurements and G3 calculations in kJ/mol, respectively.

Functional group			Benzene based compound				
Name	Structure	Symbol	Name	Structure	$\Delta H_{fExp}^g$	$\Delta H_{fG3}^g$	Error
hydro	H $\cdot$	-H	benzene	Ph-H	82.9	87.3	4.4
nitro	$O_2\dot{N}^+$	-NO <sub>2</sub>	nitrobenzene	Ph- $\overset{O}{\parallel}N^+$	68.5	63.4	-5.1
hydroxy	$\dot{O}H$	-OH	phenol	Ph-OH	-96.4	-89.5	6.9
methoxy	$O\dot{-}CH_3$	-OCH <sub>3</sub>	anisole	Ph- $O-CH_3$	-67.9	-69.3	-1.4
methyl	$\dot{C}H_3$	-CH <sub>3</sub>	toluene	Ph-CH <sub>3</sub>	50.5	54.2	3.7
carboxy	$HO-C\dot{-}O$	-COOH	benzoic acid	Ph- $\overset{O}{\parallel}C-OH$	-294.0	-294.3	-0.3
amino	$\dot{N}H_2$	-NH <sub>2</sub>	aniline	Ph-NH <sub>2</sub>	87.5	92.2	4.7
cyano	$C\dot{-}N$	-CN	benzonitrile	Ph- $\equiv N$	215.7	218.6	2.9
acetyl	$H_3C-C\dot{-}O$	-COCH <sub>3</sub>	acetophenone	Ph- $\overset{O}{\parallel}C-CH_3$	-86.7	-81.5	5.2
formyl	$HC\dot{-}O$	-CHO	benzaldehyde	Ph- $\overset{O}{\parallel}C-H$	-36.7	-34.9	1.8

acetylamino		-NHC(=O)CH <sub>3</sub>	<i>N</i> -phenylacetamide			-105.0		
tert-butyl		-C(CH <sub>3</sub> ) <sub>3</sub>	tert-butylbenzene		-23.0	-22.8	0.2	
dimethylamino		-N(CH <sub>3</sub> ) <sub>2</sub>	<i>N,N</i> -dimethylaniline			102.3		
carbamoyl		-CONH <sub>2</sub>	benzamide		-100.9	-94.5	6.4	
ethanoxy		-OCH <sub>2</sub> CH <sub>3</sub>	ethoxybenzene		-101.6	-99.8	1.8	
isopropyl		-CH(CH <sub>3</sub> ) <sub>2</sub>	<b>cumene</b>			<b>4.9</b>		
acetoxyl		-OOCCH <sub>3</sub>	phenyl acetate			-275.0		
hydroxymethyl		-CH <sub>2</sub> OH	phenylmethanol			-88.5		
carboxymethyl		-CH <sub>2</sub> COOH	phenylacetic acid			-297.3		
(hydroxyimino)methyl		-CHNOH	benzaldehyde oxime			134.5		
hydrazinecarbonyl		-CONHNH <sub>2</sub>	benzohydrazide			21.0		
methylamino		-NHCH <sub>3</sub>	<i>N</i> -methylaniline			97.9		
ethyl		-CH <sub>2</sub> CH <sub>3</sub>	ethylbenzene		29.9	32.3	2.4	
formamino		-NHCHO	<i>N</i> -phenylformamide			-55.7		
prop-2-yn-1-oxy		-OCH <sub>2</sub> C≡CH	(prop-2-yn-1-yloxy)benzene			191.6		
isopropylamino		-NHCH(CH <sub>3</sub> ) <sub>2</sub>	<i>N</i> -isopropylaniline			35.6		
ethynyl		-C≡CH	ethynylbenzene			322.5		
methylcarbamoyl		-CONHCH <sub>3</sub>	<i>N</i> -methylbenzamide			-96.1		

<i>N'</i> -hydroxycarbami midoyl		-CNH <sub>2</sub> NOH	<i>N'</i> -hydroxybenzimidamide		114.0	
cyanomethoxy		-OCH <sub>2</sub> CN	phenoxyacetonitrile		90.4	
cyanomethyl		-CH <sub>2</sub> CN	phenylacetonitrile		201.3	
1-(hydroxyimino)ethyl		-CCH <sub>3</sub> NOH	1-phenylethan-1-one oxime		77.3	
methoxymethoxy		-OCH <sub>2</sub> OCH <sub>3</sub>	(methoxymethoxy) benzene		-225.7	
propionyl		-COCH <sub>2</sub> CH <sub>3</sub>	propiophenone		-103.7	
propylamino		-NHCH <sub>2</sub> CH <sub>2</sub> CH <sub>3</sub>	<i>N</i> -propylaniline		48.2	
methyl(nitro)amino		-NCH <sub>3</sub> NO <sub>2</sub>	<i>N</i> -methyl- <i>N</i> -phenylnitramide		132.8	
azido		-NNN	azidobenzene		419.9	
3-oxoprop-1-en-1-yl		-CHCHCHO	cinnamaldehyde		27.9	
2-hydroxypropan-2-yl		-COH(CH <sub>3</sub> ) <sub>2</sub>	2-phenylpropan-2-ol		-170.9	
prop-1-en-1-yl		-CHCHCH <sub>3</sub>	prop-1-en-1-ylbenzene		120.8	

### (B) HOF calculations for a solid

As most energetic compounds are in the solid state, the calculation of detonation properties requires solid-phase heat of formation ( $\Delta H_f^s$ ). According to Hess's law of constant heat summation, the solid-phase heat of formation can be acquired from the gas-phase heat of formation ( $\Delta H_f^g$ ) and heat of sublimation ( $\Delta H_{sub}$ ):

$$\Delta H_f^s = \Delta H_f^g - \Delta H_{sub}$$

As for the heat of sublimation, Politzer et al.<sup>3</sup> reported that it correlates with the molecular surface

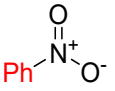
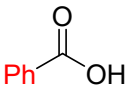
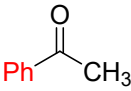
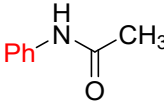
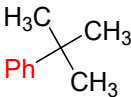
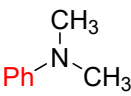
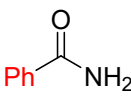
area and the electrostatic interaction  $v\sigma_{tot}^2$  index for energetic compounds. The empirical expression of this approach is as follows:

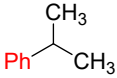
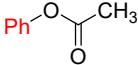

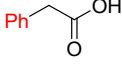
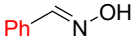
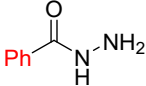
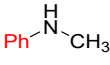
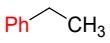
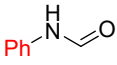
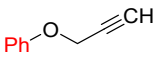
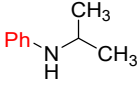
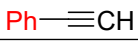
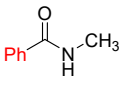
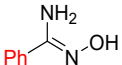
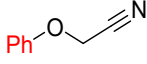
$$\Delta H_{sub} = aA^2 + b(v\sigma_{tot}^2)^{0.5} + c$$

where  $A$  represents the surface area of the 0.001 electrons bohr<sup>-3</sup> isosurface of the electronic density of the molecule,  $v$  describes the degree of balance between positive potential and negative potential on the isosurface, and  $\sigma_{tot}^2$  means a measure of the variability of the electrostatic potential on the molecular surface. The coefficients  $a$ ,  $b$ , and  $c$  have been obtained by Rice et al. for the energetic materials:  $a = 2.670 \times 10^{-4}$  kcal mol<sup>-1</sup> Å<sup>-4</sup>,  $b = 1650$  kcal mol<sup>-1</sup>, and  $c = 2.966$  kcal mol<sup>-1</sup>.<sup>4</sup> The descriptors  $A$ ,  $v$  and  $\sigma_{tot}^2$  were calculated using the Multiwfn program.<sup>5</sup>

## S2: BDE calculations.

**Table S3.** The calculated BDE (in kJ/mol) of forty mono-substituted benzene molecules.  $BDE_{G3}$  and  $BDE_{b3lyp}$  denote BDE calculated by B3LYP/6-31g(d)+D3 and G3 methods, respectively.

Name	Structure	BDE reaction	$BDE_{G3}$	$BDE_{b3lyp}$	Error
benzene	Ph-H	Ph → Ph• + •H	472.6	458.9	-2.9%
nitrobenzene		PhNO <sub>2</sub> → Ph• + •NO <sub>2</sub>	316.0	300.0	-5.1%
phenol	Ph-OH	PhOH → Ph• + •OH	467.8	455.7	-2.6%
anisole	Ph-O-CH <sub>3</sub>	PhOCH <sub>3</sub> → Ph• + •OCH <sub>3</sub>	435.1	406.2	-6.6%
		PhOCH <sub>3</sub> → PhO• + •CH <sub>3</sub>	266.0	253.6	-4.7%
toluene	Ph-CH <sub>3</sub>	PhCH <sub>3</sub> → Ph• + •CH <sub>3</sub>	430.4	418.9	-2.7%
benzoic acid		PhCOOH → Ph• + •COOH	463.7	445.7	-3.9%
aniline	Ph-NH <sub>2</sub>	PhNH <sub>2</sub> → Ph• + •NH <sub>2</sub>	436.2	419.8	-3.8%
benzonitrile	Ph-C≡N	PhCN → Ph• + •CN	572.3	564.2	-1.4%
acetophenone		<b>PhCOCH<sub>3</sub> → Ph• + •COCH<sub>3</sub></b>	<b>416.5</b>	<b>401.3</b>	<b>-3.6%</b>
		PhCOCH <sub>3</sub> → PhCO• + •CH <sub>3</sub>	346.0	341.2	-1.4%
benzaldehyde	Ph-CHO	PhCHO → Ph• + •CHO	419.8	409.6	-2.4%
<i>N</i> -phenylacetamide		PhNHCOCH <sub>3</sub> → Ph• + •NHCOCH <sub>3</sub>	469.7	442.6	-5.8%
		PhNHCOCH <sub>3</sub> → PhNH• + •COCH <sub>3</sub>	351.2	352.0	-2.0%
		PhNHCOCH <sub>3</sub> → PhNHCO• + •CH <sub>3</sub>	359.0	336.3	-4.2%
tert-butylbenzene		PhC(CH <sub>3</sub> ) <sub>3</sub> → Ph• + •C(CH <sub>3</sub> ) <sub>3</sub>	422.0	380.1	-9.9%
<i>N,N</i> -dimethylaniline		PhN(CH <sub>3</sub> ) <sub>2</sub> → Ph• + •N(CH <sub>3</sub> ) <sub>2</sub>	404.4	372.4	-7.9%
benzamide		PhCONH <sub>2</sub> → Ph• + •CONH <sub>2</sub>	427.6	407.6	-4.7%
		PhCONH <sub>2</sub> → PhCO• + •NH <sub>2</sub>	403.0	392.9	-2.5%
ethoxybenzene	Ph-O-CH <sub>2</sub> -CH <sub>3</sub>	PhOCH <sub>2</sub> CH <sub>3</sub> → Ph• + •OCH <sub>2</sub> CH <sub>3</sub>	432.6	402.0	-7.1%
		PhOCH <sub>2</sub> CH <sub>3</sub> → PhO• + •CH <sub>2</sub> CH <sub>3</sub>	276.7	255.5	-7.6%

cumene		$\text{PhCH}(\text{CH}_3)_2 \rightarrow \text{Ph}\cdot + \cdot\text{CH}(\text{CH}_3)_2$	429.8	398.7	-7.2%
phenyl acetate		$\text{PhOOCCH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{OOCCH}_3$	447.0	396.9	-11.2%
phenylmethanol		$\text{PhCH}_2\text{OH} \rightarrow \text{Ph}\cdot + \cdot\text{CH}_2\text{OH}$	417.3	402.9	-3.5%
phenylacetic acid		$\text{PhCH}_2\text{COOH} \rightarrow \text{Ph}\cdot + \cdot\text{CH}_2\text{COOH}$	428.1	405.8	-5.2%
		$\text{PhCH}_2\text{COOH} \rightarrow \text{PhCH}_2\cdot + \cdot\text{COOH}$	333.2	310.4	-6.8%
benzaldehyde oxime		$\text{PhCHNOH} \rightarrow \text{Ph}\cdot + \cdot\text{CHNOH}$	491.8	461.8	-6.1%
		$\text{PhCHNOH} \rightarrow \text{PhCHN}\cdot + \cdot\text{OH}$	246.4	222.7	-9.6%
benzohydrazide		$\text{PhCONHNH}_2 \rightarrow \text{Ph}\cdot + \cdot\text{CONHNH}_2$	435.1	413.2	-5.0%
		$\text{PhCONHNH}_2 \rightarrow \text{PhCONH}\cdot + \cdot\text{NH}_2$	310.0	294.5	-5.0%
<i>N</i> -methylaniline		$\text{PhNHCH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{NHCH}_3$	<b>426.6</b>	<b>401.9</b>	<b>-5.8%</b>
		$\text{PhNHCH}_3 \rightarrow \text{PhNH}\cdot + \cdot\text{CH}_3$	296.4	285.3	-3.8%
ethylbenzene		$\text{PhCH}_2\text{CH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{CH}_2\text{CH}_3$	431.6	405.6	-6.0%
<i>N</i> -phenylformamide		$\text{PhNHCHO} \rightarrow \text{Ph}\cdot + \cdot\text{NHCHO}$	475.4	449.2	-5.5%
(prop-2-yn-1-yloxy)benzene		$\text{PhOCH}_2\text{CCH} \rightarrow \text{Ph}\cdot + \cdot\text{OCH}_2\text{CCH}$	434.9	403.5	-7.2%
		$\text{PhOCH}_2\text{CCH} \rightarrow \text{PhO}\cdot + \cdot\text{CH}_2\text{CCH}$	215.7	184.4	-14.5%
<i>N</i> -isopropylaniline		$\text{PhNHCH}(\text{CH}_3)_2 \rightarrow \text{Ph}\cdot + \cdot\text{NHCH}(\text{CH}_3)_2$	431.8	405.5	-6.1%
		$\text{PhNHCH}(\text{CH}_3)_2 \rightarrow \text{PhNH}\cdot + \cdot\text{CH}(\text{CH}_3)_2$	309.5	280.4	-9.4%
ethynylbenzene		$\text{PhCCH} \rightarrow \text{Ph}\cdot + \cdot\text{CCH}$	591.8	581.6	-1.7%
<i>N</i> -methylbenzamide		$\text{PhCONHCH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{CONHCH}_3$	432.4	410.1	-5.2%
		$\text{PhCONHCH}_3 \rightarrow \text{PhCO}\cdot + \cdot\text{NHCH}_3$	401.5	382.1	-4.8%
<i>N'</i> -hydroxybenzimidamide		$\text{PhCNH}_2\text{NOH} \rightarrow \text{Ph}\cdot + \cdot\text{CNH}_2\text{NOH}$	470.6	444.8	-5.5%
phenoxyacetonitrile		$\text{PhOCH}_2\text{CN} \rightarrow \text{Ph}\cdot + \cdot\text{OCH}_2\text{CN}$	436.5	405.1	-7.2%



1-phenylethan-1-one oxime		$\text{PhCH}_2\text{CN} \rightarrow \text{Ph}\cdot + \cdot\text{CH}_2\text{CN}$	402.2	371.6	-7.6%
1-phenylethan-1-one oxime		$\text{PhCCH}_3\text{NOH} \rightarrow \text{Ph}\cdot + \cdot\text{CCH}_3\text{NOH}$	475.1	445.7	-6.2%
(methoxymethoxy)benzene		$\text{PhOCH}_2\text{OCH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{OCH}_2\text{OCH}_3$	425.2	389.9	-8.3%
		$\text{PhOCH}_2\text{OCH}_3 \rightarrow \text{PhOCH}_2\cdot + \cdot\text{OCH}_3$	365.5	339.5	-7.1%
		$\text{PhOCH}_2\text{OCH}_3 \rightarrow \text{PhOCH}_2\text{O}\cdot + \cdot\text{CH}_3$	343.2	324.9	-5.3%
propiophenone		$\text{PhCOCH}_2\text{CH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{COCH}_2\text{CH}_3$	418.5	401.8	-4.0%
		$\text{PhCOCH}_2\text{CH}_3 \rightarrow \text{PhCO}\cdot + \cdot\text{CH}_2\text{CH}_3$	348.1	335.1	-3.7%
<i>N</i> -propylaniline		$\text{PhNHCH}_2\text{CH}_2\text{CH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{NHCH}_2\text{CH}_2\text{CH}_3$	431.8	404.8	-6.3%
<i>N</i> -propylaniline		$\text{PhNHCH}_2\text{CH}_2\text{CH}_3 \rightarrow \text{PhNH}\cdot + \cdot\text{CH}_2\text{CH}_2\text{CH}_3$	<b>309.8</b>	<b>288.4</b>	<b>-6.9%</b>
<i>N</i> -methyl- <i>N</i> -phenylnitramide		$\text{PhNCH}_3\text{NO}_2 \rightarrow \text{Ph}\cdot + \cdot\text{NCH}_3\text{NO}_2$	416.9	391.4	-6.1%
		$\text{PhNCH}_3\text{NO}_2 \rightarrow \text{PhNCH}_3\cdot + \cdot\text{NO}_2$	153.7	134.9	-12.2%
		$\text{PhNCH}_3\text{NO}_2 \rightarrow \text{PhNNO}_2\cdot + \cdot\text{CH}_3$	294.1	285.3	-3.0%
azidobenzene		$\text{PhNNN} \rightarrow \text{Ph}\cdot + \cdot\text{NNN}(\cdot\text{N}_3)$	379.1	356.2	-6.0%
		$\text{PhNNN} \rightarrow \text{PhN}\cdot + \cdot\text{N}_2$	-0.7	5.2	-797.8%
cinnamaldehyde		$\text{PhCHCHCHO} \rightarrow \text{Ph}\cdot + \cdot\text{CHCHCHO}$	503.9	489.8	-2.8%
2-phenylpropan-2-ol		$\text{PhCOH}(\text{CH}_3)_2 \rightarrow \text{Ph}\cdot + \cdot\text{COH}(\text{CH}_3)_2$	419.6	386.6	-7.8%
prop-1-en-1-ylbenzene		$\text{PhCHCHCH}_3 \rightarrow \text{Ph}\cdot + \cdot\text{CHCHCH}_3$	493.6	480.9	-2.6%

### S3: $v_D$ calculations.

#### 1. Kamlet–Jacobs equations<sup>2</sup>:

$$p = 1.558\rho_0^2\varphi$$

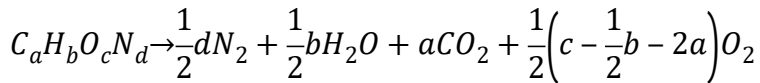
$$v_D = 1.01\varphi^{\frac{1}{2}}(1 + 1.30\rho_0)$$

$$\varphi = 0.489N\bar{M}^{\frac{1}{2}}Q^{\frac{1}{2}}$$

where  $p$  is the C-J denotation pressure, in unit of GPa;  $v_D$  is the denotation velocity, in unit of km/s;  $\rho_0$  is the density of EMs, in unit of g/cm<sup>3</sup>;  $N$  is the amount of generated gaseous products per gram EMs, in unit of mol/g;  $\bar{M}$  is the mean molar mass of gaseous products, in unit of g/mol;  $Q$  is the denotation heat of EMs, in unit of J/g.

For EMs of c.f.  $C_aH_bO_cN_d$ :

(1) When  $c \geq 2a + \frac{b}{2}$ , the reaction equation is:



The mean molar mass of the EM is:

$$M = 12a + b + 16c + 14d$$

$N$ ,  $\bar{M}$  and  $Q$  are:

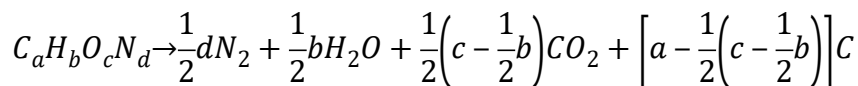
$$N = \frac{1}{4M}(b + 2c + 2d)$$

$$\bar{M} = \frac{28d + 18b + 88a + 16(2c - b - 4a)}{d + b + 2a + \left(c - \frac{1}{2}b - 2a\right)} = \frac{24a + 2b + 32c + 28d}{\frac{1}{2}b + c + d} = \frac{4M}{b + 2c + 2d}$$

$$Q = \frac{28.9b + 94.1a - 0.239\Delta H_f^0}{M} \times 4.184 \times 10^3$$

where  $\Delta H_f^0$  is the standard formation enthalpy of the EM;  $\Delta H_f^0[N_2(g)] = 0$ ,  $\Delta H_f^0[H_2O(g)] = 57.8 \text{ kcal/mol}$ ,  $\Delta H_f^0[CO_2(g)] = 94.1 \text{ kcal/mol}$ ,  $\Delta H_f^0[O_2(g)] = 0 \text{ kcal/mol}$ ,  $\Delta H_f^0[C(s)] = 0 \text{ kcal/mol}$ .

(2) When  $2a + \frac{b}{2} > c \geq \frac{b}{2}$ , the reaction equation is:



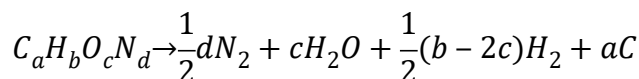
$N$ ,  $\bar{M}$  and  $Q$  are:

$$N = \frac{1}{4M}(b + 2c + 2d)$$

$$\bar{M} = \frac{56d + 88c - 8b}{b + 2c + 2d}$$

$$Q = \frac{28.9b + 94.1\left(\frac{c}{2} - \frac{b}{4}\right) - 0.239\Delta H_f^0}{M} \times 4.184 \times 10^3$$

(3) When  $\frac{b}{2} > c$ , the reaction equation is:



$N$ ,  $\bar{M}$  and  $Q$  are:

$$N = \frac{1}{2M}(b + d)$$

$$\bar{M} = \frac{2b + 32c + 28d}{b + d}$$

$$Q = \frac{57.8c - 0.239\Delta H_f^0}{M} \times 4.184 \times 10^3$$

#### S4: Oxygen balance (OB%) definition

For EMs in c.f.  $C_aH_bO_cN_d$ :

$$OB\% = \frac{c - \frac{1}{2}b - 2a}{c} \times 100\%$$

#### S5: ML results of BDE

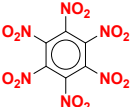
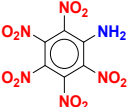
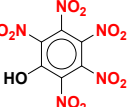
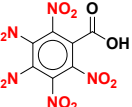
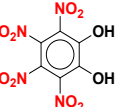
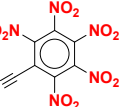
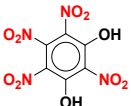
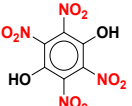
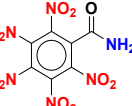
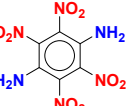
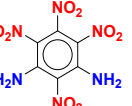
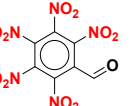
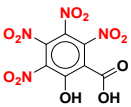
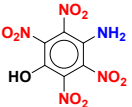
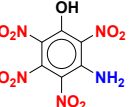
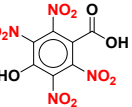
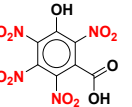

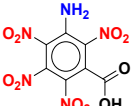
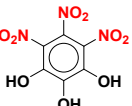
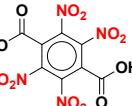
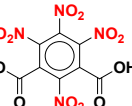
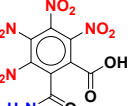
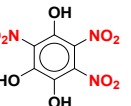
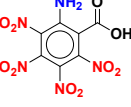
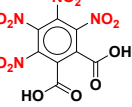
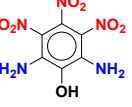
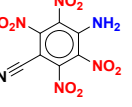
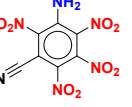
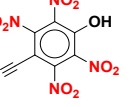
**Table S4.** Test scores of the ML models of BDE. The results of the best models are highlighted in bold.

		Ridge	Lasso	SVR	RFR	GBR	MLP	Ensemble	GRU
<b>BDE</b> <sub>C-NO<sub>2</sub></sub>	RMSE	11.60	11.42	10.96	11.89	11.37	<b>10.60</b>	10.77	11.09
(kJ·mol <sup>-1</sup> )	MAE	8.73	8.62	8.11	9.00	8.55	<b>8.02</b>	8.05	8.01

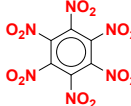
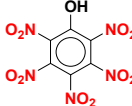
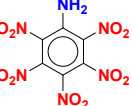
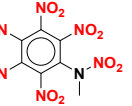
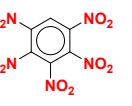
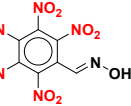
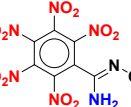
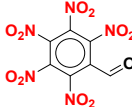
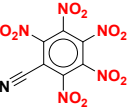
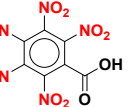

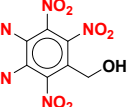
	R <sup>2</sup>	0.730	0.738	0.759	0.716	0.741	<b>0.775</b>	0.767	0.753
<b>BDE<sub>N-NO2</sub></b> (kJ·mol <sup>-1</sup> )	RMSE	13.64	<b>13.4</b>	13.91	13.68	13.71	13.97	13.51	13.71
	MAE	10.72	<b>10.61</b>	10.89	10.81	10.81	10.92	10.64	10.85
	R <sup>2</sup>	0.258	<b>0.276</b>	0.229	0.254	0.251	0.223	0.272	0.251


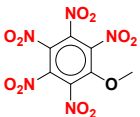
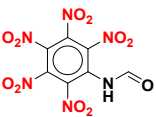
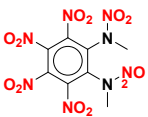
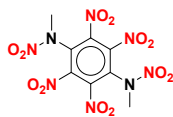
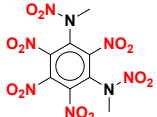
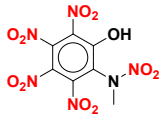
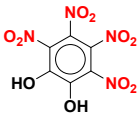

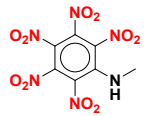
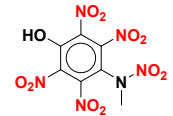
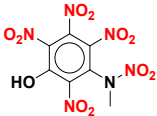

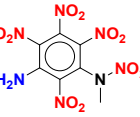
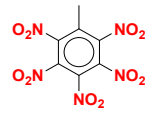
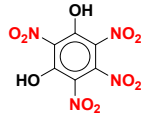
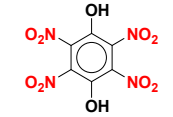

### S6: Top molecules by $\rho_{ML}$ and $\nu_{DML}$ .

**Table S5.** Top 30 Molecules by  $\rho_{ML}$ .  $\rho_{ML}$  and  $\nu_{DML}$  are in  $\text{g cm}^{-3}$  and  $\text{m s}^{-1}$ , respectively.

Structure						
$\rho$	1.942	1.925	1.923	1.916	1.910	1.904
$\nu_D$	9266	8897	8910	8664	8539	8701
Structure						
$\rho$	1.903	1.903	1.899	1.899	1.899	1.897
$\nu_D$	8468	8468	8611	8415	8415	8704
Structure						
$\rho$	1.896	1.896	1.896	1.896	1.896	1.895
$\nu_D$	8246	8427	8427	8229	8229	8207
Structure						
$\rho$	1.895	1.894	1.893	1.893	1.892	1.887
$\nu_D$	8207	8072	8037	8037	8048	7989
Structure						
$\rho$	1.886	1.886	1.885	1.884	1.884	1.883
$\nu_D$	8210	8034	8456	8264	8264	8278

**Table S6.** Top 30 Molecules by  $\nu_{DML}$ .  $\rho_{ML}$  and  $\nu_{DML}$  are in  $\text{g cm}^{-3}$  and  $\text{m s}^{-1}$ , respectively.

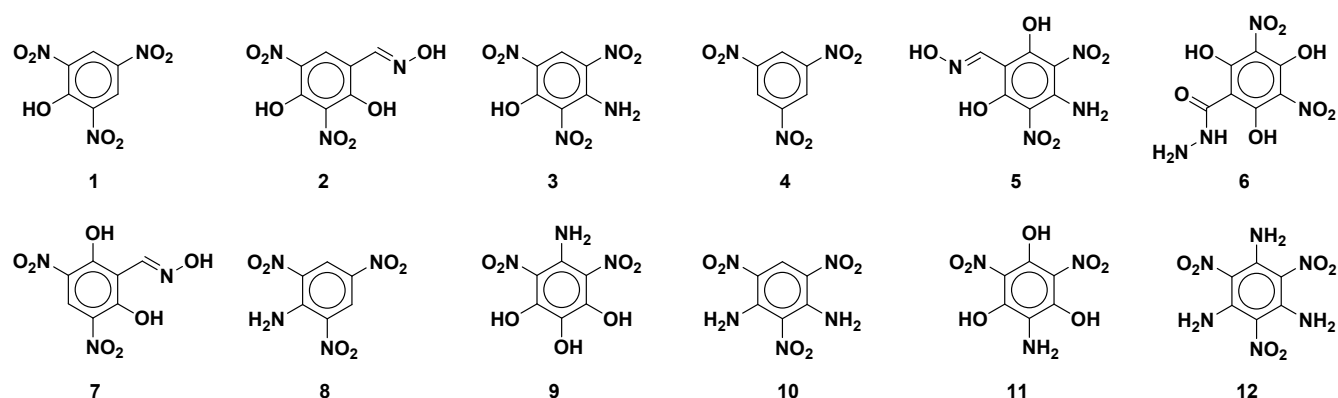
Structure						
$\nu_D$	9266	8910	8897	8889	8790	8723
$\rho$	1.942	1.923	1.925	1.883	1.874	1.876
Structure						
$\nu_D$	8716	8704	8701	8664	8657	8615
$\rho$	1.878	1.897	1.904	1.916	1.880	1.867

Structure						
$v_D$	8611	8600	8592	8586	8571	8571
$\rho$	1.899	1.853	1.876	1.837	1.834	1.834
Structure						
$v_D$	8543	8539	8530	8527	8525	8525
$\rho$	1.860	1.910	1.858	1.849	1.859	1.859
Structure						
$v_D$	8524	8524	8511	8468	8468	8456
$\rho$	1.864	1.864	1.845	1.903	1.903	1.885

## S7: Performance of ML in predicting BDE of C-NO<sub>2</sub> and N-NO<sub>2</sub>.

**Table S7.** Comparison of machine-learned BDE (BDE\_ML) and quantum chemistry calculated BDE (BDE\_QC) of 12 molecules with  $v_D > 7000$  m/s.

	$v_D$ _ML (m s <sup>-1</sup> )	BDE_ML (kJ mol <sup>-1</sup> )	BDE_QC (kJ mol <sup>-1</sup> )	Abs_BDE (kJ mol <sup>-1</sup> )	BDE_%
1	7609	260	257	3	1.2
2	7052	264	275	-11	-4.1
3	7704	267	271	-4	-1.6
4	7395	279	273	7	2.4
5	7154	285	285	0	-0.1
6	7119	288	297	-9	-3.2
7	7028	289	272	17	6.3
8	7523	291	286	6	2.0
9	7271	296	289	7	2.5
10	7685	296	300	-3	-1.1
11	7207	301	307	-6	-2.1
12	7825	304	301	3	1.1



**Figure S2.** Molecular structures for BDE verification.

## S8: References

- (1) Lide, D. R., *CRC handbook of chemistry and physics: a ready-reference book of chemical and physical data*. CRC press: 1995.
- (2) Atkins, P. W.; De Paula, J.; Keeler, J., *Atkins' physical chemistry*. 2006.
- (3) Politzer, P.; Murray, J. S., Some perspectives on estimating detonation properties of C, H, N, O compounds. *Central European Journal of Energetic Materials* **2011**, 8 (3), 209-220.
- (4) Rice, B. M.; Byrd, E. F., Evaluation of electrostatic descriptors for predicting crystalline density. *Journal of computational chemistry* **2013**, 34 (25), 2146-2151.
- (5) Fei, T.; Du, Y.; Pang, S., Theoretical design and prediction of properties for dinitromethyl, fluorodinitromethyl, and

(difluoroamino)dinitromethyl derivatives of triazole and tetrazole. *RSC Advances* **2018**, 8 (19), 10215-10227.