

Supporting Information for

CO₂ Hydrogenation to Methanol over In-doped m-ZrO₂: A DFT

Investigation into the Size-Dependent Mechanism of Oxygen

Vacancy

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Table S1. Surface Formation Energies of (111) m-ZrO₂

Exposed Phase	γ /(J.m ²) for relaxed surface				γ /(J.m ²) for unrelaxed surface			
	This work	PBE ^[1]	PW91 ^[2]	LDA ^[3]	This work	PBE	PW91	LDA
(111)	1.11	1.11	1.06	1.54	1.42	1.39	1.39	1.86

Table S2. Oxygen Vacancy Formation Energy ($E_{(vac)}$, in eV) of ZrO₂_T2, ZrO₂_T3 and ZrO₂_T4 by thermal, H₂ and CO reductions.

reduction type	surface model	a	b	c	d	e
thermal reduction	ZrO ₂ _T2	5.81	6.43	5.59	6.40	6.76
	ZrO ₂ _T3		6.76	5.76	6.23	5.59
	ZrO ₂ _T4	5.97	5.13	6.17	5.41	5.64
H ₂ reduction	ZrO ₂ _T2	3.26	2.79	3.10	3.46	2.88
	ZrO ₂ _T3		4.22	3.23	3.69	3.05
	ZrO ₂ _T4	3.43	2.60	3.63	2.87	3.1
CO reduction	ZrO ₂ _T2	2.53	2.06	2.37	2.73	2.15
	ZrO ₂ _T3		3.50	2.50	2.96	2.32
	ZrO ₂ _T4	2.71	1.87	2.91	2.15	2.37

Table S3. Calculated bond distances (in Å) between specific atoms of perfect and O_v defective In@m-ZrO₂ surfaces.

	Zr1-In	Zr5-In	Zr1-Zr5	Zr3-In	Zr4-In	Zr3-Zr5
perfect In@m-ZrO ₂	3.55	3.44	3.48	3.99	3.47	3.64
O1 _v defective In@m-ZrO ₂	3.79	3.69	3.86	3.91	3.51	3.63
O2 _v defective In@m-ZrO ₂	3.86	3.50	3.53	3.87	3.42	3.67
O4 _v defective In@m-ZrO ₂	3.43	3.45	3.44	4.32	4.14	4.68

Table S4. Reaction energies (in eV) of atomic hydrogen migration on the O1_v, O2_v and O4_v surfaces.

	ΔE					
	O4	O6	O8	O9	O10	O11
Homo-transfer ^a	O1_v					
	0.31	0.81	0.61	0.33	0.47	0.37
	O2_v					
	0.66	0.59	0.35	0.02	0.17	0.07
	O4_v					
			0.49	0.78	0.49	0.92
Heterogenous-transfer ^b	O1_v					
	0.29	0.34	0.42	0.25	0.37	0.24
	O2_v					
	0.23	0.32	0.41	0.21	0.36	0.24
	O4_v					
			0.46	0.67	0.57	0.79

^{a.} Homo-transfer is defined as fixing one of the dissociative hydrogen atoms at O7 while migration the other to O6-O10 individually.

^{b.} Heterogenous-transfer is defined as fixing one of the dissociative hydrogen atoms at In while migration the other to O6-O10 individually.

Table S5. Calculated Harmonic Vibrational Frequencies (cm^{-1}) of stable- CH_3O ($s\text{-CH}_3\text{O}$) on O1_v and O4_v surface

$s\text{-CH}_3\text{O}^*$ on O1_v	$s\text{-CH}_3\text{O}^*$ on O4_v
3047	3043
3025	3017
2941	2937
1471	1473
1453	1461
1430	1429
1171	1174
1140	1137
1035 ^a	1000 ^b
412	334
259	281
221	202
175	143
153	137
93	110

a. Frequency of C-O stretching mode for $s\text{-CH}_3\text{O}^*$ on O1_v

b. Frequency of C-O stretching mode for $s\text{-CH}_3\text{O}^*$ on O4_v

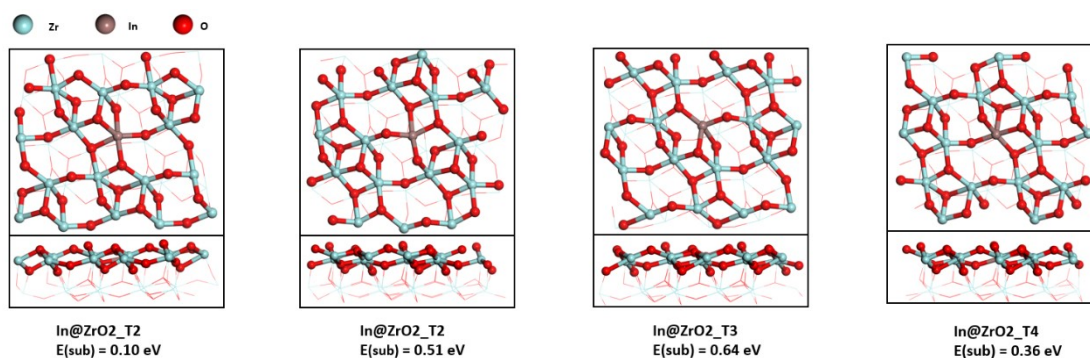


Figure S1. Optimized structures of In@m-ZrO₂_T1 to In@m-ZrO₂_T4 surfaces top (upper) and side (lower) view and their respective In substitution energy ($E_{\text{(sub)}}$)

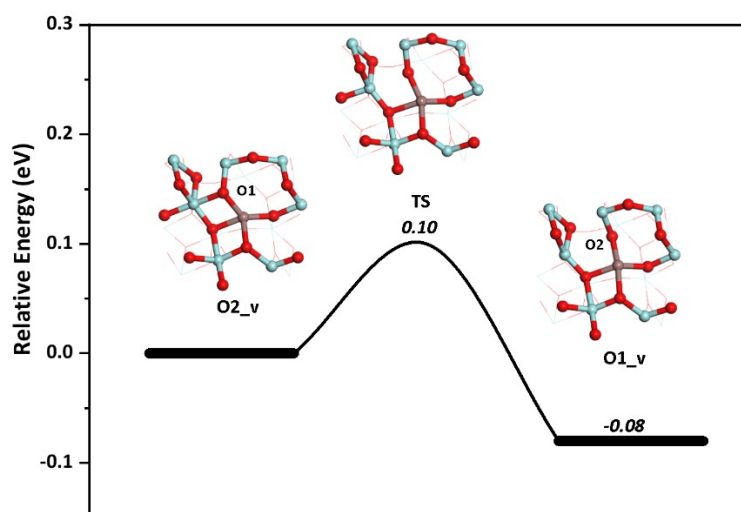


Figure S2. Potential energy diagram of dynamic equilibrium between O1_v and O2_v defective In@m-ZrO₂.

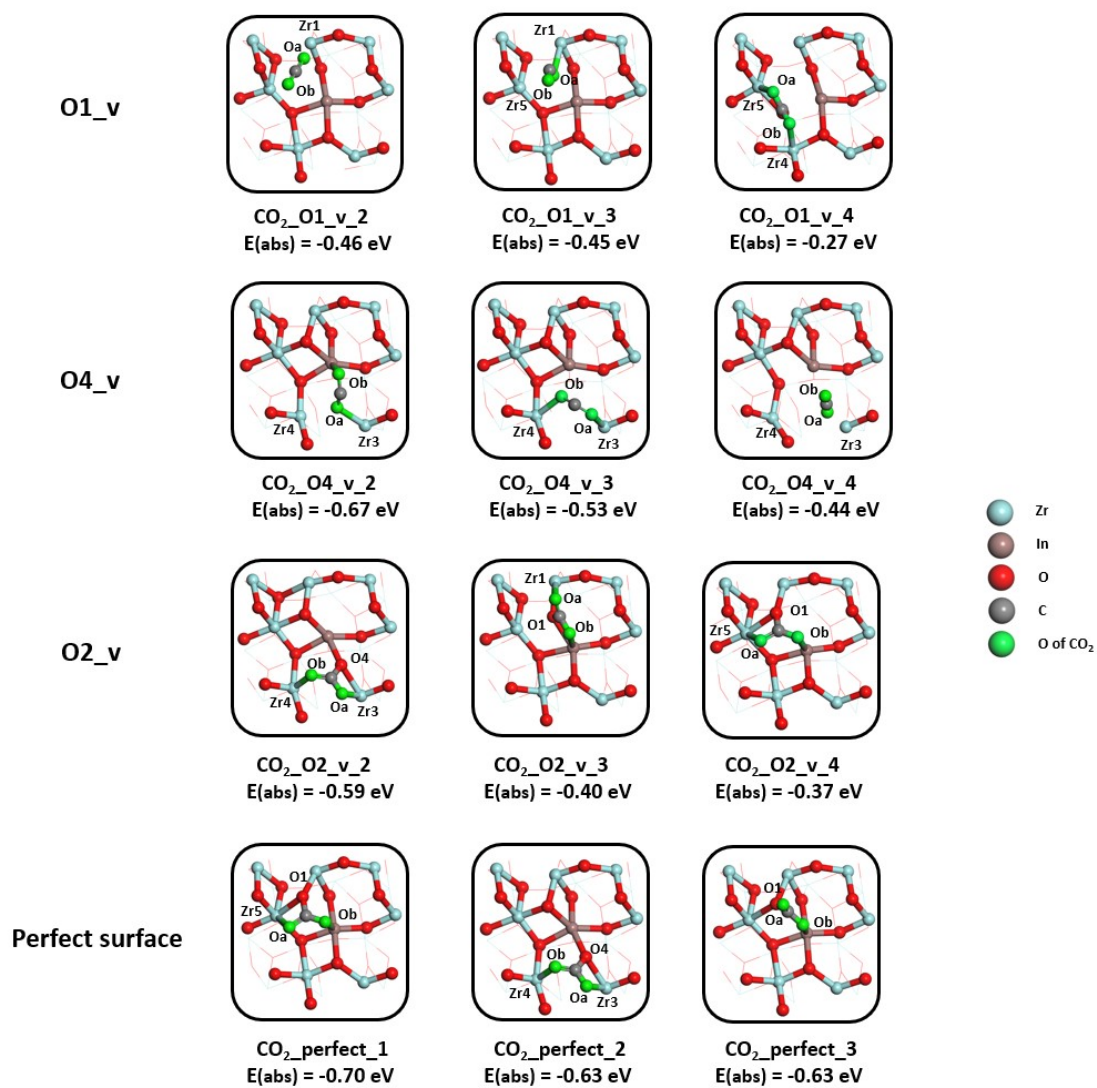
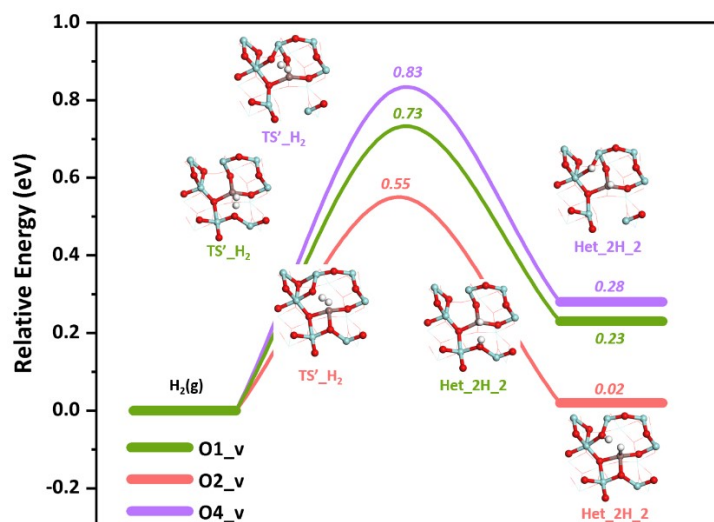
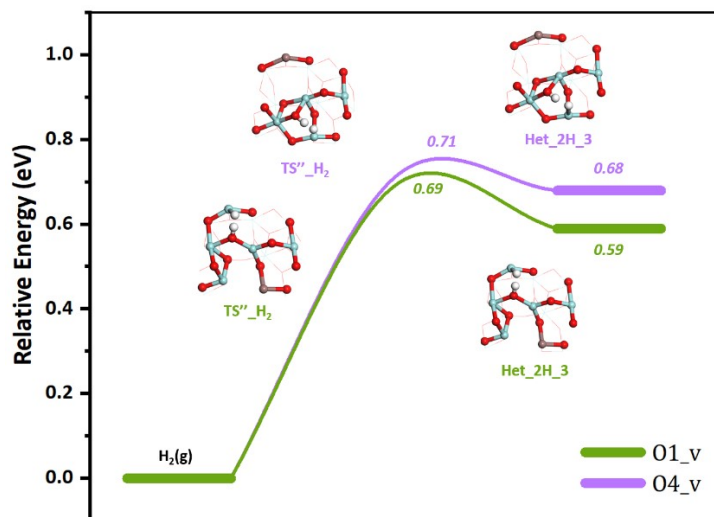


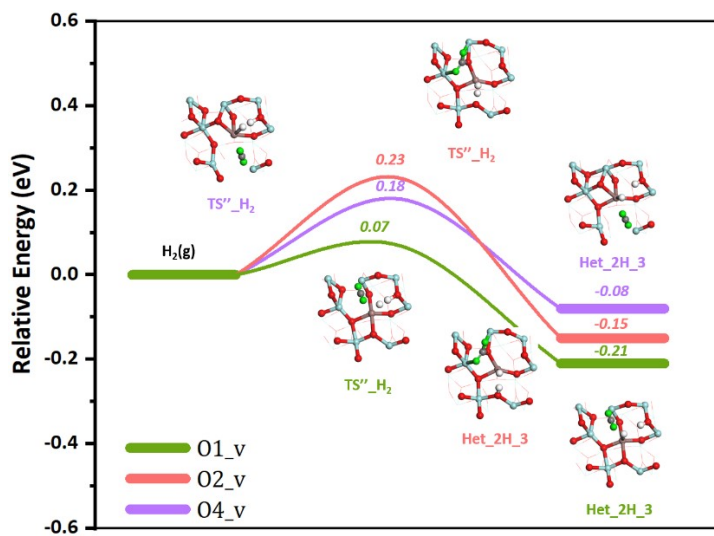
Figure S3. Other optimized structures of CO₂ adsorption on O1_v defective In@m-ZrO₂, O4_v defective In@m-ZrO₂, O2_v defective In@m-ZrO₂ and perfect In@m-ZrO₂.



a



b



c

Figure S4. Potential energy diagram of (a) less favorable H₂ heterolytic dissociation between In and O on O1_v (green), O4_v (purple) and O2_v (pink) surfaces; (b) H₂ heterolytic dissociation

between Zr and O on O1_v (green) and O4_v (purple); (c) H₂ heterolysis dissociation between In and O on O1_v (green), O2_v (red) and O4_v (purple) in the presence of CO₂ adsorption.

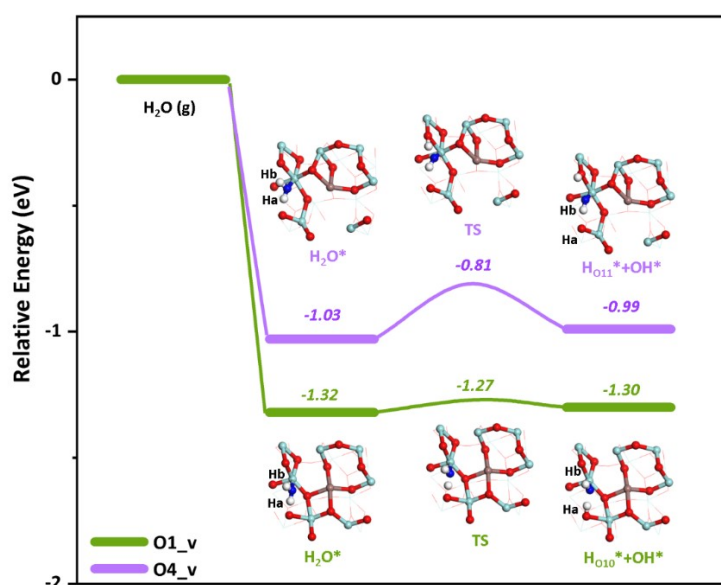


Figure S5. Potential energy diagram of H₂O dissociation on O1_v (green) and O4_v (purple) surfaces. Atoms in blue color represents oxygen atom from dissociated H₂O.

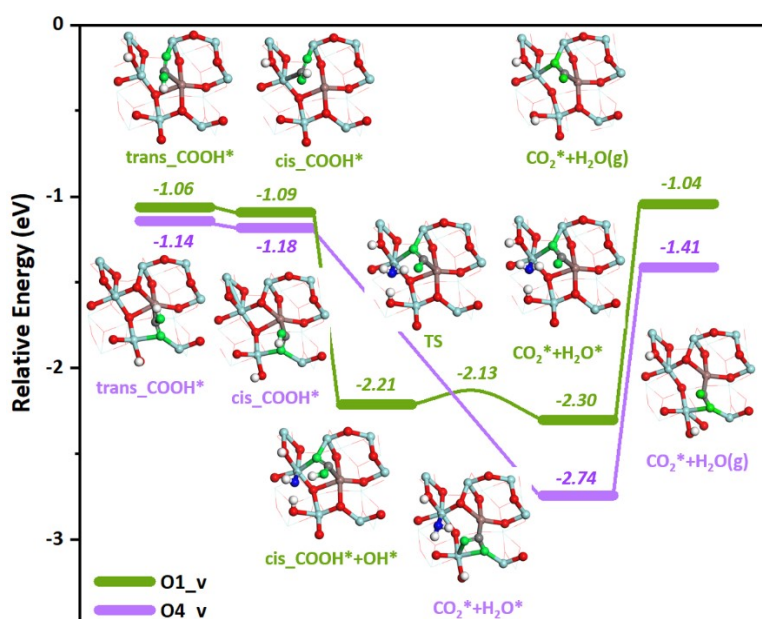


Figure S6. Potential energy diagram of OH* assisted deprotonation of COOH on O1_v (green) and O4_v (purple) surfaces. Atom in blue and green colors represents oxygen atoms from H₂O and CO₂, respectively.

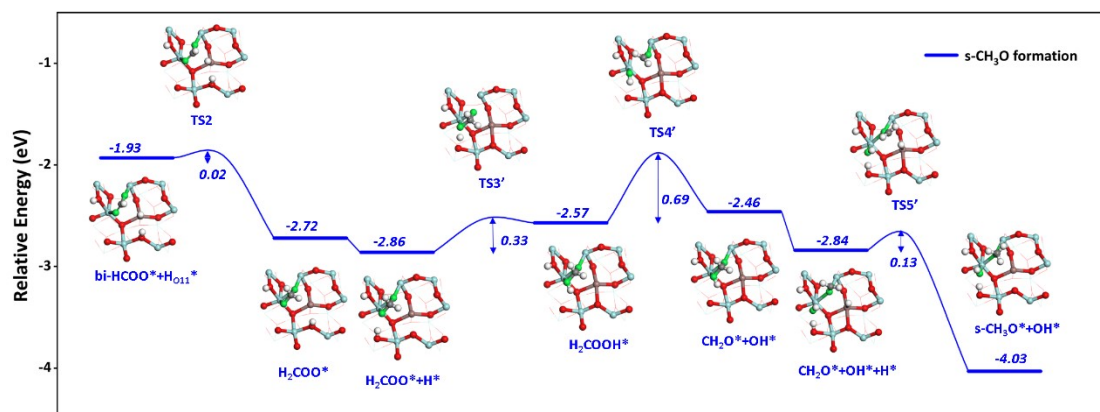


Figure S7. Potential energy diagram of stable-CH₃O(s-CH₃O) formation on O1_v surface.

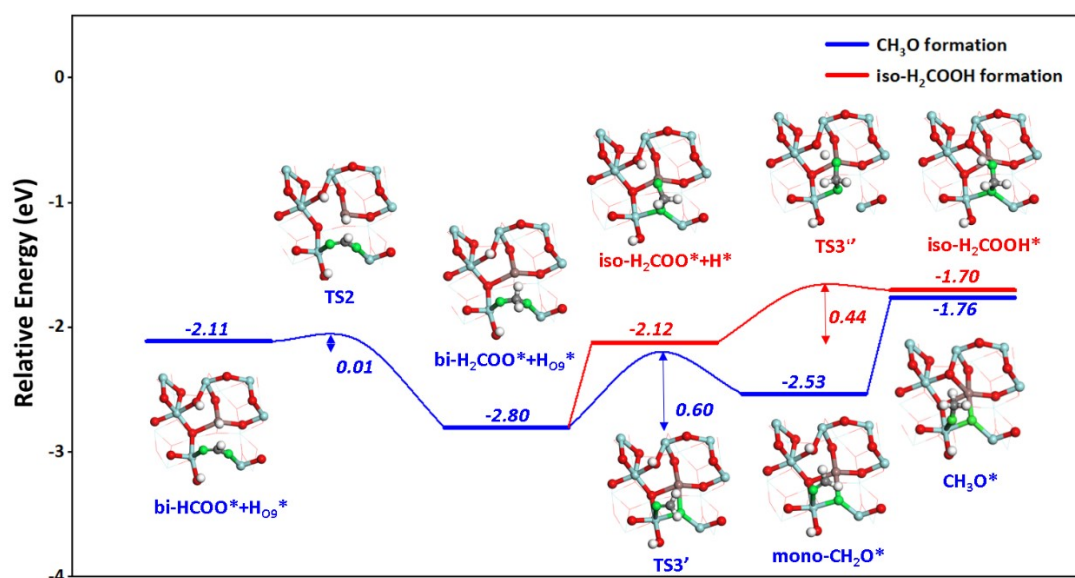


Figure S8. Potential energy diagram of other reactions during CO₂ hydrogenation on O4_v surface.

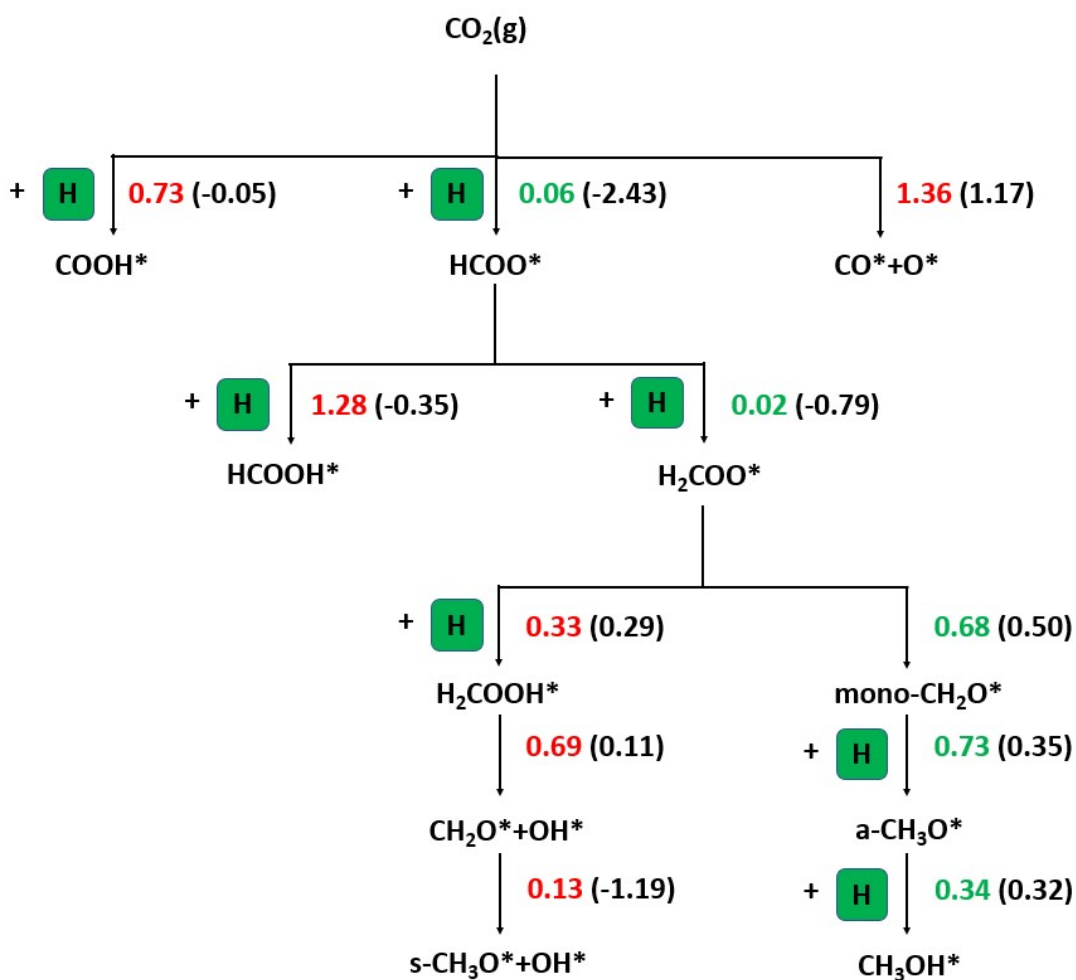


Figure S9. Reaction network of CO_2 hydrogenation on O1_v defective In@m-ZrO_2 . The reaction barrier is marked with number in either green (the most preferred route leading to methanol synthesis) or red (other routes). The reaction energy is marked with black number in the bracket. Unit of relative energy are given in electronic voltage (eV).

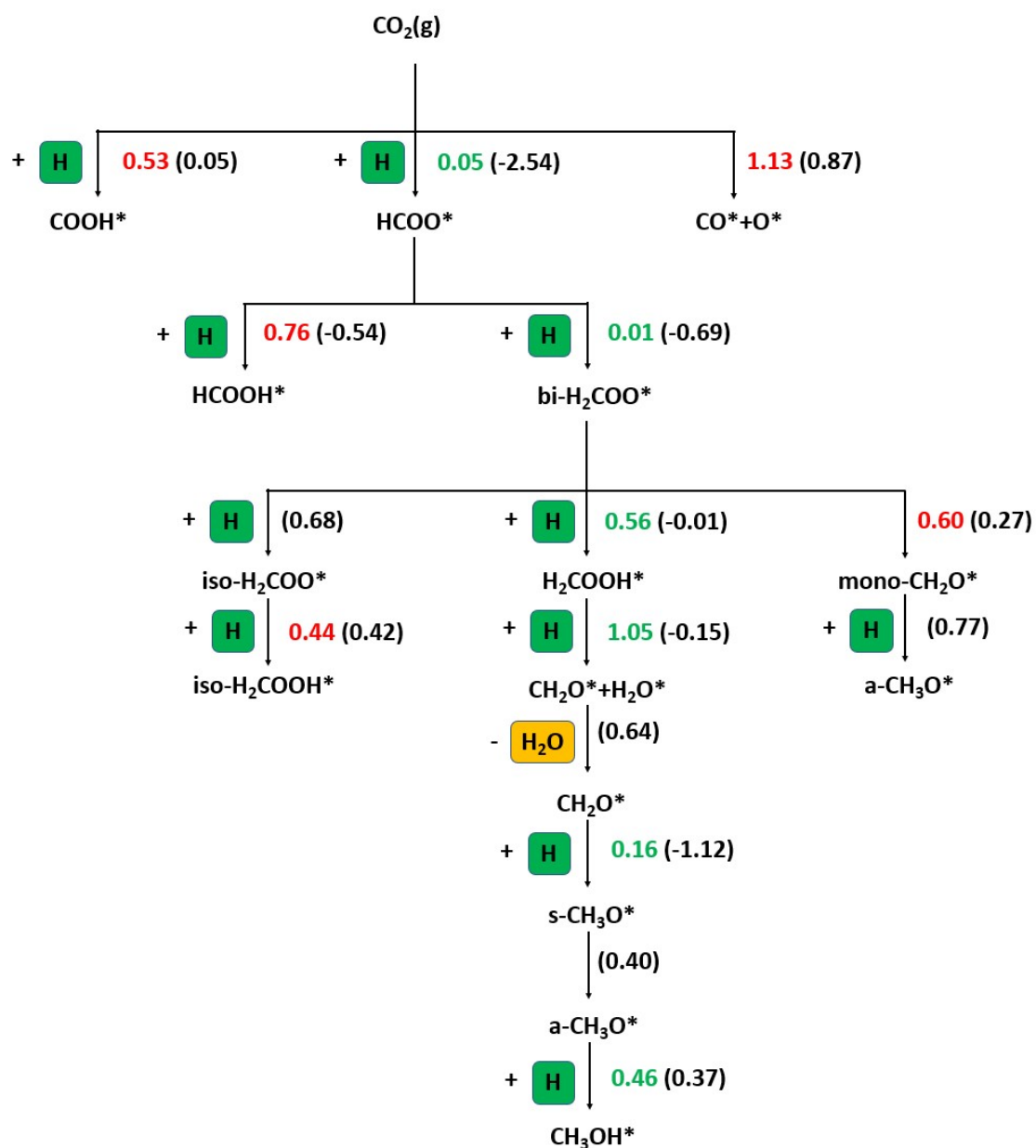


Figure S10. Reaction network of CO₂ hydrogenation on O_{4_v} defective In@m-ZrO₂. The reaction barrier is marked with number in either green (the most preferred route leading to methanol synthesis) or red (other routes). The reaction energy is marked with black number in the bracket. Unit of relative energy are given in electronic voltage (eV).