

Supplementary Information for “Doping-induced magnetism and magnetoelectric coupling in one-dimensional NbOCl₃ and NbOBr₃”

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Table S1. Total magnetic moments of different elements in the top and bottom cell as well as their moment differences for n-L nanochain of NbOCl₃, electing the doping concentration of $2.9 \times 10^{14}/\text{cm}^2$ and $\Delta\mu = \mu_{top} - \mu_{bot}$.

| | 2-L | 3-L | 4-L | 5-L | 6-L |
|------------------|--------|--------|--------|--------|--------|
| Nb_{top} | 0.696 | 0.806 | 0.95 | 1.006 | 1.036 |
| Nb_{bot} | 0.242 | 0.294 | 0.304 | 0.344 | 0.354 |
| $\Delta\mu_{Nb}$ | 0.454 | 0.512 | 0.646 | 0.662 | 0.682 |
| Cl_{top} | 0.074 | 0.072 | 0.09 | 0.09 | 0.09 |
| Cl_{bot} | 0.008 | 0.014 | 0.004 | 0.006 | 0.006 |
| $\Delta\mu_{Cl}$ | 0.066 | 0.058 | 0.086 | 0.084 | 0.084 |
| O_{top} | -0.032 | -0.04 | -0.044 | -0.048 | -0.05 |
| O_{bot} | -0.016 | -0.018 | -0.022 | -0.024 | -0.024 |
| $\Delta\mu_O$ | -0.016 | -0.022 | -0.022 | -0.024 | -0.026 |

Table S2. Total magnetic moments of different elements in the top and bottom cell as well as their moment differences for n-L nanochain of NbOBr₃, electing the doping concentration of $2.9 \times 10^{14}/\text{cm}^2$ and $\Delta\mu = \mu_{top} - \mu_{bot}$.

| | 2-L | 3-L | 4-L | 5-L | 6-L |
|------------------|--------|--------|--------|--------|--------|
| Nb_{top} | 0.76 | 0.794 | 1.068 | 1.04 | 1.11 |
| Nb_{bot} | 0.264 | 0.29 | 0.232 | 0.288 | 0.326 |
| $\Delta\mu_{Nb}$ | 0.496 | 0.504 | 0.836 | 0.752 | 0.784 |
| Br_{top} | 0.034 | 0.024 | 0.098 | 0.098 | 0.099 |
| Br_{bot} | 0.01 | 0.014 | -0.008 | 0 | 0.002 |
| $\Delta\mu_{Br}$ | 0.024 | 0.01 | 0.106 | 0.098 | 0.097 |
| O_{top} | -0.048 | -0.054 | -0.052 | -0.052 | -0.056 |
| O_{bot} | -0.016 | -0.016 | -0.02 | -0.02 | -0.024 |
| $\Delta\mu_O$ | -0.032 | -0.038 | -0.032 | -0.032 | -0.032 |

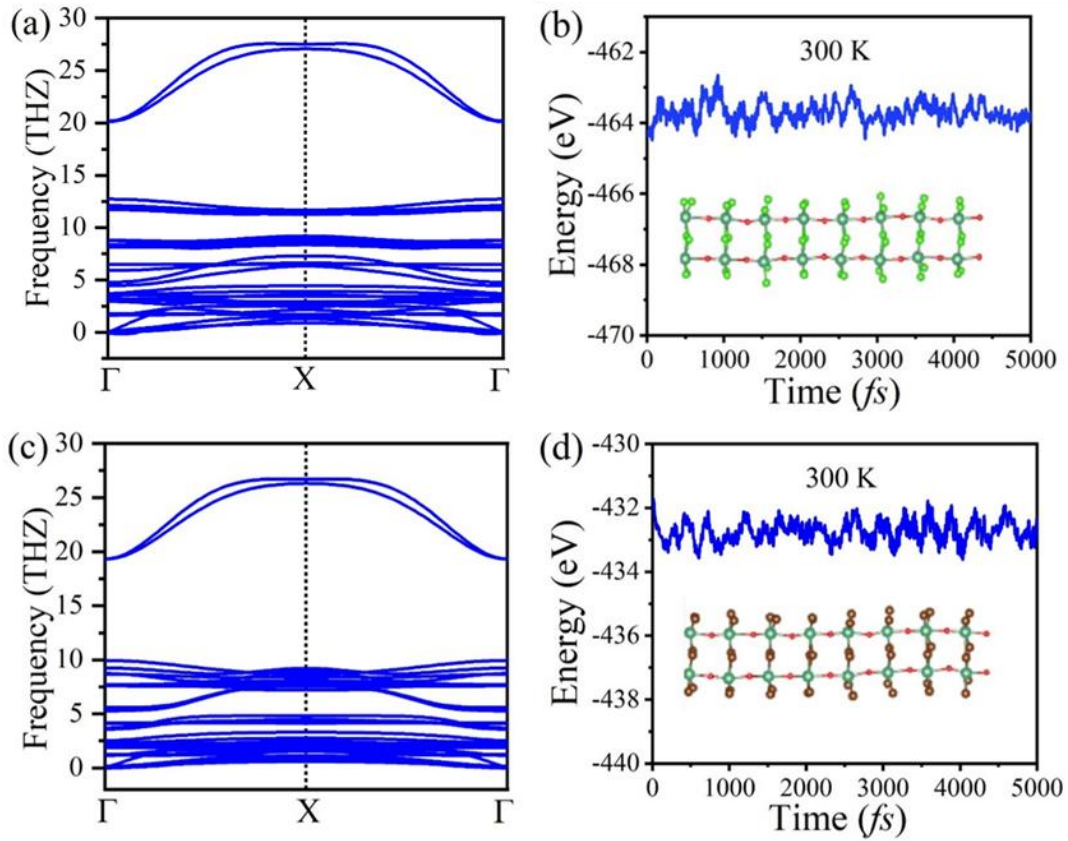


Figure S1. The phonon spectra of (a) 1D NbOCl₃ and (c) 1D NbOBr₃. The evolutions of the total energy of (b) 1D NbOCl₃ and (d) 1D NbOBr₃ with time at 300K through the AIMD simulations, and illustrations are the final atomic structures.

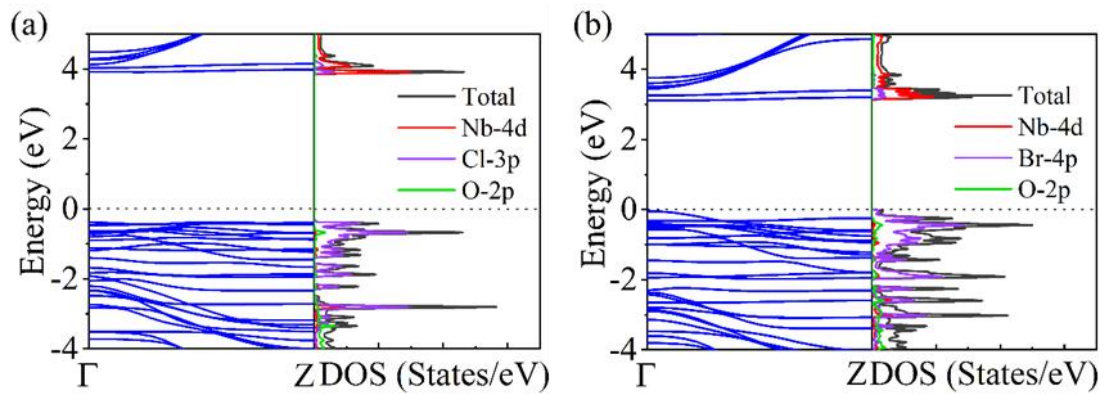


Figure S2. The band structures and projected densities of orbital states of (a) 1D NbOCl₃ and (b) 1D NbOBr₃ calculated by HSE method.

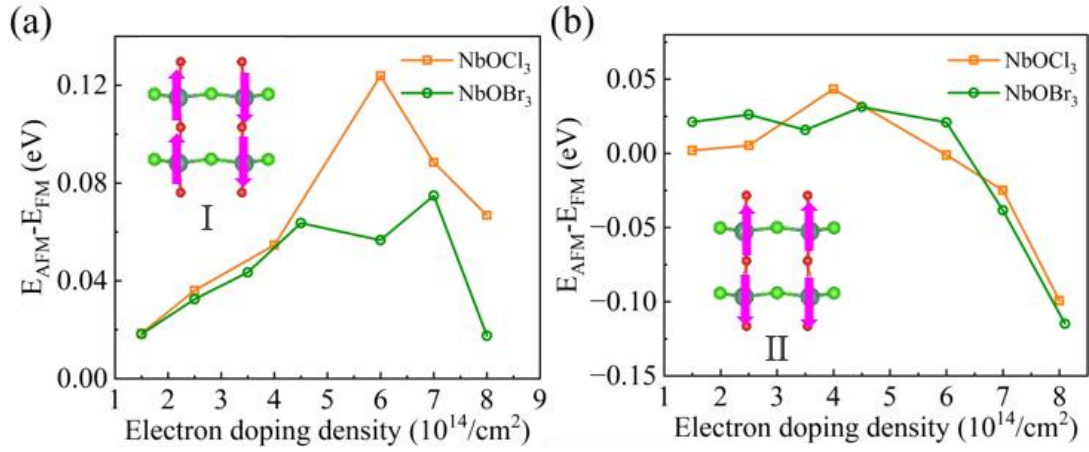


Figure S3. (a) and (b) are the energy difference of FM and two types of AFM ($\Delta E = E_{\text{AFM}} - E_{\text{FM}}$) as a function of the electron-doping concentration in 1D NbOX₃ (X=Cl, Br), the illustrations are the corresponding schematic diagrams of two types of antiferromagnetic orders.

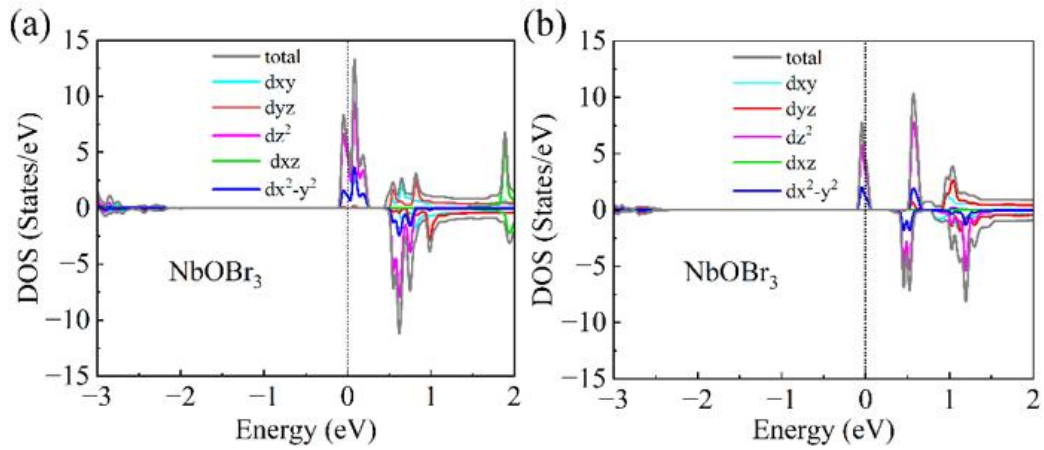


Figure S4. The PDOS of Nb-d orbital for (a) 1D NbOCl₃ at the concentration of $4.0 \times 10^{14}/\text{cm}^2$ and (b) 1D NbOBr₃ at the concentration of $3.9 \times 10^{14}/\text{cm}^2$.

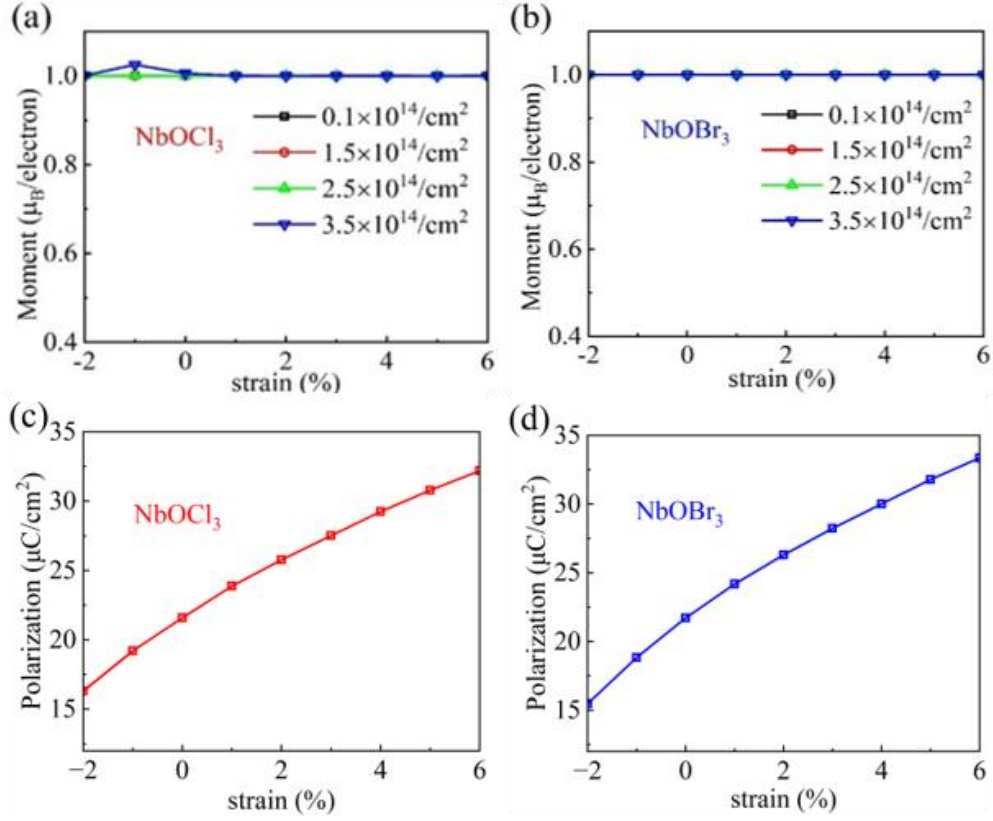


Figure S5. The doping-induced magnetic moment vs strain in (a) 1D NbOCl_3 and (b) 1D NbOBr_3 at different doping-electrons concentrations. The ferroelectric polarization under different strains without doping in (c) 1D NbOCl_3 and (d) 1D NbOBr_3 .

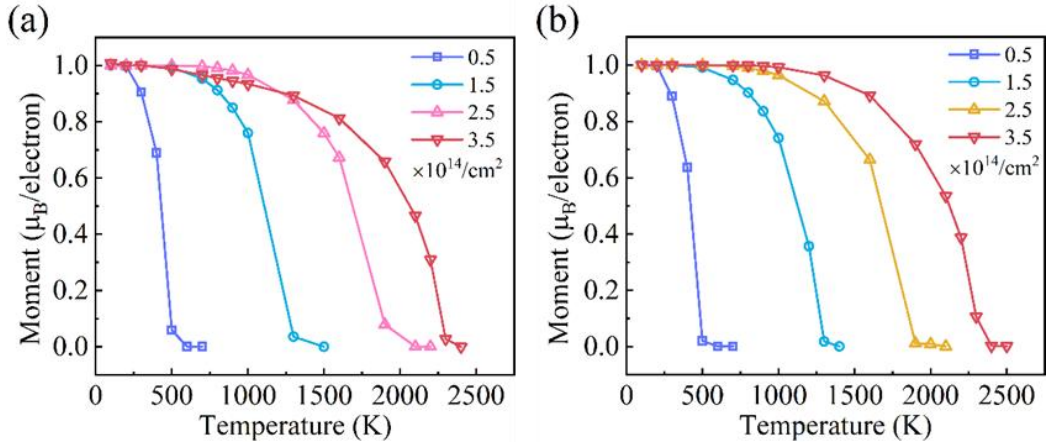


Figure S6. The spin magnetic moment vs temperature for (a) 1D NbOCl_3 and (b) 1D NbOBr_3 at different doping concentrations. In this simulation, the magnetic carriers are approximated to satisfy the Fermi-Dirac distribution function $f\left(\frac{\varepsilon-\mu}{\sigma}\right) = \frac{1}{\exp\left(\frac{\varepsilon-\mu}{\sigma}+1\right)}$, where μ is the chemical potential, and $\sigma = \kappa_B T$ is the energy broadening factor that introduces temperature effect.

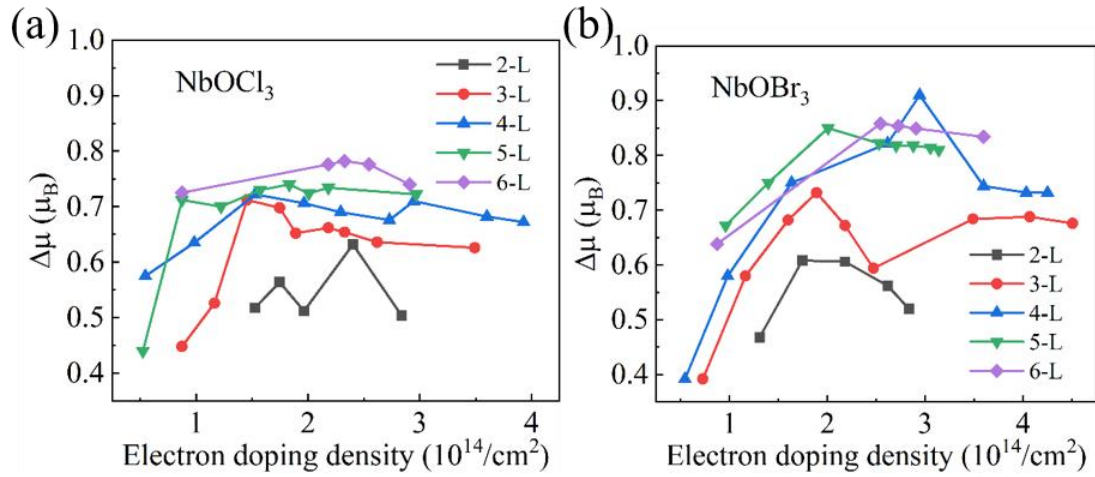


Figure S7. The magnetic moment difference ($\Delta\mu = \mu_{top} - \mu_{bot}$) of (a) n-L NbOCl₃ and (b) n-L NbOBr₃ nanochains under different doping concentrations.

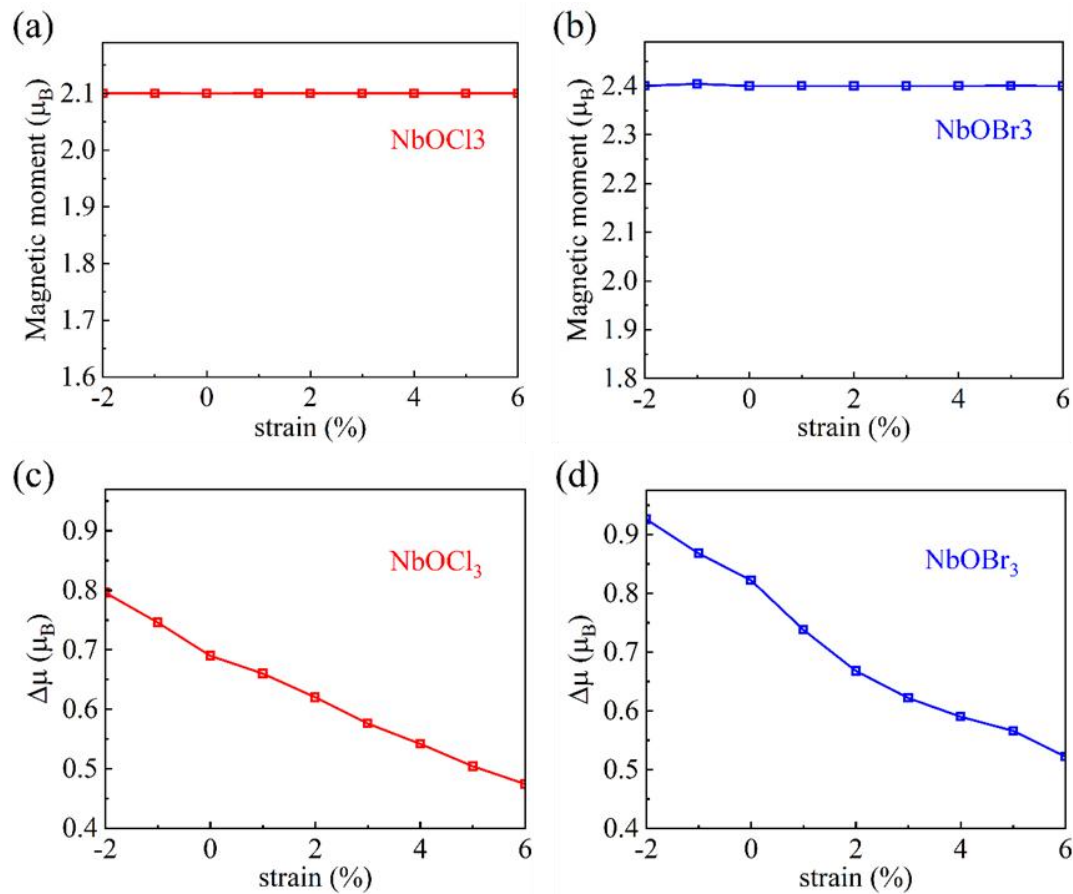


Figure S8. Under different strains, (a) the total magnetic moments and (b) magnetic moment differences of 4-L NbOCl₃ at the concentration of $2.29 \times 10^{14}/\text{cm}^2$ (doping about 2.1 electrons), (a) the total magnetic moments and (b) magnetic moment differences of 4-L NbOBr₃ at the concentration of $2.62 \times 10^{14}/\text{cm}^2$ (doping about 2.4 electrons).