

Supporting Information

Enhancing the osmotic energy conversion of a nanoporous membrane: influence of pore density, pH, and temperature

Ding-Cheng Zheng and Jyh-Ping Hsu*

Department of Chemical Engineering, National Taiwan University, Taipei 10617, Taiwan

Tel: 886-2-23637448; e-mail: jphsu@ntu.edu.tw

Table S1. Dependence of pore density on pore-pore distance.

Pore-pore distance a_1 (nm)	Pore density (pores/cm ²)
200	2.5×10^9
320	9.8×10^8
450	5.0×10^8
600	2.8×10^8
800	1.6×10^8
1000	1.0×10^8
2000	2.5×10^7
3200	1.0×10^7
10000	1.0×10^6

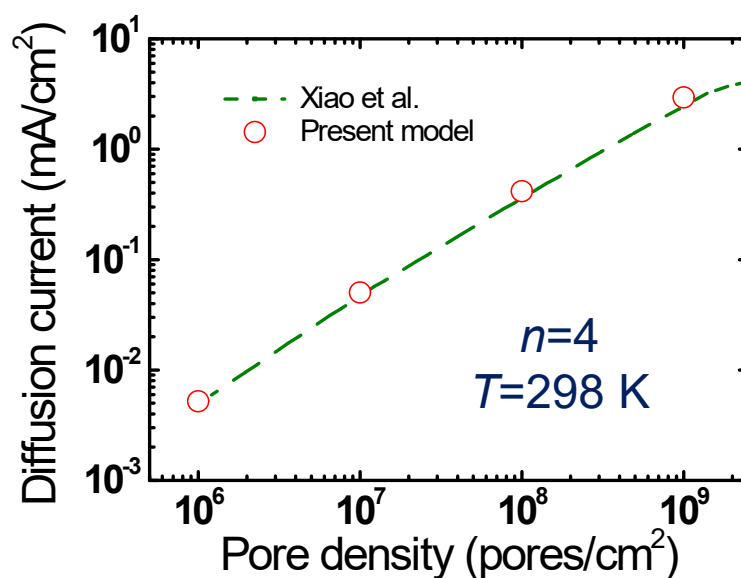


Fig. S1 Variation of diffusion current with pore density for a multi-pore system with $a_0=5$ μm (infinite reservoir). Parameters used: $L=1000$ nm, $d=10$ nm, $\sigma_s=-0.06$ C/m², $C_H/C_L=100$ mM/1 mM, and $T=298$ K, $n=4$, and $H_{\text{res}}=2000$ nm. The pore density is adjusted by the pore-pore distance a_1 (Table S1).

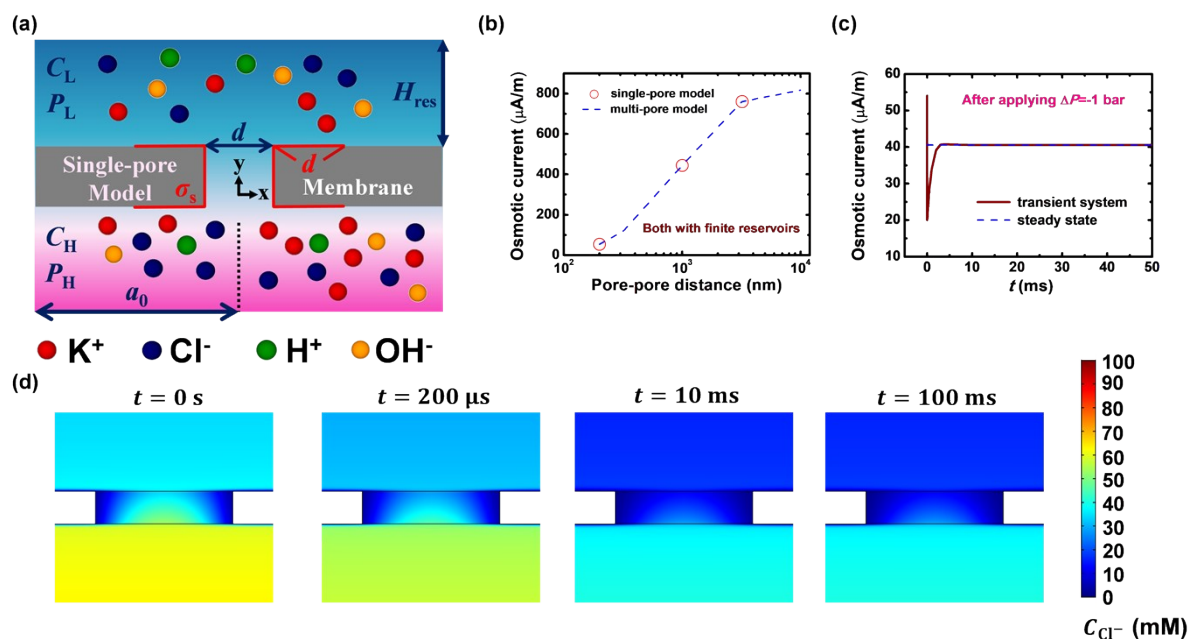


Fig. S2 (a) Schematic representation of a single-pore system, where a cylindrical nanopore connects two large, identical reservoirs with a_0 being half width. The boundary marked red has the surface charge density σ_s . (b) Variation of osmotic current with pore-pore distance; both the results for single-pore and those for multi-pore are presented. Temporal variation of osmotic current, (c), and Cl^- concentration, (d), after a $\Delta P = -1$ bar is applied for the case of $a_1 = 200$ nm. The parameters used in (b)-(d) are $L = 50$ nm, $d = 10$ nm, pH 8, $C_H/C_L = 100$ mM/1 mM, $T = 298$ K, $H_{\text{res}} = 2000$ nm, and $a_0 = a_1/2$.

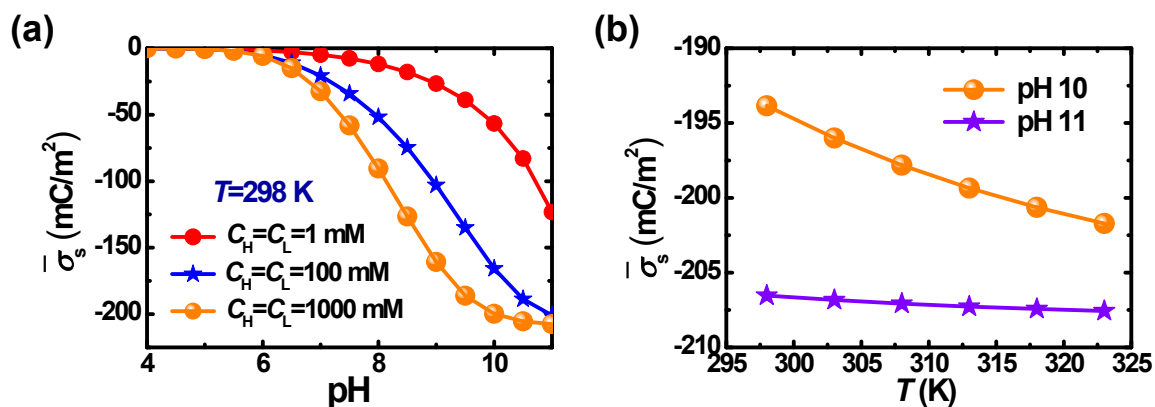


Fig. S3 (a) Variation of averaged surface charge density of the wall $\bar{\sigma}_s$ with pH for different bulk concentrations. (b) Variation of $\bar{\sigma}_s$ with temperature for two pH levels. The parameters used in (b) are $L=600$ nm, $d=10$ nm, $C_H/C_L=1000$ mM/1 mM, $H_{res}=2000$ nm, and $a_0=a_1/2=100$ nm.

Table S2. Dependence of pore density on pore-pore distance and the corresponding porosity.

Pore-pore distance a_1 (nm)	Pore density (pores/cm ²)	Porosity (%) when $d=10$ nm
50	4.0×10^{10}	3.142
100	1.0×10^{10}	0.785
140	5.1×10^9	0.401
200	2.5×10^9	0.196

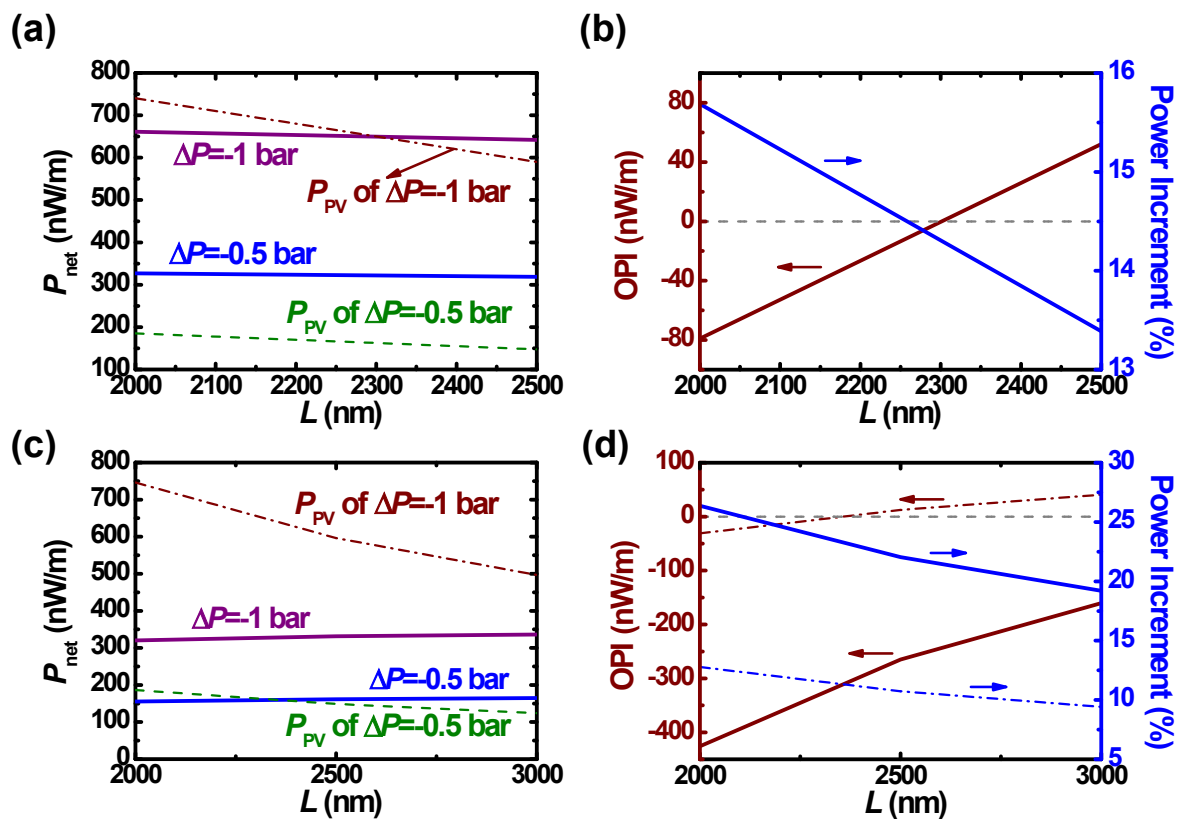


Fig. S4 Variation of the net power P_{net} , (a) and (c), and overall power increment OPI and power increment PI, (b) and (d), with pore length. In (a) and (c), green dashed curve: power of PV work P_{PV} of $\Delta P = -0.5$ bar; wine dash-dotted curve: power of PV work P_{PV} of $\Delta P = -1$ bar. In (b) and (d), gray dashed curve: OPI=0. In (d), dash-dotted curve: $\Delta P = -0.5$ bar; solid curve: $\Delta P = -1$ bar. Parameters used are $d=10$ nm, $C_H/C_L=1000$ mM/1 mM, $T=323$ K, pH 11, $H_{res}=2000$ nm, and $a_0=a_1/2$. In (a) and (b), $a_1=100$ nm. In (c) and (d), $a_1=50$ nm.