# Magnetic anisotropy of two tetrahedral $\mathbf{C o}(\mathrm{II})$-halide complexes with triphenylphosphine ligands 

Wei Lv, ${ }^{a}$ Hui-Hui Cui, ${ }^{\text {a }}$ Lei Chen, ${ }^{\text {b }}$ Yi-Quan Zhang,* ${ }^{\text {c }}$ Xue-Tai Chen, ${ }^{*}$ Z Zhenxing
Wang,*d Zhong-Wen Ouyang ${ }^{\text {d }}$ and Zi-Ling Xue ${ }^{e}$
${ }^{\text {a State Key Laboratory of Coordination Chemistry, School of Chemistry and Chemical }}$ Engineering, Nanjing University, Nanjing 210023, China
${ }^{b}$ School of Environmental and Chemical Engineering, Jiangsu University of Science and Technology, Zhenjiang 212003, China
${ }^{〔}$ Jiangsu Key Laboratory for NSLSCS, School of Physical Science and Technology, Nanjing Normal University, Nanjing 210023, China
d Wuhan National High Magnetic Field Center \& School of Physics, Huazhong
University of Science and Technology, Wuhan 430074, China
${ }^{\text {e}}$ Department of Chemistry, University of Tennessee, Knoxville, Tennessee 37996, USA

## Electronic Supplementary Information

Table S1 Complexes with $\left[\mathrm{CoAB}_{3}\right]$ moiety and their structure/magnetic parameters

| Complex |
| :--- | :--- | :--- | :--- | :--- | :--- |

a. Ligands: $\mathrm{L}^{1}=2$-methyl-3-(pyridin-2-yl)imidazo[1,5-a]pyridinium cation; $\left.\mathrm{L}^{2}=\mathrm{CH}_{3} \mathrm{C}_{2} \mathrm{CH}_{2} \mathrm{~N}=\mathrm{CN}\left(\mathrm{CH}_{3}\right)_{2}\right]_{3} ; \mathrm{L}^{3}=\mathrm{N}^{\prime} \mathrm{N}^{\prime}, \mathrm{N}^{\prime}$ '-[nitrilotris-(ethane-2,1-diyl) $]$ tris(2,4,6-trimethylbenzenesulfonamide); $\mathrm{L}^{4}=\mathrm{N}\left[\mathrm{CH}_{2} \mathrm{C}(\mathrm{O}) \mathrm{NC}\left(\mathrm{CH}_{3}\right)_{3}\right]_{3} ; \mathrm{L}^{5}=\left[\left(\mathrm{Me}_{3} \mathrm{SiNCH}_{2} \mathrm{CH}_{2}\right)_{3} \mathrm{~N}\right]^{3-}$. b. The applied field used in the measurement is indicated in the parenthesis. c. No Orbach mechanism is found. d. Not reported.

Table S2 Complexes with $\left[\mathrm{CoP}_{2} \mathrm{X}_{2}\right]$ moiety and their structure/magnetic parameters
$\left.\begin{array}{llllll}\hline \text { Complex } & \begin{array}{l}\text { Coordination } \\ \text { moiety }\end{array} & \begin{array}{l}D \\ / \mathrm{cm}^{-1}\end{array} & \begin{array}{l}|E| \\ / \mathrm{cm}^{-1}\end{array} & U_{\text {eff }} / \mathrm{K}^{\mathrm{c}}\end{array}\right]$ Reference
a. Ligands: $\mathrm{L}^{6}=$ DPEphos $=2,2^{\prime}$-bis(diphenyl-phosphino) diphenyl ether; $\mathrm{L}^{7}=$ Xantphos $=9,9$-dimethyl-4,5-bis(diphenyl-phosphino) xanthenes; $\mathrm{L}^{8}=\operatorname{bis}\left(2\right.$-(diphenylphosphaneyl)-4-methylphenyl)amine; $\mathrm{L}^{9}=9,9$-dimethyl-4,5-bis(diphenylphosphino)xanthenes; dppf = $1,1^{\prime}$-ferrocenediyl-bis(diphenylphosphine). b. Not reported. c. The applied field used in the measurement is indicated in the parenthesis.

Table S3 Summary of crystal data and refinement for $\mathbf{1}$ and $\mathbf{2}$

|  | $\mathbf{1}$ | $\mathbf{2}$ |
| :--- | :--- | :--- |
| Molecular formula | $\mathrm{C}_{26} \mathrm{H}_{35} \mathrm{NPCl}_{3} \mathrm{Co}$ | $\mathrm{C}_{26} \mathrm{H}_{35} \mathrm{NPBr}_{3} \mathrm{Co}$ |
| CCDC no | 2074688 | 2074732 |
| Formula weight | 557.80 | 691.18 |
| Temperature $/ \mathrm{K}$ | $296(2)$ | $296(2)$ |
| Crystal system | Cubic | Cubic |
| Space group | $P a$ | $P a$ |
| $a / \AA$ | $17.5892(2)$ | $17.86950(10)$ |
| $b / \AA$ | $17.5892(2)$ | $17.86950(10)$ |
| $c / \AA$ | $17.5892(2)$ | $17.86950(10)$ |
| $\alpha\left(^{\circ}\right)$ | 90 | 90 |
| $\beta\left(^{\circ}\right)$ | 90 | 90 |
| $\gamma\left(^{\circ}\right)$ | 90 | 90 |
| $V / \AA^{\circ}$ | $5441.75(19)$ | $5706.17(10)$ |
| Z | 8 | 8 |
| $\mathrm{D}_{\text {calc }}, \mathrm{g} /$ cm ${ }^{3}$ | 1.362 | 1.609 |
| $\mu / \mathrm{mm}^{-1}$ | 0.999 | 4.873 |
| $\mathrm{~F}(000)$ | 2328.0 | 2760.0 |
| $\theta$ range [ $\left.{ }^{\circ}\right]$ | $2.005 / 25.977$ | $1.974 / 25.974$ |
| Reflns collected | 42768 | 45367 |
| $\mathrm{R}_{\text {int }}$ | 0.0574 | 0.0608 |
| Indep. reflns | 1795 | 1869 |
| Data/restr. $/$ paras | $1795 / 215 / 149$ | $1869 / 203 / 149$ |
| Goodness-of-fit on $F^{2}$ | 1.064 | 1.094 |
| $\mathrm{R}_{1}, w \mathrm{R}_{2}[\mathrm{I}>2 \sigma(I)]^{\mathrm{a}}$ | $0.0600 / 0.1565$ | $0.0750 / 0.1755$ |
| $\mathrm{R}_{1}, w \mathrm{R}_{2}[\text { all data }]^{\mathrm{a}}$ | $0.0740 / 0.1700$ | $0.0946 / 0.1889$ |
| ${ }^{\mathrm{a}} \mathrm{wR}{ }_{2}=\left[\Sigma\left[w\left(\mathrm{~F}_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2}\right] / \Sigma\left[w\left(\mathrm{Fo}^{2}\right)^{2}\right]\right]^{1 / 2}, \mathrm{R}_{1}=\Sigma\| \| \mathrm{F}_{\mathrm{o}}\left\|-\left\|\mathrm{F}_{\mathrm{c}}\right\|\right\| / \Sigma\left\|\mathrm{F}_{\mathrm{o}}\right\|$. |  |  |
|  |  |  |

$\underline{\text { Table S4 Selected bond lengths (Angstroms) and angels (degree) for } \mathbf{1} \text { and } \mathbf{2}}$

|  |  |  | $\mathbf{2}$ |
| :--- | :--- | :--- | :--- |
| Co1-P1 | $2.3763(16)$ | Co1-P1 | $2.373(3)$ |
| Co1-Cl1 | $2.2508(12)$ | Co1-Br1 | $2.3827(10)$ |
| Cl1-Co1-Cl1 | $114.11(4)$ | Br1-Co1-Br1 | $113.39(4)$ |
| P1-Co1-Cl1 | $104.30(5)$ | P1-Co1-Br1 | $105.19(5)$ |



Fig. S1 XRD patterns for $\mathbf{1}$ (The red line are PXRD experimental pattern and the black line are calculated from single-crystal structure)


Fig. S2 XRD patterns for complex 2 (The red line are PXRD experimental pattern and the black line are calculated from single-crystal structure).

Table S4 The results of the continuous shape measure (CShM) analyses of $\mathbf{1}$ and $\mathbf{2}$ by SHAPE software. ${ }^{1,2}$

|  | Deviation parameter |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Square | Tetrahedron | Seesaw | Vacant trigonal bipyramid |
| 1 | 33.432 | 0.177 | 8.903 | 2.258 |
| 2 | 33.417 | 0.199 | 8.889 | 2.112 |



Fig. S3 Crsytal packing of $\mathbf{1}$ along the crystallographic a-axis.


Fig. S4 Crystal packing of $\mathbf{2}$ along the crystallographic a-axis.

PHI survey plots: In oder to check the accuracy of the set of the fitted parameters, survey features
have been performed using the PHI code. ${ }^{3}$ Among the three parameters $D, g_{x}\left(g_{y}\right)$ and $g_{z}$, one parameter was fixed and the other two are varied. All the survey plots show that the fitted parameters are in the narrow minimum regions.


Fig. S5 The survey plots of complex 1: (a) $g_{z}$ was fixed as 2.103; (b) $g_{x}\left(g_{y}\right)$ was fixed as 2.236 and (c) $D$ was fixed as $42.8 \mathrm{~cm}^{-1}$.


Fig. S6 The survey plots of complex 2: (a) $g_{z}$ was fixed as 2.136; (b) $g_{x}\left(g_{y}\right)$ was fixed as 2.262 and (c) $D$ was fixed as $41.2 \mathrm{~cm}^{-1}$.


Fig. S7 Frequency dependence of out-of-phase ac susceptibility ( $\chi_{M}{ }^{\prime \prime}$ ) at 1.8 K under the different applied static fields from 0 to 0.25 T for $\mathbf{1}$ (a) and $\mathbf{2}$ (b). The solid lines are for eye guide.


Fig. S8 Temperature dependence of (a) in-phase $\left(\chi_{M}{ }^{\prime}\right)$ and (b) out-of-phase ac susceptibility ( $\chi_{M}{ }^{\prime \prime}$ )
at different ac frequencies under the dc field of 0.12 T for $\mathbf{1}$. The solid lines are for eye guide.


Fig. S9 Temperature dependence of (a) in-phase $\left(\chi_{M}{ }^{\prime}\right)$ and (b) out-of-phase ac susceptibility ( $\chi_{M}{ }^{\prime \prime}$ )
at different ac frequencies under the dc field of 0.15 T for $\mathbf{2}$. The solid lines are for eye guide.


Fig. S10 Cole-Cole plots for $\mathbf{2}$ under 0.15 T dc field. The solid lines are the best fits to the experiments with the generalized Debye model.


Fig. S11 The plot of $\ln (\tau)$ versus $\mathrm{T}^{-1}$ for $\mathbf{2}$. The solid blue line represents the best fit by the Raman process.

Table S5 Relaxation times $\tau$ (s) and $\alpha$ values for $\mathbf{1}$ and 2

| 1 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| T (K) | $\chi_{S}$ | $\chi_{T}$ | $\tau$ (s) | $\alpha$ |
| 1.8 | 0.16775 | 0.7448 | $1.46616 \times 10^{-4}$ | 0.07053 |
| 1.9 | 0.16128 | 0.71303 | $1.33689 \times 10^{-4}$ | 0.0677 |
| 2.0 | 0.1559 | 0.68453 | $1.22337 \times 10^{-4}$ | 0.0625 |
| 2.2 | 0.15031 | 0.66035 | $1.1247 \times 10^{-4}$ | 0.06088 |
| 2.4 | 0.14531 | 0.63827 | $1.03745 \times 10^{-4}$ | 0.05875 |
| 2.6 | 0.14109 | 0.61614 | $9.56154 \times 10^{-5}$ | 0.05418 |
| 2.8 | 0.13704 | 0.5963 | $8.83302 \times 10^{-5}$ | 0.05117 |
| 3.0 | 0.13348 | 0.57683 | $8.16139 \times 10^{-5}$ | 0.04658 |
| 3.2 | 0.12929 | 0.55981 | $7.55874 \times 10^{-5}$ | 0.04619 |
| 3.4 | 0.1259 | 0.5438 | $7.01833 \times 10^{-5}$ | 0.04433 |
| 3.6 | 0.12413 | 0.52708 | $6.51943 \times 10^{-5}$ | 0.03701 |
| 3.8 | 0.12039 | 0.51323 | $6.06515 \times 10^{-5}$ | 0.03822 |
| 4.0 | 0.11787 | 0.49878 | $5.6357 \times 10^{-5}$ | 0.03462 |
| 4.4 | 0.11575 | 0.48508 | $5.2464 \times 10^{-5}$ | 0.03065 |
| 4.8 | 0.11296 | 0.47285 | $4.88591 \times 10^{-5}$ | 0.03029 |
| 5.2 | 0.11133 | 0.45994 | $4.54591 \times 10^{-5}$ | 0.02472 |
| 5.6 | 0.10949 | 0.44831 | $4.23382 \times 10^{-5}$ | 0.02156 |
| 6.0 | 0.10701 | 0.43822 | $3.93648 \times 10^{-5}$ | 0.02217 |
| 6.4 | 0.10504 | 0.42854 | $3.65816 \times 10^{-5}$ | 0.02144 |
| 6.8 | 0.1026 | 0.4181 | $3.37456 \times 10^{-5}$ | 0.01988 |
| 7.2 | 0.1023 | 0.40843 | $3.12653 \times 10^{-5}$ | 0.01367 |
| 7.6 | 0.1009 | 0.39929 | $2.87198 \times 10^{-5}$ | 0.01058 |
| 8.0 | 0.09871 | 0.39092 | $2.61773 \times 10^{-5}$ | 0.01048 |
| 2 |  |  |  |  |
| T (K) | $\chi_{S}$ | $\chi_{T}$ | $\tau$ (s) | $\alpha$ |


| 1.8 | 0.20105 | 0.71947 | $3.51115 \times 10^{-5}$ | 0.08591 |
| :---: | :---: | :---: | :---: | :---: |
| 1.9 | 0.18959 | 0.6906 | $3.11135 \times 10^{-5}$ | 0.08737 |
| 2.0 | 0.18673 | 0.66015 | $2.81235 \times 10^{-5}$ | 0.06759 |
| 2.2 | 0.16967 | 0.62287 | $2.32724 \times 10^{-5}$ | 0.06667 |
| 2.4 | 0.16144 | 0.58927 | $1.97552 \times 10^{-5}$ | 0.05378 |
| 2.6 | 0.15936 | 0.5578 | $1.69242 \times 10^{-5}$ | 0.03441 |
| 2.8 | 0.15789 | 0.52916 | $1.41798 \times 10^{-5}$ | 0.01963 |
| 3.0 | 0.14601 | 0.50458 | $1.08899 \times 10^{-5}$ | 0.02683 |
| 3.2 | 0.14768 | 0.48031 | $8.20644 \times 10^{-6}$ | 0.01659 |
| 3.4 | 0.16043 | 0.45787 | $6.05389 \times 10^{-6}$ | $8.27505 \times 10^{-4}$ |
| 3.6 | 0.22726 | 0.44122 | $5.30153 \times 10^{-6}$ | 0.00112 |
| 4.0 | 0.00937 | 0.4237 | $1.14426 \times 10^{-6}$ | 0.11771 |
| 4.2 | $1.98419 \times 10^{-7}$ | 0.40805 | $3.95027 \times 10^{-7}$ | 0.23328 |
| 4.4 | $3.04973 \times 10^{-7}$ | 0.39081 | $1.97231 \times 10-7$ | 0.24095 |
| 4.6 | $1.94707 \times 10^{-6}$ | 0.37507 | $1.37693 \times 10^{-7}$ | 0.19865 |
| 4.8 | $9.15375 \times 10^{-6}$ | 0.36211 | $2.40381 \times 10^{-8}$ | 0.34942 |
| 5.0 | $1.77633 \times 10^{-5}$ | 0.34628 | $1.55948 \times 10^{-7}$ | $7.46318 \times 10^{-9}$ |

## Compoutation Details

Complete active space second-order multiconfigurational perturbation theory (CASPT2) considering the effect of the dynamic electron correlation with MOLCAS 8.4 program package ${ }^{4}$ was performed on the basis of single-crystal X-ray determined geometries of $\mathbf{1}$ and $\mathbf{2}$ (see Fig. S8 for the calculated model structures of $\mathbf{1}$ and $\mathbf{2}$ ).


1


2

Fig. S12 Calculated model structures of individual $\mathrm{Co}^{\mathrm{II}}$ fragments. H atoms are omitted for clarity.

For the first complete-active-space self-consistent field (CASSCF) calculation, the basis sets for all atoms are atomic natural orbitals from the MOLCAS ANO-RCC library: ANO-RCC-VTZP for magnetic center ion $\mathrm{Co}^{\mathrm{II}}$; VTZ for close $\mathrm{Br}, \mathrm{Cl}$ and P atoms; VDZ for distant atoms. The calculations employed the second order Douglas-Kroll-Hess Hamiltonian, where scalar relativistic contractions were taken into account in the basis set. The active electrons in $5+5^{\prime}$ active orbitals include all d electrons $\left(\operatorname{CAS}\left(7\right.\right.$ in $\left.\left.5+5^{\prime}\right)\right)$ in the CASSCF calculations. To exclude all the doubts, we calculated all the roots in the active orbitals. The effect of the dynamical electronic correlation was applied using CASPT2 based on the first CASSCF calculation. After that, the spin-orbit coupling was handled separately in the restricted active space state interaction (RASSI-SO)
procedure. ${ }^{5,6}$ We have mixed the maximum number of spin-free state which was possible with our hardware (all from 10 quadruplets and 40 doublets). SINGLE_ANISO ${ }^{7-9}$ program was used to obtain zero-field splitting parameters $D(E)\left(\mathrm{cm}^{-1}\right), \boldsymbol{g}$ tensors, energy levels, magnetic axes, et al. based on the above CASPT2/RASSI-SO calculations.

To deeply analyze the magnetic anisotropy, ORCA 4.2 calculations ${ }^{10}$ were performed with CASSCF, followed by N-electron valence second-order perturbation theory (NEVPT2). The spinorbit coupling (SOC) operator used was the efficient implementation of the multicenter spin-orbit mean-field (SOMF) concept developed by Hess et al. ${ }^{6}$ The spin-spin contributions (SSC) to the $D$ values were also included although they are very small for our complexes. The NEVPT2 ${ }^{11-14}$ calculation with seven 3d electrons in five Co 3d-based orbitals ( $\operatorname{CAS}(7,5)$ ). In the calculations, the orbitals were determined for the average of $10 S=3 / 2$ and $40 S=1 / 2$ roots. All calculations were performed with triple- $\zeta$ with one polarization function def2-TZVP ${ }^{15-17}$ basis set for all atoms.

Table S6 Calculated spin-free energies $\left(\mathrm{cm}^{-1}\right)$ of the lowest ten terms $(S=3 / 2)$ of $\mathbf{1}$ and $\mathbf{2}$ using

## CASPT2/RASSI-SO with MOLCAS 8.4.

| spin-free states | $\mathbf{1}$ | $\mathbf{2}$ |
| :---: | :---: | :---: |
|  | $E / \mathrm{cm}^{-1}$ | $E / \mathrm{cm}^{-1}$ |
| 1 | 0.0 | 0.0 |
| 2 | 2817.1 | 2684.3 |
| 3 | 3209.6 | 3174.9 |
| 4 | 3616.5 | 3290.2 |
| 5 | 4091.9 | 3654.0 |
| 6 | 8444.8 | 7742.8 |
| 7 | 8446.9 | 7747.4 |
| 8 | 16389.8 | 16959.3 |
| 9 | 16403.9 | 16994.2 |
| 10 | 19328.5 | 18823.7 |

Table S7 Calculated weights of the five most important spin-orbit-free states for the lowest two spin-orbit states of $\mathbf{1}$ and $\mathbf{2}$ using CASPT2/RASSI-SO with MOLCAS 8.4.

| Spin-orbit <br> states | Energ <br> y <br> $\left(\mathrm{cm}^{-1}\right)$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 0.0 | $1,1.5,0.9580$ | $3,1.5,0.0171$ | $4,1.5,0.0106$ | $2,1.5,0.0102$ | $5,1.5,0.0019$ |
|  | 2 | 78.2 | $1,1.5,0.9728$ | $3,1.5,0.0091$ | $2,1.5,0.0084$ | $4,1.5,0.0073$ | $5,1.5,0.0013$ |
|  | 1 | 0.0 | $1,1.5,0.9580$ | $3,1.5,0.0178$ | $4,1.5,0.0166$ | $2,1.5,0.0038$ | $5,1.5,0.0019$ |
|  | 2 | 63.6 | $1,1.5,0.9690$ | $2,1.5,0.0101$ | $4,1.5,0.0096$ | $3,1.5,0.0089$ | $5,1.5,0.0012$ |

Table S8 Contributions of the excited states (with relative energy $\mathrm{cm}^{-1}$ ) to $D$ and $E$ values $\left(\mathrm{cm}^{-1}\right.$ )
for $\mathbf{1}$ and $\mathbf{2}$ using NEVPT2 with ORCA 4.2.

| Fragments | State No. | Mult | Energy, $\mathrm{cm}^{-1}$ | Contribution, $\mathrm{cm}^{-1}$ | Contribution, $\mathrm{cm}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $D$ | $E$ |
| 1 | 1 | 4 | 2923.4 | -10.039 | 0.000 |
|  | 2 | 4 | 2972.8 | 16.636 | 15.973 |
|  | 3 | 4 | 2974.4 | 16.618 | -15.973 |
| 2 | 1 | 4 | 2384.2 | -12.687 | 0.000 |
|  | 2 | 4 | 2705.1 | 16.733 | 16.629 |
|  | 3 | 4 | 2707.0 | 16.718 | -16.629 |

Table S9 Relative energies ( $\mathrm{cm}^{-1}$ ) of ligand field one-electron states (in the basis of d-AOs) of $\mathbf{1}$ and 2 from AILFT analysis using NEVPT2 with ORCA 4.2.

| Fragments | No. | LF one-electron state | Energy, $\mathrm{cm}^{-1}$ |
| :---: | :---: | :---: | :---: |
| 1 | 1 | $0.97 \mathrm{~d}_{\mathrm{yz}}-0.15 \mathrm{~d}_{\mathrm{xy}}-0.15 \mathrm{~d}_{\mathrm{x} 2 \mathrm{y} 2}$ | 0.0 |
|  | 2 | $0.97 \mathrm{~d}_{\mathrm{xz}}-0.16 \mathrm{~d}_{\mathrm{xy}}+0.15 \mathrm{~d}_{\mathrm{x} 2 \mathrm{y} 2}$ | 2.1 |
|  | 3 | $0.94 \mathrm{~d}_{\mathrm{xy}}+0.27 \mathrm{~d}_{\mathrm{x} 2 \mathrm{y} 2}$ | 3761.4 |
|  | 4 | $-0.94 \mathrm{~d}_{\mathrm{x} 2-\mathrm{y} 2}+0.27 \mathrm{~d}_{\mathrm{xy}}$ | 3763.9 |
|  | 5 | $1.00 \mathrm{~d}_{22}$ | 3933.5 |
| 2 | 1 | $-0.97 \mathrm{~d}_{\mathrm{yz}}-0.24 \mathrm{~d}_{\mathrm{x} 2-\mathrm{y} 2}$ | 0.0 |
|  | 2 | $0.97 \mathrm{~d}_{\mathrm{xz}}+0.24 \mathrm{~d}_{\mathrm{xy}}$ | 1.9 |
|  | 3 | $0.95 \mathrm{~d}_{\mathrm{xy}}-0.23 \mathrm{~d}_{\mathrm{xz}}$ | 3094.6 |
|  | 4 | $0.95 \mathrm{~d}_{\mathrm{x} 2 \mathrm{y} 2}-0.23 \mathrm{~d}_{\mathrm{yz}}$ | 3096.5 |
|  | 5 | $1.00 \mathrm{~d}_{22}$ | 3929.6 |



Fig. S13 Orbital energies computed for the ground states of $\mathbf{1}$ and $\mathbf{2}$ using NEVPT2 with ORCA
4.2. The percentage mention reveals the percent of the corresponding configuration mixing.


$\mathrm{d}_{\mathrm{xy}} \uparrow \uparrow \uparrow \uparrow \uparrow \mathrm{d}_{\mathrm{xy}} \uparrow \uparrow \uparrow \uparrow \uparrow \mathrm{d}_{\mathrm{xy}} \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$

 1 st $28.8 \% 27.1 \% 22.1 \% 22.0 \%$ nd $37.9 \% \quad 29.4 \% \quad 28.0 \%$ 3rd $\quad 37.9 \% \quad 28.7 \% \quad 28.6 \%$ 1


Fig. S14 Multi-determinant wavefunction of the selected excited states having important
contributions to $D$ tensor for $\mathbf{1}$ and 2. The computed CI coefficients that are larger than $10 \%$ are shown above.


Fig. S15 Comparisons of the calculated (solid line) and the experimental magnetic susceptibilities for 1-2.



Fig. S16 Orientations of the local magnetic axes (red: $g_{x}$; blue: $g_{y}$; green: $g_{z}$ ) on Co ${ }^{\text {II }}$ ions of $\mathbf{1}$ and

2 in their ground spin-orbit states using CASPT2/RASSI-SO with MOLCAS 8.4.

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