

## Supporting Information

Assembly of pinwheel/twist shaped chiral lanthanide clusters with rotor structures by annular/linear growth mechanism and their magnetic properties

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**Keywords:** Chiral lanthanide clusters; solvothermal synthesis; annular growth mechanism; linear growth mechanism; magnetic properties

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## Experimental Section

### Materials and Measurements.

All chemicals and solvents were analytical grade and were used without further purification. The infrared spectra were carried out on a Pekin-Elmer Two spectrophotometer with pressed KBr pellets. The elemental analyses were determined on a Perkin-Elmer model 240 °C elemental analyzer. The powder X-ray diffraction (PXRD) spectra were measured on a Rigaku D/Max-3c diffractometer with Cu K $\alpha$  radiation ( $\lambda = 1.5418 \text{ \AA}$ ). Thermogravimetric analyses were performed on a PerkinElmer PyrisDiamond TG-DTA instrument under an N<sub>2</sub> atmosphere using a heating rate of 5 °C min<sup>-1</sup> from room temperature up to 1000 °C. The circular dichroism (CD) spectra were recorded on a JASCO J-1500 spectropolarimeter at room temperature. Magnetic properties were performed on a Superconducting Quantum Interference Device (SQUID) magnetometer. The diamagnetism of all constituent atoms was corrected with Pascal's constant.

### X-ray crystallography.

Single-crystal X-ray diffraction (SCXRD) data were collected on a ROD, Synergy Custom DW system, HyPix diffractometer (Cu-K $\alpha$  radiation and  $\lambda = 1.54184 \text{ \AA}$ ) in  $\Phi$  and  $\omega$  scan modes. The structures were solved by direct methods, and refined by a full-matrix least-squares method on the basis of  $F^2$  by using *SHELXL*.<sup>[1]</sup> Anisotropic thermal parameters were applied to all non-hydrogen atoms. Hydrogen atoms were generated geometrically. Highly disordered free solvent molecules were removed using the SQUEEZE function of PLATON. The crystallographic data for the ligand and clusters **R-1**, **S-1**, **R-2** and **S-2** are listed in Table S1, and selected bond lengths and angles are given in Table S2–S5. The CCDC reference numbers for the crystal structures of clusters **R-1**, **S-1**, **R-2** and **S-2** are 2183488–2183491, respectively.

[1] Sheldrick, G. M. *Acta Crystallogr., Sect. C: Struct. Chem.* **2015**, *71*, 3–8.

### The synthesis method.

**Synthesis of R-1:** **R-2**-hydroxy-2-phenylacetohydrazide (0.1 mmol, 0.0166 g), 2,3-dihydroxybenzaldehyde (0.1 mmol, 0.0138 g), DyCl<sub>3</sub>·6H<sub>2</sub>O (0.5 mmol, 0.1885 g) and triethylamine (80  $\mu$ L) were dissolved in a mixed solvent of ethanol (1.0 mL) and water (0.2 mL) in a Pyrex tube. The tube was sealed and heated at 80 °C in an oven for one day, then cooled down slowly, yellow block crystals were obtained with a yield of about 60% (based on **R-2**-hydroxy-2-

phenylacetohydrazide). Elemental analysis theoretical value ( $C_{82}H_{160}Cl_8Dy_8N_8O_{60}$ ): C, 25.90%; H, 4.24%; N, 2.94%; experimental value: C, 25.85%; H, 4.21%; N, 2.92%. Infrared spectrum data (IR, KBr pellet,  $cm^{-1}$ ): 3324(s), 2984(m), 1613(s), 1457(s), 1400(m), 1263(s), 1207(m), 1065(s), 872(m), 749(m), 701(w), 611(w).

**Synthesis of S-1:** The synthesis method was similar to that for **R-1** by using **S-2-hydroxy-2-phenylacetohydrazide** instead of **R-2-hydroxy-2-phenylacetohydrazide**. The yield is 60% (based on **S-2-hydroxy-2-phenylacetohydrazide**). Elemental analysis theoretical value ( $C_{88}H_{184}Cl_8Dy_8N_8O_{66}$ ): C, 26.46%; H, 4.64%; N, 2.80%; experimental value: C, 26.41%; H, 4.62%; N, 2.76%. Infrared spectrum data (IR, KBr pellet,  $cm^{-1}$ ): 3315(s), 2978(m), 1604(s), 1554(m), 1457(s), 1393(m), 1267(s), 1212(m), 1060(s), 875(m), 746(m), 702(w), 604(w).

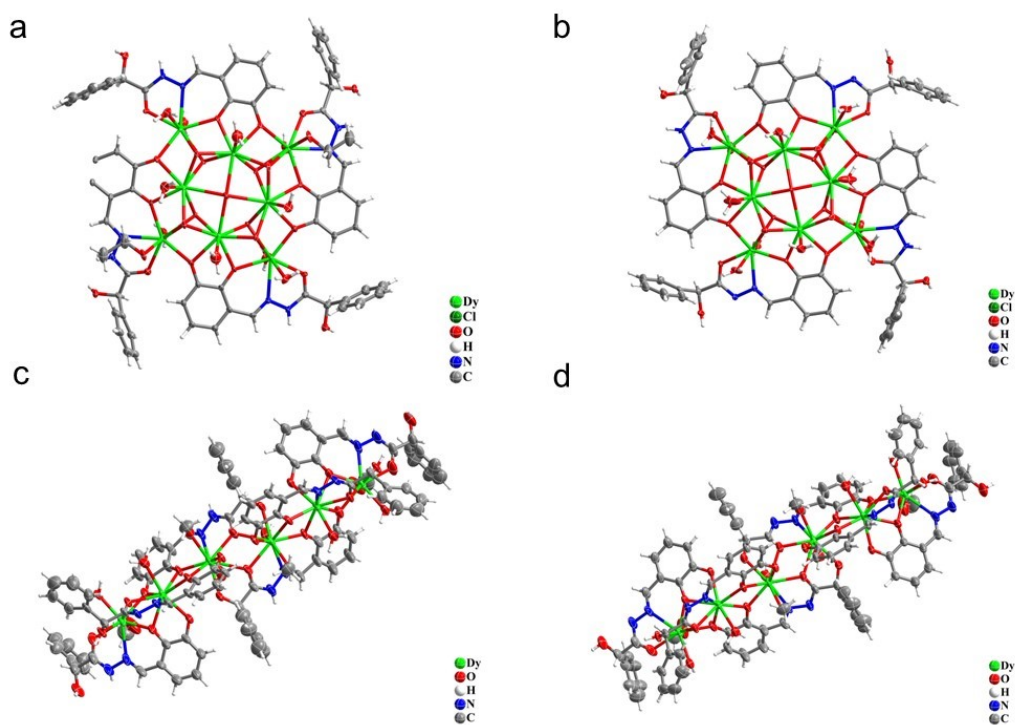
**Synthesis of R-2:** **R-2-hydroxy-2-phenylacetohydrazide** (0.1 mmol, 0.0166 g), **2,3-dihydroxybenzaldehyde** (0.1 mmol, 0.0138 g),  $Dy(NO_3)_3 \cdot 6H_2O$  (0.5 mmol, 0.1885 g) and triethylamine (80  $\mu$ L) were dissolved in a mixed solvent of methanol (1.0 mL) and water (0.2 mL) in a Pyrex tube. The tube was sealed and heated at 80 °C in an oven for one day, then cooled down slowly, yellow rhombic crystals were obtained with a yield of about 65% (based on **R-2-hydroxy-2-phenylacetohydrazide**). Elemental analysis theoretical value ( $C_{107}H_{174}Dy_6N_{14}O_{68}$ ): C, 34.55%; H, 4.71%; N, 5.27%; experimental value: C, 34.53%; H, 4.67%; N, 5.22%. Infrared spectrum data (IR, KBr pellet,  $cm^{-1}$ ): 3408(s), 2980(m), 1614(s), 1453(s), 1384(s), 1263(s), 1206(m), 1060(s), 872(m), 739(s), 602(w).

**Synthesis of S-2:** The synthesis method was similar to that for **R-2** by using **S-2-hydroxy-2-phenylacetohydrazide** instead of **R-2-hydroxy-2-phenylacetohydrazide**. The yield is 65 % (based on **S-2-hydroxy-2-phenylacetohydrazide**). Elemental analysis theoretical value ( $C_{107}H_{168}Dy_6N_{14}O_{67}$ ): C, 34.75%; H, 4.58%; N, 5.30%; experimental value: C, 34.72%; H, 4.53%; N, 5.28%. Infrared spectrum data (IR, KBr pellet,  $cm^{-1}$ ): 3415(s), 2982(s), 1607(s), 1453(s), 1387(s), 1259(s), 1205(m), 1060(s), 872(m), 738(s), 605(w).

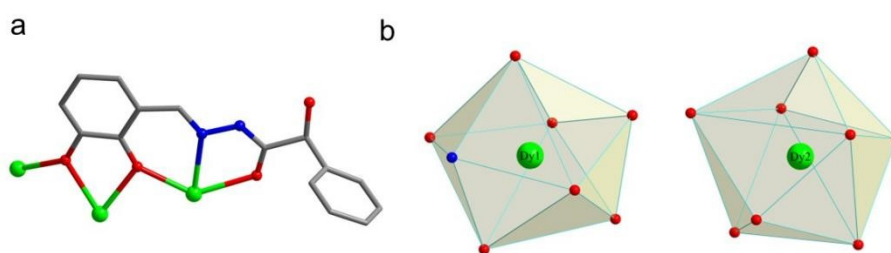
**Table S1.** Crystallographic data of the clusters **R-1**, **S-1**, **R-2** and **S-2**.

	<b>R-1</b>	<b>S-1</b>	<b>R-2</b>	<b>S-2</b>
Formula	C <sub>82</sub> H <sub>160</sub> Cl <sub>8</sub> Dy <sub>8</sub> N <sub>8</sub> O <sub>60</sub>	C <sub>88</sub> H <sub>184</sub> Cl <sub>8</sub> Dy <sub>8</sub> N <sub>8</sub> O <sub>66</sub>	C <sub>107</sub> H <sub>174</sub> Dy <sub>6</sub> N <sub>14</sub> O <sub>68</sub>	C <sub>107</sub> H <sub>168</sub> Dy <sub>6</sub> N <sub>14</sub> O <sub>67</sub>
Formula weight	3801.77	3994.02	3719.59	3697.54
<i>T</i> , K	100.00(10)	100.00(10)	100.00(10)	100.00(10)
Crystal system	monoclinic	monoclinic	tetragonal	tetragonal
Space group	<i>C2</i>	<i>C2</i>	<i>P4<sub>3</sub>2<sub>1</sub>2</i>	<i>P4<sub>1</sub>2<sub>1</sub>2</i>
<i>a</i> , Å	19.582(16)	19.561(10)	14.400(10)	14.414(10)
<i>b</i> , Å	18.453(15)	18.409(10)	14.400(10)	14.414(10)
<i>c</i> , Å	19.787(14)	19.748(10)	71.412(5)	71.463(4)
$\alpha$ , °	90	90	90	90
$\beta$ , °	92.1497(7)	92.095(10)	90	90
$\gamma$ , °	90	90	90	90
<i>V</i> , Å <sup>3</sup>	7145.45(10)	7107.00(6)	14809.2(2)	14848.7(2)
<i>Z</i>	2	2	4	4
<i>D</i> <sub>c</sub> , g cm <sup>-3</sup>	1.559	1.524	1.389	1.469
$\mu$ , mm <sup>-1</sup>	23.877	23.979	16.479	16.514
<i>F</i> (000)	3200.0	3096.0	6024.0	6432.0
2 $\theta$ range for data collection/°	4.468 to 133.192	4.478 to 154.102	4.95 to 151.65	4.946 to 151.458
Reflns coll.	44229	50425	52013	49848
Unique reflns	12550	14029	14821	14921
<i>R</i> <sub>int</sub>	0.0453	0.0432	0.0429	0.0449
<i>R</i> <sub>1</sub> <sup>a</sup> ( <i>I</i> > 2 $\sigma$ ( <i>I</i> ))	0.0676	0.0433	0.0449	0.0411
<i>wR</i> <sub>2</sub> <sup>b</sup> (all data)	0.1765	0.1171	0.1311	0.1122
GOF	1.098	1.073	1.084	1.061
Flack parameter	0.077(9)	0.019(5)	0.015(5)	0.001(2)

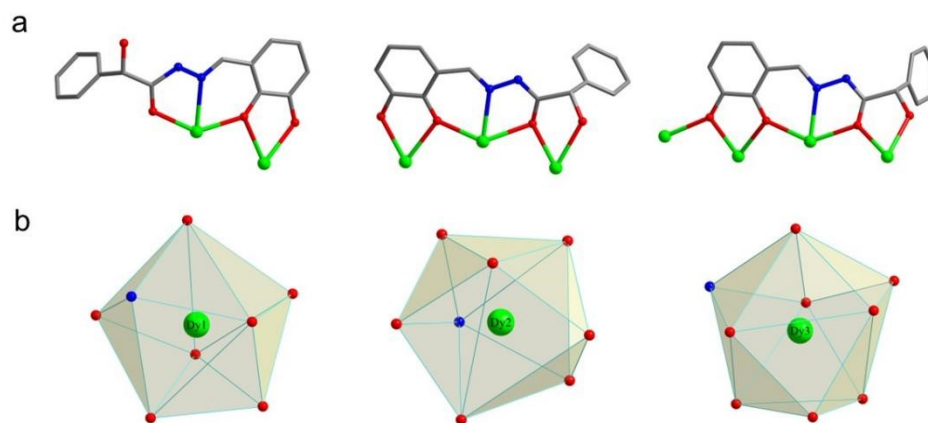
$$^a R_1 = \frac{\sum ||F_o| - |F_c||}{\sum |F_o|}, \quad ^b wR_2 = [\frac{\sum w(F_o^2 - F_c^2)^2}{\sum w(F_o^2)^2}]^{1/2}$$



**Figure S1.** Crystal structures of *R*-1 (a); *S*-1 (b); *R*-2 (c); *S*-2 (d).

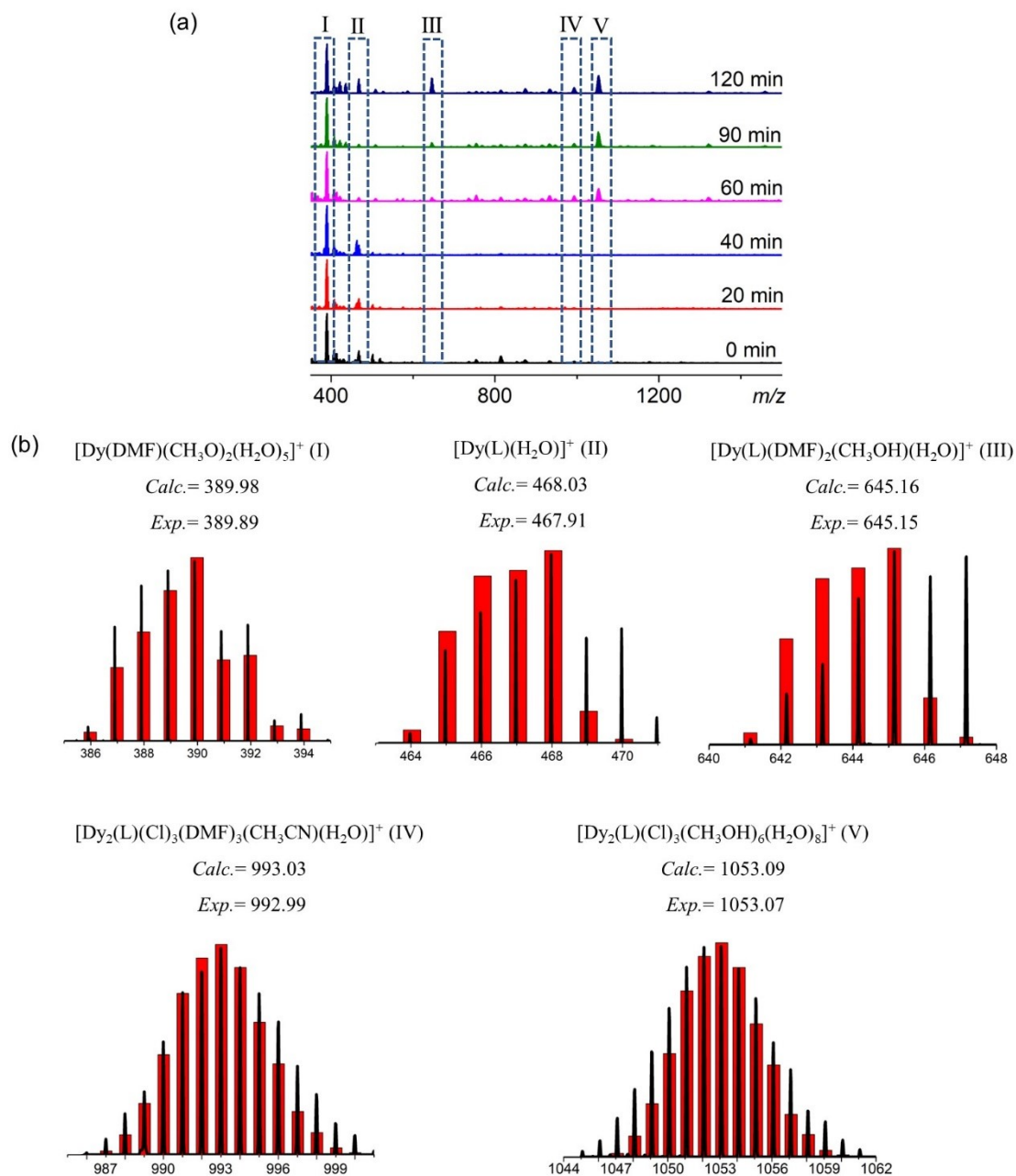


**Figure S2.** Ligand coordination mode of cluster *R*-1 (a); Coordination polyhedron around the Dy(III) ions of cluster *R*-1 (b).

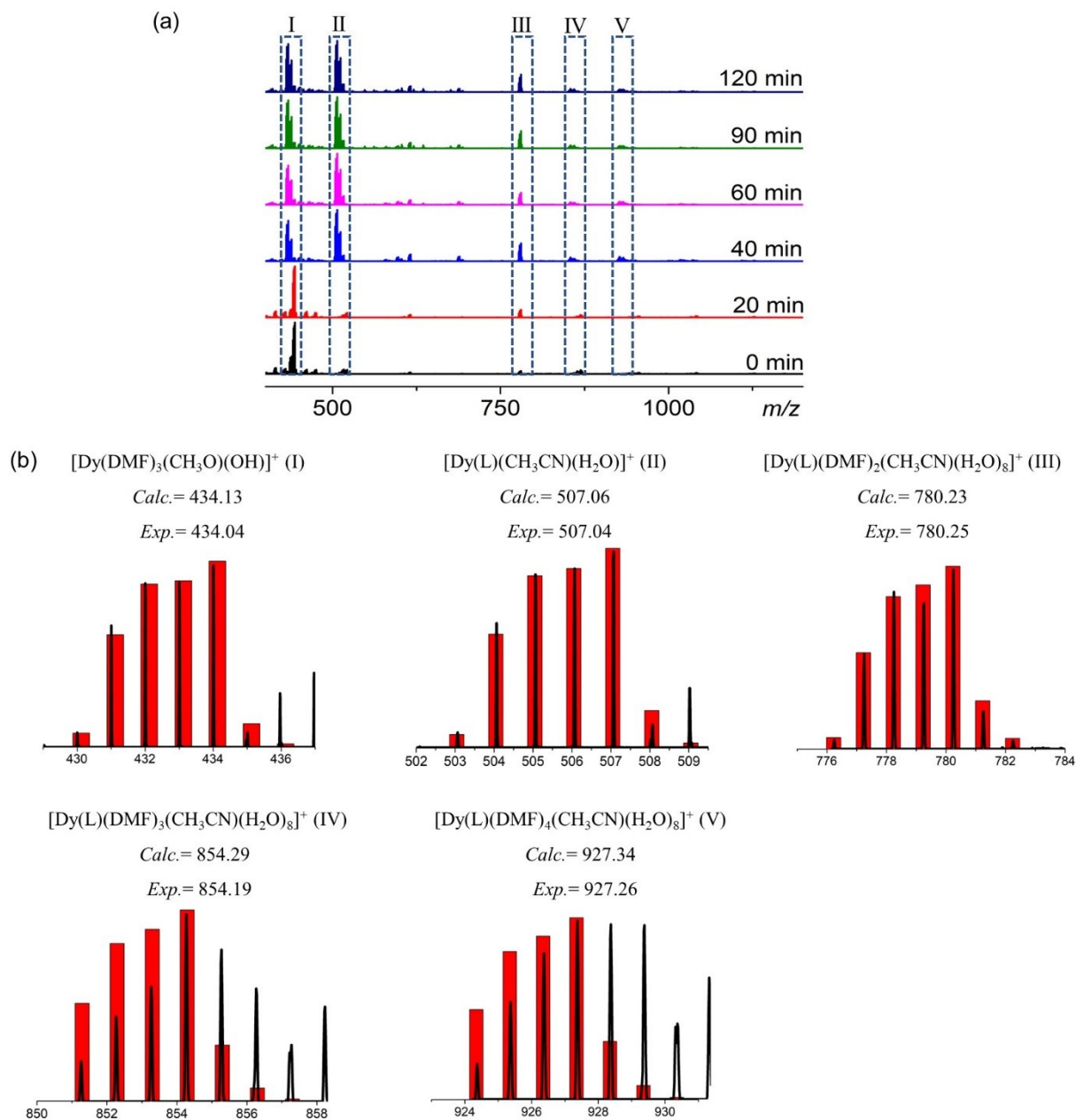


**Figure S3.** Ligand coordination mode of cluster **R-2** (a); Coordination polyhedron around the Dy(III) ions of cluster **R-2** (b).

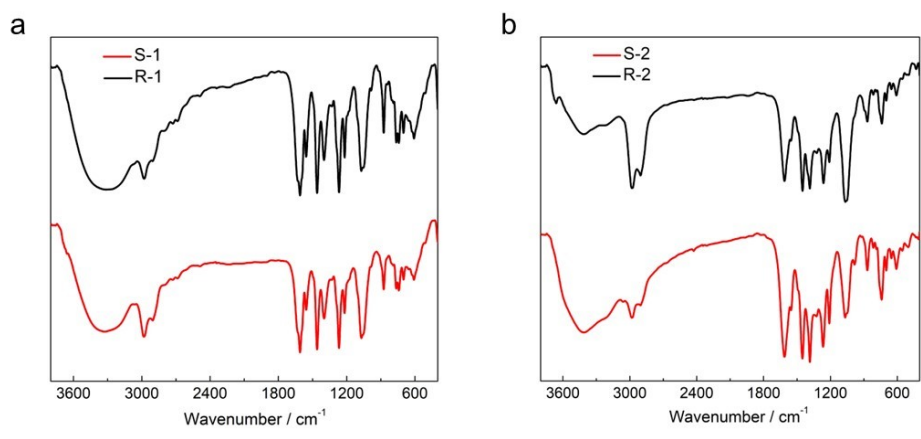




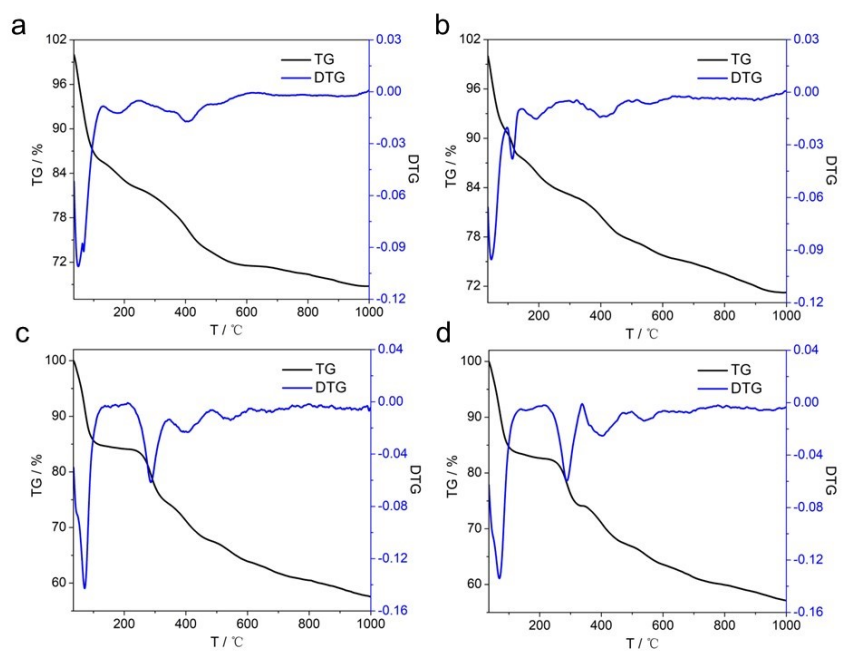
**Figure S4.** Time-dependent HRESI-MS spectra of the initial cluster **R-1** reaction in positive mode (a); Positive HRESI-MS spectra of cluster **R-1** in MeOH (0, 20, 40, 60, 90 and 120 min) (b).



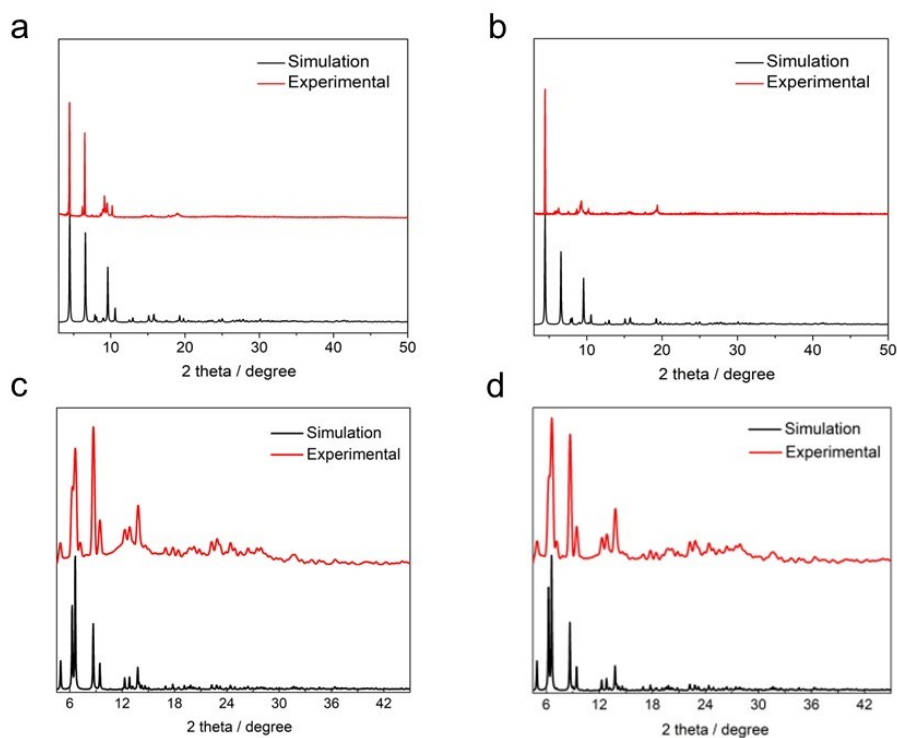
**Figure S5.** Time-dependent HRESI-MS spectra of the initial cluster **R-2** reaction in positive mode (a); Positive HRESI-MS spectra of cluster **R-2** in MeOH (0, 20, 40, 60, 90 and 120 min) (b).



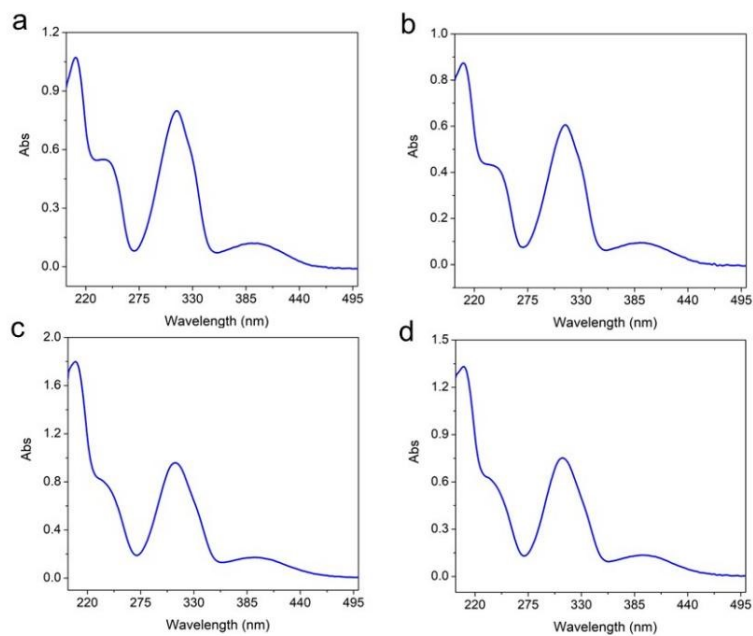
**Figure S6.** Infrared spectra (IR) of clusters *R-1*, *S-1*, *R-2* and *S-2* (a, b).



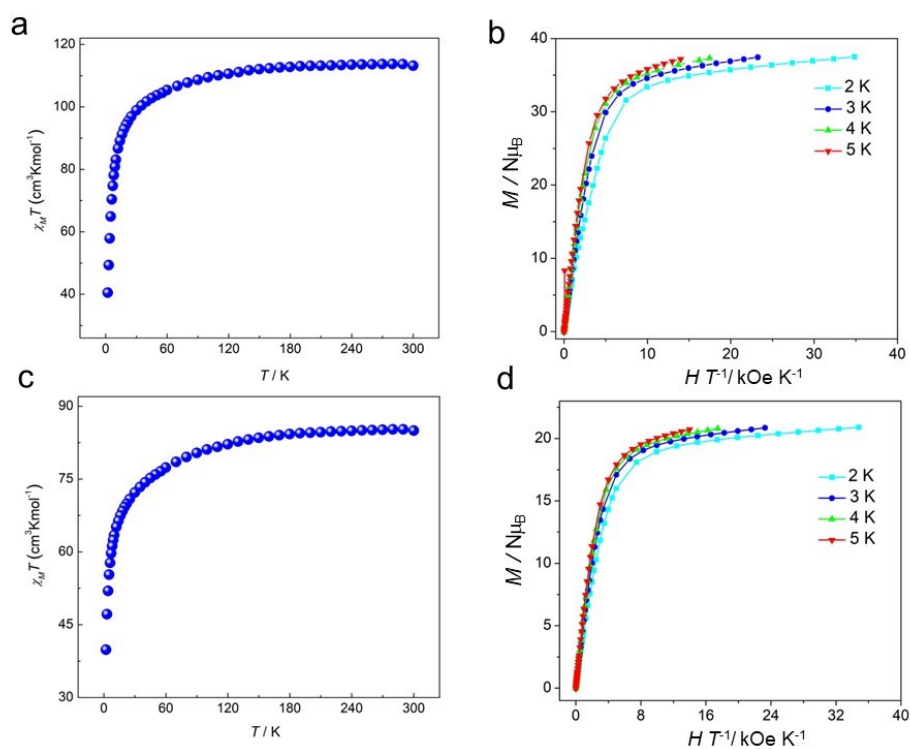
**Figure S7.** TG curve of clusters *R-1*, *S-1*, *R-2* and *S-2* (a–d).



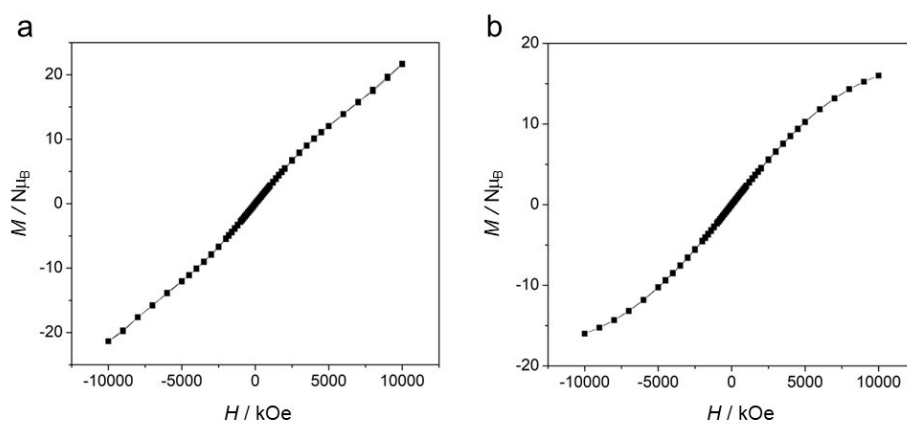
**Figure S8.** Powder diffraction pattern (PXRD) of clusters *R-1*, *S-1*, *R-2* and *S-2* (a–d).



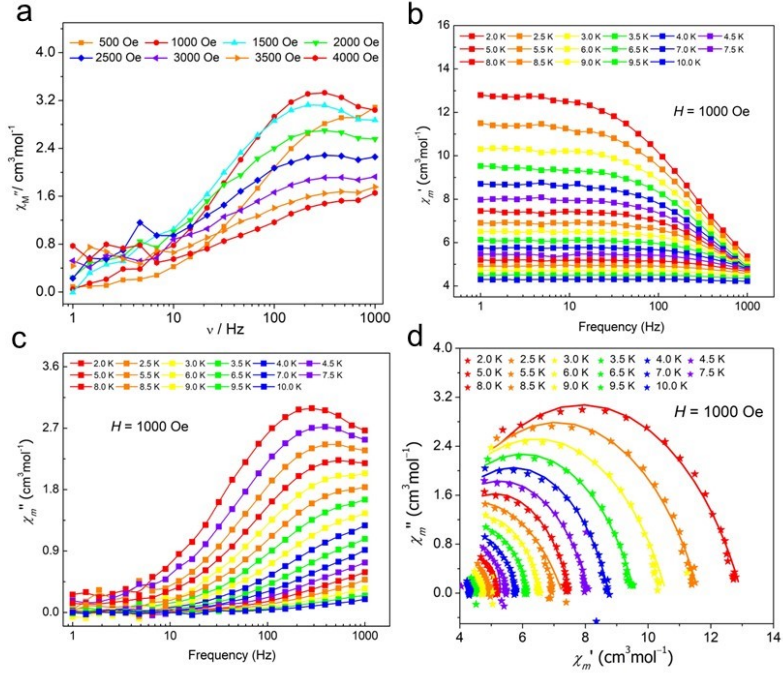
**Figure S9.** The UV-Vis absorption spectra of clusters *R-1*, *S-1*, *R-2* and *S-2* (a–d).



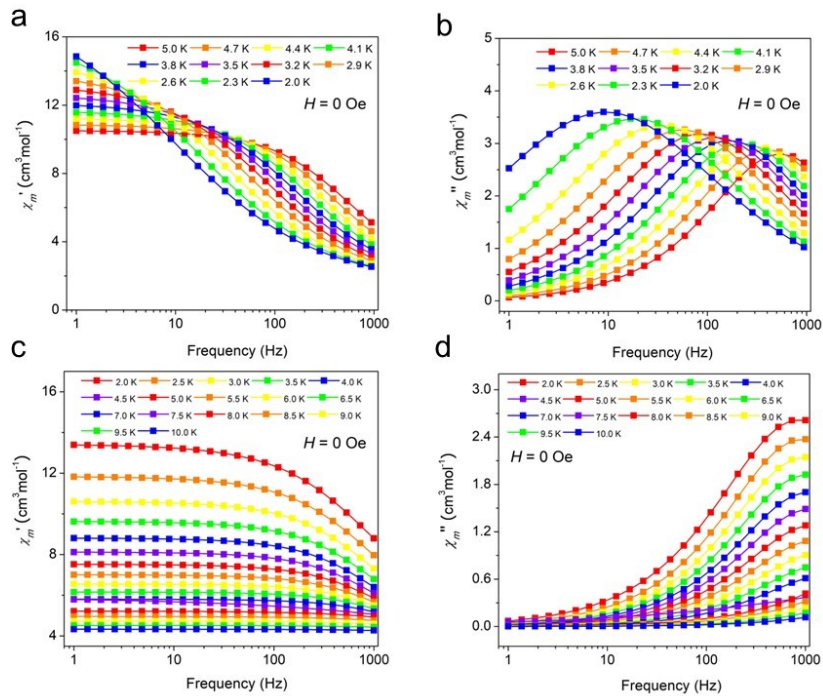
**Figure S10.** Plots of  $\chi_m T$  versus  $T$  for clusters **R-1** and **R-2** (a, c);  $M$  vs.  $H/T$  plots of clusters **R-1** and **R-2** (b, d).



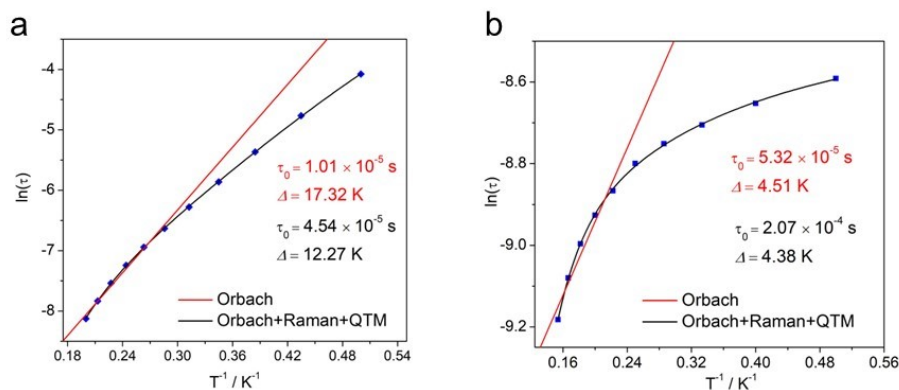
**Figure S11.** Loop curve graph of clusters **R-1** and **R-2** (a, b) at 2 K.



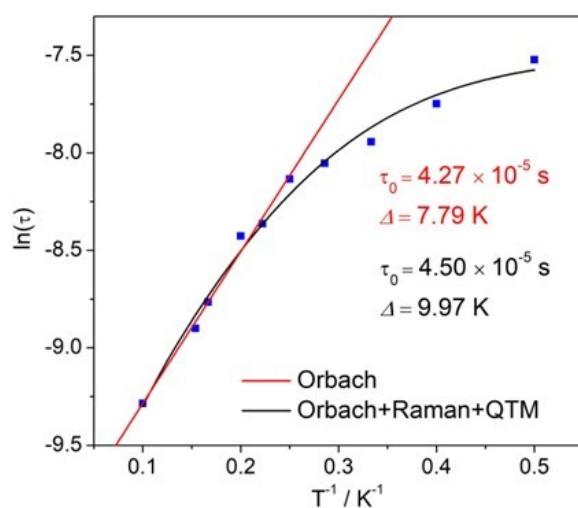
**Figure S12.** Plots of  $\chi''$  vs.  $\nu$  (10–1000 Hz) at 2 K under 500–4000 Oe dc field with a 2 Oe oscillating ac field for cluster **R-2** (a); Variable-frequency AC susceptibilities ( $H = 1000$  Oe) of cluster **R-2** at different temperatures (b, c) and Cole-Cole plots from AC susceptibilities (d).



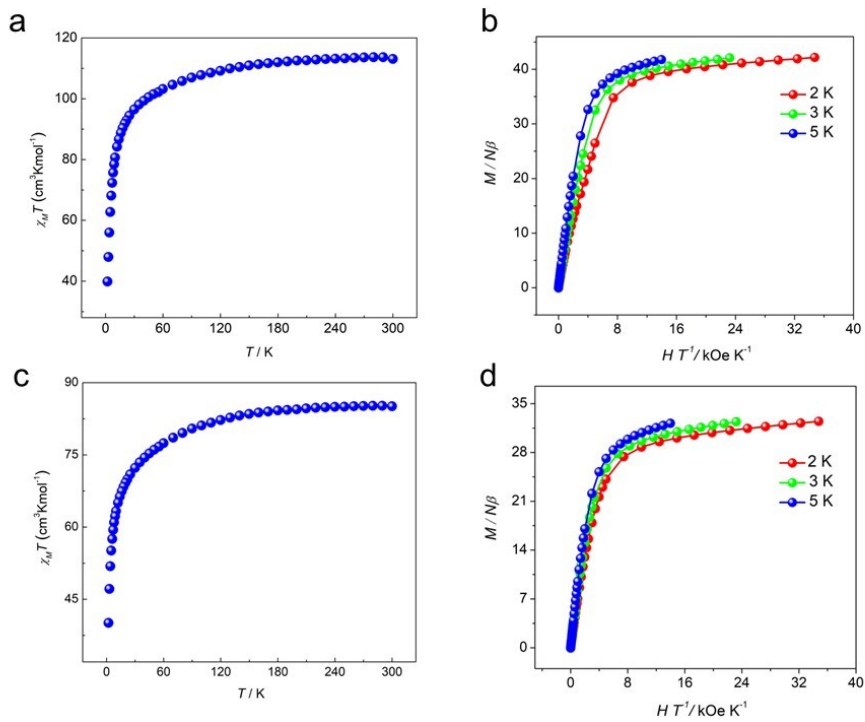
**Figure S13.** Variable-frequency AC susceptibilities ( $H = 0$  Oe) of clusters **R-1** (a, b) and **R-2** (c, d) at different temperatures.



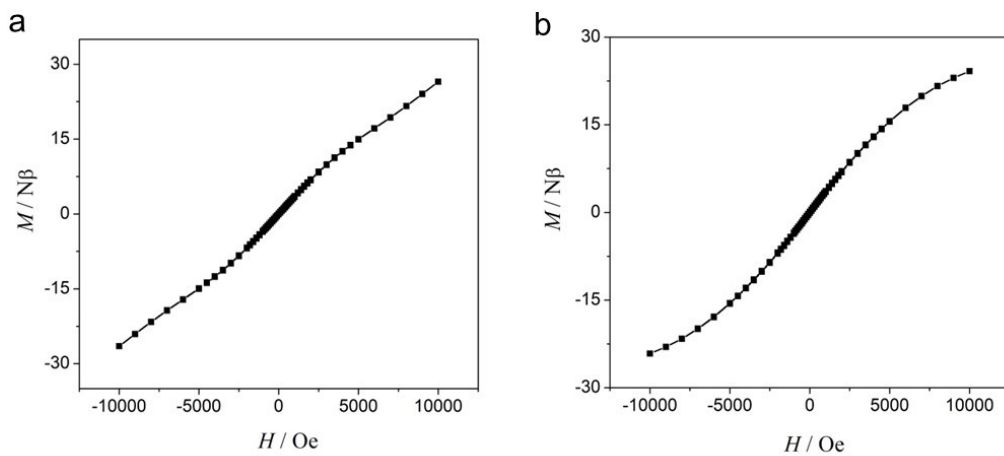
**Figure S14.** Arrhenius plots generated from the temperature-dependent relaxation times extracted from the Cole-Cole fits of the AC susceptibilities for clusters **R-1** and **R-2** under 0 Oe (a, b). Symbols show the extracted times, and the lines are least-squares fits.



**Figure S15.** Arrhenius plots generated from the temperature-dependent relaxation times extracted from the Cole-Cole fits of the AC susceptibilities for cluster **R-2** under 1000 Oe. Symbols show the extracted times, and the lines are least-squares fits.

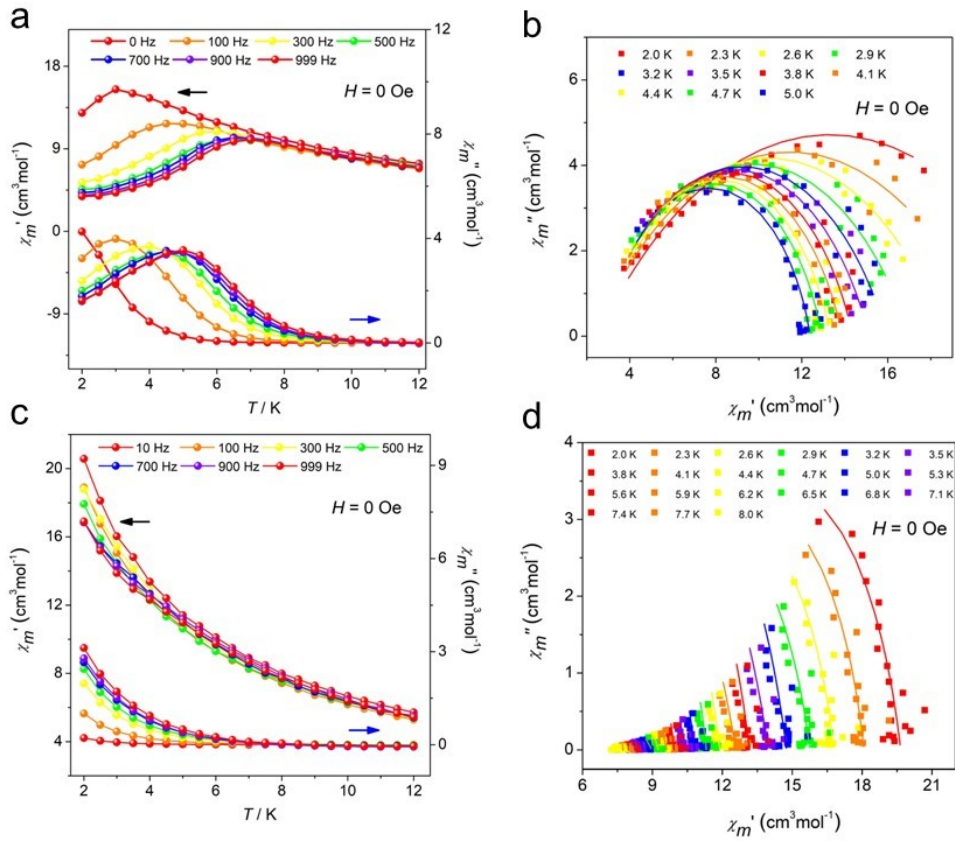


**Figure S16.** Plots of  $\chi_m T$  versus  $T$  for clusters **S-1** and **S-2** (a, c);  $M$  vs.  $H/T$  plots of clusters **S-1** and **S-2** (b, d).

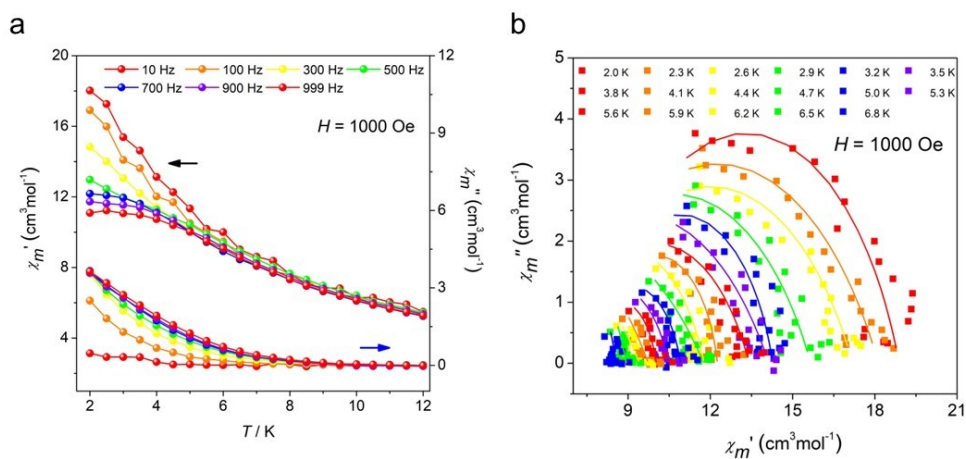


**Figure S17.** Loop curve graph of clusters **S-1** and **S-2** (a, b) at 2 K.

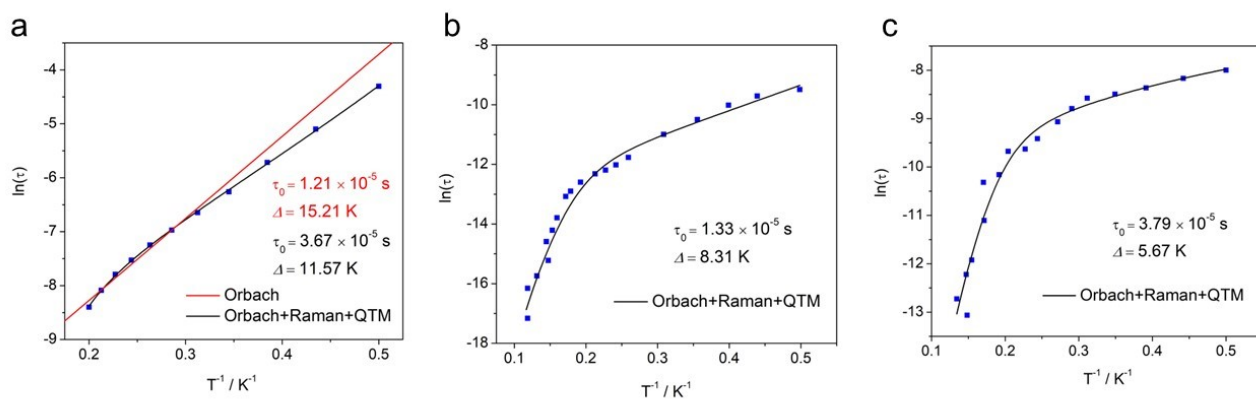




**Figure S18.** Temperature-dependent  $\chi'$  and  $\chi''$  AC susceptibilities under 0 Oe DC fields for **S-1** and **S-2** (a, c); Cole–Cole plots for **S-1** and **S-2** (b, d).



**Figure S19.** Temperature-dependent  $\chi'$  and  $\chi''$  AC susceptibilities under 1000 Oe DC fields for **S-2** (a); Cole–Cole plots for **S-2** (b).



**Figure S20.** Arrhenius plots generated from the temperature-dependent relaxation times extracted from the Cole-Cole fits of the AC susceptibilities for clusters **S-1** and **S-2** under 0 Oe (a, b) and **S-2** under 1000 Oe (c). Symbols show the extracted times, and the lines are least-squares fits.

**Table S2.** Selected bond lengths (Å) and angles (°) of cluster **R-1**.

Bond lengths (Å)					
Dy1-O10	2.416(11)	Dy2-O3	2.330(11)	Dy3-N4	2.536(13)
Dy1-O17	2.361(15)	Dy2-O9	2.412(10)	Dy3-O15	2.372(12)
Dy1-O3	2.289(10)	Dy2-O11	2.327(9)	Dy4-O12	2.323(11)
Dy1-O2	2.395(11)	Dy2-O23	2.321(18)	Dy4-O10 <sup>i</sup>	2.335(10)
Dy1-O9	2.459(10)	Dy2-O33	2.586(5)	Dy4-O9 <sup>i</sup>	2.381(10)
Dy1-O8 <sup>i</sup>	2.271(11)	Dy3-O14	2.367(12)	Dy4-O11	2.381(10)
Dy1-N2	2.543(14)	Dy3-O12	2.417(10)	Dy4-O16	2.371(11)
Dy1-O18	2.345(12)	Dy3-O4	2.255(11)	Dy4-O7	2.348(10)
Dy2-O12	2.351(10)	Dy3-O6	2.359(12)	Dy4-O8	2.334(11)
Dy2-O10	2.317(10)	Dy3-O11	2.425(10)	Dy4-O33	2.632(5)
Dy2-O4	2.357(11)	Dy3-O7	2.245(10)		
Bond angles (°)					
O10-Dy1-O9	60.6(3)	O3-Dy2-O9	73.7(4)	O14-Dy3-O12	132.7(4)
O10-Dy1-N2	129.3(4)	O3-Dy2-O33	146.5(3)	O14-Dy3-O11	73.0(4)
O17-Dy1-O10	136.9(4)	O9-Dy2-O33	77.9(4)	O14-Dy3-N4	79.2(4)
O17-Dy1-O2	72.3(5)	O11-Dy2-O12	62.2(3)	O14-Dy3-O15	149.3(4)

O17-Dy1-O9	76.6(4)	O11-Dy2-O4	77.5(4)	O15-Dy3-O12	77.8(4)
O17-Dy1-N2	78.5(5)	O11-Dy2-O3	116.6(4)	O15-Dy3-O11	137.7(4)
O3-Dy1-O10	73.4(4)	O11-Dy2-O9	83.2(3)	O15-Dy3-N4	75.5(4)
O3-Dy1-O17	90.5(5)	O11-Dy2-O33	76.6(4)	O7-Dy3-N4	71.2(4)
O3-Dy1-O2	135.7(4)	O23-Dy2-O12	77.4(5)	O12-Dy4-O10 <sup>i</sup>	133.0(4)
O3-Dy1-O9	73.5(3)	O23-Dy2-O4	79.8(5)	O12-Dy4-O9 <sup>i</sup>	141.7(3)
O3-Dy1-N2	71.4(4)	O23-Dy2-O3	85.2(5)	O12-Dy4-O11	61.8(3)
O3-Dy1-O18	97.6(5)	O23-Dy2-O9	138.7(5)	O12-Dy4-O16	75.1(4)
O2-Dy1-O10	144.6(4)	O23-Dy2-O11	138.0(5)	O12-Dy4-O7	75.0(4)
O2-Dy1-O9	136.1(4)	O23-Dy2-O33	105.4(7)	O12-Dy4-O8	138.0(4)
O2-Dy1-N2	65.4(4)	O10-Dy2-O33	76.8(3)	O12-Dy4-O33	75.4(3)
O9-Dy1-N2	136.3(4)	O4-Dy2-O9	121.1(4)	O10 <sup>i</sup> -Dy4-O9 <sup>i</sup>	62.9(4)
O8 <sup>i</sup> -Dy1-O10	72.6(4)	O4-Dy2-O33	145.4(3)	O10 <sup>i</sup> -Dy4-O11	140.3(3)
O8 <sup>i</sup> -Dy1-O17	102.9(5)	O3-Dy2-O12	137.6(4)	O10 <sup>i</sup> -Dy4-O16	77.4(4)
O8 <sup>i</sup> -Dy1-O3	142.0(4)	O12-Dy3-O11	59.9(3)	O10 <sup>i</sup> -Dy4-O7	140.4(3)
O8 <sup>i</sup> -Dy1-O2	82.3(4)	O12-Dy3-N4	133.1(4)	O10 <sup>i</sup> -Dy4-O33	75.6(3)
O8 <sup>i</sup> -Dy1-O9	75.3(4)	O4-Dy3-O14	101.6(4)	O9 <sup>i</sup> -Dy4-O33	77.5(4)
O8 <sup>i</sup> -Dy1-N2	145.8(4)	O4-Dy3-O12	72.4(4)	O11-Dy4-O9 <sup>i</sup>	85.2(3)
O8 <sup>i</sup> -Dy1-O18	92.0(4)	O4-Dy3-O6	79.7(4)	O11-Dy4-O33	74.8(4)
O18-Dy1-O10	78.7(4)	O4-Dy3-O11	77.4(4)	O16-Dy4-O9 <sup>i</sup>	138.6(4)
O18-Dy1-O17	144.0(5)	O4-Dy3-N4	143.6(4)	O16-Dy4-O11	135.8(4)
O18-Dy1-O2	77.7(5)	O4-Dy3-O15	89.0(4)	O16-Dy4-O33	104.7(6)
O18-Dy1-O9	139.2(4)	O6-Dy3-O14	74.2(4)	O7-Dy4-O9 <sup>i</sup>	115.8(4)
O18-Dy1-N2	71.2(5)	O6-Dy3-O12	144.2(4)	O7-Dy4-O11	73.3(3)
O12-Dy2-O4	71.9(4)	O6-Dy3-O11	134.8(4)	O7-Dy4-O16	87.1(4)
O12-Dy2-O9	140.4(4)	O6-Dy3-N4	65.4(4)	O7-Dy4-O33	143.9(3)
O12-Dy2-O33	75.9(3)	O6-Dy3-O15	79.7(5)	O8-Dy4-O10 <sup>i</sup>	73.0(4)
O10-Dy2-O12	136.3(4)	O11-Dy3-N4	135.0(4)	O8-Dy4-O9 <sup>i</sup>	75.6(4)

O10-Dy2-O4	136.7(4)	O7-Dy3-O14	90.3(4)	O8-Dy4-O11	123.6(4)
O10-Dy2-O3	74.5(4)	O7-Dy3-O12	75.0(4)	O8-Dy4-O16	82.3(5)
O10-Dy2-O9	62.7(4)	O7-Dy3-O4	144.5(4)	O8-Dy4-O7	68.9(4)
O10-Dy2-O11	140.3(4)	O7-Dy3-O6	135.8(4)	O8-Dy4-O33	145.5(3)
O10-Dy2-O23	77.8(5)	O7-Dy3-O11	74.3(3)		
O3-Dy2-O4	67.1(4)	O7-Dy3-O15	97.6(5)		

**Table S3.** Selected bond lengths (Å) and angles (°) of cluster **S-1**.

<b>Bond lengths (Å)</b>					
Dy1-O11	2.454(6)	Dy2-O9	2.318(6)	Dy3-O7	2.262(5)
Dy1-O12	2.440(7)	Dy2-O10	2.365(6)	Dy3-O15	2.393(7)
Dy1-O2 <sup>i</sup>	2.353(7)	Dy2-O8	2.328(6)	Dy4-O11 <sup>i</sup>	2.399(6)
Dy1-O18	2.322(9)	Dy2-O7	2.346(6)	Dy4-O12 <sup>i</sup>	2.322(6)
Dy1-O3 <sup>i</sup>	2.273(6)	Dy2-O13	2.632(3)	Dy4-O9	2.358(6)
Dy1-O8	2.277(6)	Dy3-O16	2.347(7)	Dy4-O4	2.355(6)
Dy1-N2 <sup>i</sup>	2.533(8)	Dy3-O9	2.440(6)	Dy4-O10	2.317(5)
Dy1-O19	2.352(8)	Dy3-O4	2.246(6)	Dy4-O3	2.342(6)
Dy2-O11	2.365(6)	Dy3-N4	2.489(7)	Dy4-O13	2.587(3)
Dy2-O17	2.381(8)	Dy3-O10	2.438(6)	Dy4-O14	2.388(9)
Dy2-O12	2.348(6)	Dy3-O6	2.351(6)		
<b>Bond angles (°)</b>					
O3 <sup>i</sup> -Dy1-O18	90.5(3)	O9-Dy2-O12	131.9(2)	O7-Dy3-O9	74.7(2)
O3 <sup>i</sup> -Dy1-O8	141.9(2)	O9-Dy2-O10	62.5(2)	O7-Dy3-N4	71.4(2)
O3 <sup>i</sup> -Dy1-N2 <sup>i</sup>	71.1(2)	O9-Dy2-O8	137.8(2)	O7-Dy3-O10	74.40(19)
O3 <sup>i</sup> -Dy1-O19	97.4(3)	O9-Dy2-O7	75.5(2)	O7-Dy3-O6	136.0(2)
O8-Dy1-O11	75.2(2)	O9-Dy2-O13	75.11(17)	O7-Dy3-O15	97.1(3)
O8-Dy1-O12	72.3(2)	O10-Dy2-O17	136.0(2)	O15-Dy3-O9	77.4(2)
O8-Dy1-O2 <sup>i</sup>	82.5(2)	O10-Dy2-O13	74.9(2)	O15-Dy3-N4	74.5(2)

O8-Dy1-O18	103.8(3)	O8-Dy2-O11	76.0(2)	O15-Dy3-O10	137.2(2)
O8-Dy1-N2 <sup>i</sup>	145.9(2)	O8-Dy2-O17	82.2(3)	O11 <sup>i</sup> -Dy4-O13	78.1(2)
O8-Dy1-O19	90.6(3)	O8-Dy2-O12	73.1(2)	O12 <sup>i</sup> -Dy4-O11 <sup>i</sup>	63.1(2)
O19-Dy1-O11	137.4(2)	O8-Dy2-O10	124.0(2)	O12 <sup>i</sup> -Dy4-O9	135.2(2)
O19-Dy1-O12	76.7(3)	O8-Dy2-O7	68.41(19)	O12 <sup>i</sup> -Dy4-O4	136.5(2)
O19-Dy1-O2 <sup>i</sup>	78.3(3)	O8-Dy2-O13	145.66(15)	O12 <sup>i</sup> -Dy4-O3	74.5(2)
O19-Dy1-N2 <sup>i</sup>	72.4(3)	O7-Dy2-O11	116.2(2)	O12 <sup>i</sup> -Dy4-O13	76.79(17)
O11-Dy1-N2 <sup>i</sup>	136.7(2)	O7-Dy2-O17	87.0(3)	O12 <sup>i</sup> -Dy4-O14	76.3(3)
O12-Dy1-O11	60.7(2)	O7-Dy2-O12	139.79(19)	O9-Dy4-O11 <sup>i</sup>	140.6(2)
O12-Dy1-N2 <sup>i</sup>	128.7(2)	O7-Dy2-O10	74.3(2)	O9-Dy4-O13	75.37(17)
O2 <sup>i</sup> -Dy1-O11	136.7(2)	O7-Dy2-O13	144.66(14)	O9-Dy4-O14	77.4(3)
O2 <sup>i</sup> -Dy1-O12	143.9(3)	O16-Dy3-O9	133.2(2)	O4-Dy4-O11 <sup>i</sup>	122.0(2)
O2 <sup>i</sup> -Dy1-N2 <sup>i</sup>	65.5(2)	O16-Dy3-N4	80.2(2)	O4-Dy4-O9	71.8(2)
O18-Dy1-O11	77.4(2)	O16-Dy3-O10	73.5(2)	O4-Dy4-O13	145.08(14)
O18-Dy1-O12	137.7(2)	O16-Dy3-O6	74.2(2)	O4-Dy4-O14	80.1(4)
O18-Dy1-O2 <sup>i</sup>	72.6(3)	O16-Dy3-O15	149.3(2)	O10-Dy4-O11 <sup>i</sup>	83.2(2)
O18-Dy1-N2 <sup>i</sup>	78.4(3)	O9-Dy3-N4	132.2(2)	O10-Dy4-O12 <sup>i</sup>	140.6(2)
O18-Dy1-O19	145.2(3)	O4-Dy3-O16	102.0(3)	O10-Dy4-O9	62.7(2)
O3 <sup>i</sup> -Dy1-O11	73.8(2)	O4-Dy3-O9	72.2(2)	O10-Dy4-O4	78.0(2)
O3 <sup>i</sup> -Dy1-O12	73.5(2)	O4-Dy3-N4	143.2(2)	O10-Dy4-O3	116.8(2)
O3 <sup>i</sup> -Dy1-O2 <sup>i</sup>	135.6(2)	O4-Dy3-O10	77.6(2)	O10-Dy4-O13	76.6(2)
O11-Dy2-O17	138.3(2)	O4-Dy3-O6	79.7(2)	O10-Dy4-O14	138.7(3)
O11-Dy2-O10	85.2(2)	O4-Dy3-O7	144.3(2)	O3-Dy4-O11 <sup>i</sup>	73.6(2)
O11-Dy2-O13	77.8(2)	O4-Dy3-O15	88.5(3)	O3-Dy4-O9	138.1(2)
O17-Dy2-O13	103.6(3)	O10-Dy3-O9	59.8(2)	O3-Dy4-O4	67.7(2)
O12-Dy2-O11	63.3(2)	O10-Dy3-N4	136.1(2)	O3-Dy4-O13	146.40(17)
O12-Dy2-O17	76.6(2)	O6-Dy3-O9	143.8(2)	O3-Dy4-O14	85.6(4)
O12-Dy2-O10	140.4(2)	O6-Dy3-N4	65.5(2)	O14-Dy4-O11 <sup>i</sup>	137.9(3)

O12-Dy2-O13	75.45(17)	O6-Dy3-O10	135.2(2)	O14-Dy4-O13	104.2(5)
O9-Dy2-O11	142.1(2)	O6-Dy3-O15	79.6(3)		
O9-Dy2-O17	74.5(2)	O7-Dy3-O16	90.9(3)		

**Table S4.** Selected bond lengths (Å) and angles (°) of cluster *R-2*.

<b>Bond lengths (Å)</b>					
Dy1-O5	2.446(7)	Dy2-O12	2.292(6)	Dy3-O9 <sup>i</sup>	2.377(6)
Dy1-O12	2.365(6)	Dy2-O3	2.435(6)	Dy3-O10	2.382(5)
Dy1-O3	2.246(6)	Dy2-O11	2.366(5)	Dy3-O10 <sup>i</sup>	2.543(6)
Dy1-O14	2.290(7)	Dy2-N4	2.431(7)	Dy3-O11	2.305(5)
Dy1-O6	2.391(6)	Dy2-O4	2.301(6)	Dy3-O16	2.480(7)
Dy1-N2	2.513(9)	Dy2-O15	2.438(7)	Dy3-N6	2.517(8)
Dy1-O2	2.358(7)	Dy2-O6	2.368(5)	Dy3-O17	2.428(7)
Dy1-O13	2.392(10)	Dy3-O7	2.423(5)		
Dy2-O7	2.277(5)	Dy3-O8	2.293(6)		
<b>Bond angles (°)</b>					
O5-Dy1-N2	78.1(2)	O7-Dy2-N4	76.2(2)	O8-Dy3-O10 <sup>i</sup>	70.06(19)
O12-Dy1-O5	134.9(2)	O7-Dy2-O4	77.4(2)	O8-Dy3-O10	76.34(18)
O12-Dy1-O6	70.1(2)	O7-Dy2-O15	81.4(2)	O8-Dy3-O11	134.9(2)
O12-Dy1-N2	130.9(2)	O7-Dy2-O6	133.6(2)	O8-Dy3-O16	74.8(2)
O12-Dy1-O13	74.7(3)	O12-Dy2-O3	69.3(2)	O8-Dy3-N6	128.9(2)
O3-Dy1-O5	94.2(2)	O12-Dy2-O11	70.7(2)	O8-Dy3-O17	141.6(2)
O3-Dy1-O12	71.3(2)	O12-Dy2-N4	137.8(2)	O9 <sup>i</sup> -Dy3-O7	71.9(2)
O3-Dy1-O14	143.8(2)	O12-Dy2-O4	114.0(2)	O9 <sup>i</sup> -Dy3-O10	124.0(2)
O3-Dy1-O6	68.2(2)	O12-Dy2-O15	84.3(2)	O9 <sup>i</sup> -Dy3-O10 <sup>i</sup>	61.66(17)
O3-Dy1-N2	71.0(2)	O12-Dy2-O6	71.8(2)	O9 <sup>i</sup> -Dy3-O16	147.8(2)
O3-Dy1-O2	135.9(3)	O3-Dy2-O15	133.4(2)	O9 <sup>i</sup> -Dy3-N6	140.7(3)
O3-Dy1-O13	95.5(4)	O11-Dy2-O3	124.4(2)	O9 <sup>i</sup> -Dy3-O17	70.2(3)

O14-Dy1-O5	87.4(2)	O11-Dy2-N4	145.5(2)	O10-Dy3-O7	139.4(2)
O14-Dy1-O12	82.1(2)	O11-Dy2-O15	77.4(2)	O10-Dy3-O10 <sup>i</sup>	62.4(2)
O14-Dy1-O6	80.1(2)	O11-Dy2-O6	131.9(2)	O10-Dy3-O16	78.8(2)
O14-Dy1-N2	143.8(2)	N4-Dy2-O3	88.9(2)	O10-Dy3-N6	64.3(2)
O14-Dy1-O2	79.0(2)	N4-Dy2-O15	85.8(2)	O10-Dy3-O17	89.8(2)
O14-Dy1-O13	100.8(4)	O4-Dy2-O3	66.41(19)	O11-Dy3-O7	70.2(2)
O6-Dy1-O5	64.95(19)	O4-Dy2-O11	97.8(2)	O11-Dy3-O9 <sup>i</sup>	90.2(2)
O6-Dy1-N2	121.2(3)	O4-Dy2-N4	87.0(2)	O11-Dy3-O10	137.5(2)
O6-Dy1-O13	144.4(3)	O4-Dy2-O15	158.7(2)	O11-Dy3-O10 <sup>i</sup>	144.1(2)
O2-Dy1-O5	72.9(3)	O4-Dy2-O6	124.61(19)	O11-Dy3-O16	83.5(2)
O2-Dy1-O12	145.3(3)	O6-Dy2-O3	65.6(2)	O11-Dy3-N6	73.2(2)
O2-Dy1-O6	133.4(2)	O6-Dy2-N4	66.3(2)	O11-Dy3-O17	78.2(2)
O2-Dy1-N2	65.1(3)	O6-Dy2-O15	70.0(2)	O16-Dy3-O10 <sup>i</sup>	132.3(2)
O2-Dy1-O13	80.6(3)	O7-Dy3-O10 <sup>i</sup>	115.8(2)	O16-Dy3-N6	66.9(3)
O13-Dy1-O5	150.3(3)	O7-Dy3-O16	76.3(2)	N6-Dy3-O10 <sup>i</sup>	113.8(2)
O13-Dy1-N2	78.6(4)	O7-Dy3-N6	130.2(2)	O17-Dy3-O10 <sup>i</sup>	71.8(2)
O7-Dy2-O12	141.8(2)	O7-Dy3-O17	129.8(2)	O17-Dy3-O16	137.9(3)
O7-Dy2-O3	141.5(2)	O8-Dy3-O7	66.47(17)	O17-Dy3-N6	71.6(3)
O7-Dy2-O11	71.69(19)	O8-Dy3-O9 <sup>i</sup>	88.1(2)		

**Table S5.** Selected bond lengths (Å) and angles (°) of cluster **S-2**.

Bond lengths (Å)					
Dy1-O12	2.370(5)	Dy2-O12	2.294(5)	Dy3-O9 <sup>i</sup>	2.378(6)
Dy1-O5	2.438(6)	Dy2-O15	2.428(6)	Dy3-O10	2.373(4)
Dy1-O3	2.248(6)	Dy2-O11	2.358(5)	Dy3-O10 <sup>i</sup>	2.554(5)
Dy1-O14	2.282(6)	Dy2-O3	2.434(5)	Dy3-O11	2.314(4)
Dy1-O6	2.405(5)	Dy2-O4	2.299(5)	Dy3-O16	2.456(7)
Dy1-O2	2.352(6)	Dy2-O6	2.379(5)	Dy3-N6	2.517(7)

Dy1-N2	2.552(8)	Dy2-N4	2.421(7)	Dy3-O17	2.414(7)
Dy1-O13	2.391(9)	Dy3-O7	2.427(5)		
Dy2-O7	2.289(4)	Dy3-O8	2.300(5)		
<b>Bond angles (°)</b>					
O12-Dy1-O5	135.23(18)	O7-Dy2-O3	141.6(2)	O8-Dy3-O10	76.46(17)
O12-Dy1-O6	70.45(18)	O7-Dy2-O4	77.68(19)	O8-Dy3-O11	134.50(18)
O12-Dy1-N2	131.0(2)	O7-Dy2-O6	133.08(19)	O8-Dy3-O16	75.0(2)
O12-Dy1-O13	74.6(2)	O7-Dy2-N4	76.17(18)	O8-Dy3-N6	128.6(2)
O5-Dy1-N2	77.5(2)	O12-Dy2-O15	84.4(2)	O8-Dy3-O17	142.3(2)
O3-Dy1-O12	71.5(2)	O12-Dy2-O11	70.51(17)	O9 <sup>i</sup> -Dy3-O7	71.71(19)
O3-Dy1-O5	93.8(2)	O12-Dy2-O3	69.6(2)	O9 <sup>i</sup> -Dy3-O10 <sup>i</sup>	61.91(16)
O3-Dy1-O14	143.30(19)	O12-Dy2-O4	113.9(2)	O9 <sup>i</sup> -Dy3-O16	147.6(2)
O3-Dy1-O6	68.0(2)	O12-Dy2-O6	72.20(19)	O9 <sup>i</sup> -Dy3-N6	141.2(2)
O3-Dy1-O2	136.3(2)	O12-Dy2-N4	137.80(19)	O9 <sup>i</sup> -Dy3-O17	70.9(2)
O3-Dy1-N2	71.0(2)	O15-Dy2-O3	133.32(18)	O10-Dy3-O7	139.19(18)
O3-Dy1-O13	95.3(4)	O11-Dy2-O15	77.2(2)	O10-Dy3-O9 <sup>i</sup>	124.37(18)
O14-Dy1-O12	82.1(2)	O11-Dy2-O3	124.8(2)	O10-Dy3-O10 <sup>i</sup>	62.5(2)
O14-Dy1-O5	87.2(2)	O11-Dy2-O6	131.89(19)	O10-Dy3-O16	78.8(2)
O14-Dy1-O6	79.5(2)	O11-Dy2-N4	145.56(19)	O10-Dy3-N6	64.27(18)
O14-Dy1-O2	79.0(2)	O4-Dy2-O15	158.67(19)	O10-Dy3-O17	89.7(2)
O14-Dy1-N2	144.01(18)	O4-Dy2-O11	98.08(19)	O11-Dy3-O7	70.13(19)
O14-Dy1-O13	101.8(4)	O4-Dy2-O3	66.42(17)	O11-Dy3-O9 <sup>i</sup>	90.20(19)
O6-Dy1-O5	64.88(16)	O4-Dy2-O6	124.55(17)	O11-Dy3-O10	137.36(19)
O6-Dy1-N2	120.8(2)	O4-Dy2-N4	87.0(2)	O11-Dy3-O10 <sup>i</sup>	144.37(19)
O2-Dy1-O12	145.0(3)	O6-Dy2-O15	69.94(18)	O11-Dy3-O16	82.9(2)
O2-Dy1-O5	73.0(3)	O6-Dy2-O3	65.53(18)	O11-Dy3-N6	73.13(18)
O2-Dy1-O6	133.2(2)	O6-Dy2-N4	65.9(2)	O11-Dy3-O17	78.2(2)
O2-Dy1-N2	65.5(2)	N4-Dy2-O15	85.8(2)	O16-Dy3-O10 <sup>i</sup>	132.58(18)



O2-Dy1-O13	80.8(3)	N4-Dy2-O3	88.5(2)	O16-Dy3-N6	66.3(2)
O13-Dy1-O5	150.1(2)	O7-Dy3-O10 <sup>i</sup>	115.86(19)	N6-Dy3-O10 <sup>i</sup>	114.0(2)
O13-Dy1-O6	144.5(2)	O7-Dy3-O16	76.21(19)	O17-Dy3-O7	130.1(2)
O13-Dy1-N2	78.7(3)	O7-Dy3-N6	129.8(2)	O17-Dy3-O10 <sup>i</sup>	72.2(2)
O7-Dy2-O12	141.73(19)	O8-Dy3-O7	66.23(16)	O17-Dy3-O16	137.1(3)
O7-Dy2-O15	81.1(2)	O8-Dy3-O9 <sup>i</sup>	88.1(2)	O17-Dy3-N6	71.4(3)
O7-Dy2-O11	71.80(18)	O8-Dy3-O10 <sup>i</sup>	70.30(18)		

**Table S6.** *SHAPE* analysis of the Dy(III) in cluster **R-1**.

Label	Shape	Symmetry	Distortion (°)			
			Dy1	Dy2	Dy3	Dy4
OP-8	$D_{8h}$	Octagon	29.039	26.380	28.903	25.933
HPY-8	$C_{7v}$	Heptagonal pyramid	23.562	20.673	24.159	21.238
HBPY-8	$D_{6h}$	Hexagonal bipyramid	15.482	16.685	15.109	16.540
CU-8	$O_h$	Cube	12.733	11.994	12.535	12.412
SAPR-8	$D_{4d}$	Square antiprism	2.343	1.381	2.549	1.405
TDD-8	$D_{2d}$	Triangular dodecahedron	0.988	2.007	1.144	2.157
JGBF-8	$D_{2d}$	Johnson-Gyrobifastigium (J26)	11.566	15.608	11.001	14.908
JETBPY-8	$D_{3h}$	Johnson-Elongated triangular bipyramid (J14)	26.905	25.956	27.183	26.131
JBTP-8	$C_{2v}$	Johnson-Biaugmented trigonal prism (J50)	2.272	2.874	2.349	2.707
BTPR-8	$C_{2v}$	Biaugmented trigonal prism	2.007	1.780	2.101	1.679
JSD-8	$D_{2d}$	Snub disphenoid (J84)	2.074	4.669	2.142	4.537
TT-8	$T_d$	Triakis tetrahedron	13.451	12.327	13.230	12.891
ETBPY-8	$D_{3h}$	Elongated trigonal bipyramid	23.431	21.220	23.916	21.790

**Table S7.** *SHAPE* analysis of the Dy(III) in cluster **S-1**.

Label	Shape	Symmetry	Distortion (°)			
			Dy1	Dy2	Dy3	Dy4
OP-8	$D_{8h}$	Octagon	28.913	26.853	28.939	26.120
HPY-8	$C_{7v}$	Heptagonal pyramid	23.556	20.752	23.962	21.381
HBPY-8	$D_{6h}$	Hexagonal bipyramid	15.551	16.618	14.923	16.306
CU-8	$O_h$	Cube	12.685	11.874	12.407	12.373
SAPR-8	$D_{4d}$	Square antiprism	2.2853	1.434	2.516	1.387
TDD-8	$D_{2d}$	Triangular dodecahedron	0.997	1.894	1.179	2.046
JGBF-8	$D_{2d}$	Johnson-Gyrobifastigium (J26)	11.671	15.434	10.862	14.732
JETBPY-8	$D_{3h}$	Johnson-Elongated triangular bipyramid (J14)	26.883	26.364	27.075	26.640
JBTP-8	$C_{2v}$	Johnson-Biaugmented trigonal prism (J50)	2.198	2.805	2.409	2.698
BTPR-8	$C_{2v}$	Biaugmented trigonal prism	1.937	1.679	2.157	1.619
JSD-8	$D_{2d}$	Snub disphenoid (J84)	2.095	4.595	2.104	4.471
TT-8	$T_d$	Triakis tetrahedron	13.408	12.213	13.174	12.825
ETBPY-8	$D_{3h}$	Elongated trigonal bipyramid(see8)	23.374	21.678	23.815	22.345

**Table S8.** SHAPE analysis of the Dy(III) in cluster **R-2**.

Label	Shape	Symmetry	Distortion (°)	
			Dy1	Dy2
OP-8	$D_{8h}$	Octagon	30.797	31.379
HPY-8	$C_{7v}$	Heptagonal pyramid	23.531	23.404
HBPY-8	$D_{6h}$	Hexagonal bipyramid	16.395	13.466
CU-8	$O_h$	Cube	11.640	12.415
SAPR-8	$D_{4d}$	Square antiprism	3.024	3.501
TDD-8	$D_{2d}$	Triangular dodecahedron	0.898	2.599

JGBF-8	$D_{2d}$	Johnson-Gyrobifastigium (J26)	12.666	10.371
JETBPY-8	$D_{3h}$	Johnson-Elongated triangular bipyramid (J14)	29.434	27.263
JBTP-8	$C_{2v}$	Johnson-Biaugmented trigonal prism (J50)	3.148	2.912
BTPR-8	$C_{2v}$	Biaugmented trigonal prism	2.696	1.767
JSD-8	$D_{2d}$	Snub disphenoid (J84)	2.747	4.335
TT-8	$T_d$	Triakis tetrahedron	12.372	13.149
ETBPY-8	$D_{3h}$	Elongated trigonal bipyramid	24.815	22.827

Label	Shape	Symmetry	Distortion (°)	
			Dy3	
EP-9	$D_{9h}$	Enneagon	34.168	
OPY-9	$C_{8v}$	Octagonal pyramid	22.796	
HBPY-9	$D_{7h}$	Heptagonal bipyramid	17.267	
JTC-9	$C_{3v}$	Triangular cupola J3	15.016	
JCCU-9	$C_{4v}$	Capped cube (J8)	8.664	
CCU-9	$C_4$	Capped cube	7.378	
JCSAPR-9	$C_{4v}$	Capped sq. antiprism	2.254	
CSAPR-9	$C_{4v}$	Capped square antiprism	1.229	
JTCTPR-9	$D_{3h}$	Tricapped trigonal prism J51	2.012	
TCTPR-9	$D_{3h}$	Tricapped trigonal prism	1.251	
JTDIC-9	$C_{3v}$	Tridiminished icosahedron J63	12.771	
HH-9	$C_{2v}$	Hula-hoop	10.110	
MFF-9	$C_s$	Muffin	1.335	

**Table S9.** *SHAPE* analysis of the Dy(III) in cluster *S-2*.

Label	Shape	Symmetry	Distortion (°)	
			Dy1	Dy2
OP-8	$D_{8h}$	Octagon	30.940	31.285

HPY-8	$C_{7v}$	Heptagonal pyramid	23.682	23.506
HBPY-8	$D_{6h}$	Hexagonal bipyramid	16.282	13.509
CU-8	$O_h$	Cube	11.733	12.523
SAPR-8	$D_{4d}$	Square antiprism	3.081	3.505
TDD-8	$D_{2d}$	Triangular dodecahedron	0.887	2.627
JGBF-8	$D_{2d}$	Johnson-Gyrobifastigium (J26)	12.734	10.331
JETBPY-8	$D_{3h}$	Johnson-Elongated triangular bipyramid (J14)	29.067	27.142
JBTP-8	$C_{2v}$	Johnson-Biaugmented trigonal prism (J50)	3.178	2.954
BTPR-8	$C_{2v}$	Biaugmented trigonal prism	2.549	1.832
JSD-8	$D_{2d}$	Snub disphenoid (J84)	2.561	4.313
TT-8	$T_d$	Triakis tetrahedron	12.410	13.212
ETBPY-8	$D_{3h}$	Elongated trigonal bipyramid	25.398	22.628

<b>Label</b>	<b>Shape</b>	<b>Symmetry</b>	<b>Distortion (°)</b> <b>Dy3</b>
EP-9	$D_{9h}$	Enneagon	34.183
OPY-9	$C_{8v}$	Octagonal pyramid	22.825
HBPY-9	$D_{7h}$	Heptagonal bipyramid	17.247
JTC-9	$C_{3v}$	Triangular cupola J3	15.035
JCCU-9	$C_{4v}$	Capped cube (J8)	8.579
CCU-9	$C_4$	Capped cube	7.350
JCSAPR-9	$C_{4v}$	Capped sq. antiprism	2.255
CSAPR-9	$C_{4v}$	Capped square antiprism	1.227
JTCTPR-9	$D_{3h}$	Tricapped trigonal prism J51	1.961
TCTPR-9	$D_{3h}$	Tricapped trigonal prism	1.257
JTDIC-9	$C_{3v}$	Tridiminished icosahedron J63	12.762

HH-9	$C_{2v}$	Hula-hoop	10.137
MFF-9	$C_s$	Muffin	1.314

**Table S10.** Parameters from the fitting result of the Cole-Cole plots for the **R-1** under 0 Oe field.

Temp.(K)	<b>R-1</b>		
	$\tau$	$\alpha$	residual
5.0	0.296032E-03	0.244656E+00	0.143606E+00
4.7	0.396460E-03	0.264993E+00	0.191508E+00
4.4	0.531762E-03	0.285873E+00	0.243871E+00
4.1	0.715844E-03	0.303777E+00	0.318819E+00
3.8	0.966411E-03	0.323445E+00	0.380225E+00
3.5	0.131679E-02	0.344271E+00	0.453641E+00
3.2	0.187588E-02	0.364864E+00	0.525670E+00
2.9	0.285038E-02	0.388242E+00	0.584445E+00
2.6	0.466894E-02	0.413761E+00	0.887917E+00
2.3	0.851159E-02	0.446712E+00	0.550999E+00
2.0	0.169600E-01	0.490874E+00	0.394759E+00

**Table S11.** Parameters from the fitting result of the Cole-Cole plots for the **R-2** under 0 Oe field.

Temp.(K)	<b>R-2</b>		
	$\tau$	$\alpha$	residual
2.0	0.185721E-03	0.305145E+00	0.702823E-01
2.5	0.174744E-03	0.273494E+00	0.682148E-01
3.0	0.165713E-03	0.256340E+00	0.588019E-01
3.5	0.158271E-03	0.244586E+00	0.545725E-01
4.0	0.150792E-03	0.236670E+00	0.456045E-01
4.5	0.141043E-03	0.234421E+00	0.352555E-01
5.0	0.132836E-03	0.227043E+00	0.328097E-01
5.5	0.123869E-03	0.222413E+00	0.263064E-01
6.0	0.113927E-03	0.215366E+00	0.218576E-01
6.5	0.102865E-03	0.211176E+00	0.156278E-01
7.0	0.924204E-04	0.204779E+00	0.118463E-01
7.5	0.632913E-06	0.691005E+00	0.365156E+01
8.0	0.516291E-05	0.337087E+00	0.127491E-01
8.5	0.396282E-05	0.313579E+00	0.767048E-02
9.0	0.303176E-05	0.287576E+00	0.500746E-02
9.5	0.233652E-05	0.254981E+00	0.396000E-02
10.0	0.124680E-05	0.280504E+00	0.839930E-01

**Table S12.** Parameters from the fitting result of the Cole-Cole plots for the **R-2** under 1000 Oe field.

Temp.(K)	<b>R-2</b>		
	$\tau$	$\alpha$	residual
2.0	0.541202E-03	0.309313E+00	0.331614E+00
2.5	0.431551E-03	0.298966E+00	0.191431E+00
3.0	0.355077E-03	0.307415E+00	0.923385E+00
3.5	0.317890E-03	0.281377E+00	0.101769E+00
4.0	0.293437E-03	0.249301E+00	0.590389E+00
4.5	0.233407E-03	0.275505E+00	0.937777E+00
5.0	0.218947E-03	0.240321E+00	0.811918E-01
5.5	0.116915E-03	0.376318E+00	0.500788E+01
6.0	0.155960E-03	0.237343E+00	0.364479E-01
6.5	0.136306E-03	0.218145E+00	0.321418E-01
7.0	0.112108E-03	0.216957E+00	0.229871E-01
7.5	0.131769E-03	0.437632E+00	0.468881E+01
8.0	0.182822E-03	0.505731E+00	0.488010E-01
8.5	0.155999E-03	0.102493E+00	0.406885E-01
9.0	0.204887E-03	0.129780E+00	0.440238E+00
9.5	0.127147E-03	0.510891E+00	0.448092E-01
10.0	0.928791E-04	0.130480E+00	0.105949E-01

**Table S13.** Parameters from the fitting result of the Cole-Cole plots for the **S-1** under 0 Oe field.

Temp.(K)	<b>S-1</b>		
	$\tau$	$\alpha$	residual
2.0	0.135298E-01	0.476624E+00	0.271138E+01
2.3	0.610367E-02	0.440763E+00	0.413320E+01
2.6	0.328692E-02	0.400390E+00	0.187731E+01
2.9	0.191202E-02	0.359570E+00	0.303056E+01
3.2	0.129758E-02	0.322138E+00	0.338158E+01
3.5	0.938169E-03	0.291340E+00	0.307369E+01
3.8	0.712833E-03	0.256317E+00	0.311767E+01
4.1	0.538181E-03	0.246634E+00	0.243062E+01
4.4	0.413947E-03	0.218830E+00	0.294600E+01
4.7	0.307372E-03	0.211419E+00	0.232269E+01
5.0	0.224999E-03	0.188957E+00	0.214014E+01

**Table S14.** Parameters from the fitting result of the Cole-Cole plots for the **S-2** under 0 Oe field.

	<b>S-2</b>		

Temp.(K)	$\tau$	$\alpha$	residual
2.0	0.880020E-04	0.225023E+00	0.361788E+01
2.3	0.706370E-04	0.206747E+00	0.267288E+01
2.6	0.523292E-04	0.214592E+00	0.278556E+01
2.9	0.345059E-04	0.246159E+00	0.210347E+01
3.2	0.132563E-04	0.250346E+00	0.236751E+01
3.5	0.802929E-05	0.282038E+00	0.170793E+01
3.8	0.770223E-05	0.234678E+00	0.185850E+01
4.1	0.476622E-05	0.299269E+00	0.136504E+01
4.4	0.506427E-05	0.235104E+00	0.123434E+01
4.7	0.446807E-05	0.215544E+00	0.130343E+01
5.0	0.337152E-05	0.235373E+00	0.153139E+01
5.3	0.230348E-05	0.271925E+00	0.135585E+01
5.6	0.249579E-05	0.208922E+00	0.992459E+00
5.9	0.609087E-06	0.393802E+00	0.738501E+00
6.2	0.248039E-06	0.468510E+00	0.109518E+01
6.5	0.445975E-08	0.672717E+00	0.110266E+01
6.8	0.101401E-06	0.487992E+00	0.865128E+00
7.1	0.710081E-06	0.239767E+00	0.628120E+00
7.4	0.115485E-05	0.111022E+00	0.710321E+00
7.7	0.429028E-06	0.229864E+00	0.749382E+00
8.0	0.628262E-07	0.392412E+00	0.513175E+00

**Table S15.** Parameters from the fitting result of the Cole-Cole plots for the **S-2** under 1000 Oe field.

Temp.(K)	<b>S-2</b>		
	$\tau$	$\alpha$	residual
2.0	0.336352E-03	0.245833E+00	0.632162E+01
2.3	0.242788E-03	0.353511E+00	0.439253E+01
2.6	0.238893E-03	0.350188E+00	0.252197E+01
2.9	0.140517E-03	0.347542E+00	0.459260E+01
3.2	0.180169E-03	0.199521E+00	0.280702E+01
3.5	0.719531E-04	0.398869E+00	0.296640E+01
3.8	0.121984E-03	0.325708E+00	0.200484E+01
4.1	0.146031E-03	0.145569E+00	0.242994E+01
4.4	0.658355E-04	0.266245E+00	0.348647E+01
4.7	0.123830E-04	0.480555E+00	0.215046E+01
5.0	0.949058E-04	0.214635E+00	0.163073E+01
5.3	0.591531E-04	0.260118E+00	0.226805E+01
5.6	0.832576E-04	0.169373E+00	0.125811E+01
5.9	0.344110E-05	0.430653E+00	0.169145E+01
6.2	0.212198E-05	0.461314E+00	0.133442E+01

6.5	0.496981E-05	0.259048E+00	0.169675E+01
6.8	0.492712E-05	0.210584E+00	0.845698E+00