

†Supporting information

Measuring Pb, Th, and U inter-element ratios in geological materials using extreme ultraviolet laser ablation and ionization mass spectrometry

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Table S1 Expected/literature mass fractions (in $\mu\text{g/g}$) of Pb, Th, and U and their respective 1 standard deviation ($\pm 1\text{SD}$) uncertainties for the samples investigated in this study. The mass fractions and their associated uncertainties listed for the synthetic glasses (NIST610, USGS GSE-1G and STDP5) and iron manganese (FeMnOx-1) material were used to calculate the $^{206}\text{Pb}/^{238}\text{U}$ and $^{232}\text{Th}/^{238}\text{U}$ ratio values found in the main text in Table 1. (Mass fractions for most samples can be found in the GeoRem Database: <http://georem.mpch-mainz.gwdg.de/>; mass fraction measurements for SR1, EA, 14971, SL-B, Mogok 2A, Mogok 2C, and Mogok 1 were directly provided by the USGS and are readily available to readers upon request via the corresponding author's email address).

Sample	Pb _{total}	$\pm 1\text{SD}$	^{206}Pb	$\pm 1\text{SD}$	^{232}Th	$\pm 1\text{SD}$	U _{total}	$\pm 1\text{SD}$	^{238}U	$\pm 1\text{SD}$
NIST610	426	1	102.7*	0.2	457.2	1.2	461.5	1.1	460.4	1.1
USGS GSE-1G	378	12	91*	3	380	20	420	30	417*	30
STDP5	1414	61.5	341*	15	1235	133	1378	5	1368*	5
FeMnOx-1	1624	280	391*	67	534	40	547	17	543*	17
SR1	n/a	n/a	218**	3	185	4	n/a	n/a	2455	35
EA	n/a	n/a	70**	1	292	8	n/a	n/a	803	15
14971										
LA ICP-MS	n/a	n/a	173*	3	37819	2404	n/a	n/a	1141	22
ID-TIMS	1904	94	238	13	41914	2335	1580	90	1569	89
Bananeira†	n/a	n/a	243	40	68252	5574	n/a	n/a	972	179
Diamantina†	n/a	n/a	93	11	3588	1822	n/a	n/a	355	41
SL-B	n/a	n/a	29688**	618	543556	7088	n/a	n/a	277039	5732
Mogok 2A	n/a	n/a	3735**	25	528320	2270	n/a	n/a	341808	2266
Mogok 2C	n/a	n/a	4716**	46	418880	4480	n/a	n/a	450034	4421
Mogok 1	n/a***	n/a	n/a***	n/a	24310	2101	n/a	n/a	290841	3683

*Calculated ^{206}Pb and ^{238}U mass fractions from total Pb and U content, respectively, assuming natural isotopic abundance. (Note: The $^{206}\text{Pb}/^{208}\text{Pb}$ ratio has been measured for USGS GSE-1G using LA ICP-MS and SIMS, obtaining a ratio value of approximately 1.96,^{1,2} whereas the natural $^{206}\text{Pb}/^{208}\text{Pb}$ ratio is 2.17. Nonetheless, the natural Pb abundance was assumed here because the measured isotope abundance was not directly available)

**Calculated radiogenic Pb mass fractions from direct ratio measurements of $^{206}\text{Pb}/^{238}\text{U}$ and mass fraction measurements of ^{238}U

***Sample has too high common Pb to give calculated Pb content

†Mass fraction values measured with LA Q-ICP-MS^{3,4}

Table S2 The ion counts of ^{206}Pb , ^{232}Th , ^{238}U , $^{232}\text{Th}^{16}\text{O}$, $^{238}\text{U}^{16}\text{O}$, $^{232}\text{Th}^{16}\text{O}_2$, and $^{238}\text{U}^{16}\text{O}_2$ measured with the EUV TOF in each super crater ablated on the samples analyzed in this study. The corresponding Pb/U and Th/U ratios for each super crater with its $\pm 2\sigma$ uncertainty is also listed, where the ratio considers all oxide species detected in the super crater, unless otherwise specified. The weighted average of the Pb/U and Th/U ratios is also shown alongside the $\pm 2\sigma$ uncertainty, which is calculated using the equations in Table S3.

Sample: NIST 610 (silicate glass)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	^{206}Pb	^{232}Th	^{238}U	$^{232}\text{Th}^{16}\text{O}$	$^{238}\text{U}^{16}\text{O}$	$^{232}\text{Th}^{16}\text{O}_2$	$^{238}\text{U}^{16}\text{O}_2$	Pb/U	$\pm 2\sigma$	Th/U	$\pm 2\sigma$
1*	58	316	250	274	264	n/a	60	0.101	0.03	1.03	0.17
2*	55	332	278	304	284	n/a	62	0.089	0.03	1.02	0.17
3*	64	249	191	240	208	n/a	59	0.140	0.04	1.07	0.20
4*	77	322	243	307	280	n/a	47	0.136	0.04	1.10	0.19
5*	83	377	336	286	270	n/a	69	0.123	0.03	0.98	0.15
6*	82	408	324	276	258	n/a	66	0.127	0.03	1.06	0.16
7	44	174	90	193	167	n/a	78	0.131	0.05	1.10	0.24
8	44	119	59	147	148	n/a	68	0.161	0.06	0.97	0.27
9	44	113	90	136	125	n/a	81	0.149	0.05	0.84	0.22
10	47	97	88	100	94	n/a	68	0.189	0.07	0.79	0.23
11	44	71	67	111	98	n/a	77	0.184	0.07	0.75	0.25
12	39	52	50	63	78	n/a	69	0.200	0.08	0.58	0.24
13	42	42	49	68	57	n/a	53	0.267	0.11	0.70	0.31
14*	127	729	651	539	479	n/a	66	0.106	0.02	1.06	0.12
15*	133	724	628	489	480	n/a	74	0.112	0.02	1.02	0.12
16*	137	662	555	485	483	n/a	77	0.123	0.03	1.03	0.12
17*	167	906	809	676	693	n/a	126	0.102	0.02	0.97	0.09
18*	168	809	764	637	619	n/a	119	0.112	0.02	0.96	0.09
19*	169	849	726	707	654	n/a	122	0.113	0.02	1.04	0.10
<i>Weighted average of ratios</i>								0.112	0.007	0.99	0.03

*Values used in the calculation of the Pb/U weighted average ratio because these runs have total U counts >400.

Sample: USGS GSE-1G (basalt glass)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	195	919	955	785	779	n/a	136	0.104	0.02	0.91	0.08
2	234	942	1078	809	785	n/a	174	0.115	0.02	0.86	0.07
3	228	954	981	760	794	n/a	175	0.117	0.02	0.88	0.07
<i>Weighted average of ratios</i>								0.11	0.01	0.88	0.04

Sample: STDP5 (phosphate glass)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	420	1585	1347	1375	1411	n/a	477	0.13	0.01	0.91	0.05
2	386	1539	1227	1401	1373	n/a	498	0.12	0.01	0.95	0.06
3	414	n/a*	1281	1350	1409	n/a	468	0.13	0.01	n/a	n/a
4	662	2456	2289	1817	1779	n/a	353	0.15	0.01	0.97	0.05
5	393	1179	995	1013	992	n/a	365	0.17	0.02	0.93	0.06
6	309	1006	945	986	926	n/a	347	0.14	0.02	0.90	0.07
<i>Weighted average of ratios</i>								0.138	0.006	0.94	0.04

*²³²Th signal could not be resolved from ringing induced by a large peak at m/z = 231

Sample: FeMnOx-1 (iron manganese oxide powder)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	674	1228	1165	462	426	n/a	n/a	0.42	0.04	1.06	0.07
2	500	831	717	439	378	n/a	n/a	0.46	0.04	1.16	0.10
3	399	703	656	429	356	n/a	n/a	0.39	0.04	1.12	0.10
<i>Weighted average of ratios</i>								0.42	0.02	1.10	0.05

Sample: SR1 (zircon)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th*	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	500	Interf.	4865	492	6179	n/a	2396	0.037	0.003	0.080	0.007
2	431	Interf.	3706	385	5481	n/a	2058	0.038	0.004	0.070	0.007
3	414	Interf.	2669	338	4667	n/a	1919	0.045	0.004	0.072	0.008
<i>Weighted average of ratios</i>								0.039	0.002	0.074	0.004

*²³²Th signal had interference (interf.) from ⁹²Zr₂¹⁶O₃ at m/z = 232, so only ²³²Th¹⁶O and ²³⁸U¹⁶O signals are used for the Th/U ratio

Sample: EA (zircon)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb*	²³² Th**	²³⁸ U**	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂ ***	Pb/U	±2σ	Th/U	±2σ
1	n/a	Interf.	Intef.	235	729	n/a	472	n/a	n/a	0.32	0.05
2	n/a	Interf.	Interf.	241	671	n/a	502	n/a	n/a	0.36	0.05
3	n/a	Interf.	Interf.	177	577	n/a	457	n/a	n/a	0.31	0.05
<i>Weighted average of ratios</i>								n/a	n/a	0.33	0.03

*²⁰⁶Pb was below EUV TOF detection limits; **²³²Th signal had interference (interf.) from ⁹²Zr₂¹⁶O₃ and ²³⁸U had interference from ⁹⁴Zr⁹⁶Zr¹⁶O₃;***²³⁸U¹⁶O₂ was not used for any ratio measurements, but the detected ion counts are shown here for reference.

Sample: 14971 (monazite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	118	27041	806	15320	486	258	325	0.07	0.01	26.4	1
2	94	17317	505	10739	372	219	268	0.08	0.02	24.7	1
3	92	25344	677	13107	408	162	180	0.07	0.02	30.5	1
4	96	25481	779	12833	409	152	164	0.07	0.02	28.4	1
5	83	23818	826	11972	420	141	129	0.06	0.01	26.1	1
<i>Weighted average of ratios</i>								0.071	0.007	26.8	0.5

Sample: Bananeira (monazite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	87	57923	1661	28233	848	195	176	0.032	0.007	32.2	1
2	86	59232	1640	28013	904	171	139	0.032	0.007	32.6	1
3	74	57971	1703	28931	897	163	173	0.027	0.007	31.4	1
<i>Weighted average of ratios</i>								0.030	0.004	32.0	0.7

Sample: Diamantina-1 (monazite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U*	±2σ
1	43	1346	868	660	414	n/a	n/a	0.03	0.01	1.6	0.1
2	55	1800	911	966	506	n/a	n/a	0.04	0.01	2.0	0.1
3	77	1633	923	845	505	n/a	n/a	0.05	0.01	1.7	0.1
<i>Weighted average of ratios</i>								0.041	0.006	1.74	0.06

*Measured Th/U ratio is shown here only for reference because Th content is not homogenous in this sample (i.e., ID-TIMS measures Th/U ranging from 0.22 to 16.2)

Sample: SL-B (uraninite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	23200	504047	297496	295621	142027	2074	51837	0.0472	6E-4	1.627	0.005
2	24273	517072	305737	303395	145600	2152	52238	0.0482	6E-4	1.629	0.005
3	24568	517426	304387	303324	143688	2230	52146	0.0491	6E-4	1.641	0.005
<i>Weighted average of ratios</i>								0.0482	4E-4	1.633	0.003

Sample: Mogok 2A (uraninite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	6264	493398	317625	311687	165432	2707	62002	0.0115	3E-4	1.482	0.005
2	6479	488538	317485	318125	166445	2736	61050	0.0119	3E-4	1.485	0.005
3	6346	529630	335358	325728	163402	2549	57256	0.0114	3E-4	1.543	0.006
<i>Weighted average of ratios</i>								0.0116	2E-4	1.503	0.003

Sample: Mogok 2C (uraninite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	7646	539295	443682	269825	204991	1465	68656	0.0107	2E-4	1.130	0.005
2	7101	442467	398372	282723	229631	2039	88310	0.0099	2E-4	1.015	0.004
3	7207	458963	407723	273318	224713	2010	82944	0.0101	2E-4	1.026	0.004
<i>Weighted average of ratios</i>								0.0102	1E-4	1.051	0.002

Sample: Mogok 1 (thorite)

Super crater #	<i>Measured Counts</i>							<i>Measured Ratios</i>			
	²⁰⁶ Pb	²³² Th	²³⁸ U	²³² Th ¹⁶ O	²³⁸ U ¹⁶ O	²³² Th ¹⁶ O ₂	²³⁸ U ¹⁶ O ₂	Pb/U	±2σ	Th/U	±2σ
1	345	19316	211434	22249	241916	n/a	131263	0.00059	6E-5	0.071	0.001
2	305	15162	167792	18895	206792	n/a	123775	0.00061	7E-5	0.068	0.001
3	268	15066	167220	19490	207045	n/a	120478	0.00054	7E-5	0.070	0.001
<i>Weighted average of ratios</i>								0.00058	4E-5	0.0698	6E-4

Table S3 Equations used for calculating the weighted average of the ratios. The equations below specifically represent calculations for $^{206}\text{Pb}/^{238}\text{U}$ ratios. For $^{232}\text{Th}/^{238}\text{U}$ ratio calculations, ^{206}Pb is replaced with ^{232}Th ion counts. Eqtns. (5) and (6) are bold and represent the final ratio values c and their uncertainty σ , respectively, reported in the main text.

Eqtn. (1)	$\text{Ratio} = a_n = \frac{[206\text{Pb (counts)}]}{[238\text{U (counts)}]}$
Eqtn. (2)	$\text{Ratio uncertainty} = \delta_n = \frac{[206\text{Pb (counts)}]}{[238\text{U (counts)}]} * \sqrt{\left(\frac{1}{206\text{Pb (counts)}} + \frac{1}{238\text{U (counts)}}\right)}$
Eqtn. (3)	$\text{Ratio weight} = b_n = \frac{\frac{[206\text{Pb (counts)}]}{[238\text{U (counts)}]}}{\delta_n^2}$
Eqtn. (4)	$\text{Ratio uncertainty weight} = \alpha_n = \frac{1}{\delta_n^2}$
Eqtn. (5)	$\text{Weighted average ratio} = c = \frac{\sum (b_1, b_2 \dots b_n)}{\sum (\alpha_1, \alpha_2, \dots \alpha_n)}$
Eqtn. (6)	$\text{Weighted uncertainty of ratio} = \sigma = \sqrt{\frac{1}{\sum (\alpha_1, \alpha_2, \dots \alpha_n)}}$

Where $n = 1, 2, 3, \dots, n+1$ and represents each ratio measured on the sample.

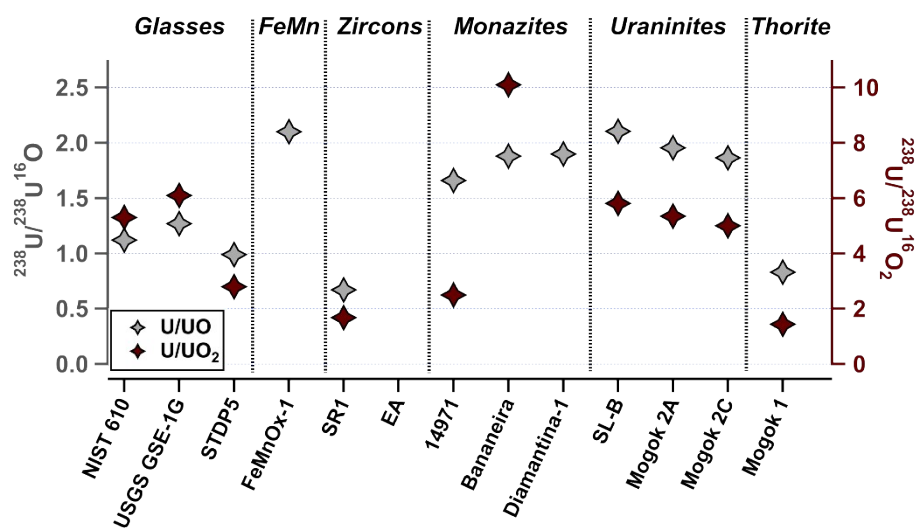


Fig. S1 $^{238}\text{U}/^{238}\text{U}^{16}\text{O}$ and $^{238}\text{U}/^{238}\text{U}^{16}\text{O}_2$ ratios measured with the EUV TOF in the different matrices. Note that ratios are not shown for EA because ^{238}U has a large interference in this sample.

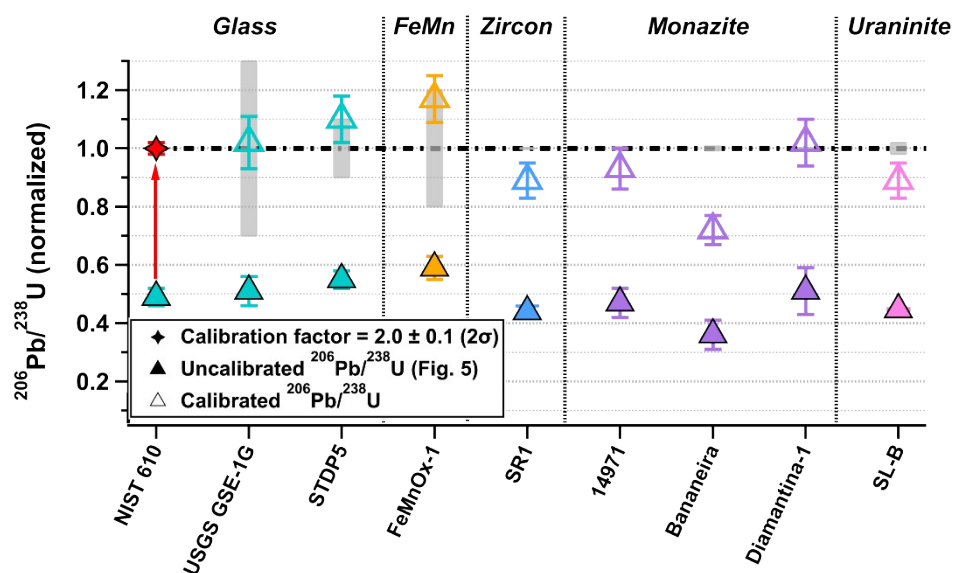


Fig. S2 Uncalibrated and calibrated $^{206}\text{Pb}/^{238}\text{U}$ ratios (normalized to 1) measured with the EUV TOF. The direct uncalibrated (i.e., raw) $^{206}\text{Pb}/^{238}\text{U}$ ratios are from Fig. 5 and are shown as solid triangles. The open triangles represent calibrated $^{206}\text{Pb}/^{238}\text{U}$ ratios using the NIST 610 CRM as the calibration standard, where the calibration factor is 2.0 ± 0.1 (2σ). The error bars on each point are $\pm 2\sigma$. The black dotted line represents the expected normalized ratios (i.e., 1). The gray bars are the corresponding $\pm 2\sigma$ uncertainty for the expected ratios. The Mogok uraninites and thorite are not shown on this plot because they significantly deviate from the expected values by $>50\%$ when the calibration factor is applied.

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