

Supporting Information for An unprecedented C₈₀ cage that violates the isolated pentagon rule

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Isolation of Lu₂O@C₁(31876)-C₈₀ and Lu₂O@C_{2v}(5)-C₈₀. Separation and purification of Lu₂O@C_{2v}(5)-C₈₀ and Lu₂O@C₁(31876)-C₈₀ were achieved by a multiple-stage HPLC process using toluene as the eluent. The first stage was performed on a Buckyprep column (20 mm × 250 mm, Cosmosil Nacalai Tesque), and one fraction, which is named as Fr7, was collected (Figure S1a). Then, Fr7 was injected into a Buckyprep-M column (20 mm × 250 mm, Cosmosil Nacalai Tesque) for the second stage separation, and a fraction named Fr7-3 was obtained (Figure S1b). After that, Fr7-3 was injected into a 5PBB column (20 mm × 250 mm, Cosmosil Nacalai Tesque), and a fraction named Fr7-3-2 was collected (Figure S1c). Fr7-3-2 was then injected into a Buckyprep column (20 mm × 250 mm, Cosmosil Nacalai Tesque) for recycling separation, and Lu₂O@C_{2v}(5)-C₈₀ (Fr7-3-2-3) and Lu₂O@C₁(31876)-C₈₀ (Fr7-3-2-4) were finally obtained (Figure S1d). Their high purity was demonstrated by the analytical HPLC chromatograms and the mass spectra (Figure S2).

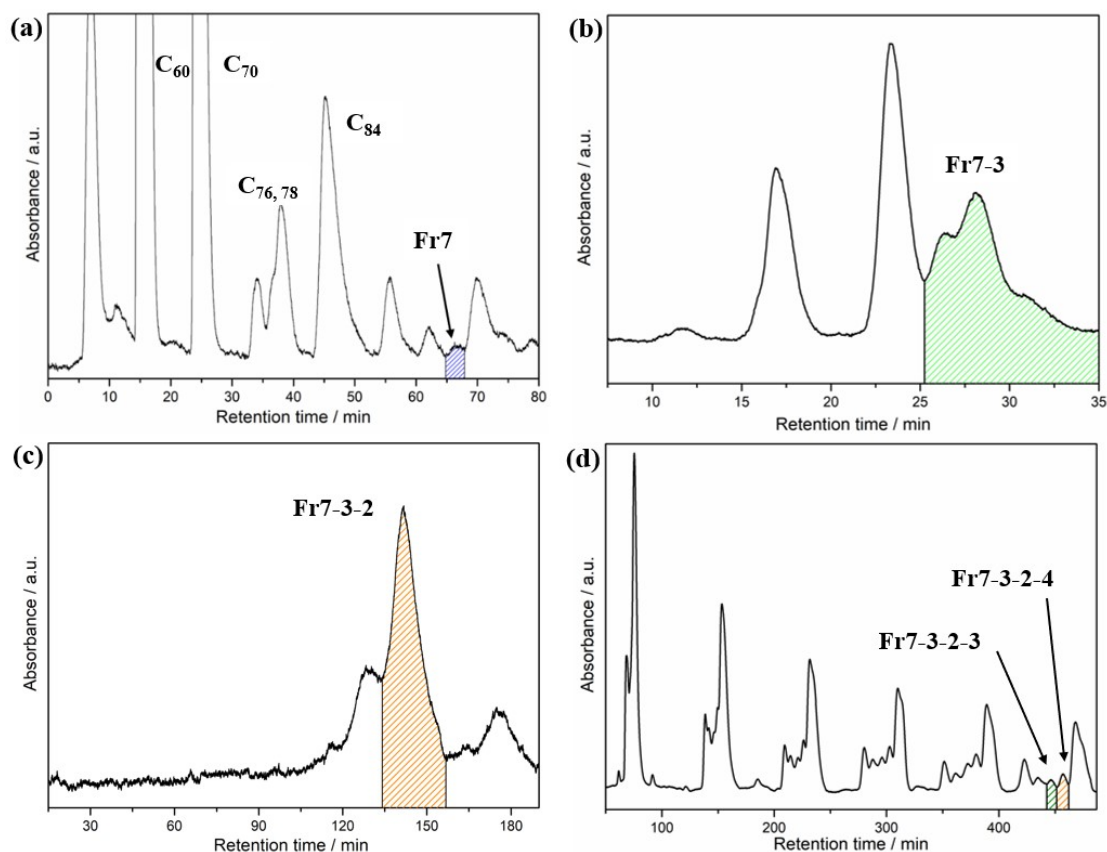


Figure S1. (a) Isolation scheme of fullerene extract on a Buckyprep column. Conditions: 20 mL inject volume; 10 mL/min toluene flow; (b) Isolation scheme of Fr7 on a Buckyprep-M column. Conditions: 15 mL inject volume; 10 mL/min toluene flow; (c) Isolation scheme of Fr7-3 on a 5PBB column. Conditions: 10 mL injection volume; 10 mL/min chlorobenzene flow. (d) Recycling HPLC chromatogram of Fr7-3-2 on a Buckyprep column. Conditions: 5 mL injection volume; 10 mL/min toluene flow. All the detection wavelengths are 330 nm.

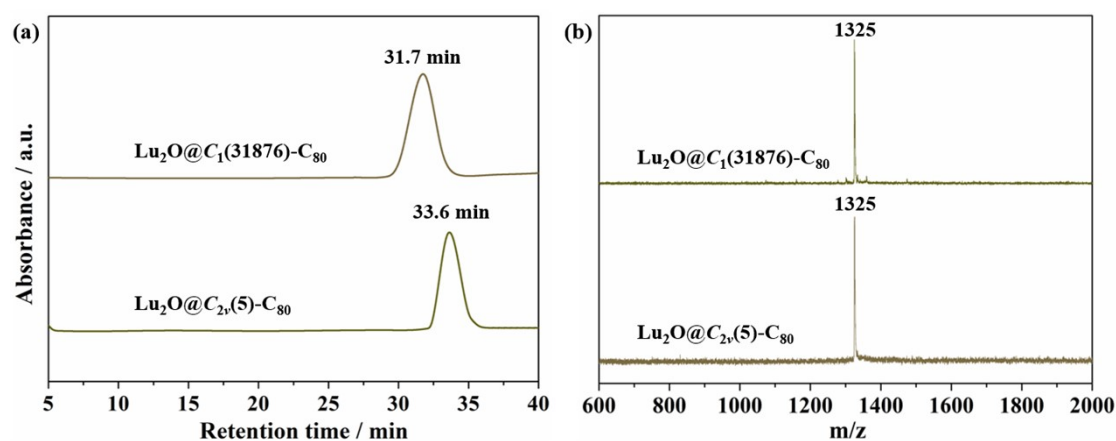


Figure S2. (a) HPLC chromatograms and (b) LDI-TOF mass spectra of Lu₂O@C₁(31876)-C₈₀ and Lu₂O@C_{2_v}(5)-C₈₀. HPLC conditions: Buckyprep column ($\phi = 4.6 \times 250$ mm); 20 μ L injection volume; 1 mL min⁻¹ toluene flow; 330 nm detection wavelength; 40 °C.

Table S1. Crystallographic data of $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}\cdot\text{Ni}^{\text{II}}(\text{OEP})\cdot 2(\text{C}_6\text{H}_6)$ and $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}\cdot\text{Ni}^{\text{II}}(\text{OEP})\cdot 2(\text{C}_6\text{H}_6)$.

| | $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}\cdot\text{Ni}^{\text{II}}(\text{OEP})\cdot 2(\text{C}_6\text{H}_6)$ | $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}\cdot\text{Ni}^{\text{II}}(\text{OEP})\cdot 2(\text{C}_6\text{H}_6)$ |
|-----------------------------------|---|--|
| <i>T</i> , K | 100(2) | 100(2) |
| λ , Å | 0.7336 | 0.7336 |
| color / habit | black / block | black / block |
| crystal size, mm | 0.08×0.06×0.04 | 0.14×0.10×0.10 |
| empirical formula | $\text{C}_{128}\text{H}_{56}\text{Lu}_2\text{N}_4\text{NiO}$ | $\text{C}_{128}\text{H}_{56}\text{Lu}_2\text{N}_4\text{NiO}$ |
| fw | 2074.42 | 2074.42 |
| crystal system | monoclinic | monoclinic |
| space group | <i>C2/m</i> | <i>C2/m</i> |
| <i>a</i> , Å | 25.2864(13) | 25.2000(3) |
| <i>b</i> , Å | 15.1800(8) | 15.1832(18) |
| <i>c</i> , Å | 19.7371(10) | 19.6920(3) |
| α , deg | 90 | 90 |
| β , deg | 95.204(2) | 94.432(5) |
| γ , deg | 90 | 90 |
| <i>V</i> , Å ³ | 7544.8(7) | 7511.7(16) |
| <i>Z</i> | 4 | 4 |
| ρ , g/cm ³ | 1.826 | 1.834 |
| μ , mm ⁻¹ | 2.915 | 3.163 |
| <i>R</i> ₁ (all data) | 0.1316 | 0.1020 |
| <i>wR</i> ₂ (all data) | 0.2640 | 0.2526 |

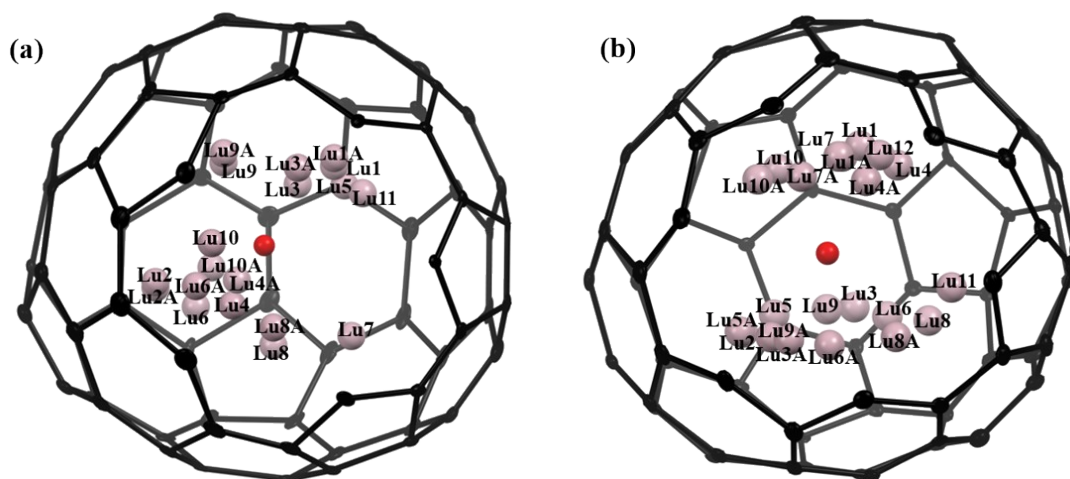


Figure S3. Positions of the disordered lutetium atoms in (a) $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}$ and (b) $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}$ relative to a cage orientation. Those Lu atoms labeled with an “A” are generated by crystallographic operation. Some cage carbon atoms are omitted for clarity.

Table S2. Fractional occupancies of the Lu positions in $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}$ and $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}$.

| EMFs | Fractional occupancy of the Lu positions | | | | | |
|--|--|----------|----------|------------|----------|----------|
| $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}$ | Lu1/Lu1A | Lu2/Lu2A | Lu3/Lu3A | Lu4/Lu4A | Lu5/Lu5A | Lu6/Lu6A |
| | 0.24 | 0.24 | 0.11 | 0.10 | 0.09 | 0.06 |
| | Lu7 | Lu8/Lu8A | Lu9/Lu9A | Lu10/Lu10A | Lu11 | |
| | 0.06 | 0.04 | 0.04 | 0.02 | 0.02 | |
| $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}$ | Lu1/Lu1A | Lu2 | Lu3/Lu3A | Lu4/Lu4A | Lu5/Lu5A | Lu6/Lu6A |
| | 0.21 | 0.25 | 0.16 | 0.10 | 0.06 | 0.06 |
| | Lu7/Lu7A | Lu8/Lu8A | Lu9/Lu9A | Lu10/Lu10A | Lu11 | Lu12 |
| | 0.06 | 0.05 | 0.05 | 0.05 | 0.04 | 0.03 |

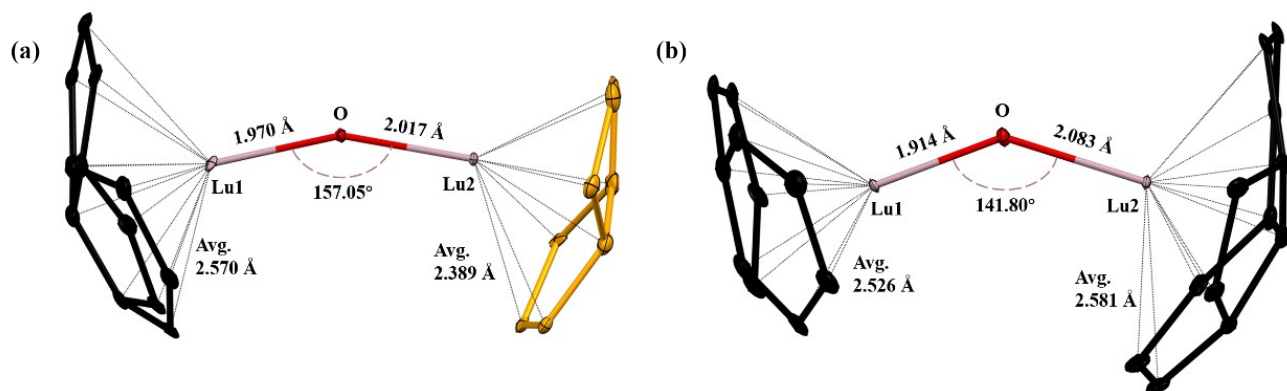


Figure S4. Structures of the major Lu_2O sites with respect to the nearest carbon atoms in the (a) $C_1(31876)\text{-C}_{80}$ and (b) $C_{2v}(5)\text{-C}_{80}$ cages. C, O, and Lu atoms are shown in black, red, and purple, respectively.

Table S3. Details of the oxide clusters at the major sites for $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}$, $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}$ and $\text{Sc}_2\text{O}@C_{2v}(5)\text{-C}_{80}$.

| $\text{Lu}_2\text{O}@C_1(31876)\text{-C}_{80}$ | | $\text{Lu}_2\text{O}@C_{2v}(5)\text{-C}_{80}$ | | $\text{Sc}_2\text{O}@C_{2v}(5)\text{-C}_{80}$ ^{S1} | |
|--|----------------|---|----------------|---|----------------|
| Lu1-cage | 2.570 Å (avg.) | Lu1-cage | 2.526 Å (avg.) | Sc1-cage | 2.519 Å (avg.) |
| Lu2-cage | 2.389 Å (avg.) | Lu2-cage | 2.581 Å (avg.) | Sc2-cage | 2.503 Å (avg.) |
| Lu1-O | 1.970 Å | Lu1-O | 1.914 Å | Sc1-O | 1.861 Å |
| Lu2-O | 2.017 Å | Lu2-O | 2.083 Å | Sc2-O | 2.017 Å |
| Lu1-O-Lu2 | 157.05° | Lu1-O-Lu2 | 141.80° | Sc1-O-Sc2 | 160.79° |

Table S4. Relative energy (ΔE / kcal·mol⁻¹) and the energy gaps (Gap / eV) between HOMO and LUMO of Lu₂O@C₈₀ isomers on the PBE/6-31G(d)-SDD level.

| Isomer ^a | APP ^b | Multiplicity | ΔE | Gap |
|--|------------------|----------------|------------|-------------|
| Lu ₂ O@I _h (7)-C ₈₀ | 0 | Singlet | 0.0 | 0.13 |
| Lu ₂ O@D _{5h} (6)-C ₈₀ | 0 | Singlet | 3.4 | 0.20 |
| Lu₂O@C₁(31876)-C₈₀ | 1 | Singlet | 6.3 | 0.77 |
| Lu₂O@C_{2v}(5)-C₈₀ | 0 | Singlet | 6.9 | 0.73 |
| Lu ₂ O@C ₁ (28324)-C ₈₀ | 1 | Singlet | 15.5 | 0.86 |
| Lu ₂ O@C _{2v} (3)-C ₈₀ | 0 | Singlet | 16.4 | 0.35 |
| Lu ₂ O@C ₁ (31891)-C ₈₀ | 1 | Singlet | 19.1 | 0.17 |

^aIsomer number according to the spiral algorithm of Fowler and Manolopoulos.^{S2} The simplified number is used for the IPR isomers. ^bAPP: number of adjacent pentagon pairs.

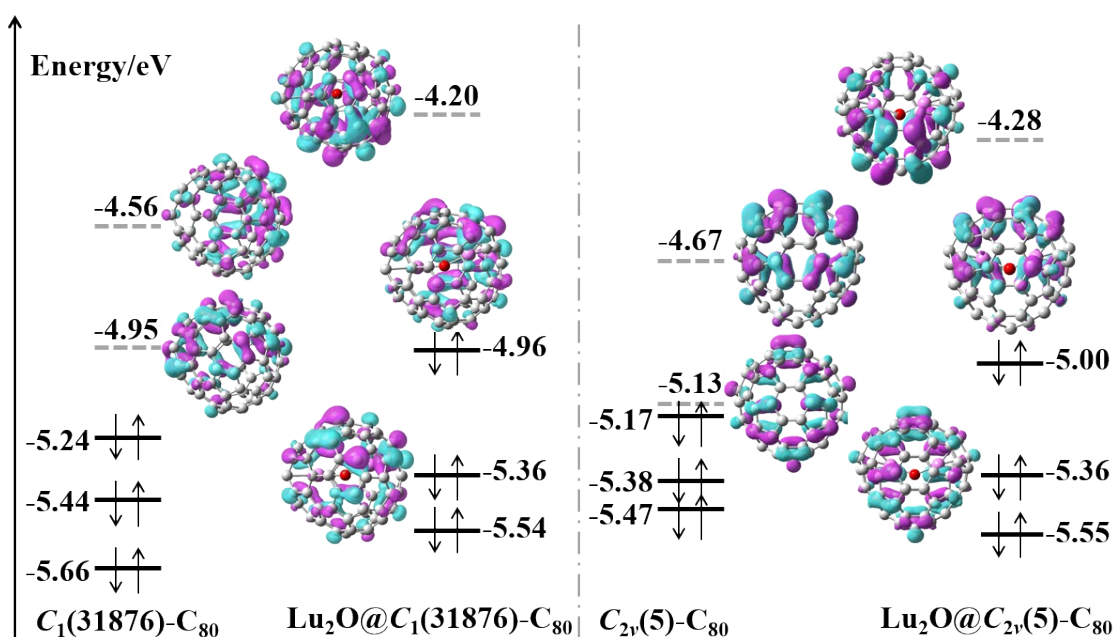


Figure S5. Energies of frontier molecular orbitals of C₁(31876)-C₈₀, C_{2v}(5)-C₈₀, Lu₂O@C₁(31876)-C₈₀, and Lu₂O@C_{2v}(5)-C₈₀, maps of LUMO and LUMO+1 of C₁(31876)-C₈₀ and C_{2v}(5)-C₈₀, and LUMO, HOMO and HOMO-1 of Lu₂O@C₁(31876)-C₈₀ and Lu₂O@C_{2v}(5)-C₈₀ on the PBE/6-311G(d,p)-def2-TZVP//6-31G(d)-SDD.

Frontier molecular orbital analyses. Based on the frontier molecular orbital analyses, it can be clearly confirmed that the LUMO and LUMO+1 of C₈₀ clearly become the HOMO-1 and HOMO of Lu₂O@C₈₀, respectively, indicating the four-electron transfer

from Lu_2O to C_{80} , *i.e.*, $(\text{Lu}_2\text{O})^{4+}@\text{C}_{80}^{4-}$. Furthermore, the HOMO and LUMO orbitals of $\text{Lu}_2\text{O}@\text{C}_1(31876)\text{-C}_{80}$ and $\text{Lu}_2\text{O}@\text{C}_{2v}(5)\text{-C}_{80}$ are mainly located on the cage frameworks, and their the HOMO-LUMO gaps are 0.76 eV and 0.72 eV, respectively.

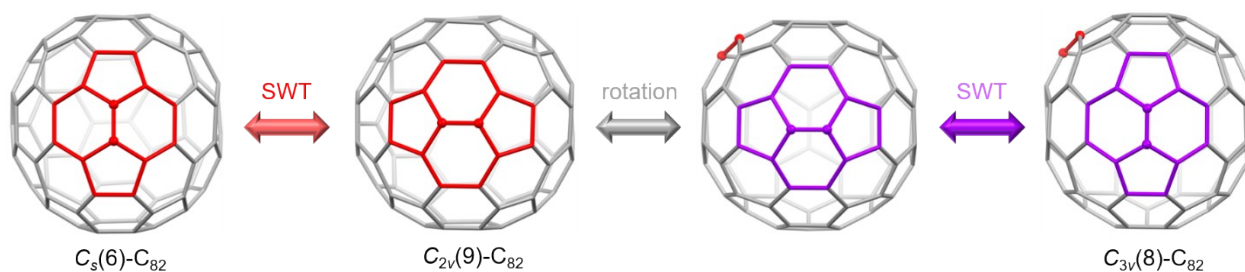


Figure S6. Transformation between $C_s(6)\text{-C}_{82}$, $C_{2v}(9)\text{-C}_{82}$ and $C_{3v}(8)\text{-C}_{82}$.

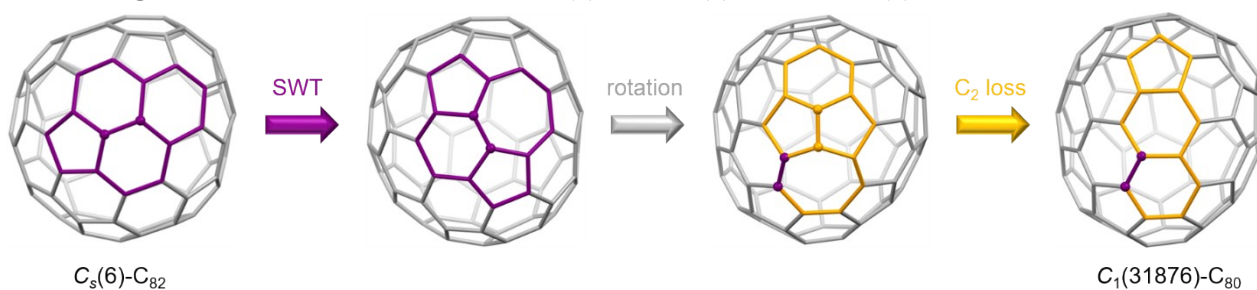


Figure S7. Transformation from $C_s(6)\text{-C}_{82}$ to $C_1(31876)\text{-C}_{80}$.

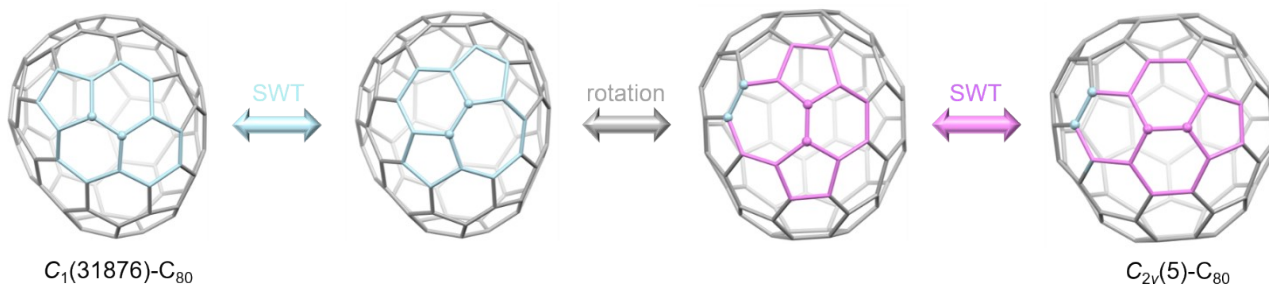


Figure S8. Transformation between $C_1(31876)\text{-C}_{80}$ and $C_{2v}(5)\text{-C}_{80}$.

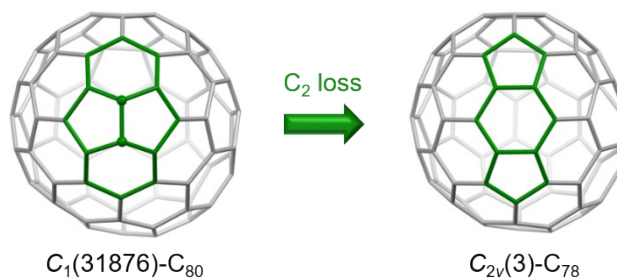


Figure S9. Transformation from $C_1(31876)\text{-C}_{80}$ to $C_{2v}(3)\text{-C}_{78}$.

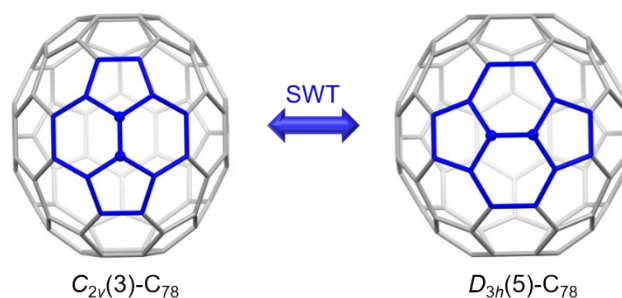


Figure S10. Transformation between $C_{2v}(3)-C_{78}$ and $D_{3h}(5)-C_{78}$.

Table S5. Cartesian coordinates of the four low-energy $\text{Lu}_2\text{O}@C_{80}$ isomers.

| $\text{Lu}_2\text{O}@I_h(7)-C_{80}$ | | | | $\text{Lu}_2\text{O}@D_{5h}(6)-C_{80}$ | | | |
|-------------------------------------|-------------|-------------|-------------|--|-------------|-------------|-------------|
| C | -0.03901400 | -0.01862200 | 0.05269100 | C | -0.04448500 | -0.03361000 | 0.11727000 |
| C | 1.40502100 | -0.02732000 | 0.06776600 | C | 1.40269300 | -0.02396000 | 0.11882800 |
| C | 2.16884500 | 1.21580800 | 0.07166900 | C | 2.14258200 | 1.20690600 | 0.08707400 |
| C | 3.39931500 | 1.00570500 | -0.66291500 | C | 3.41239000 | 1.16018900 | -0.57199500 |
| C | 4.05020200 | 2.06183700 | -1.39902200 | C | 3.94367100 | 2.32438500 | -1.25325400 |
| C | 4.69657500 | 1.67831000 | -2.63372600 | C | 4.64758700 | 1.90644800 | -2.45646100 |
| C | 4.70036300 | 2.55549500 | -3.80457700 | C | 4.59859000 | 2.68761600 | -3.65772500 |
| C | 4.62280800 | 1.69080300 | -4.97381400 | C | 4.68671900 | 1.95740100 | -4.88849100 |
| C | 3.93249700 | 2.07323800 | -6.17678400 | C | 4.02101200 | 2.42565100 | -6.09485500 |
| C | 3.32741600 | 1.04383600 | -6.96451400 | C | 3.51246700 | 1.29128200 | -6.84071000 |
| C | 2.08623900 | 1.28077600 | -7.64895900 | C | 2.26449700 | 1.36639200 | -7.53771000 |
| C | 1.31922000 | 0.04129900 | -7.62544400 | C | 1.52678100 | 0.13828900 | -7.64423800 |
| C | -0.12460500 | 0.04885300 | -7.56905500 | C | 0.08030100 | 0.12944100 | -7.68930500 |
| C | -0.77452600 | -1.01895500 | -6.86118300 | C | -0.41220400 | -1.00382500 | -6.95763800 |
| C | -2.02309300 | -0.81863900 | -6.15248100 | C | -1.60737900 | -0.91445000 | -6.17800400 |
| C | -2.02550900 | -1.69678800 | -4.98293700 | C | -1.66502100 | -1.76013200 | -5.01906400 |
| C | -2.68204200 | -1.31968900 | -3.74326900 | C | -2.40532700 | -1.37624700 | -3.85465100 |
| C | -1.95641400 | -1.67050800 | -2.54378900 | C | -1.70208500 | -1.80854600 | -2.68427700 |
| C | -1.92746200 | -0.83669400 | -1.35338600 | C | -1.68206500 | -1.01243500 | -1.48956000 |
| C | -0.69681800 | -1.08351900 | -0.64253700 | C | -0.51256400 | -1.13518000 | -0.67640200 |

| | | | | | | | |
|---|-------------|-------------|-------------|---|-------------|-------------|-------------|
| C | -0.68899500 | 1.24680800 | 0.11368300 | C | -0.75223700 | 1.17634800 | 0.13124700 |
| C | -1.93062500 | 1.48501500 | -0.57552700 | C | -1.94981900 | 1.32202100 | -0.64783700 |
| C | -2.54091500 | 0.45355800 | -1.35641400 | C | -2.42446400 | 0.25662300 | -1.47474300 |
| C | -3.24725600 | 0.82571200 | -2.56720100 | C | -3.14008200 | 0.65016100 | -2.65579100 |
| C | -3.41197400 | -0.04634100 | -3.73188200 | C | -3.11960700 | -0.15467500 | -3.84043900 |
| C | -3.38591000 | 0.84093300 | -4.91811300 | C | -3.10331000 | 0.69881900 | -4.99047800 |
| C | -2.66081100 | 0.47778100 | -6.12987600 | C | -2.34988000 | 0.35457100 | -6.16352300 |
| C | -2.00521700 | 1.52581200 | -6.87316700 | C | -1.84944800 | 1.45313800 | -6.92950500 |
| C | -0.77611700 | 1.30626200 | -7.60021500 | C | -0.62750200 | 1.33942600 | -7.67545600 |
| C | -0.00892100 | 2.54956800 | -7.59380500 | C | 0.08985100 | 2.59487700 | -7.61592300 |
| C | 1.43613200 | 2.54471000 | -7.58492200 | C | 1.52293700 | 2.63403600 | -7.52303000 |
| C | 2.09265500 | 3.61070800 | -6.88776500 | C | 2.07631900 | 3.74612900 | -6.81195300 |
| C | 3.32049700 | 3.36470500 | -6.17356400 | C | 3.32186100 | 3.62056400 | -6.08084300 |
| C | 3.34667100 | 4.20703300 | -4.98753600 | C | 3.25232600 | 4.40947000 | -4.86000500 |
| C | 4.06786200 | 3.86339900 | -3.78324600 | C | 3.85810600 | 3.95390800 | -3.64304700 |
| C | 3.48549600 | 4.30522900 | -2.51064800 | C | 3.21346400 | 4.35851000 | -2.42804200 |
| C | 3.47453900 | 3.39990600 | -1.33800400 | C | 3.24459900 | 3.51934700 | -1.23962600 |
| C | 2.18129300 | 3.53682900 | -0.68569600 | C | 1.97631000 | 3.61527300 | -0.54392100 |
| C | 1.52026300 | 2.47042600 | 0.03725100 | C | 1.40113600 | 2.47461900 | 0.10158500 |
| C | 0.07744000 | 2.48159100 | 0.08930000 | C | -0.03411300 | 2.43265200 | 0.14689300 |
| C | -0.68430200 | 3.47218400 | -0.59857000 | C | -0.83318100 | 3.38416400 | -0.57179700 |
| C | -1.92979800 | 2.86331100 | -1.02064900 | C | -2.02670000 | 2.71106500 | -1.07338300 |
| C | -2.51661200 | 3.22985600 | -2.25716900 | C | -2.69053000 | 3.12095700 | -2.27694300 |
| C | -3.18519800 | 2.19587700 | -3.00920400 | C | -3.23553000 | 2.04529600 | -3.06936000 |
| C | -3.24085400 | 2.20882200 | -4.44447900 | C | -3.21222300 | 2.07543900 | -4.52208700 |
| C | -2.56485600 | 3.25602500 | -5.18198100 | C | -2.64194200 | 3.18235100 | -5.25071300 |
| C | -1.98540900 | 2.90188200 | -6.42063400 | C | -1.94083200 | 2.82327200 | -6.44926800 |
| C | -0.74934900 | 3.52626800 | -6.87968400 | C | -0.73249700 | 3.51588600 | -6.88379300 |

| | | | | | | | |
|---|-------------|-------------|-------------|---|-------------|-------------|-------------|
| C | -0.08901700 | 4.54406800 | -6.09607400 | C | -0.16510800 | 4.54392100 | -6.06989700 |
| C | 1.34039400 | 4.59813400 | -6.15697900 | C | 1.25317600 | 4.66395800 | -6.07553400 |
| C | 2.10465300 | 4.96213000 | -4.98899600 | C | 1.98429400 | 5.06710100 | -4.86807400 |
| C | 1.46629900 | 5.31142500 | -3.75940600 | C | 1.28807700 | 5.33849900 | -3.65505700 |
| C | 2.16836000 | 4.94342900 | -2.54523600 | C | 1.94542900 | 5.01613500 | -2.43295000 |
| C | 1.39983100 | 4.50040500 | -1.40964200 | C | 1.17650800 | 4.56382300 | -1.26718300 |
| C | -0.04243500 | 4.48018600 | -1.40328000 | C | -0.24090900 | 4.44522100 | -1.32326400 |
| C | -0.70831600 | 4.94995000 | -2.56266000 | C | -0.93366300 | 4.87353400 | -2.53182700 |
| C | -1.93493800 | 4.31651000 | -3.00299500 | C | -2.19972700 | 4.31227400 | -2.99097100 |
| C | -1.94314100 | 4.32013500 | -4.42960300 | C | -2.17530600 | 4.34232000 | -4.47223000 |
| C | -0.72710200 | 4.96570000 | -4.89491000 | C | -0.89592300 | 4.92140300 | -4.86691100 |
| C | 0.03671200 | 5.35334600 | -3.73728200 | C | -0.15748600 | 5.26759700 | -3.67959900 |
| C | 2.14430300 | -0.98912400 | -0.66741500 | C | 3.83918800 | 0.01083300 | -1.31993300 |
| C | 3.38282400 | -0.36371000 | -1.12425100 | C | 4.59874700 | 0.47912800 | -2.48560100 |
| C | 3.96503800 | -0.72232000 | -2.36442300 | C | 4.54543800 | -0.23075500 | -3.71970600 |
| C | 4.64479600 | 0.30697200 | -3.10134300 | C | 4.63809300 | 0.53009700 | -4.92069100 |
| C | 4.61829800 | 0.31981300 | -4.53809200 | C | 3.91619300 | 0.11132700 | -6.12832400 |
| C | 3.92673100 | -0.69820500 | -5.28210300 | C | 3.11650700 | -1.06634200 | -6.13490800 |
| C | 3.32618400 | -0.33147300 | -6.51247600 | C | 1.93376100 | -1.04236800 | -6.93632800 |
| C | 2.07727100 | -0.94200900 | -6.93324600 | C | 0.74194300 | -1.76328900 | -6.50200400 |
| C | 1.43129600 | -1.96354800 | -6.13887300 | C | 0.72337000 | -2.57203800 | -5.31761900 |
| C | -0.00590300 | -2.00505700 | -6.15244700 | C | -0.51346100 | -2.53701600 | -4.57558900 |
| C | -0.75212200 | -2.40287500 | -4.98851200 | C | -0.53663900 | -2.56649700 | -3.12307000 |
| C | -0.06883600 | -2.77654600 | -3.77896300 | C | 0.67581600 | -2.63140700 | -2.34453700 |
| C | -0.71194000 | -2.42381600 | -2.55216400 | C | 0.65594500 | -1.87571500 | -1.12585100 |
| C | 0.05344800 | -2.06411800 | -1.38447100 | C | 1.83279900 | -1.17442300 | -0.62421100 |
| C | 1.48411200 | -2.01235400 | -1.44590000 | C | 3.04014300 | -1.16515200 | -1.38825000 |
| C | 2.12260200 | -2.43611200 | -2.64470200 | C | 3.06177900 | -1.95745100 | -2.61134400 |

| | | | | | | | |
|----|-------------|-------------|-------------|----|-------------|-------------|-------------|
| C | 3.34261600 | -1.79048200 | -3.11257300 | C | 3.77525800 | -1.45575700 | -3.75791400 |
| C | 3.32838800 | -1.78172600 | -4.53418200 | C | 3.10049700 | -1.91064200 | -4.94687100 |
| C | 2.10006700 | -2.41902900 | -4.97475900 | C | 1.97139900 | -2.74793300 | -4.55496600 |
| C | 1.36063600 | -2.82701400 | -3.79899700 | C | 1.94701600 | -2.77668300 | -3.07377700 |
| Lu | 2.25373200 | 2.37955600 | -3.16161100 | Lu | -0.72597600 | 2.61689000 | -3.74068100 |
| Lu | -1.13316500 | 0.51253300 | -4.09952500 | Lu | 1.19340600 | -0.64712500 | -3.78985600 |
| O | 0.62610200 | 1.35953600 | -3.69597800 | O | 0.76906200 | 1.29971000 | -3.75071000 |

| Lu₂O@C₁(31876)-C₈₀ | | | | Lu₂O@C_{2v}(5)-C₈₀ | | | |
|--|-------------|-------------|-------------|---|-------------|------------|-------------|
| C | 12.75074800 | 9.23706500 | 13.83271500 | C | 16.56554100 | 7.58461400 | -0.21818300 |
| C | 12.17940700 | 7.97204700 | 13.45741500 | C | 15.22292100 | 7.47033100 | 0.29475600 |
| C | 12.29174100 | 7.81831400 | 12.01905300 | C | 17.48257800 | 6.49491400 | -0.13714200 |
| C | 12.95793600 | 8.98493900 | 11.48460200 | C | 18.87538300 | 6.82479800 | 0.09507500 |
| C | 13.16777200 | 9.90987400 | 12.59910200 | C | 19.65132700 | 5.99300900 | 0.97849800 |
| C | 14.24878100 | 10.86066500 | 12.60194200 | C | 19.13923700 | 4.78284400 | 1.57373000 |
| C | 14.80530800 | 11.20756600 | 13.86974100 | C | 17.84247500 | 4.37381000 | 1.14450600 |
| C | 14.46933900 | 10.44871600 | 15.06565500 | C | 16.99826800 | 5.25625400 | 0.35306400 |
| C | 13.57166800 | 9.33625700 | 15.01841800 | C | 15.63318000 | 5.12765600 | 0.83358000 |
| C | 13.90458400 | 8.11604400 | 15.78955500 | C | 15.62098200 | 4.09781100 | 1.83960000 |
| C | 13.47920300 | 6.80792900 | 15.26523200 | C | 19.63446200 | 4.40948800 | 2.89803800 |
| C | 12.62878900 | 6.75989600 | 14.09606600 | C | 17.44058800 | 3.24572700 | 3.28261700 |
| C | 12.93731600 | 5.80957200 | 13.03077400 | C | 16.55802600 | 3.35474400 | 4.43182600 |
| C | 12.80374000 | 6.50036100 | 11.74699300 | C | 15.25031700 | 3.82827000 | 4.26532100 |
| C | 13.80895500 | 6.30060000 | 10.72300300 | C | 14.76493100 | 4.19876300 | 2.94972700 |
| C | 14.39092200 | 7.48501300 | 10.04222100 | C | 16.97957500 | 3.61985300 | 2.01575000 |
| C | 13.99230000 | 8.84600500 | 10.47603600 | C | 13.89921800 | 5.33871600 | 3.09102100 |
| C | 14.96401200 | 9.90578600 | 10.40309000 | C | 18.77707100 | 3.59640300 | 3.69972100 |
| C | 15.08777700 | 10.91724700 | 11.44321300 | C | 20.68091000 | 5.23995600 | 5.00116900 |
| C | 16.47681300 | 11.28011100 | 11.56191100 | C | 21.09086600 | 6.38230500 | 5.78030500 |

| | | | | | | | |
|---|-------------|-------------|-------------|---|-------------|-------------|------------|
| C | 17.03935400 | 11.58974000 | 12.83378900 | C | 21.54897500 | 7.54017700 | 5.13877100 |
| C | 16.18046700 | 11.61354000 | 13.98255800 | C | 21.14185700 | 6.47727300 | 2.91579000 |
| C | 16.66441700 | 11.18825500 | 15.26888200 | C | 20.63212000 | 5.26581200 | 3.57413200 |
| C | 15.61173300 | 10.44634400 | 15.91896500 | C | 21.59183700 | 7.57832600 | 3.70318000 |
| C | 15.89047300 | 9.35744200 | 16.79367300 | C | 20.66246900 | 6.80816600 | 1.58914000 |
| C | 15.01949300 | 8.17568600 | 16.73612000 | C | 13.81184900 | 5.65736600 | 4.51087600 |
| C | 15.53993100 | 6.94787600 | 17.23340600 | C | 19.64888700 | 4.57156400 | 5.76595400 |
| C | 15.17153400 | 5.67765500 | 16.64133500 | C | 14.84579500 | 8.76613300 | 0.78780900 |
| C | 14.24558700 | 5.59443300 | 15.57591800 | C | 13.51453200 | 7.67908300 | 2.56808500 |
| C | 14.44168800 | 4.54689500 | 14.55477300 | C | 13.87914800 | 6.36974000 | 2.10134400 |
| C | 13.86501000 | 4.73660000 | 13.22009400 | C | 18.72302600 | 3.77647800 | 5.13402900 |
| C | 14.56617000 | 4.29914000 | 12.06063900 | C | 17.34090700 | 3.78055600 | 5.56578400 |
| C | 14.58992200 | 5.10800800 | 10.84661400 | C | 19.25015400 | 5.41366000 | 6.87249000 |
| C | 15.92011400 | 5.02506500 | 10.30821500 | C | 17.86825900 | 5.60786500 | 7.17549700 |
| C | 16.45871100 | 6.11658000 | 9.62561800 | C | 16.86924000 | 4.75430400 | 6.49787600 |
| C | 15.68866400 | 7.32941700 | 9.45837300 | C | 14.70854900 | 4.74889800 | 5.22617000 |
| C | 16.64006100 | 8.41387000 | 9.40356600 | C | 19.81620000 | 7.75553400 | 7.38499600 |
| C | 16.28030400 | 9.68111300 | 9.87926800 | C | 18.44772500 | 7.97244000 | 7.77536900 |
| C | 17.22995300 | 10.49221600 | 10.59887200 | C | 17.47964200 | 6.93207600 | 7.65919000 |
| C | 18.54536400 | 10.00532800 | 10.86427100 | C | 20.20768500 | 6.49217400 | 6.92898500 |
| C | 19.20850400 | 10.49598000 | 12.06382900 | C | 16.11693600 | 7.35523100 | 7.44615000 |
| C | 18.41572300 | 11.21565600 | 13.04860300 | C | 15.94605700 | 9.67023800 | 0.63962700 |
| C | 18.91727500 | 10.87726400 | 14.34725200 | C | 16.21448800 | 10.67626500 | 1.61694800 |
| C | 18.02974500 | 10.83195300 | 15.48276700 | C | 13.33063300 | 7.98566700 | 3.98068700 |
| C | 18.31797500 | 9.89621800 | 16.50467100 | C | 15.48579400 | 5.22073700 | 6.32540200 |
| C | 17.25422500 | 9.21187900 | 17.20792600 | C | 13.49712400 | 6.96672100 | 4.99702700 |
| C | 17.76375800 | 7.93735300 | 17.63334400 | C | 17.59149600 | 11.06218600 | 1.75727200 |
| C | 16.90346000 | 6.83242700 | 17.70257500 | C | 18.09390700 | 11.53086600 | 3.01254500 |

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|---|-------------|------------|-------------|---|-------------|-------------|-------------|
| C | 17.40011400 | 5.51723200 | 17.35300700 | C | 17.23566600 | 11.66392100 | 4.12830000 |
| C | 16.30773400 | 4.78568900 | 16.74720800 | C | 15.85760900 | 11.29359200 | 4.01214600 |
| C | 16.55120900 | 3.87282100 | 15.71957800 | C | 15.32661600 | 10.79219500 | 2.78504000 |
| C | 15.60131300 | 3.72787800 | 14.64869800 | C | 19.24372600 | 9.93315700 | 6.74188500 |
| C | 16.36051500 | 3.39792100 | 13.45625400 | C | 20.98054500 | 9.71681200 | 4.48707700 |
| C | 15.86705800 | 3.70058000 | 12.19868400 | C | 19.94887100 | 10.70594800 | 4.47632400 |
| C | 16.74591300 | 4.22805400 | 11.18414900 | C | 19.05295600 | 10.82548700 | 5.64191600 |
| C | 18.08548500 | 4.60646800 | 11.49507600 | C | 17.71542400 | 11.31389500 | 5.43654100 |
| C | 18.63683900 | 5.74634800 | 10.75304700 | C | 19.44283900 | 11.06909100 | 3.18114600 |
| C | 17.84304800 | 6.45131300 | 9.80488900 | C | 14.22456500 | 9.87825400 | 2.90615500 |
| C | 17.96273300 | 7.90056300 | 9.64198500 | C | 14.00656700 | 8.86293900 | 1.92165700 |
| C | 18.91308000 | 8.66482700 | 10.37997200 | C | 14.76878400 | 6.26174100 | 0.92966500 |
| C | 19.89904600 | 7.92208800 | 11.14274600 | C | 15.11520400 | 6.52188600 | 6.84424500 |
| C | 20.62991900 | 8.46023600 | 12.27935700 | C | 14.06437000 | 7.37582500 | 6.28595300 |
| C | 20.27699300 | 9.78868600 | 12.75882300 | C | 15.74402800 | 8.73055300 | 7.23633900 |
| C | 20.04844600 | 9.97255900 | 14.18984900 | C | 14.47693400 | 8.77938600 | 6.51645400 |
| C | 20.21715400 | 8.90221500 | 15.16883500 | C | 20.56179500 | 8.16665500 | 1.05119300 |
| C | 19.43666100 | 8.97167800 | 16.37056700 | C | 19.41144300 | 8.18058700 | 0.11830900 |
| C | 19.11173100 | 7.78605400 | 17.12280400 | C | 16.78652400 | 9.73345200 | 7.13469400 |
| C | 19.55875300 | 6.52386000 | 16.69382800 | C | 18.11502700 | 9.35071500 | 7.44739600 |
| C | 18.70800000 | 5.36457500 | 16.85256500 | C | 14.37386300 | 9.78016400 | 5.43773400 |
| C | 18.93372500 | 4.50206300 | 15.70300800 | C | 13.76611900 | 9.36063900 | 4.19618300 |
| C | 17.89203300 | 3.74089500 | 15.16879200 | C | 15.43721100 | 10.74111700 | 5.29868700 |
| C | 17.76681100 | 3.56492600 | 13.73876400 | C | 16.59994400 | 10.76378600 | 6.16575600 |
| C | 18.61903300 | 4.25931600 | 12.82275900 | C | 20.76958000 | 9.26777800 | 1.99730300 |
| C | 19.70388300 | 5.05861600 | 13.40417300 | C | 21.30069100 | 8.95113800 | 3.28865700 |
| C | 20.21748100 | 6.16469700 | 12.64416900 | C | 17.03337700 | 8.94232900 | -0.01247200 |
| C | 19.69717700 | 6.49593400 | 11.36014200 | C | 18.42385500 | 9.27569500 | 0.15855000 |

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|----|-------------|------------|-------------|----|-------------|-------------|------------|
| C | 20.75916500 | 7.37781300 | 13.24432300 | C | 21.15907100 | 8.85100100 | 5.62169100 |
| C | 20.61560100 | 7.56609400 | 14.67883000 | C | 20.30082900 | 8.95598100 | 6.72976500 |
| C | 20.27236200 | 6.40826500 | 15.44457900 | C | 19.83140800 | 10.37143900 | 1.96219300 |
| C | 19.86398000 | 5.15205600 | 14.81390000 | C | 18.68056900 | 10.37047200 | 1.06589600 |
| Lu | 14.56081500 | 7.79965700 | 12.95321800 | Lu | 15.79323300 | 7.87619800 | 4.76012000 |
| Lu | 18.43506900 | 8.35602500 | 13.19613600 | Lu | 18.58899000 | 8.14130900 | 2.34438600 |
| O | 16.54347700 | 7.71319400 | 13.23096200 | O | 17.49784300 | 7.43617200 | 3.84443500 |

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