

Supporting Information

Hexameric poly-fluoroberyllophosphate $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ with moderate birefringence and deep-ultraviolet transmission as potential zero-order-waveplate crystal

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Table S1. Selected bond distances (Å) and angles (deg) for (a)Na₄Be₂PO₄F₅ and (b) KBe[PO₃(OH)]F.

(a)			
Be(1)–O(3)	1.6120 (15)	Na(2)–F(5)	2.2622 (8)
Be(1)–F(11)	1.5519 (15)	Na(3)–O(3b)	2.4561 (9)
Be(1)–F(2)	1.5339 (15)	Na(3)–O(4j)	2.2726 (9)
Be(1)–F(5c)	1.5719 (15)	Na(3)–F(1h)	2.4350 (8)
Be(2)–O(1)	1.6096 (15)	Na(3)–F(1)	2.2682 (8)
Be(2)–O(2)	1.6506 (15)	Na(3)–F(3)	2.3838 (10)
Be(2)–F(3c)	1.5464 (15)	Na(3)–F(4i)	2.4604 (11)
Be(2)–F(4)	1.5596 (15)	Na(4)–O(2k)	2.3886 (10)
P(1)–O(1c)	1.5361 (9)	Na(4)–O(3)	2.4698 (12)
P(1)–O(2)	1.5500 (8)	Na(4)–F(1c)	2.5749 (9)
P(1)–O(3)	1.5452 (8)	Na(4)–F(3c)	2.2281 (8)
P(1)–O(4)	1.5079 (8)	Na(4)–F(4k)	2.6931 (8)
Na(1)–O(4b)	2.3578 (9)	Na(4)–F(5l)	2.2706 (8)
Na(1)–O(4d)	2.3578 (9)	Na(4)–F(5c)	2.6444 (9)
Na(1)–F(2e)	2.3101 (7)	Na(5)–O(2f)	2.5881 (10)
Na(1)–F(2)	2.3101 (7)	Na(5)–O(2d)	2.5881 (10)
Na(1)–F(4f)	2.3048 (7)	Na(5)–F(2)	2.3606 (8)
Na(1)–F(4g)	2.3048 (7)	Na(5)–F(2c)	2.3606 (8)
Na(2)–O(1c)	2.3789 (9)	Na(5)–F(4d)	2.6557 (10)
Na(2)–O(4b)	2.3418 (10)	Na(5)–F(4f)	2.6557 (10)

Na(2)–F(1)	2.7835 (11)	Na(5)–F(5c)	2.4787 (9)
Na(2)–F(2)	2.2564 (10)	Na(5)–F(5)	2.4787 (9)
Na(2)–F(3)	2.3517 (8)		
O(3)–Be(1)–F(11)	104.80 (8)	O(4b)–Na(2)–F(1)	76.18 (3)
O(1)–Be(2)–O(2)	113.10 (9)	O(4j)–Na(3)–O(3b)	144.39 (3)
O(1)–Be(2)–F(3c)	104.57 (9)	O(3b)–Na(3)–F(4i)	92.18 (3)
O(1)–Be(2)–F(4)	115.89 (9)	O(2k)–Na(4)–O(3)	125.38 (4)
O(1c)–P(1)–O(3)	108.69 (4)	O(2k)–Na(4)–F(1c)	102.76 (3)
O(3)–P(1)–O(2)	108.65 (5)	O(2f)–Na(5)–O(2d)	81.11 (4)
O(4d)–Na(1)–O(4b)	180.0	O(2d)–Na(5)–F(4f)	91.31 (3)

Symmetry transformations used to generate equivalent atoms:

(a) $x, y-1, z$; (b) $-x+1, -y+2, -z+1$; (c) $-x+1, y, -z+1/2$; (d) $x, y+1, z$; (e) $-x+1, -y+3, -z+1$;
(f) $-x+1, y+1, -z+1/2$; (g) $x, -y+2, z+1/2$; (h) $-x+3/2, y-1/2, -z+3/2$; (i) $x+1/2, y+1/2, z+1$;
(j) $x+1/2, -y+3/2, z+1/2$; (k) $-x+1/2, -y+3/2, -z$; (l) $x-1/2, -y+5/2, z-1/2$; (m) $-x+1/2, -y+5/2, -z$;
(n) $-x+3/2, y+1/2, -z+3/2$; (o) $x+1/2, -y+5/2, z+1/2$; (p) $-x+1, y-1, -z+1/2$; (q) $x-1/2, y-1/2, z-1$;
(r) $x-1/2, -y+3/2, z-1/2$.

(b)

Be(1)–O(7)	1.634 (2)	K(1)–O(1c)	2.7364 (13)
Be(1)–O(6)	1.626 (2)	K(1)–O(2)	2.7642 (13)
Be(1)–O(3)	1.626 (2)	K(1)–O(3e)	2.9253 (12)
Be(1)–F(2)	1.541 (2)	K(1)–O(5b)	2.7591 (12)
P(1)–O(1)	1.5745 (13)	K(1)–O(6d)	2.9663 (13)
P(1)–O(3h)	1.5280 (13)	K(1)–O(8b)	2.8648 (12)
P(1)–O(6g)	1.5177 (11)	K(1)–F(1c)	2.6268 (10)

P(1)–O(8)	1.5174 (12)	K(1)–F(2)	2.7921 (11)
Be(2h)–O(4)	1.633 (2)	K(2)–O(1a)	2.9518 (14)
Be(2)–O(5)	1.632 (2)	K(2)–O(2e)	2.8552 (13)
Be(2)–O(8)	1.638 (2)	K(2)–O(3e)	3.0155 (12)
Be(2)–F(1)	1.529 (2)	K(2)–O(5)	3.1588 (13)
P(2)–O(2)	1.5734 (13)	K(2)–O(6c)	3.2165 (12)
P(2)–O(4)	1.5314 (13)	K(2)–O(7c)	2.7851 (12)
P(2)–O(5)	1.5138 (11)	K(2)–O(8)	3.3385 (12)
P(2)–O(7)	1.5098 (11)	K(2)–F(1c)	2.7633 (11)
O(1)–H(1)	0.68 (2)	K(2)–F(1)	2.7476 (11)
O(2)–H(2)	0.82 (3)	K(2)–F(2c)	3.4069 (11)
O(3)–Be(1)–O(7)	111.38 (14)	O(4h)–Be(2)–O(8)	111.27 (14)
O(3)–Be(1)–F(2)	109.56 (14)	O(8)–Be(2)–F(1)	111.15 (14)
O(3h)–P(1)–O(1)	105.93 (7)	O(4)–P(2)–O(2)	106.22 (7)
O(6g)–P(1)–O(1)	107.73 (7)	O(1a)–K(2)–O(3e)	49.03 (3)
O(1c)–K(1)–O(2)	150.53 (4)	O(1a)–K(2)–O(5)	129.50 (3)
O(1c)–K(1)–O(5b)	84.37 (4)	O(1a)–K(2)–F(2c)	115.31 (3)
O(2)–K(1)–F(2)	71.93 (3)	O(2e)–K(2)–F(2c)	99.99 (3)
O(5b)–K(1)–F(2)	70.04 (3)	O(3e)–K(2)–F(2c)	157.41 (3)

Symmetry codes: (a) $x+1/2, -y+1/2, z-1/2$; (b) $-x+1/2, y+1/2, -z+1/2$; (c) $-x+1, -y+1, -z+1$; (d) $x+1/2, -y+3/2, z-1/2$; (e) $-x+1/2, y-1/2, -z+1/2$; (f) $x-1/2, -y+1/2, z+1/2$; (g) $x, y-1, z$; (h) $-x, -y+1, -z+1$; (i) $x-1/2, -y+3/2, z+1/2$; (j) $x, y+1, z$.

Table S2. Atomic coordinates, equivalent isotropic displacement parameters (\AA^2) for (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$. $U(\text{eq})$ is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

(a)

Atom	Wyck.	Site	x/a	y/b	z/c	BVS
P1	8f	1	0.40923(2)	0.82091(3)	0.27680(2)	5.00
Be1	8f	1	0.36665(9)	1.20614(18)	0.22229(13)	1.98
Be2	8f	1	0.39721(9)	0.76191(18)	0.05890(13)	1.98
Na1	4a	-1	1/2	1.50000	1/2	1.16
Na2	8f	1	0.59347(3)	1.14243(6)	0.49146(4)	1.06
Na3	8f	1	0.77023(3)	0.96832(6)	0.77727(4)	1.05
Na4	8f	1	0.23233(3)	1.00435(6)	-0.02314(4)	1.02
Na5	4e	2	1/2	1.44808(9)	1/4	0.94
O1	8f	1	0.48885(5)	0.87466(10)	0.12516(7)	1.97
O2	8f	1	0.38671(5)	0.71226(11)	0.16311(7)	1.98
O3	8f	1	0.35017(5)	0.99343(10)	0.21939(8)	2.04
O4	8f	1	0.38760(5)	0.71072(11)	0.34321(7)	1.98
F1	8f	1	0.78190(4)	1.20409(9)	0.68668(7)	0.98
F2	8f	1	0.45753(4)	1.28672(9)	0.34678(6)	1.04
F3	8f	1	0.68233(4)	0.88235(9)	0.55471(6)	1.02
F4	8f	1	0.39072(4)	0.57208(9)	0.00581(6)	0.96
F5	8f	1	0.63796(5)	1.25309(9)	0.39172(6)	1.04

Atom	U_{11}	U_{22}	U_{33}	U_{12}	U_{13}	U_{23}
P1	0.00859(13)	0.00772(13)	0.00897(13)	0.00029(8)	0.00626(11)	0.00011(8)
Be1	0.0132(6)	0.0105(6)	0.0130(6)	0.0002(4)	0.0092(5)	-0.0003(4)
Be2	0.0107(5)	0.0113(6)	0.0124(6)	0.0002(4)	0.0082(5)	-0.0001(4)
Na1	0.0152(3)	0.0147(3)	0.0149(3)	0.0024(2)	0.0108(2)	0.0016(2)
Na2	0.0219(2)	0.0173(2)	0.0177(2)	0.00361(17)	0.0144(2)	0.00074(17)
Na3	0.0168(2)	0.0183(2)	0.0192(2)	0.00239(16)	0.01320(19)	0.00354(17)
Na4	0.0161(2)	0.0191(2)	0.0192(2)	0.00063(17)	0.0102(2)	-0.00178(17)
Na5	0.0208(3)	0.0166(3)	0.0265(3)	0.00000	0.0174(3)	0.00000
O1	0.0102(3)	0.0141(4)	0.0147(4)	0.0001(3)	0.0078(3)	0.0024(3)
O2	0.0170(4)	0.0162(4)	0.0144(3)	-0.0049(3)	0.0125(3)	-0.0047(3)
O3	0.0114(3)	0.0094(4)	0.0199(4)	0.0015(3)	0.0086(3)	0.0018(3)
O4	0.0163(4)	0.0156(4)	0.0142(4)	-0.0010(3)	0.0118(3)	0.0017(3)
F1	0.0186(3)	0.0151(3)	0.0236(3)	-0.0048(2)	0.0158(3)	-0.0022(2)
F2	0.0158(3)	0.0159(3)	0.0154(3)	-0.0028(2)	0.0077(3)	-0.0037(2)
F3	0.0118(3)	0.0181(3)	0.0146(3)	-0.0034(2)	0.0066(3)	-0.0035(2)
F4	0.0232(3)	0.0138(3)	0.0216(3)	-0.0011(2)	0.0175(3)	-0.0039(2)
F5	0.0234(3)	0.0205(3)	0.0186(3)	-0.0034(3)	0.0169(3)	-0.0033(3)

(b)

Atom	Wyck.	Site	x/a	y/b	z/c	BVS
P1	4e	1	0.16300(5)	0.08053(4)	0.60944(4)	5.01
P2	4e	1	0.10578(5)	0.57972(4)	0.37624(4)	5.04
Be1	4e	1	0.1815(3)	0.8614(2)	0.43811(19)	2.03
Be2	4e	1	0.2115(3)	0.3638(2)	0.54256(19)	2.02
K1	4e	1	0.47035(5)	0.70855(4)	0.21330(3)	1.03
K2	4e	1	0.52610(5)	0.31339(5)	0.39494(4)	0.89
F1	4e	1	0.38493(12)	0.40709(10)	0.59238(9)	0.96
F2	4e	1	0.33227(13)	0.89187(11)	0.36955(9)	0.74
O1	4e	1	0.27211(16)	0.11254(13)	0.72939(11)	2.13
O2	4e	1	0.15963(16)	0.61113(13)	0.24831(11)	2.16
O3	4e	1	0.01535(14)	0.91488(12)	0.35996(10)	2.01
O4	4e	1	-0.08263(14)	0.58385(12)	0.36413(10)	1.78
O5	4e	1	0.16891(15)	0.43485(11)	0.41129(10)	2.06
O6	4e	1	0.20649(15)	0.93443(11)	0.56919(10)	2.02
O7	4e	1	0.17771(14)	0.69220(11)	0.46006(10)	2.01
O8	4e	1	0.19944(15)	0.19409(12)	0.52125(10)	1.98
H1	4e	1	0.298(3)	0.052(2)	0.757(2)	0.89
H2	4e	1	0.150(4)	0.539(3)	0.208(3)	0.78

Atom	U ₁₁	U ₂₂	U ₃₃	U ₁₂	U ₁₃	U ₂₃
K1	0.0172(2)	0.01511(19)	0.0189(2)	0.00067(15)	-0.00182(15)	0.00036(15)
P1	0.0125(2)	0.00720(19)	0.0095(2)	0.00022(16)	-0.00092(16)	0.00033(16)
K2	0.0232(2)	0.0314(2)	0.0229(2)	-0.00468(19)	0.00110(17)	-0.00498(18)
P2	0.0119(2)	0.00711(19)	0.0088(2)	-0.00006(16)	0.00080(16)	0.00007(16)
F1	0.0133(5)	0.0200(5)	0.0199(5)	-0.0014(4)	-0.0024(4)	0.0006(4)
F2	0.0185(5)	0.0199(5)	0.0235(5)	0.0011(4)	0.0086(4)	0.0040(4)
O8	0.0204(7)	0.0095(6)	0.0124(6)	0.0012(5)	0.0013(5)	0.0012(5)
O7	0.0168(6)	0.0090(5)	0.0143(6)	-0.0004(5)	-0.0026(5)	-0.0008(5)
O6	0.0227(7)	0.0087(5)	0.0119(6)	0.0021(5)	-0.0019(5)	-0.0004(5)
O5	0.0245(7)	0.0077(5)	0.0117(6)	0.0016(5)	-0.0002(5)	0.0008(5)
O4	0.0117(6)	0.0165(6)	0.0158(6)	-0.0008(5)	0.0008(5)	-0.0054(5)
O2	0.0215(7)	0.0124(6)	0.0126(6)	0.0006(5)	0.0057(5)	0.0017(5)
O1	0.0192(7)	0.0107(6)	0.0136(6)	-0.0003(5)	-0.0059(5)	0.0017(5)
O3	0.0136(6)	0.0159(6)	0.0162(6)	0.0012(5)	0.0003(5)	0.0035(5)
Be1	0.0158(11)	0.0097(10)	0.0099(10)	-0.0006(8)	-0.0001(8)	-0.0001(8)
Be2	0.0143(11)	0.0094(10)	0.0114(10)	0.0001(8)	-0.0005(8)	0.0004(8)

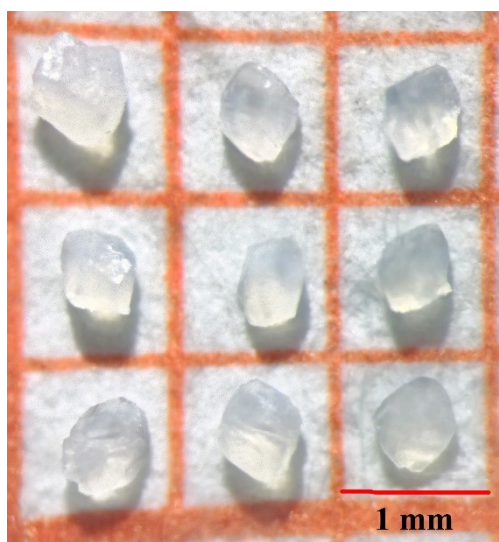
Table S3. Energy-Dispersive Spectrometry (EDS) for Na₄Be₂PO₄F₅ and KBe[PO₃(OH)]F.

(a)

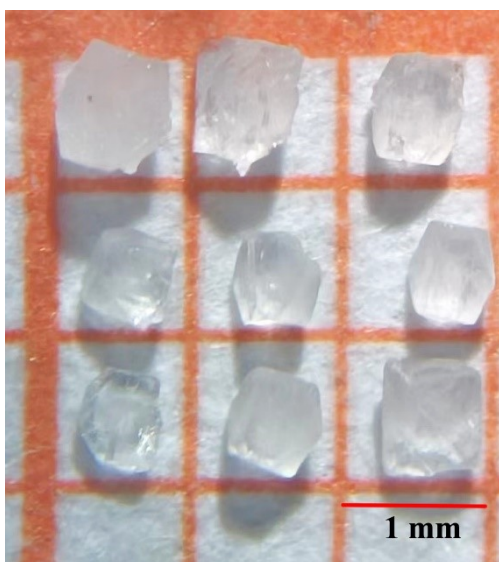
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Element	Weight%	Atomic%	Formula	Element	Weight%	Atomic%	Formula
O K	23.10	28.95		O K	24.02	30.08	
F K	36.90	34.96	5.27	F K	33.87	35.72	4.95
Na M	31.15	27.17	4.45	Na M	30.96	26.98	3.74
P M	6.98	10.78	1	P M	11.15	7.21	1
Totals	100.00			Totals	100.00		
Point 3				The average Na:P:F molar ratio: 4.16:1:5.08			
Element	Weight%	Atomic%	Formula				
O K	28.95	35.72					
F K	30.13	31.30	5.02				
Na M	31.15	26.75	4.29				
P M	9.77	6.23	1				
Totals	100.00						

(b)

Point 1				Point 2			
Element	Weight%	Atomic%	Formula	Element	Weight%	Atomic%	Formula
O K	3.41	54.37		O K	43.02	58.29	
F K	4.94	15.93	1.15	F K	11.81	13.47	1.04
KK	1.79	13.80	1	KK	23.23	12.88	1
P K	1.65	15.90	1.15	P K	21.93	15.35	1.19
Totals	100.00			Totals	100.00		
Point 3				The average K:P:F molar ratio: 1:1.15:1.09			
Element	Weight%	Atomic%	Formula				
O K	57.13	69.78					
F K	10.23	10.29	1.08				
KK	19.52	9.46	1				
P K	15.28	10.47	1.11				
Totals	100.00						

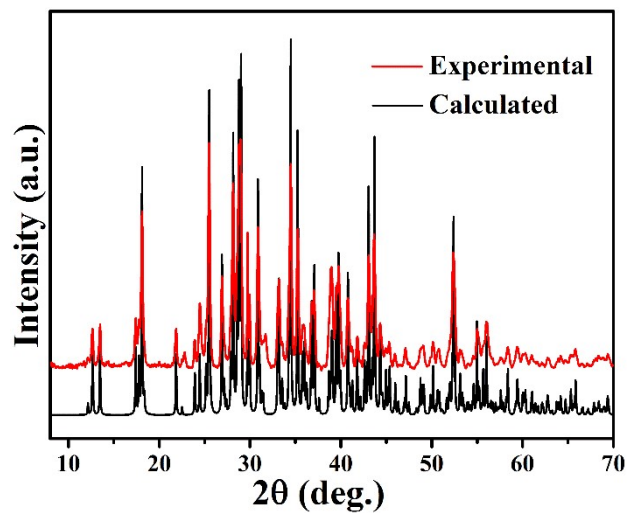


(a)

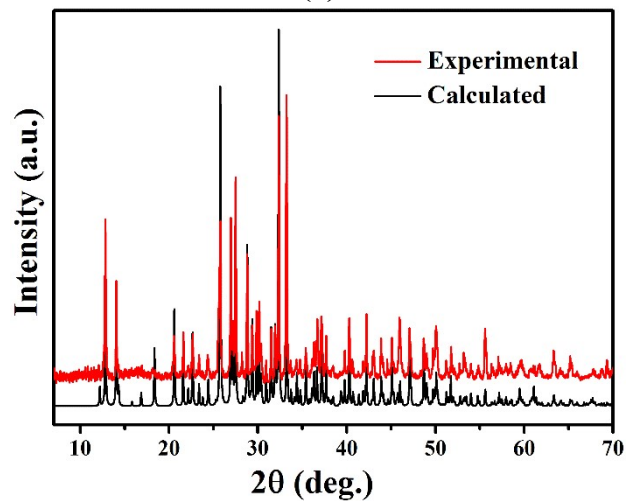


(b)

Figure S1. Photos of the crystals (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$.

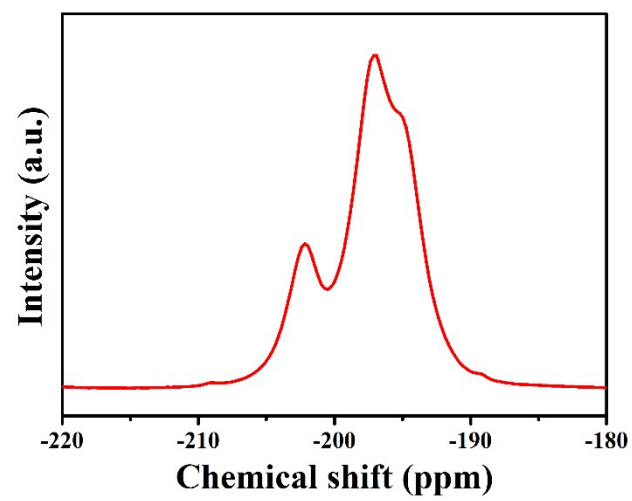


(a)

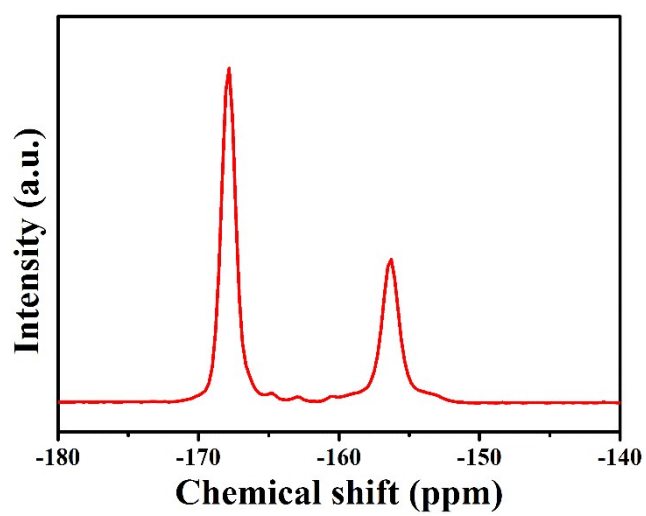


(b)

Figure S2. Powder XRD patterns for (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$.

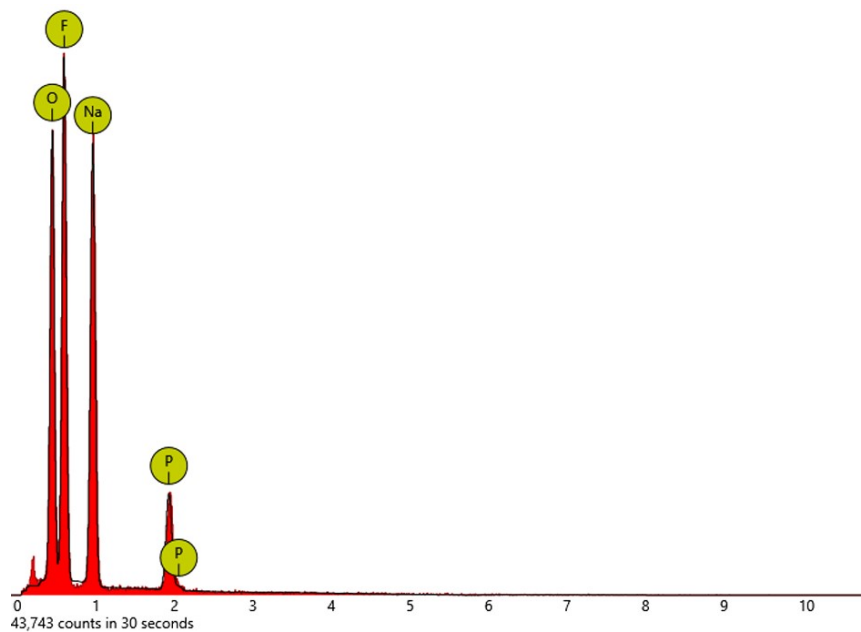


(a)

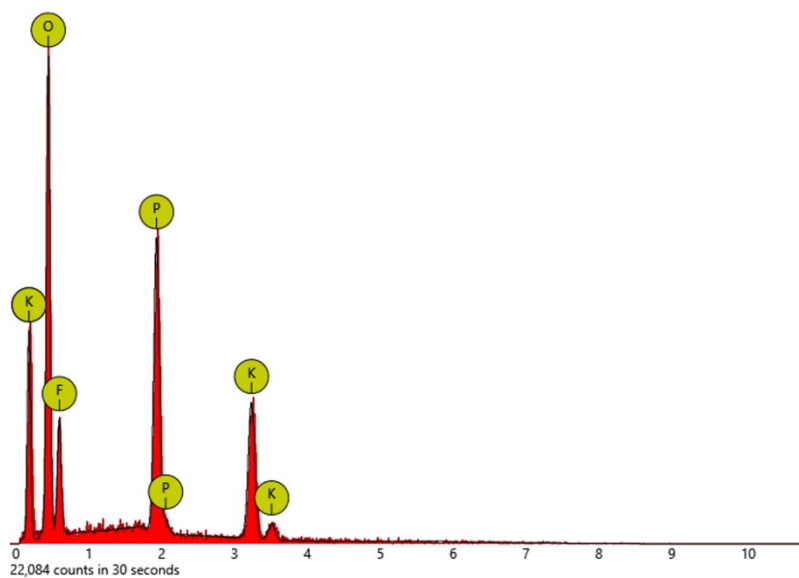


(b)

Figure S3. ^{19}F MAS NMR spectra of (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$.

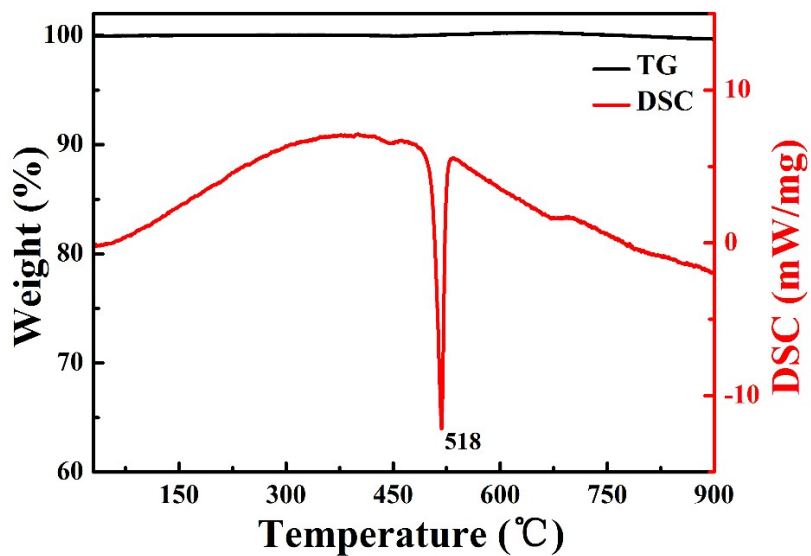


(a)

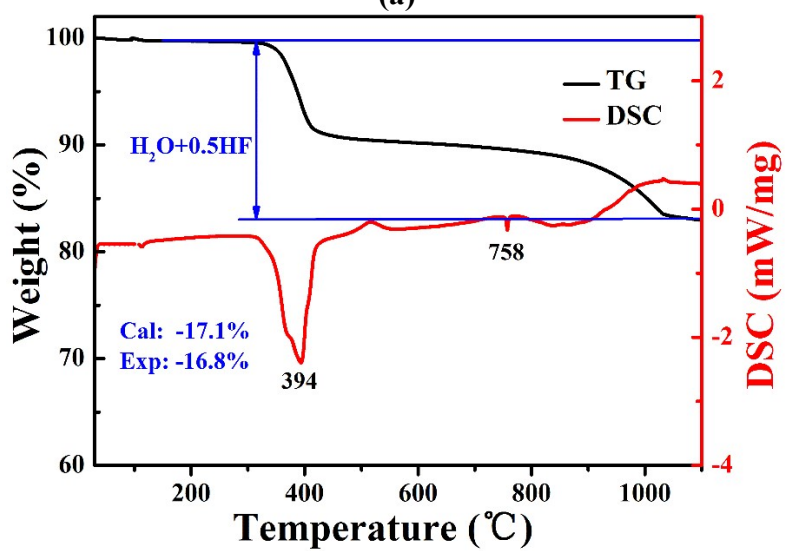


(b)

Figure S4. Energy-Dispersive Spectrometry (EDS) for (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$.

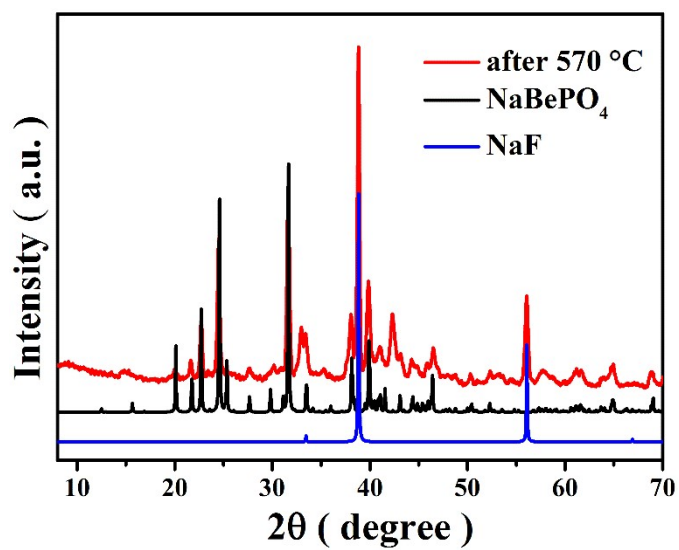


(a)

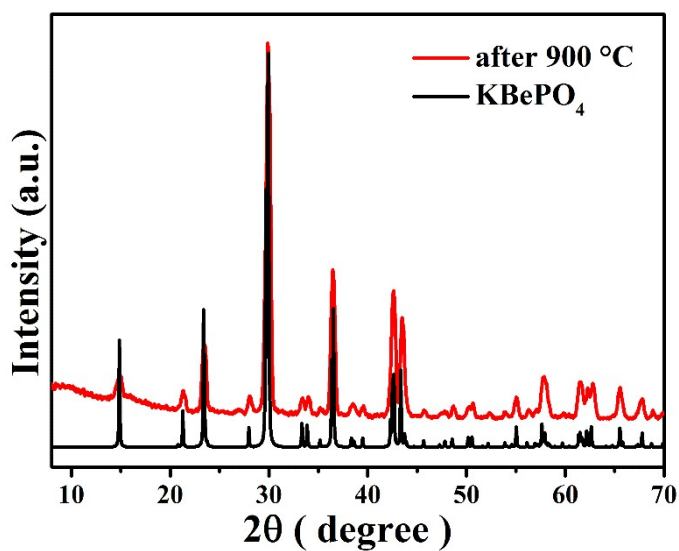


(b)

Figure S5. TG and DSC curves for (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$.

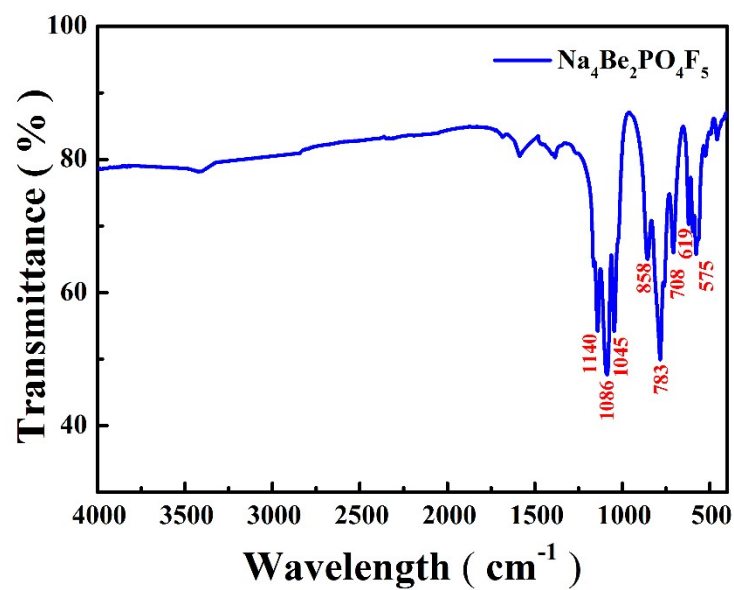


(a)

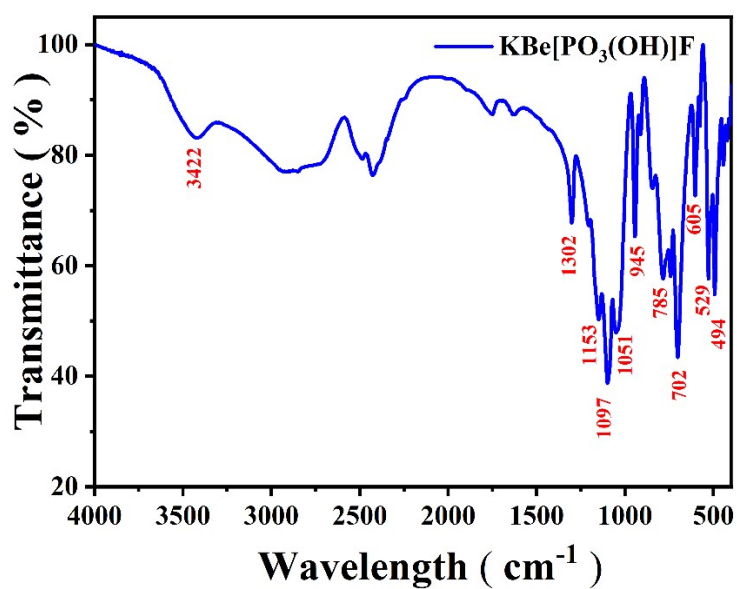


(b)

Figure S6. XRD patterns for (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ after 570 °C and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$ after 900 °C.

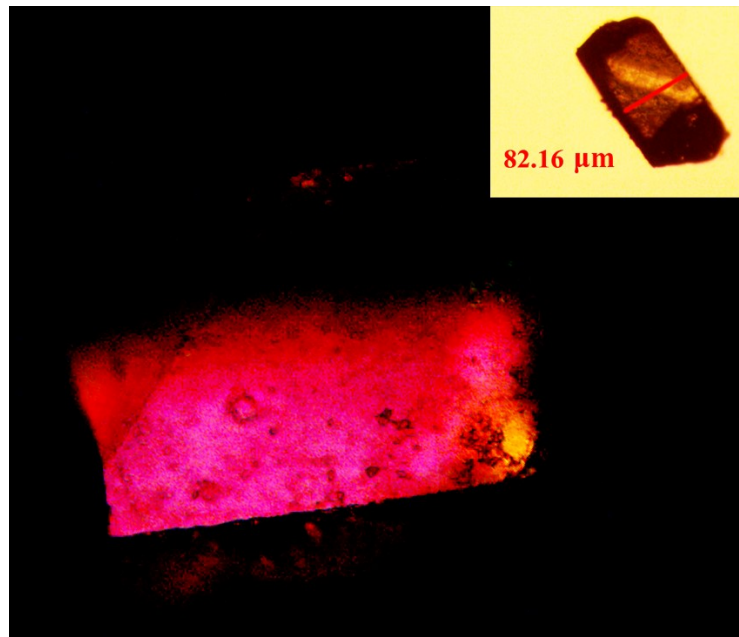


(a)

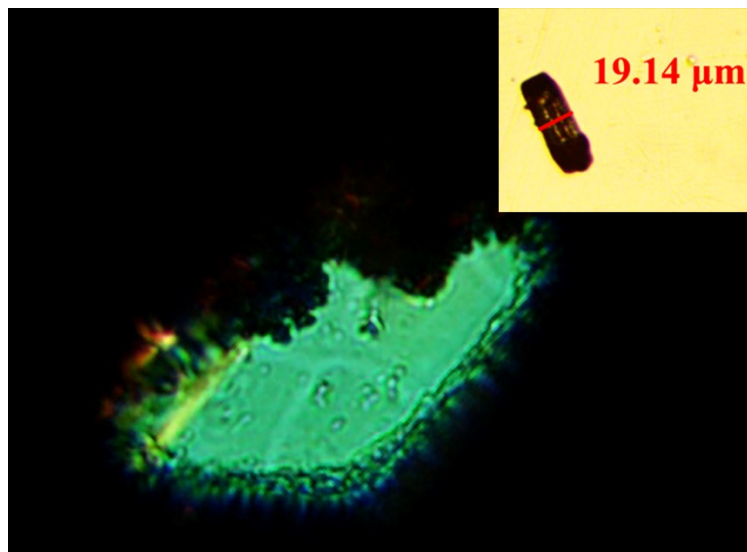


(b)

Figure S7. IR spectra of (a) $\text{Na}_4\text{Be}_2\text{PO}_4\text{F}_5$ and (b) $\text{KBe}[\text{PO}_3(\text{OH})]\text{F}$.



(a)



(b)

Figure S8. Birefringence measurements of Na₄Be₂PO₄F₅ (a) and KBe[PO₃(OH)]F(b) crystal under a cross-polarizing microscope. Na₄Be₂PO₄F₅ and KBe[PO₃(OH)]F have the thicknesses of 82.16 and 19.14 μm, respectively. Optical path differences of two tested crystal are about 540 and 710 nm, with the first-order pink and second-order green, respectively, according to Michal–Levy diagram.