

## Supporting Information

### Direct Tuning of Large-Gap Quantum Spin Hall Effect in Mono-Transition Metal Carbide MXenes

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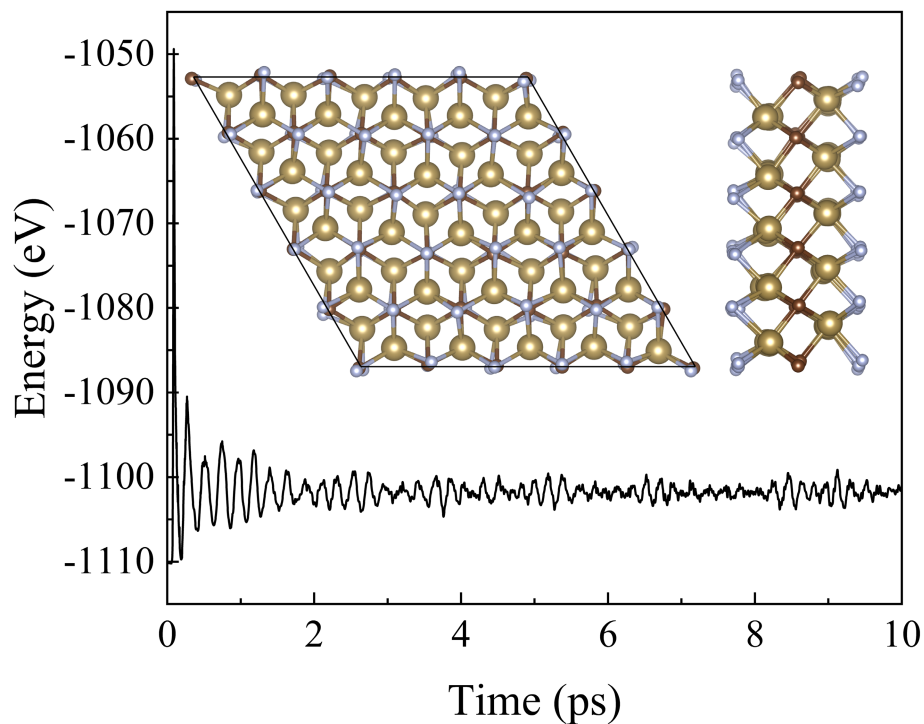
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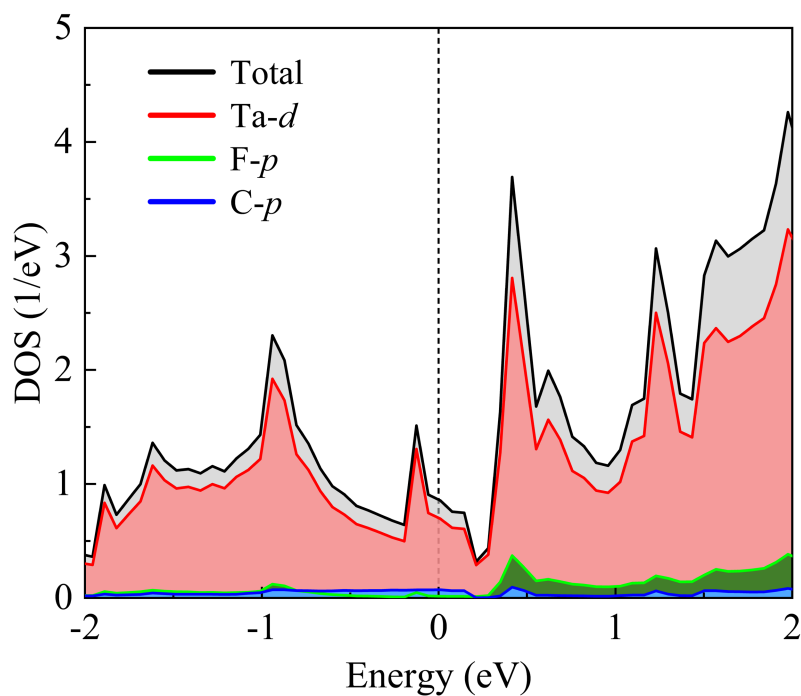
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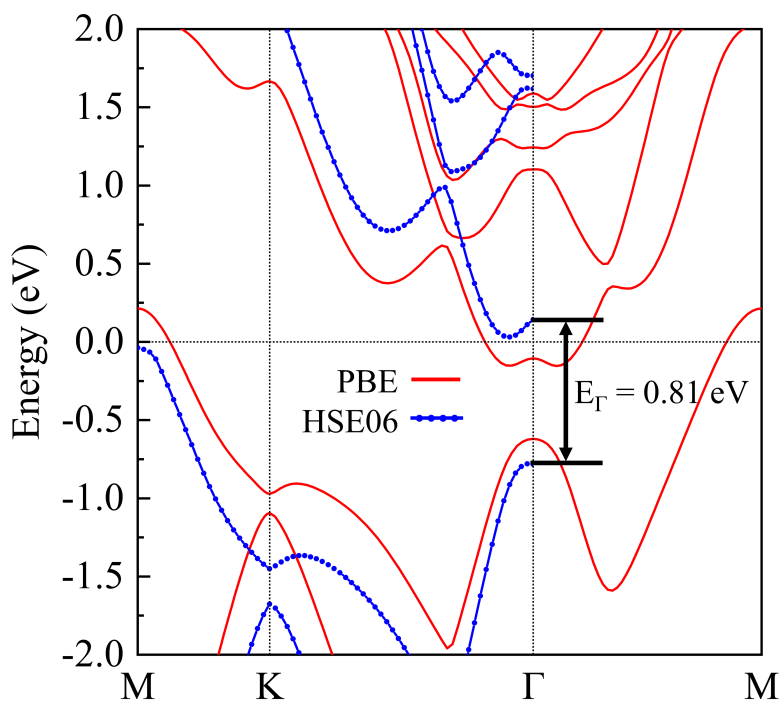
Supporting information consists of 5 Figures (Figure S1-S7) and 2 Tables (Table S1-S2).



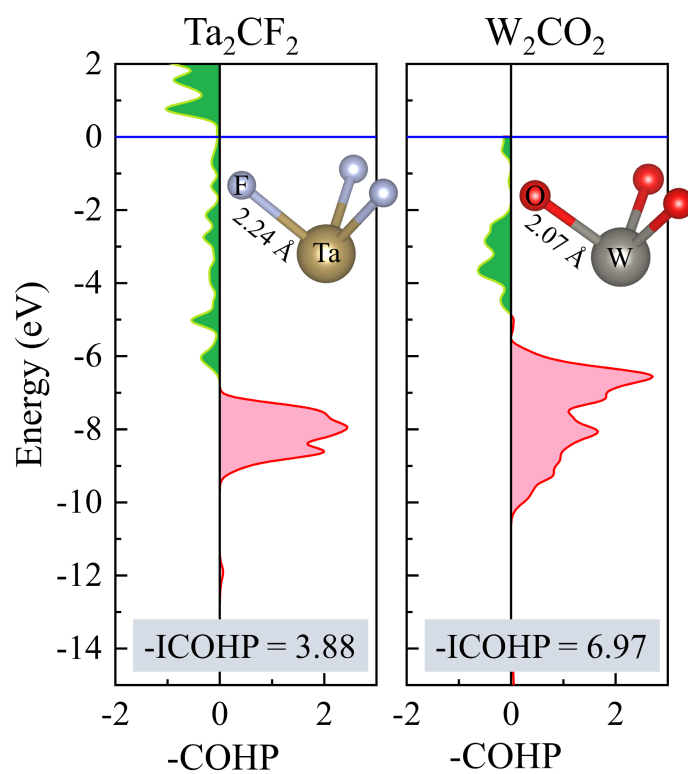
**Figure S1.** Fluctuations of total energies of Ta<sub>2</sub>CF<sub>2</sub> monolayer and a snapshot of the equilibrium structure at the end of 10 ps MD simulations at the temperature of 500 K.



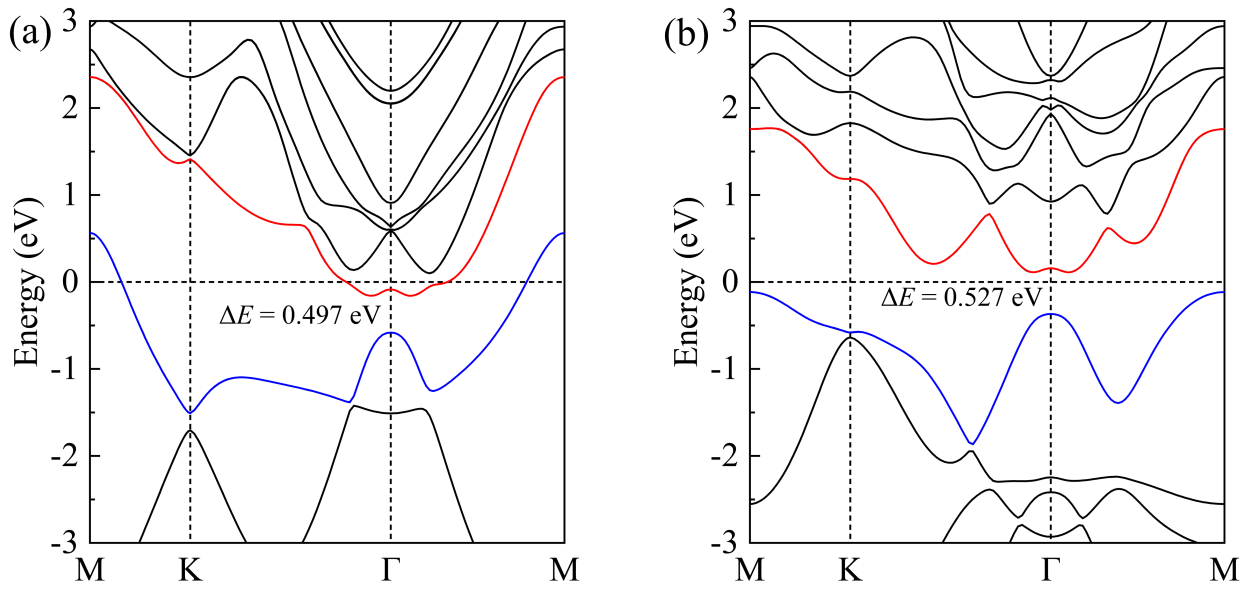
**Figure S2.** The projected partial densities of states (PDOS) of atoms orbitals with SOC by using the PBE functionals.



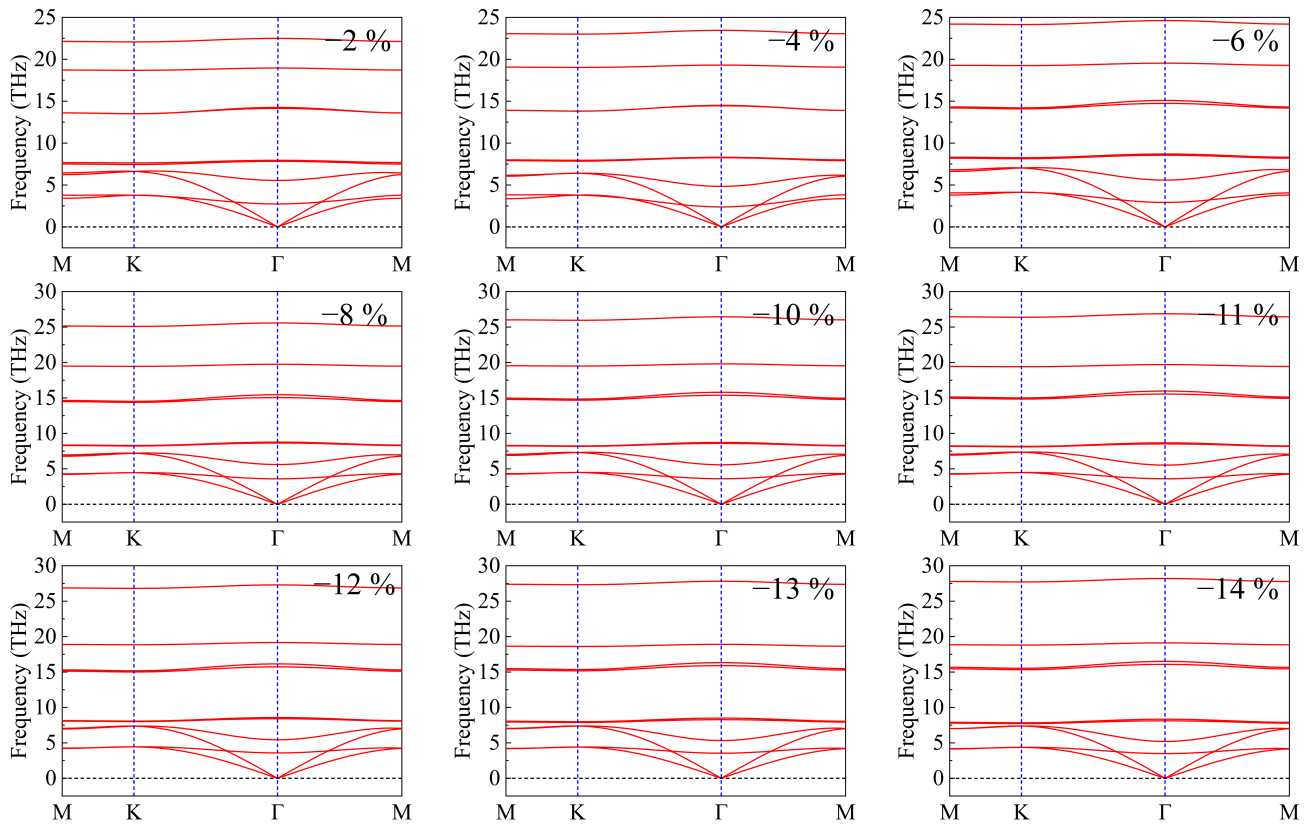
**Figure S3.** Band structure for Ta<sub>2</sub>CF<sub>2</sub> monolayer calculated with SOC by using the PBE (red lines) and HSE06 (blue lines) functionals.



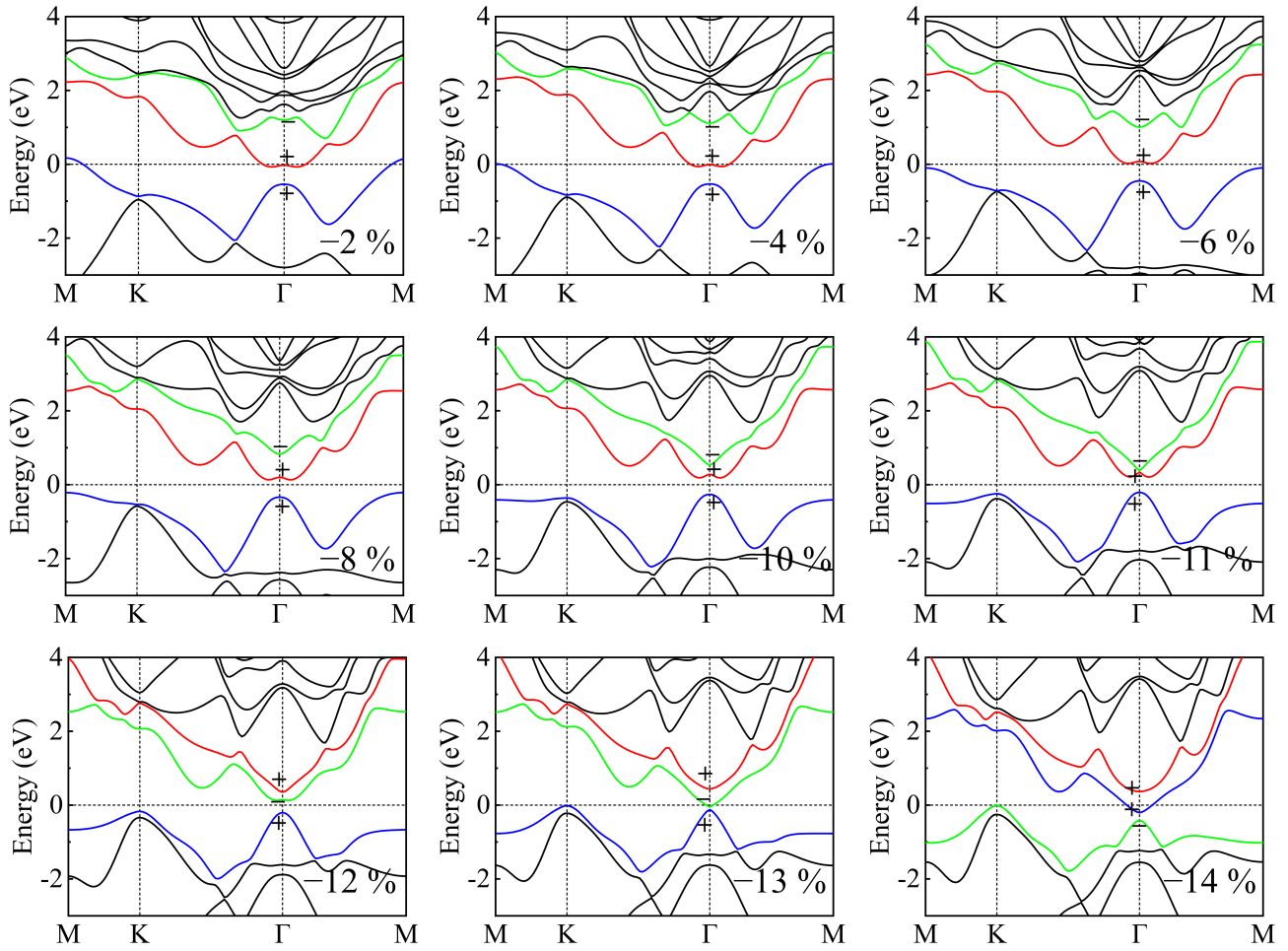
**Figure S4.** The -COHP and -ICOHP values for chemical bonds in the Ta<sub>2</sub>CF<sub>2</sub> and W<sub>2</sub>CO<sub>2</sub> monolayer. The pink color corresponds to bonding states, and green color corresponds to antibonding states.



**Figure S5.** The electronic band structures of Ta<sub>2</sub>CF<sub>2</sub> monolayer under the thickness ( $\Delta h$ ) of 4.79 Å (a) and 6.39 Å (b) between F and F atoms, respectively.



**Figure S6.** The phonon spectrum of Ta<sub>2</sub>CF<sub>2</sub> monolayer under different hydrostatic strains (the compressing of the lattice from 2% to 14%).



**Figure S7.** The electronic band structures of  $\text{Ta}_2\text{CF}_2$  monolayer under different hydrostatic strains by using the PBE functionals (the compressing of the lattice from 2% to 14%), the evolution for the relative parameters is shown in Table S2. Parities of the Bloch states at the  $\Gamma$ -point are denoted by +, -.

**Table S1.** In different GGA+ $U$  studies, the nontrivial gaps at the  $\Gamma$ -point ( $E_{\Gamma}$ ) under the thickness ( $\Delta h$ ) of 4.79 Å, 5.59 Å and 6.39 Å, respectively.

$\Delta h$	$U = 0$	$U = 1$	$U = 2$
4.79 Å	0.497 eV	0.533 eV	0.573 eV
5.59 Å	0.515 eV	0.564 eV	0.631 eV
6.39 Å	0.527 eV	0.597 eV	0.687 eV

**Table S2.** Lattice parameters ( $a$ ), thickness of F and F atoms ( $\Delta h$ ), nontrivial gaps at the  $\Gamma$ -point ( $E_{\Gamma}$ ), and  $\mathbb{Z}_2$  topological invariants for the Ta<sub>2</sub>CF<sub>2</sub> monolayer under different hydrostatic strains. The values of  $E_{\Gamma}$  calculated using the PBE functional.

Strains (%)	$a$ (Å)	$\Delta h$ (Å)	$E_{\Gamma}$ (eV)	$\mathbb{Z}_2$
0	2.97	5.59	0.515	1
-2	2.91	5.66	0.518	1
-4	2.85	5.74	0.523	1
-6	2.79	5.83	0.528	1
-8	2.73	5.92	0.536	1
-10	2.68	6.02	0.546	1
-11	2.65	6.07	0.551	1
-12	2.62	6.12	0.353	1
-13	2.59	6.18	0.074	1
-14	2.56	6.24	0.211	0