

Supplementary Information

Inverse CO₂/C₂H₂ Separation Assisted by Coordinated Water in a Dysprosium (III) Metal–Organic Frameworks

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Materials and Methods

1.1 Generals

All chemicals and solvents used were commercially available and used without further purifications. Powder X-ray diffraction (PXRD) data were collected with a Rigaku-Miniflex-600 X-ray powder diffractometer or a Rigaku SmartLab using Cu K α radiation ($\lambda = 1.5406 \text{ \AA}$ nm). Field emission scanning electron microscope (FE-SEM) experiments were characterized by FEI Verios G4 SEM. Thermogravimetric analysis (TGA) was carried out in a flow of nitrogen using a TGA-2 (METTLER TOLEDO) with a heating rate of 10 °C/min.

1.2 Preparation of Dy-F-oxa

The powder sample of **Dy-F-oxa** were prepared according to the literature report with some modifications^{1,2}. To a 100 mL Teflon vial, 20 mL Dy(NO₃)₃·6H₂O (0.02 M), 20 mL NaF (0.02 M) and 20 mL Na₂C₂O₄ (0.02 M) aqueous solutions were added and heated to *ca.* 60 °C under stirring. The precipitate was collected by filtration and washed with distilled water. Yield (based on Dy): 90.5%.

1.3 Gas adsorption

A Micromeritics 3Flex instrument was used for recording all gas sorption isotherms, CO₂ (195, 273 and 298 K) and C₂H₂ (273 and 298 K). For N₂ adsorption isotherms, the temperature was controlled at 77 K using a Dewar containing 4 L liquid N₂. Precise control of 273 K and 298 K temperatures was implemented by a dc-2006 from Ningbo Scientz Biotechnology, which contained a cyclic control system of ethylene glycol and water mixture (*v/v* = 1:1). Helium was used for the estimation of dead space for gas and water adsorption measurements. The activation of the **Dy-F-oxa** sample was achieved by degassing for 4 h at 80 °C under a dynamical vacuum using a degassing station.

1.4 Isotheric heat of adsorption

A virial-type expression of the below form was used to fit the combined isotherm data of CO₂ and C₂H₂ at 273 and 298 K, where P is the pressure described in Pa, N is the adsorbed amount in mmol/g, T is the temperature in K, a_i and b_i are virial coefficients, and m and n are the number of coefficients used to describe the isotherms. Q_{st} is the coverage-dependent enthalpy of adsorption and R is the universal gas constant

$$\ln P = \ln N + \frac{1}{T} \sum_{i=0}^m a_i N^i + \sum_{j=0}^n b_j N^j$$

$$Q_{st} = -R \sum_{i=0}^5 a_i N^i$$

1.5 Langmuir-Freundlich fitting

The isothermal for different gases at 298 K were fitted using the Langmuir-Freundlich model as following:

$$q = q_{sat} \frac{b_A p^n}{1 + b_A p^n}$$

where q and q_{sat} are gas loading at a specific pressure and saturation respectively, b_A is Langmuir-Freundlich constant at A site, n is Freundlich exponent and p is pressure.

1.6 IAST calculations of adsorption selectivity

The selectivity of equimolar CO₂/C₂H₂ binary mixtures at 298 K was calculated using ideal adsorption solution theory (IAST) method³, and the selectivity is defined as following:

$$S = \frac{x_A/x_B}{y_A/y_B}$$

where S is the selectivity of A towards B, x_A and x_B are the molar fractions of A and B in the adsorbent respectively, y_A and y_B are the molar fractions of A and B in the gas mixture respectively.

1.7 Computational details

To understand the host-guest interactions between the framework and CO₂ and C₂H₂ molecules, the Grand Canonical Monte Carlo (GCMC) simulations were performed using the Sorption module in Material Studio software package. The simulation box for **Dy-F-oxa** was built from the single-crystal

structure with $1 \times 1 \times 1$ supercell after making *P1* and the CIF files were adapted from Cambridge Crystallographic Data Centre (CCDC) for free. All the frameworks and gas molecules were both treated as rigid bodies and the Q_{eq} fitted charge and the ESP charge were assigned to the hosts and guests respectively. The loading steps, equilibration steps, and production steps were all set to 2.0×10^7 . The Metropolis method was applied during the simulation⁴. All the host-guest interaction behavior was described using Universal force field (UFF⁵). The cut-off radius used for the Lennard–Jones interactions is 18.5 Å.

1.8 Breakthrough experiments

The breakthrough curves were recorded on a homemade apparatus. Activated **Dy-F-oxa** 3.2g particles were prepared and packed into a stainless-steel column. An equimolar gas mixture of CO₂ and C₂H₂ (total gas pressure and flow: 100 kPa and 1 cm³/min) passes through the packing column at 298 K, and the outlet gas concentration was monitored by a gas chromatography analyzer (TCD-Thermal Conductivity Detector, detection limit 0.1 ppm). During gas breakthrough cycling tests, the sample in the column was regenerated under He flow of 20 cm³/min at 80 °C for 8 hours, after each breakthrough experiment.

Productivity of C₂H₂ is derived from breakthrough experiments following this definition:

$$p = \frac{F \times y_{\text{C}_2\text{H}_2} \times \int_{t_1}^{t_2} \frac{C(t)}{C_0} dt}{V_m}$$

where P is the C₂H₂ productivity in mmol/g, t_1 is the C₂H₂ breakthrough time in min/g, t_2 is the breakthrough time of other gas, F is the inlet gas volume flow rate, $y_{\text{C}_2\text{H}_2}$ is the volume fraction of C₂H₂ in mixed gas, $C(t)$ is the C₂H₂ concentration in the outlet gas, C_0 is the C₂H₂ concentration in the inlet gas, V_m is molar volume of gas.

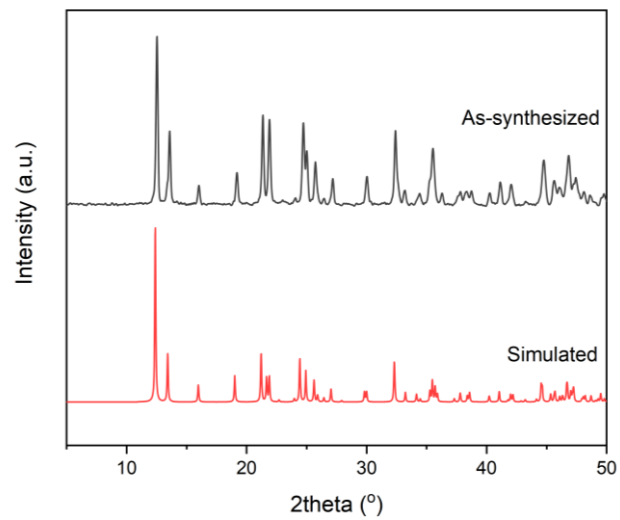


Fig. S1 As-synthesized (black) and simulated (red) PXRD patterns of **Dy-F-oxa**.

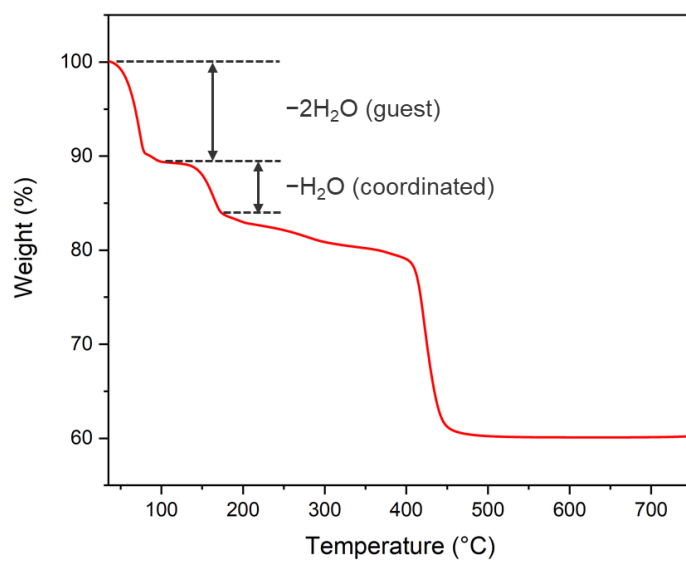


Fig. S2 TGA curve of **Dy-F-oxa**.

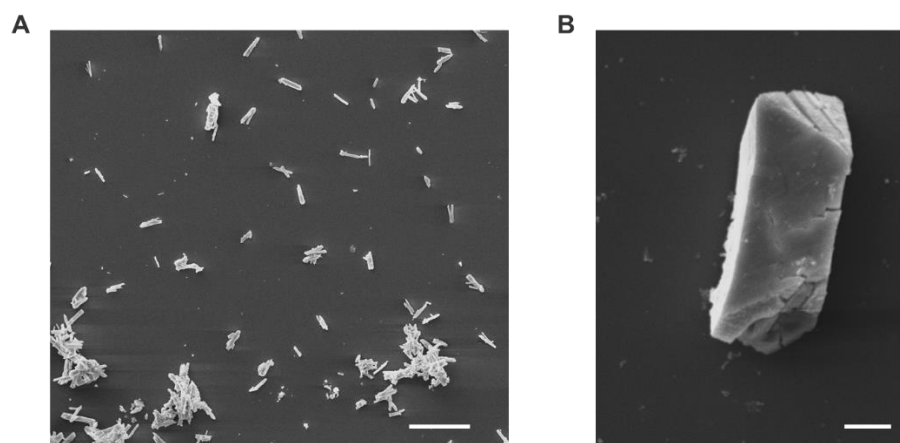


Fig. S3. The FESEM images of **Dy-F-oxa** samples. Scale bars on the image (A) and (B) are 10 and 2 μm , respectively.

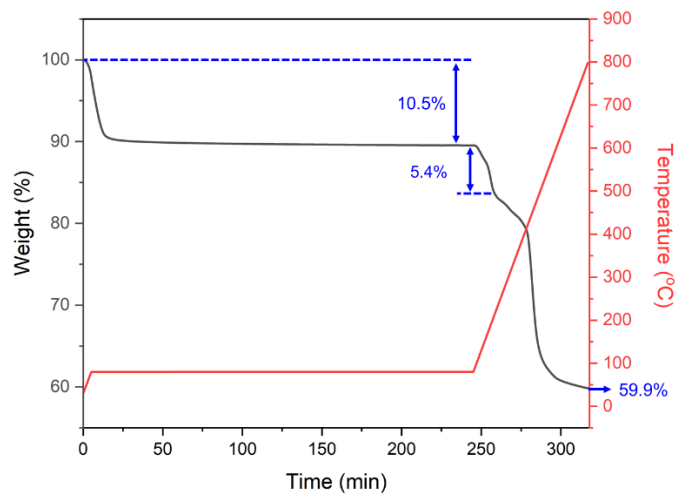


Fig. S4 TGA curve of activated **Dy-F-oxa**. With the heating rate of 10 °C/min, the sample was heated to 80 °C and keep this temperature for 4 hours. Then the activated sample was heated to 800 °C.

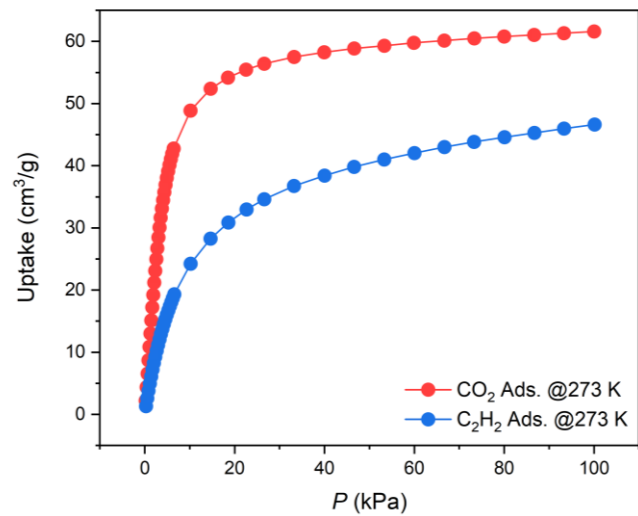


Fig. S5 CO₂ and C₂H₂ adsorption isotherms at 273 K of **Dy-F-oxa**.

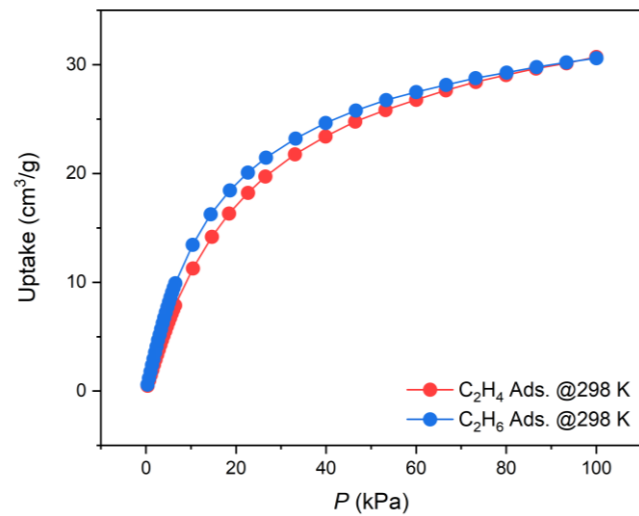
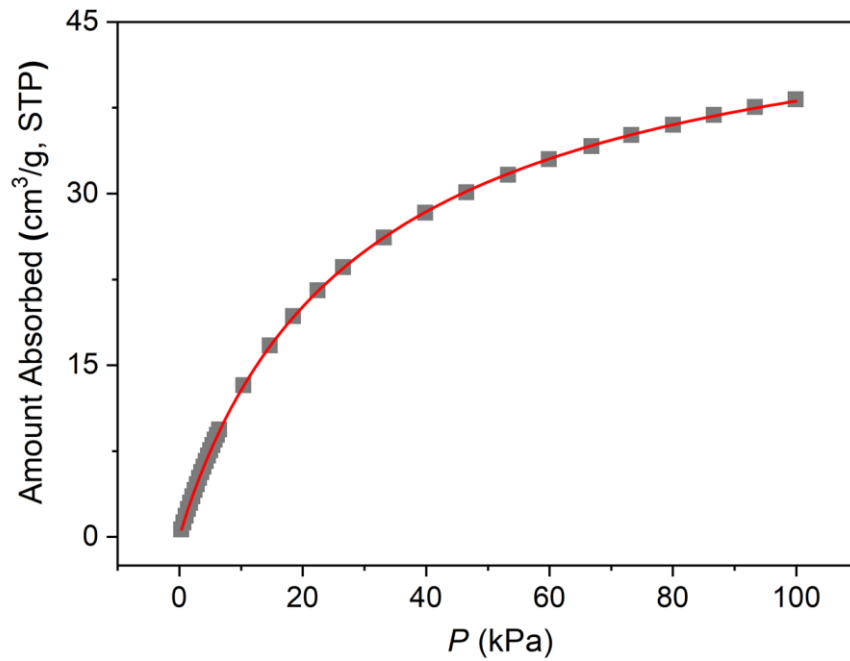
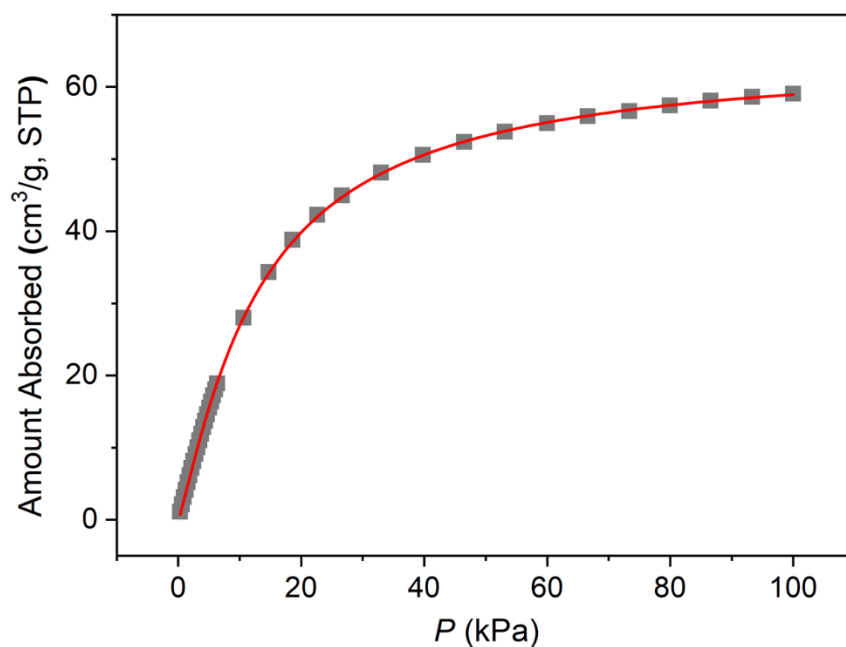


Fig. S6 C₂H₄ and C₂H₆ adsorption isotherms at 298 K of **Dy-F-oxa**.



Equation	$A1 \cdot B1 \cdot x^{C1} / (1 + B1 \cdot x^{C1})$	
Reduced Chi-Sqr	0.00395	
Adj. R-Square	0.99998	
	Value	Standard Error
A1 (q_{sat})	50.07238	0.16576
B1 (b_A)	0.03721	1.64328E-4
C1 (n)	0.96589	0.00297

Fig. S7 The Langmuir-Freundlich fitting details of C_2H_2 adsorption isotherm at 298 K for **Dy-F-oxa** and the solid lines are the best fit for the data.



Equation	$A1 \cdot B1 \cdot x^{C1} / (1 + B1 \cdot x^{C1})$	
Reduced Chi-Sqr	0.03952	
Adj. R-Square	0.99991	
	Value	Standard Error
A1 (q_{sat})	64.42253	0.18893
B1 (b_A)	0.04785	4.83903E-4
C1 (n)	1.17589	0.00635

Fig. S8 The Langmuir-Freundlich fitting details of CO₂ adsorption isotherm at 298 K for **Dy-F-oxa** and the solid lines are the best fit for the data.

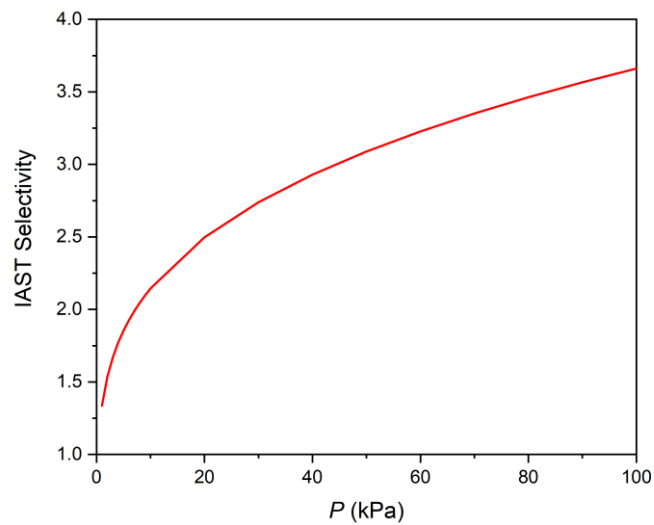


Fig. S9 Calculated IAST selectivity of **Dy-F-oxa** for CO₂/C₂H₂ with 1:1 ratio at 298 K.

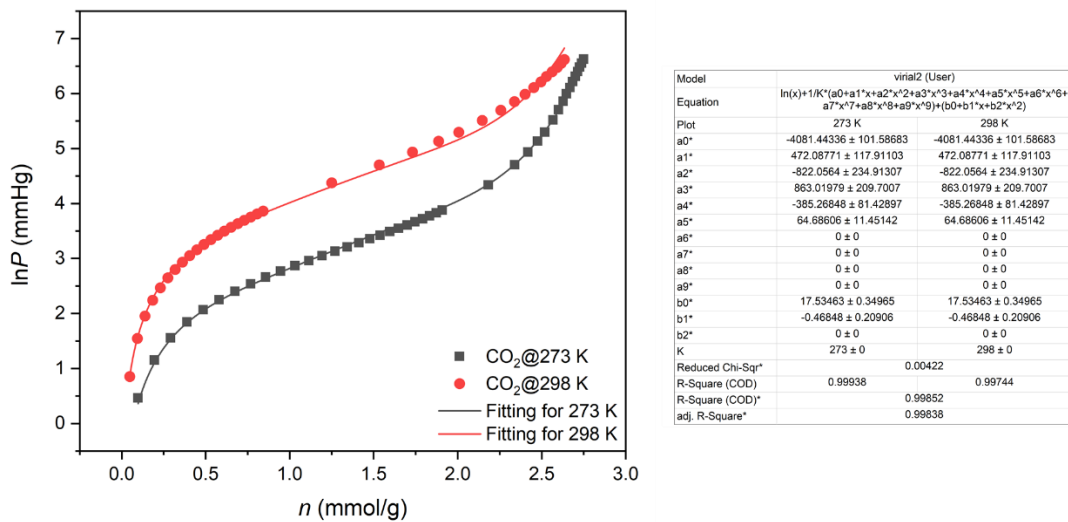
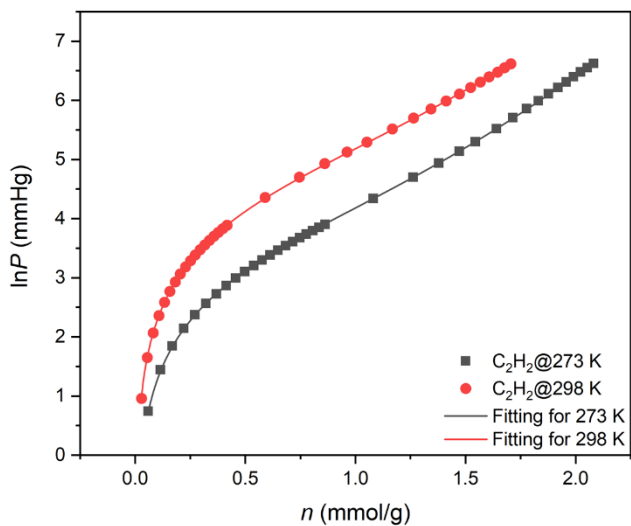


Fig. S10 Virial equation (lines) fitting of the experimental CO₂ adsorption data (symbols) for **Dy-F-oxa**.



Model	virial2 (User)	
Equation	$\ln(x)+1/K(a_0+a_1x+a_2x^2+a_3x^3+a_4x^4+a_5x^5+a_6x^6+a_7x^7+a_8x^8+a_9x^9)+(b_0+b_1x+b_2x^2)$	
Plot	273 K	298 K
a0*	-3290.05916 ± 15.56158	-3290.05916 ± 15.56158
a1*	24.51663 ± 26.68188	24.51663 ± 26.68188
a2*	-60.66684 ± 59.67348	-60.66684 ± 59.67348
a3*	66.74638 ± 74.01187	66.74638 ± 74.01187
a4*	7.04742 ± 39.68621	7.04742 ± 39.68621
a5*	-4.67162 ± 7.62763	-4.67162 ± 7.62763
a6*	0 ± 0	0 ± 0
a7*	0 ± 0	0 ± 0
a8*	0 ± 0	0 ± 0
a9*	0 ± 0	0 ± 0
b0*	15.5606 ± 0.05296	15.5606 ± 0.05296
b1*	0.55093 ± 0.05493	0.55093 ± 0.05493
b2*	0 ± 0	0 ± 0
K	273 ± 0	298 ± 0
Reduced Chi-Sqr*		1.04496E-4
R-Square (COD)*	0.99997	0.99995
R-Square (COD)*		0.99996
adj. R-Square*		0.99996

Fig. S11 Virial equation (lines) fitting of the experimental C_2H_2 adsorption data (symbols) for **Dy-F-oxa**.

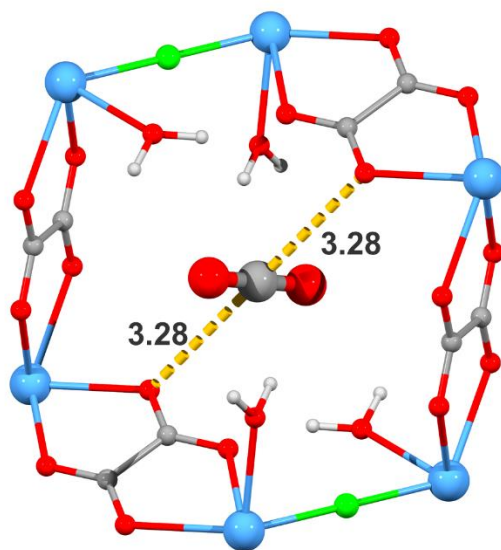


Fig. S12 Interactions between electropositive $C^{\delta+}$ atom of CO_2 and nearby O atoms of two carboxyl groups in **Dy-F-oxa**. Distances are given in Å.

References.

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