

Aromaticity in P₈ Allotropes and (CH)₈ Analogues: Significance of their 40 Valence Electrons?

Amr A. A. Attia,¹ Alvaro Muñoz-Castro,^{*2} Alexandru Lupan,^{*1} and R. Bruce King^{*3}

¹*Faculty of Chemistry and Chemical Engineering, Babeş-Bolyai University, Cluj-Napoca, Romania*

²*Laboratorio de Química Inorgánica y Materiales Moleculares, Facultad de Ingeniería, Universidad Autónoma de Chile, El Llano Subercaseaux 2801, Santiago, Chile*

³*Department of Chemistry, University of Georgia, Athens, Georgia, 30602, USA*

Supporting Information

Complete Gaussian09 Reference.

Table S1: Initial 8-vertex starting structures.

Table S2: Distance matrices and energy rankings for the lowest energy P₈ structures.

Table S3: Distance matrices and energy rankings for the lowest energy C₈H₈ structures.

Table S4: Orbital energies and HOMO-LUMO gaps for the lowest lying P₈ and C₈H₈ structures.

Table S5: QTAIM analysis for the lowest lying P₈ structures.

Table S6: Calculated molar magnetic susceptibility in cgs ppm units (10⁻⁶ cm³ mol⁻¹) for the lowest lying P₈ and C₈H₈ structures.

Figure S1: Correlation between the calculated χ_M and relative energy (kcal/mol) for the lowest lying P₈ and C₈H₈ structures.

Complete Gaussian09 Reference.

Gaussian 09, Revision E.01, M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, B. Mennucci, G. A. Petersson, H. Nakatsuji, M. Caricato, X. Li, H. P. Hratchian, A. F. Izmaylov, J. Bloino, G. Zheng, J. L. Sonnenberg, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, T. Vreven, J. A. Montgomery, Jr., J. E. Peralta, F. Ogliaro, M. Bearpark, J. J. Heyd, E. Brothers, K. N. Kudin, V. N. Staroverov, R. Kobayashi, J. Normand, K. Raghavachari, A. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, N. Rega, J. M. Millam, M. Klene, J. E. Knox, J. B. Cross, V. Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R. E. Stratmann, O. Yazyev, A. J. Austin, R. Cammi, C. Pomelli, J. W. Ochterski, R. L. Martin, K. Morokuma, V. G. Zakrzewski, G. A. Voth, P. Salvador, J. J. Dannenberg, S. Dapprich, A. D. Daniels, O. Farkas, J. B. Foresman, J. V. Ortiz, J. Cioslowski, and D. J. Fox, Gaussian, Inc., Wallingford CT, 2016.

Table S1: Initial 8-vertex polyhedra upon which the starting structures are based.

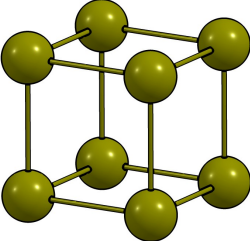
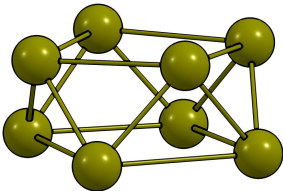
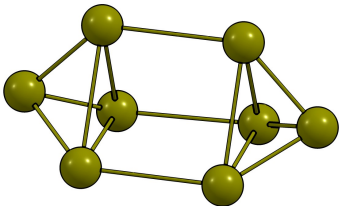
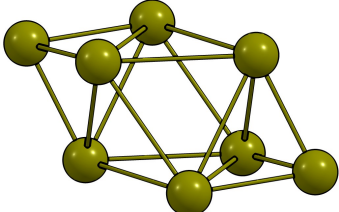
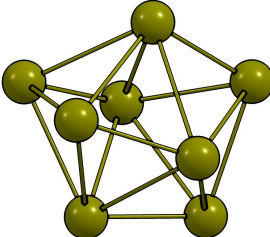
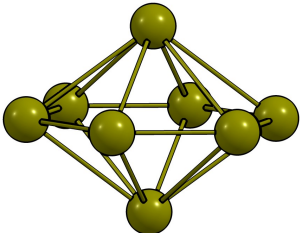
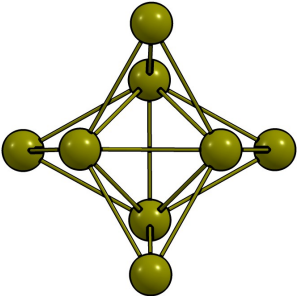
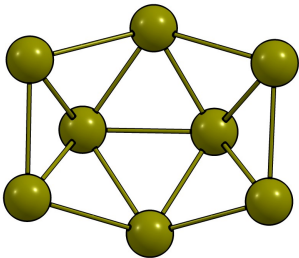
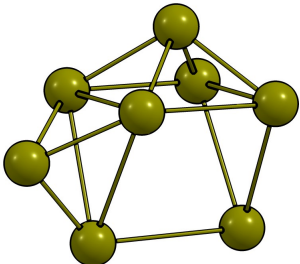
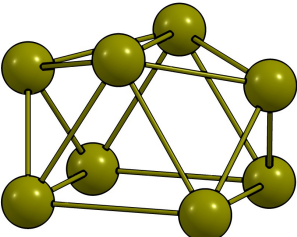
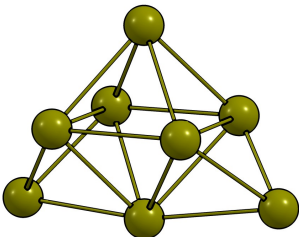
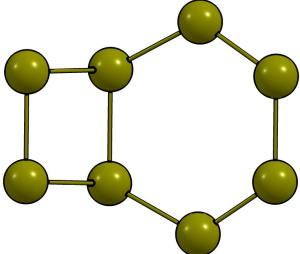
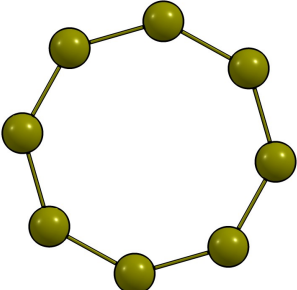
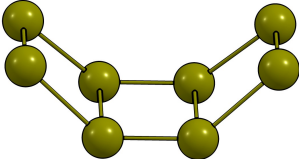
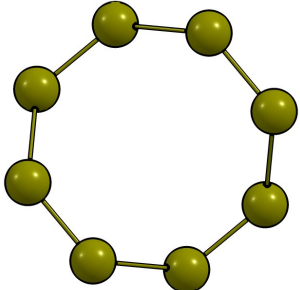
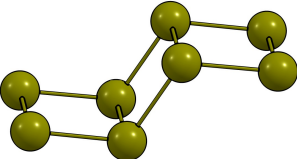
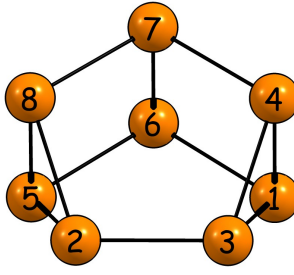
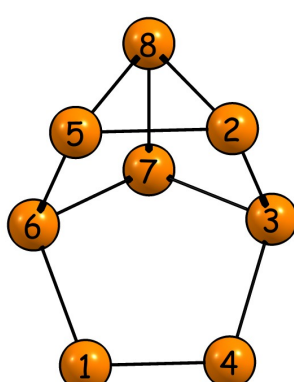
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 <p>4. Trigonal Antiprism</p>	 <p>5. Bisdisphenoid</p>	 <p>6. Hexagonal bipyramid</p>
 <p>7. All-capped tetrahedron</p>	 <p>8. Nido structure</p>	 <p>9. Diccapped trigonal prism (C_s)</p>
 <p>10. Diccapped trigonal prism (C_{2v})</p>	 <p>11. Diccapped octahedron</p>	 <p>12. Bicyclooctatriene</p>
 <p>13. Cyclooctatetraene (planar)</p>	 <p>14. <i>cis</i>-Tricyclooctadiene</p>	 <p>15. Cyclooctatetraene (non-planar)</p>
 <p>16. <i>trans</i>-Tricyclooctadiene</p>		

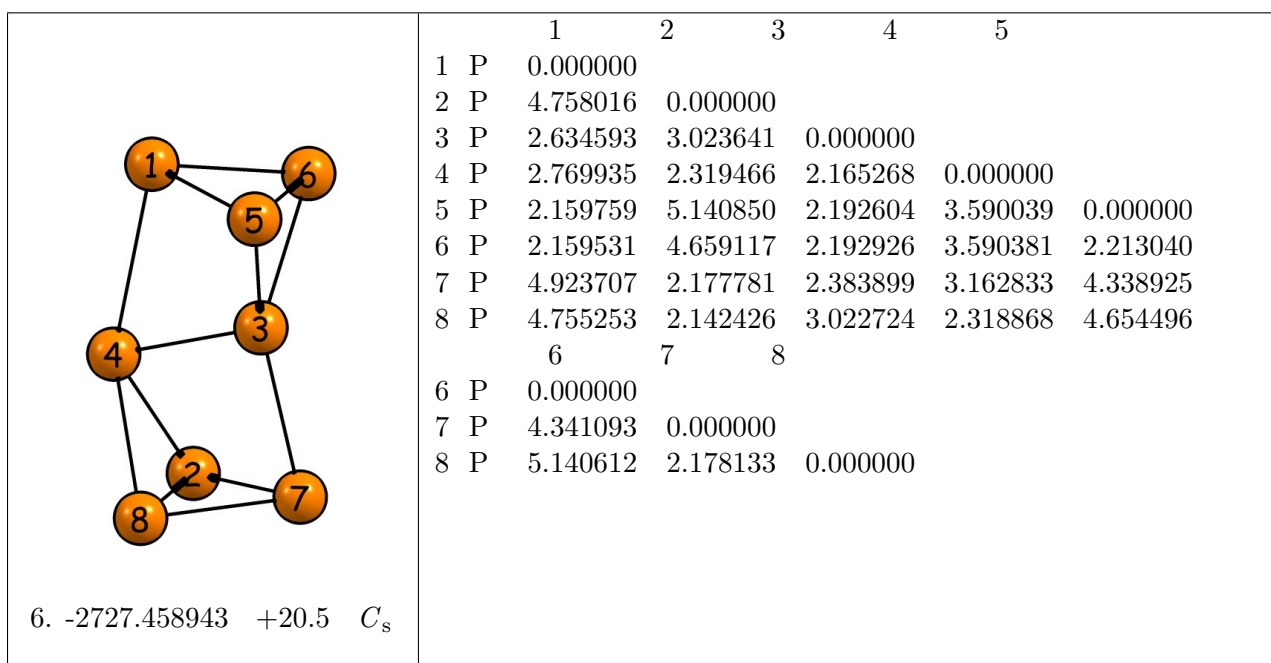
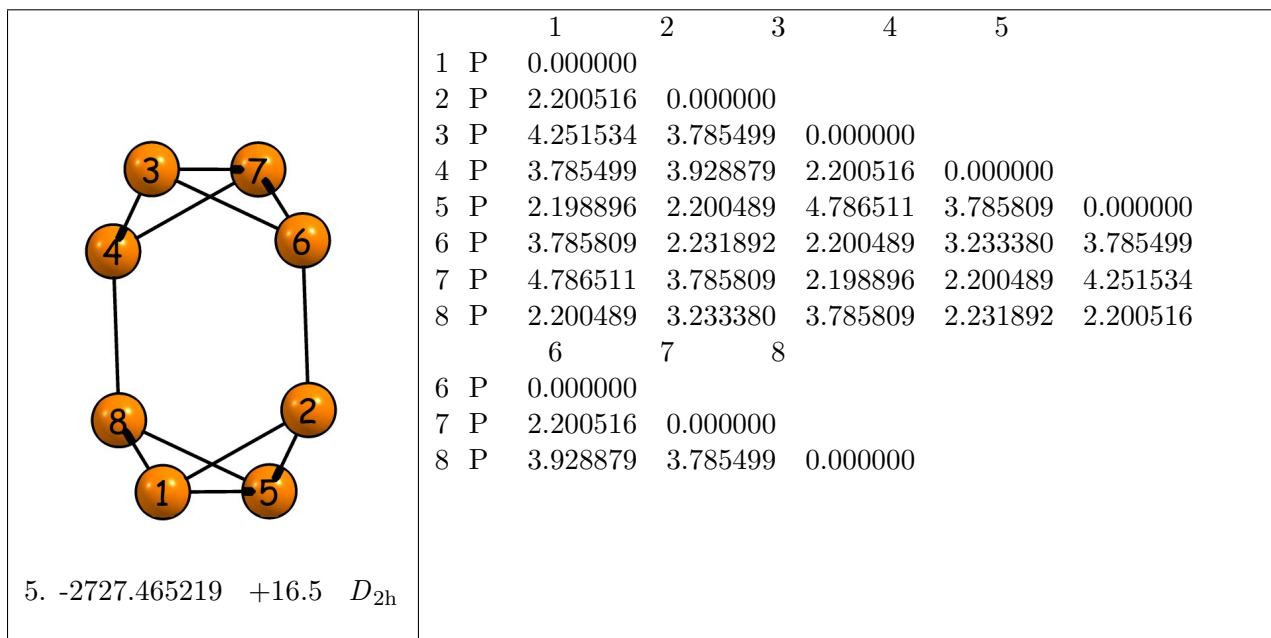
Table S2: Distance table for the lowest-lying P_8 optimized structures obtained at the M11/def2-TZVP level of theory. Included are the zero-point corrected absolute energy in (a.u.) at the DLPNO-CCSD(T)/def2-QZVP level of theory with zero-point energy obtained from the M11/def2-TZVP computations, relative energy in (kcal/mol) and symmetry.

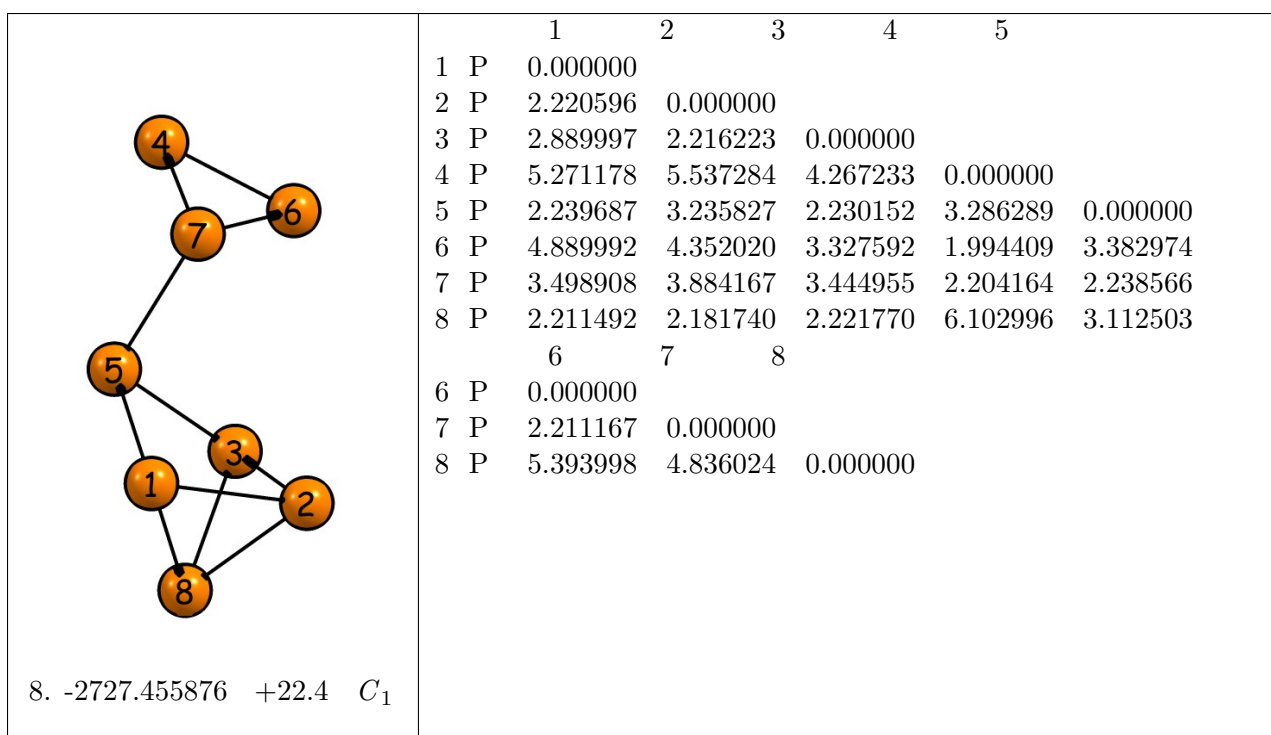
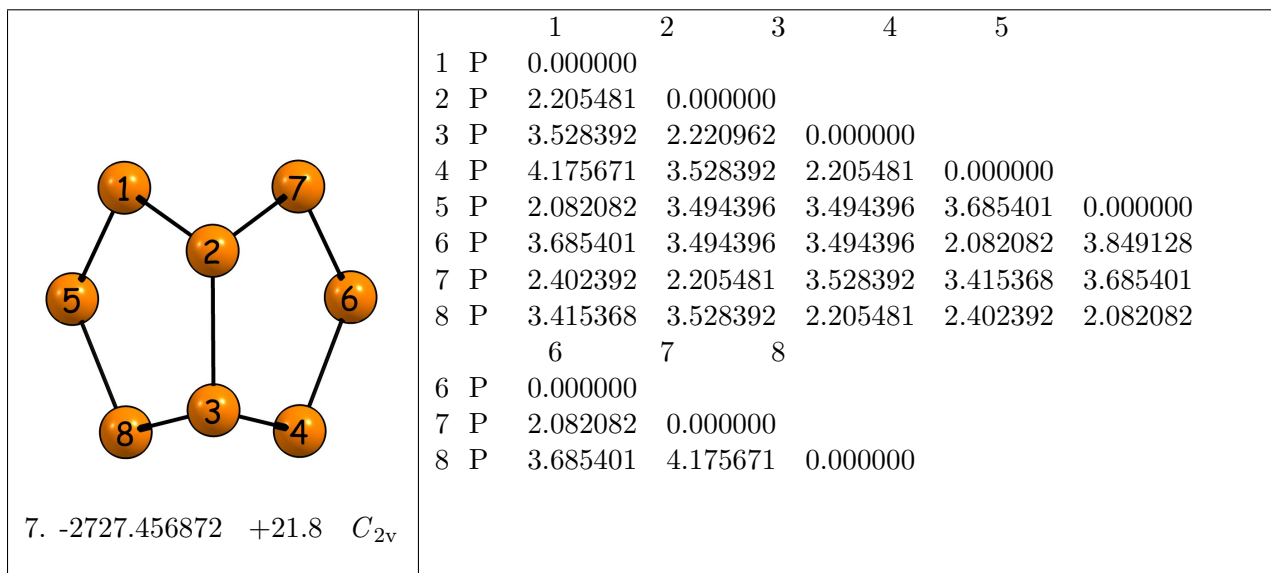
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	4 P	2.280445	3.548872	2.180495	0.000000	
	5 P	3.547119	2.180494	3.548862	4.216929	0.000000
	6 P	2.236614	3.466450	3.466445	3.164638	2.236612
	7 P	3.164660	3.466451	3.466447	2.236611	3.164649
	8 P	4.216933	2.180497	3.548865	3.547129	2.280440
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7 P	2.198067	0.000000				
8 P	3.164643	2.236608	0.000000			

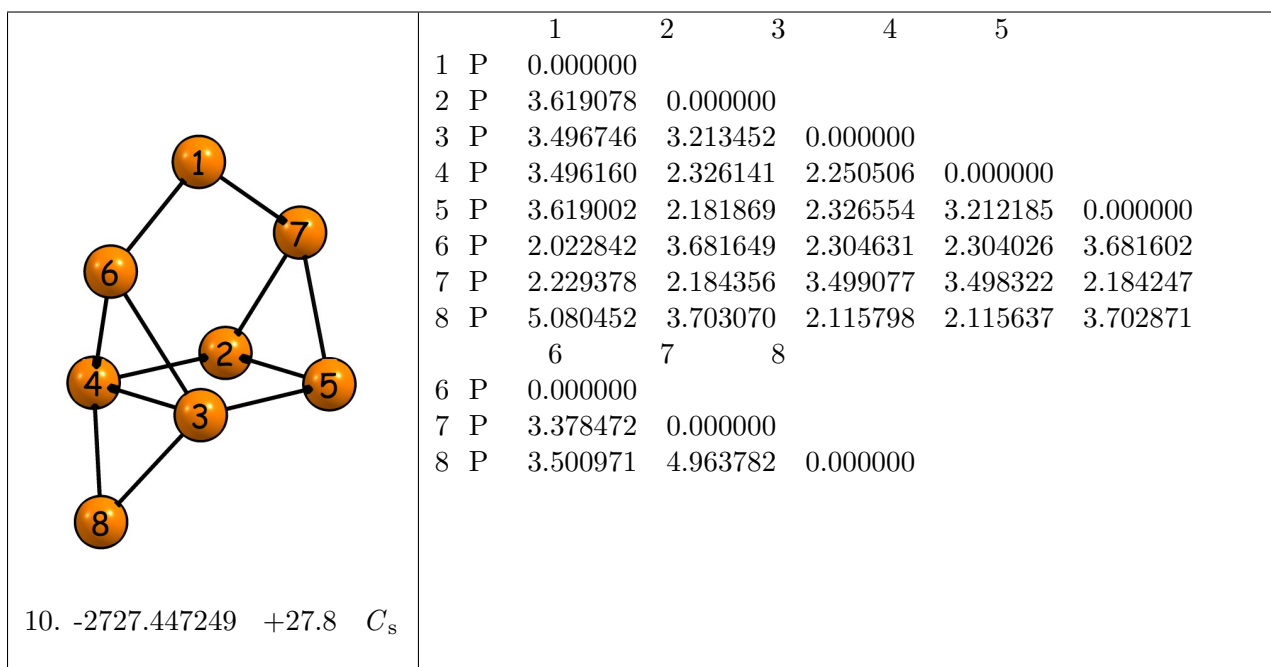
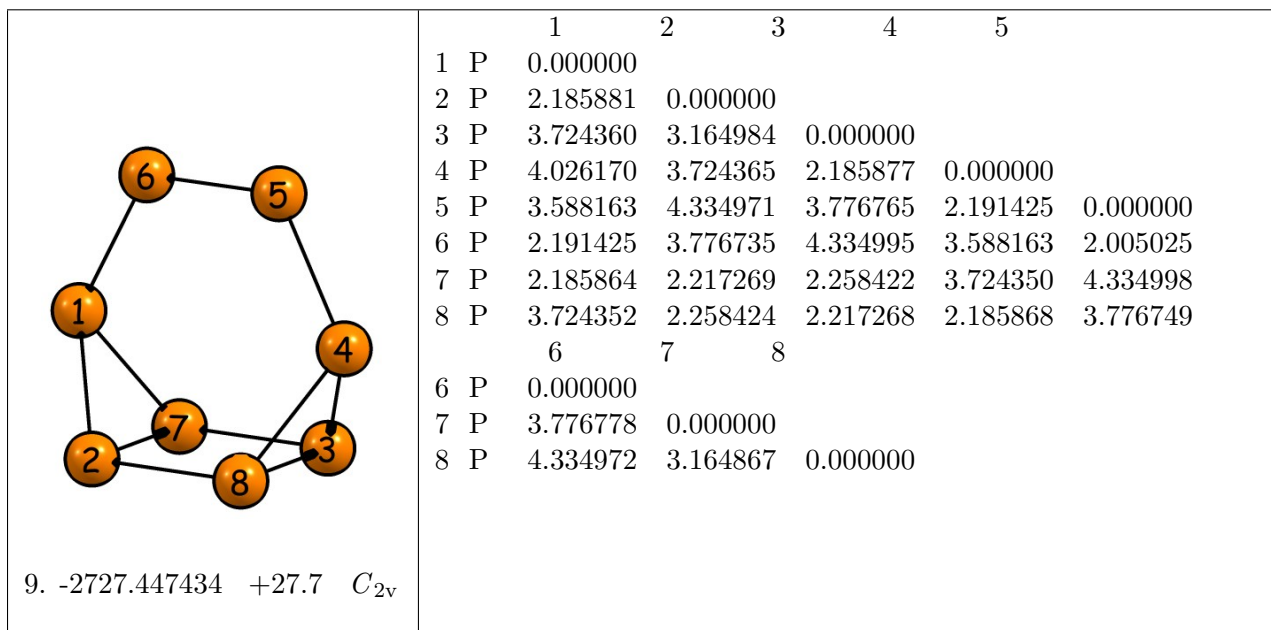
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	4 P	2.015391	3.410715	2.206398	0.000000	
	5 P	3.410707	2.187033	3.509487	4.004971	0.000000
	6 P	2.206376	3.509589	3.334449	3.404146	2.241505
	7 P	3.486326	3.218339	2.194622	3.486344	3.218334
	8 P	4.607047	2.224056	3.009563	4.607019	2.224064
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7 P	2.194625	0.000000				
8 P	3.009536	2.296244	0.000000			

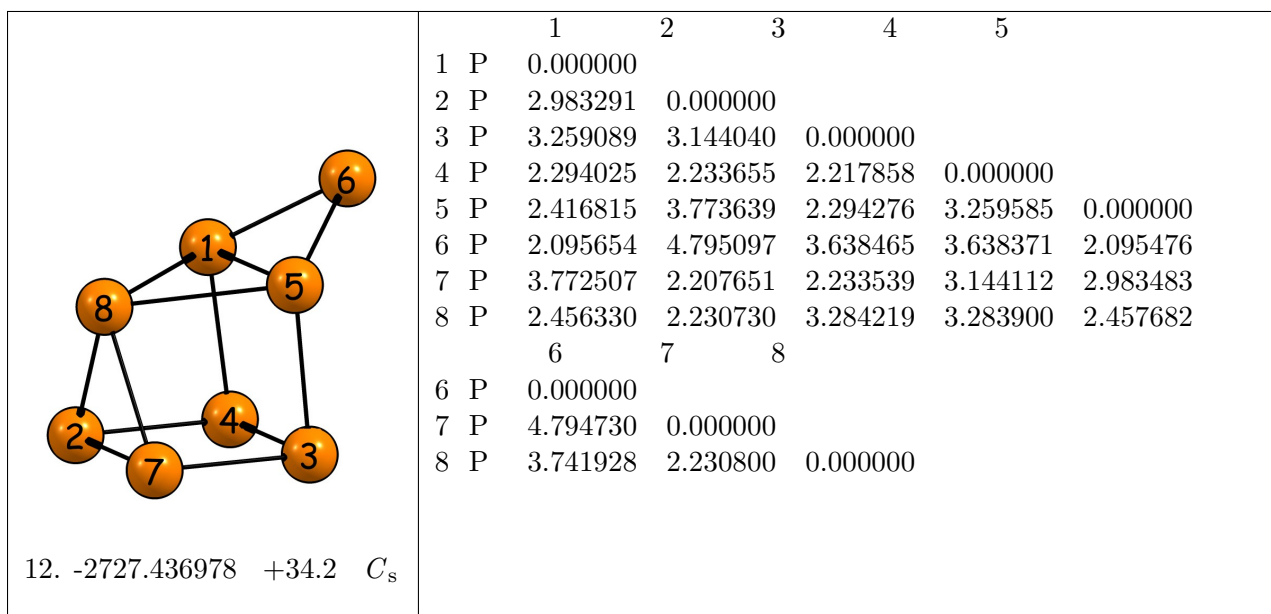
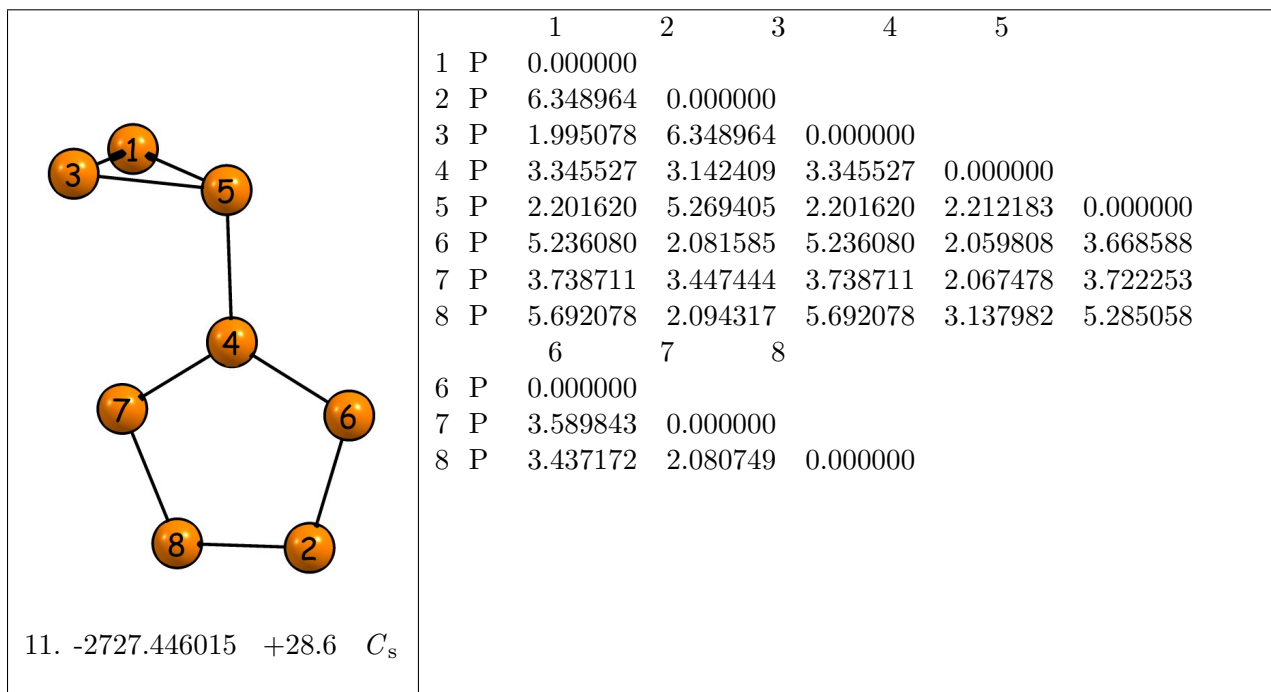
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	2 P	3.879415	0.000000			
	3 P	2.198256	3.361203	0.000000		
	4 P	3.556607	3.065659	3.446342	0.000000	
	5 P	3.556607	2.220461	2.190181	2.207016	0.000000
	6 P	2.209599	4.911601	2.203242	3.484419	3.484419
	7 P	3.879415	2.024370	4.218070	2.220461	3.065659
	8 P	2.198256	4.218070	3.208124	2.190181	3.446342
		6	7	8		
6 P	0.000000					
7 P	4.911601	0.000000				
8 P	2.203242	3.361203	0.000000			
3. -2727.473942 +11.0 C_s						

	1	2	3	4	5	
	1 P	0.000000				
	2 P	3.682724	0.000000			
	3 P	4.397099	2.128154	0.000000		
	4 P	2.225681	3.428232	3.434931	0.000000	
	5 P	2.391854	2.225643	3.550229	2.160775	0.000000
	6 P	2.225681	3.428232	3.434931	3.150228	3.547572
	7 P	2.391854	2.225643	3.550229	3.547572	2.512934
	8 P	3.176388	3.216579	2.103177	2.248391	3.450144
		6	7	8		
6 P	0.000000					
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8 P	2.248391	3.450144	0.000000			
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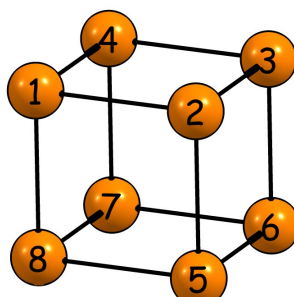
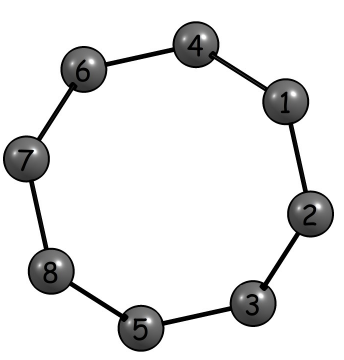
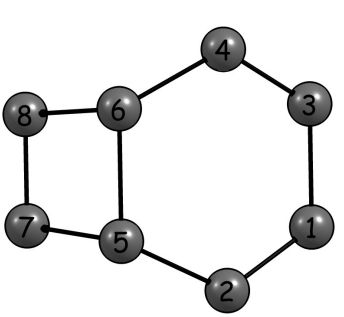
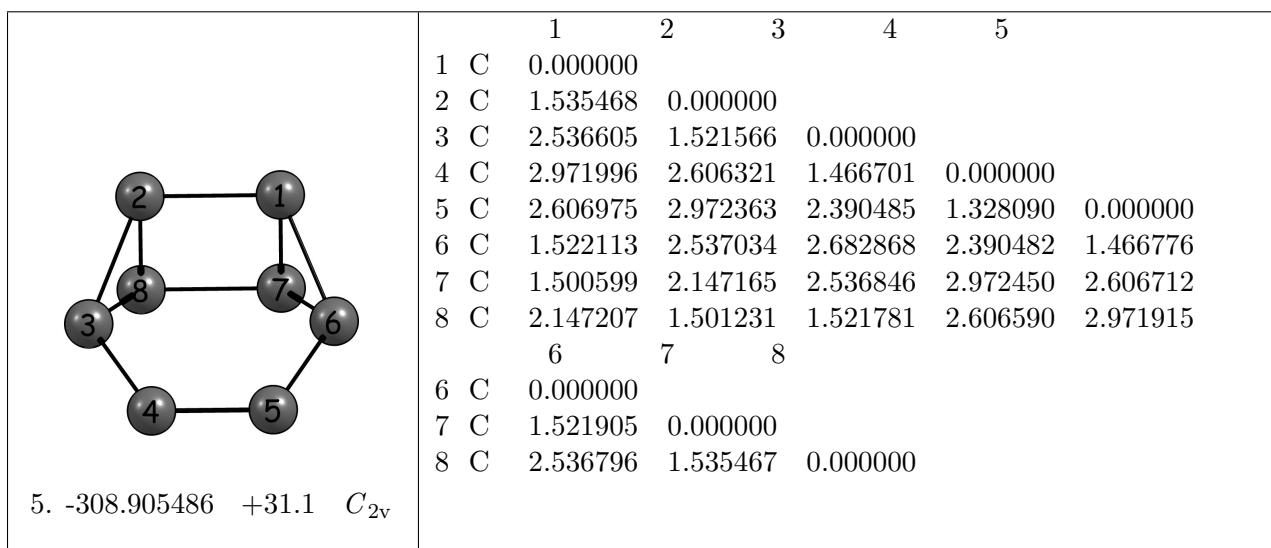
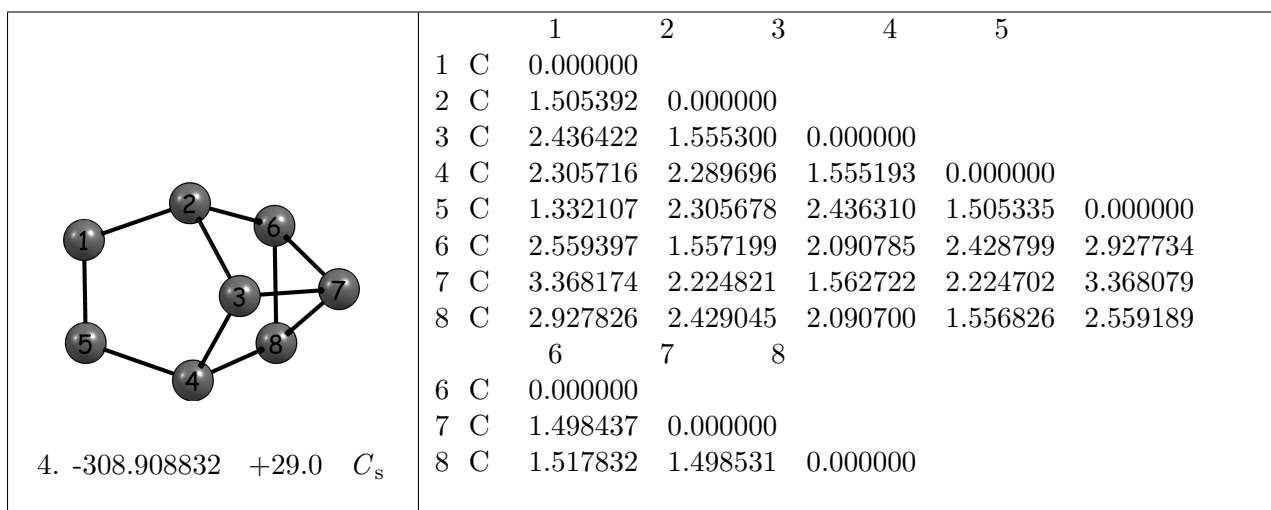
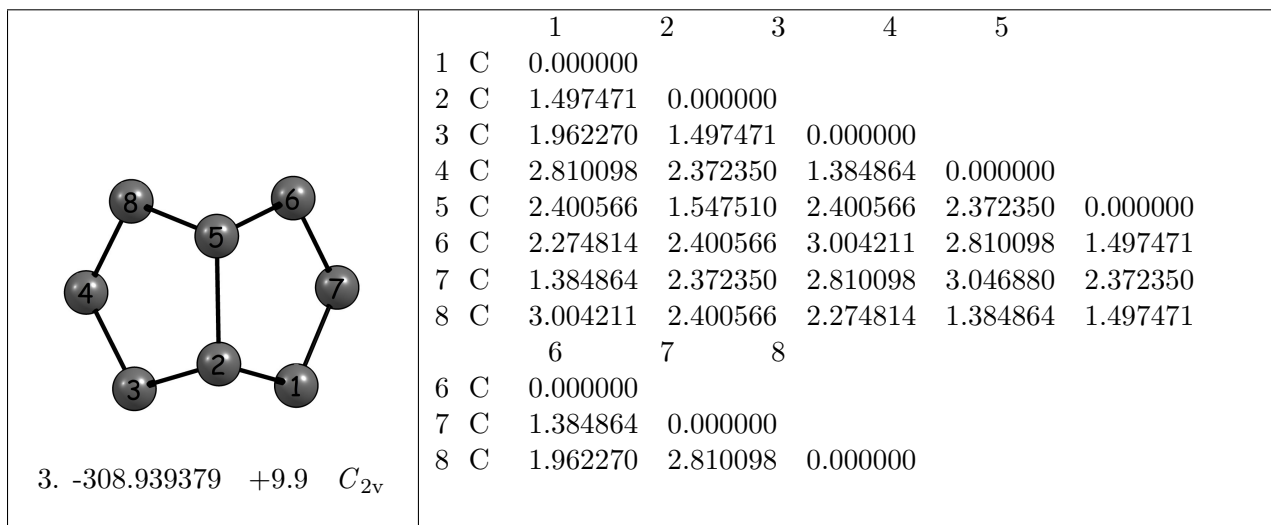
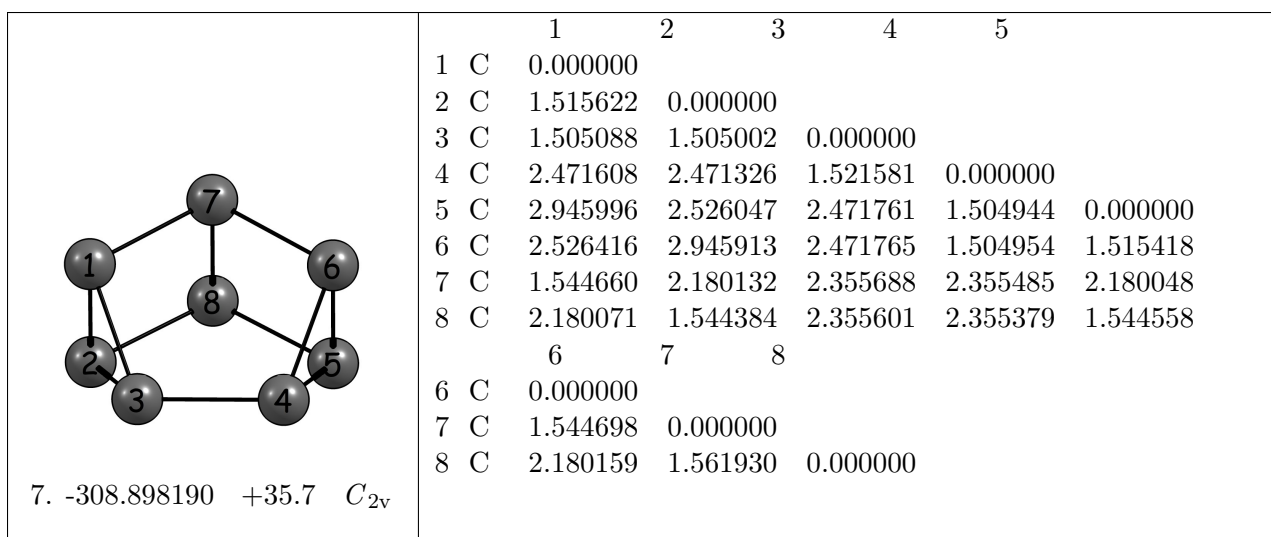
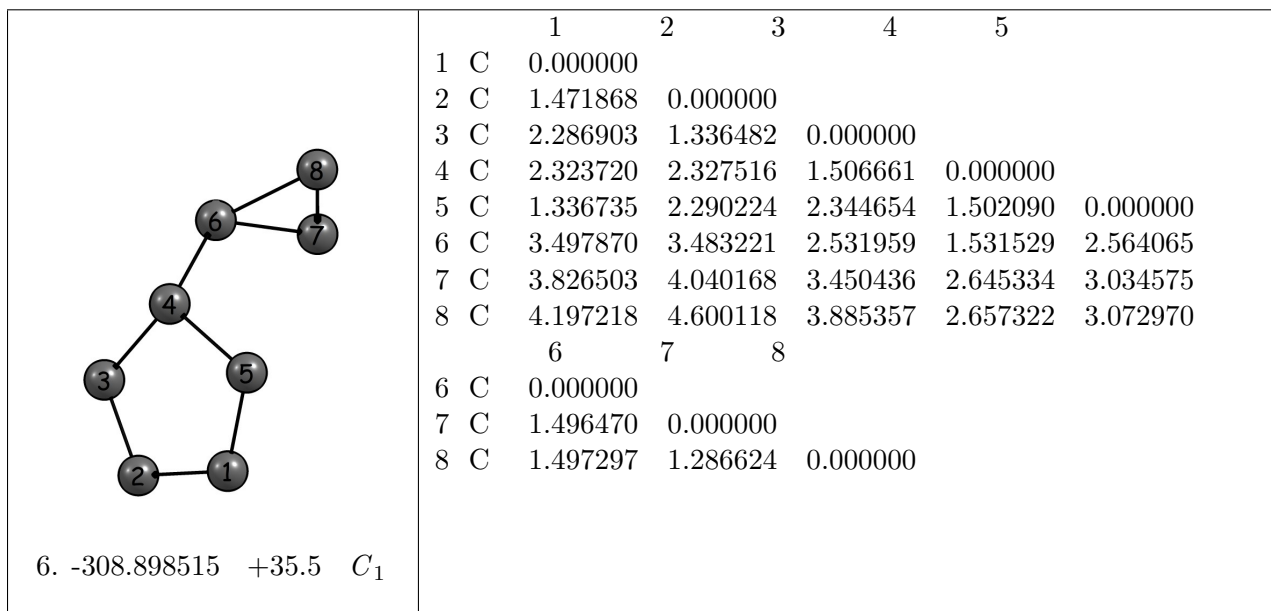
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	2 P	2.264933	0.000000			
	3 P	3.202774	2.264723	0.000000		
	4 P	2.264723	3.203127	2.264933	0.000000	
	5 P	3.203536	2.264933	3.202774	3.922858	0.000000
	6 P	3.922858	3.203127	2.264933	3.202662	2.264723
	7 P	3.202774	3.922858	3.203536	2.264933	3.202774
	8 P	2.264933	3.202662	3.922858	3.203127	2.264933
		6	7	8		
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7 P	2.264933	0.000000				
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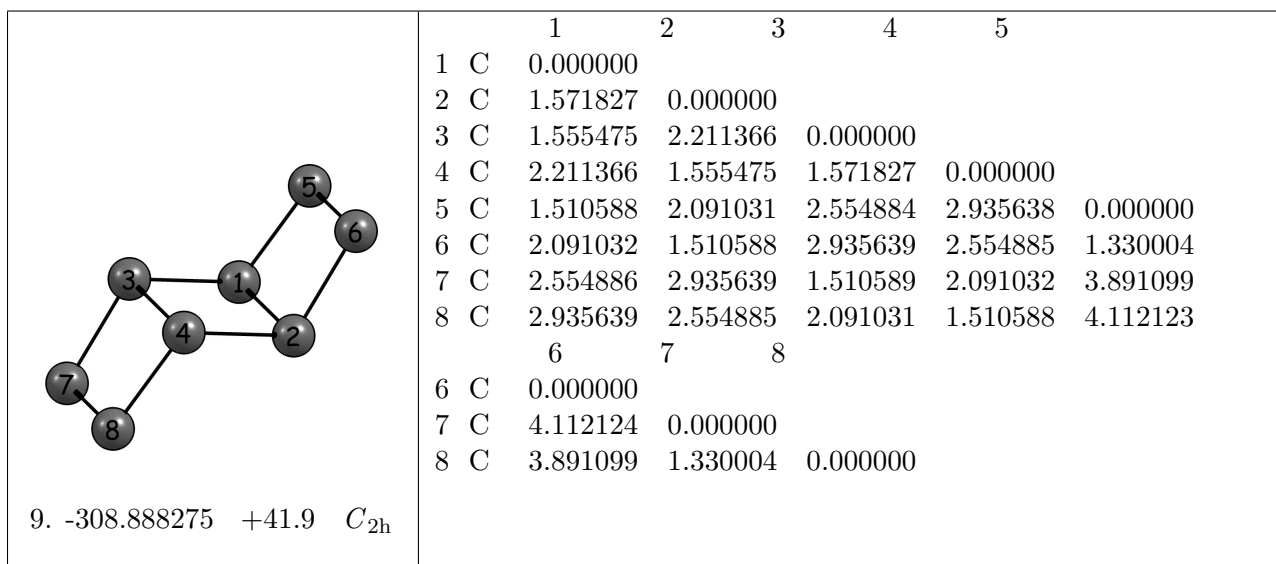
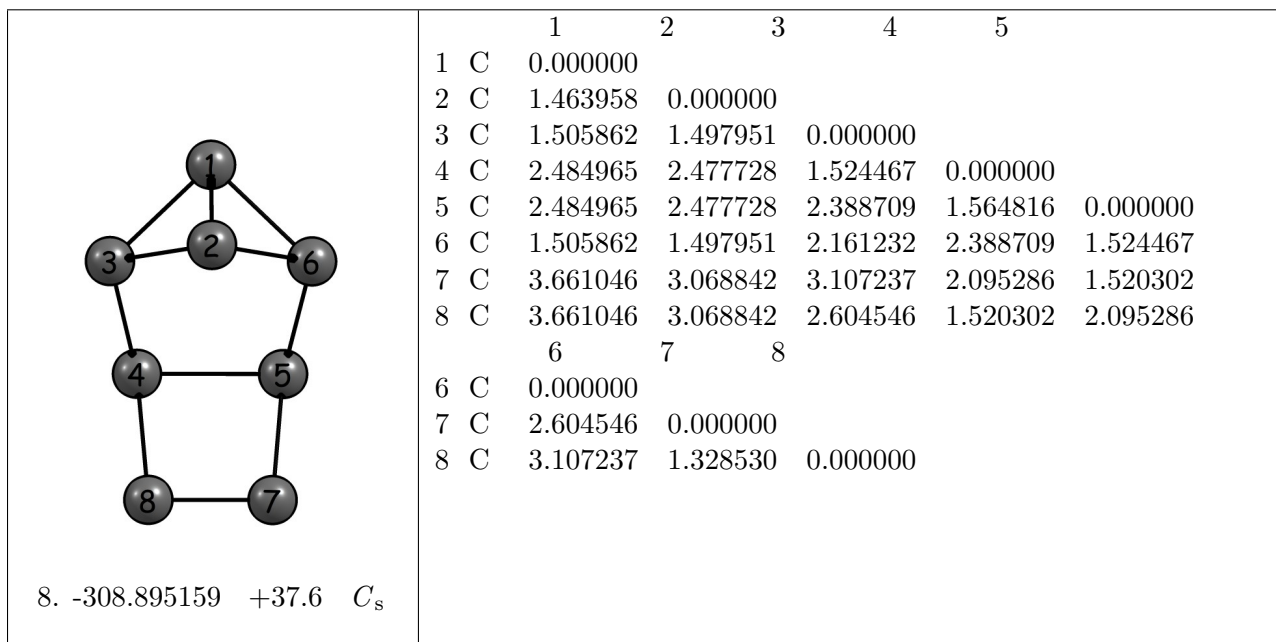
Table S3: Distance table for the lowest-lying C₈H₈ optimized structures obtained at the M11/def2-TZVP level of theory. Included are the zero-point corrected absolute energy in (a.u.) at the DLPNO-CCSD(T)/def2-QZVP level of theory with zero-point energy obtained from the M11/def2-TZVP computations, relative energy in (kcal/mol) and symmetry. H atoms are omitted for clarity

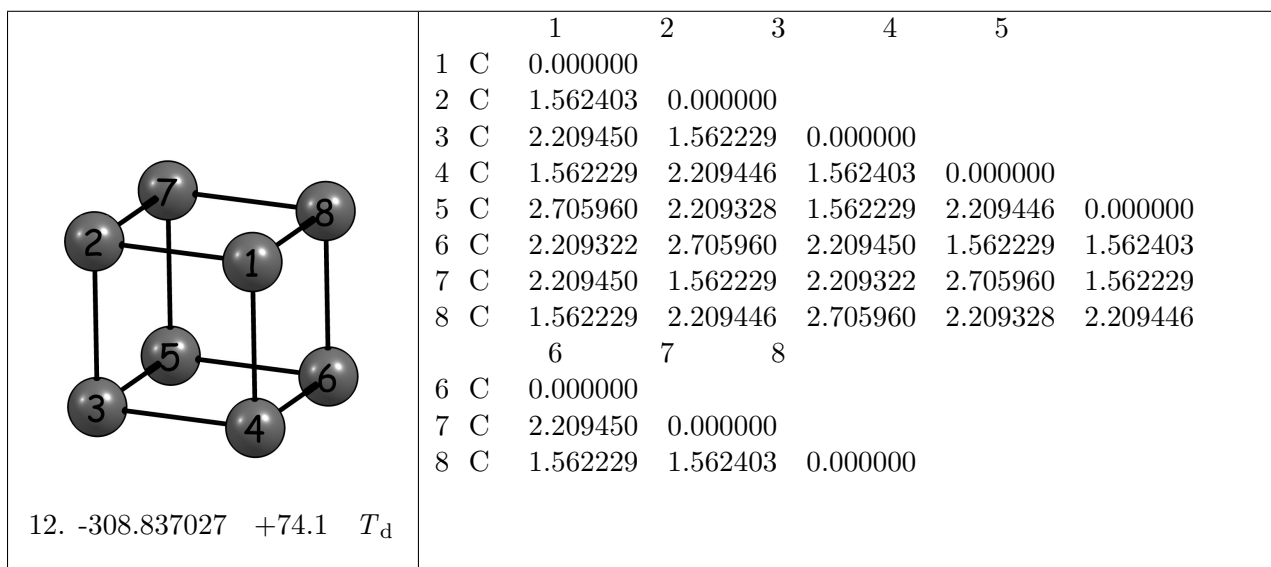
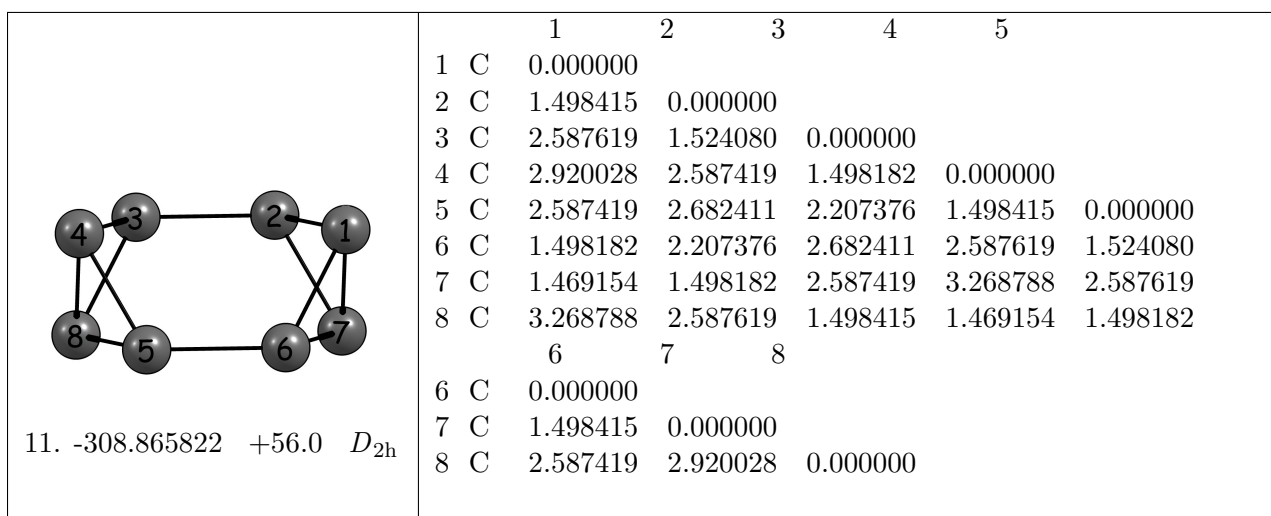
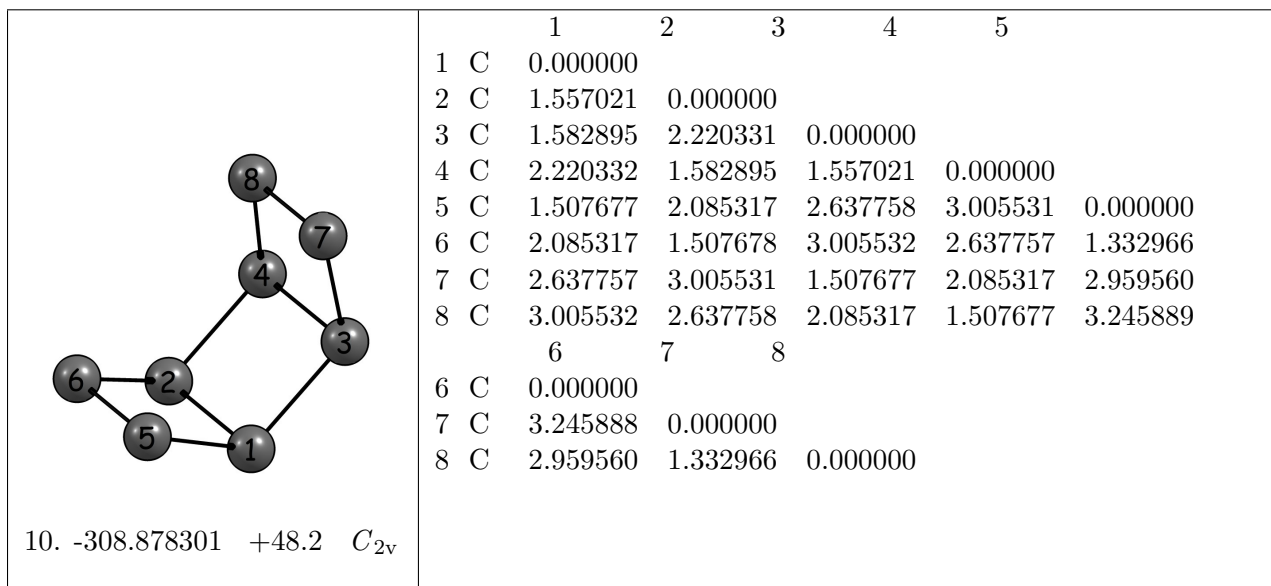
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	3 C	2.499143	1.473756	0.000000		
	4 C	1.473756	2.499144	3.067169	0.000000	
	5 C	3.212394	2.499144	1.328182	3.342393	0.000000
	6 C	2.499143	3.212395	3.342393	1.328183	3.067168
	7 C	3.067169	3.342394	3.212394	2.499144	2.499143
	8 C	3.342393	3.067169	2.499143	3.212395	1.473756
		6	7	8		
6 C	0.000000					
7 C	1.473756	0.000000				
8 C	2.499143	1.328182	0.000000			

 <p>2. -308.942539 +7.9 C_s</p>		1	2	3	4	5
	1 C	0.000000				
	2 C	1.329682	0.000000			
	3 C	1.467354	2.446565	0.000000		
	4 C	2.446565	2.874307	1.329682	0.000000	
	5 C	2.479400	1.499065	2.908740	2.603584	0.000000
	6 C	2.908739	2.603584	2.479400	1.499065	1.576538
	7 C	3.386879	2.541760	3.663375	3.206093	1.520105
	8 C	3.663374	3.206093	3.386880	2.541761	2.098840
		6	7	8		
6 C	0.000000					
7 C	2.098841	0.000000				
8 C	1.520105	1.328488	0.000000			









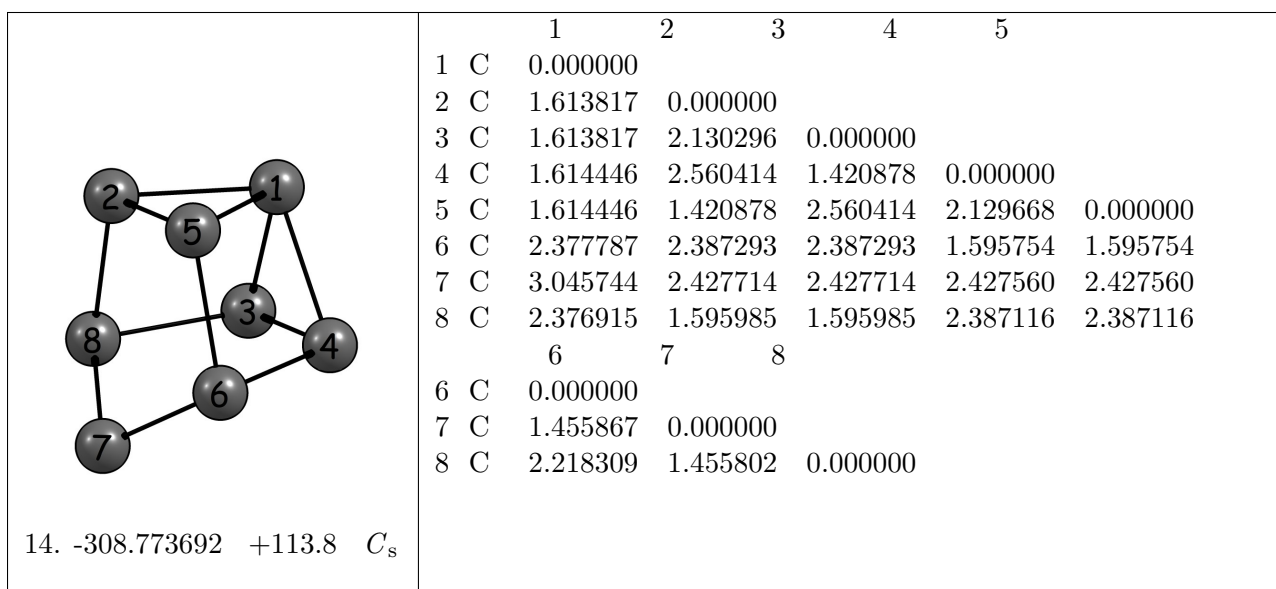
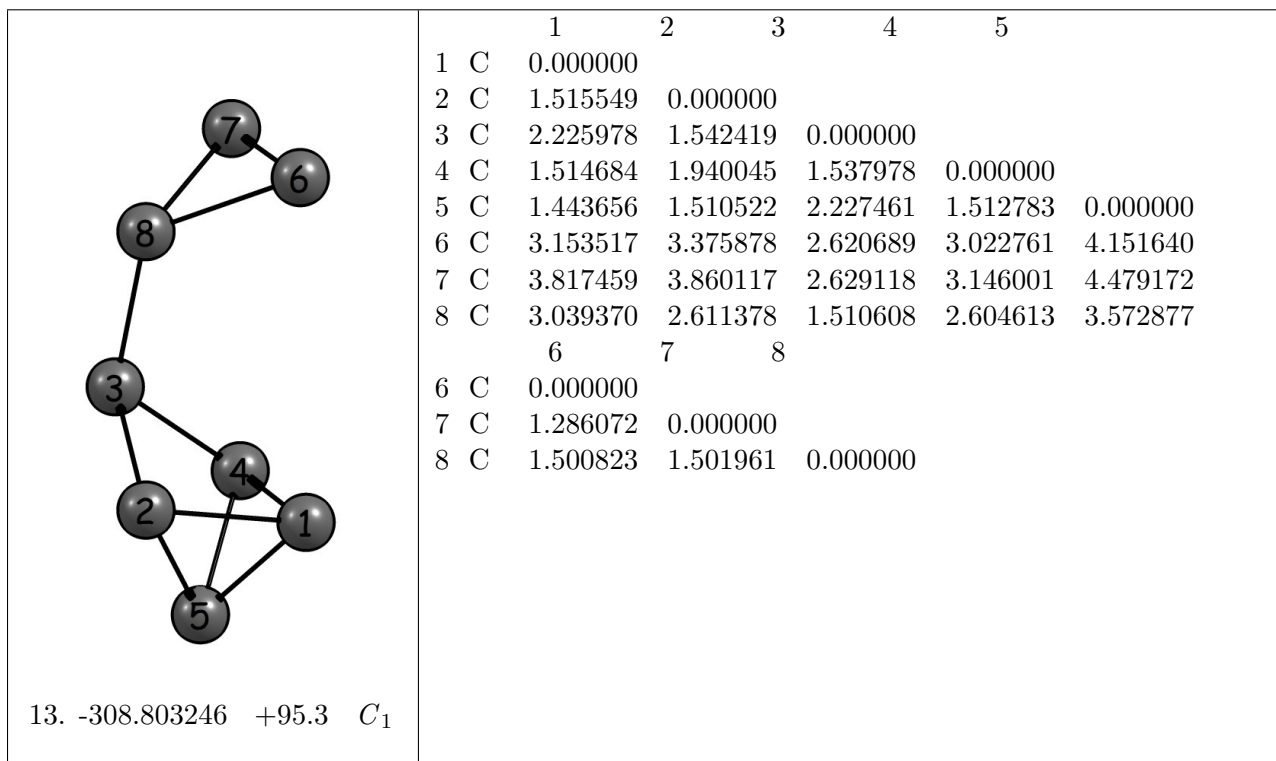


Table S4: HOMO-LUMO gaps for the lowest-lying structures at the M11/def2-TZVP level of theory.

Structure	HOMO (a.u.)	LUMO (a.u.)	H/L gap (a.u.)	H/L gap (eV)
C8H8-1	-0.315898	0.030773	0.346671	9.43
C8H8-2	-0.309530	0.044760	0.354290	9.64
C8H8-3	-0.293892	0.079567	0.373459	10.16
C8H8-4	-0.338868	0.081737	0.420605	11.45
C8H8-5	-0.315435	0.093390	0.408825	11.12
C8H8-6	-0.316555	0.056530	0.373085	10.15
C8H8-7	-0.344320	0.110697	0.455017	12.38
C8H8-8	-0.333994	0.090825	0.424819	11.56
C8H8-9	-0.335069	0.077562	0.412631	11.23
C8H8-10	-0.341370	0.075014	0.416384	11.33
C8H8-11	-0.319572	0.110094	0.429666	11.69
C8H8-12	-0.354960	0.116205	0.471165	12.82
C8H8-13	-0.329993	0.084032	0.414025	11.27
C8H8-14	-0.201368	0.082285	0.283653	7.72
P8-1	-0.307112	-0.034318	0.272794	7.42
P8-2	-0.329071	-0.070062	0.259009	7.05
P8-3	-0.325684	-0.058883	0.266801	7.26
P8-4	-0.298353	-0.033674	0.264679	7.20
P8-5	-0.311281	-0.028855	0.282426	7.69
P8-6	-0.290550	-0.004223	0.286327	7.79
P8-7	-0.317724	-0.091970	0.225754	6.14
P8-8	-0.307449	-0.054637	0.252812	6.88
P8-9	-0.325472	-0.067391	0.258081	7.02
P8-10	-0.306154	-0.064388	0.241766	6.58
P8-11	-0.324445	-0.071090	0.253355	6.89
P8-12	-0.301829	-0.052821	0.249008	6.78
P8-13	-0.297076	-0.052037	0.245039	6.67

Table S5: QTAIM analysis for the lowest-lying P₈ structures.

Structure	N° P-Atom	N° P'-Atom	Distance (Å)	Nalewajski-Mrozek BO	BCP Rho	BCP-Laplacian
P-P (P ₂ H ₄)	1	2	2.264	1.05	0.1037	-0.1119
P=P (P ₂ H ₂)	1	2	2.046	2.05	0.1427	-0.2041
P8-1	1	3	2.180	0.99	0.1107	-0.0923
	1	4	2.280	0.96	0.0956	-0.0517
	1	6	2.237	0.97	0.1071	-0.1061
	2	3	2.210	0.99	0.1082	-0.1081
	2	5	2.180	0.99	0.1107	-0.0923
	2	8	2.180	0.99	0.1107	-0.0923
	3	4	2.180	0.99	0.1107	-0.0923
	4	7	2.237	0.97	0.1071	-0.1061
	5	6	2.237	0.97	0.1071	-0.1061
	5	8	2.280	0.96	0.0956	-0.0517
P8-2	6	7	2.198	1.02	0.1162	-0.1364
	7	8	2.237	0.97	0.1071	-0.1061
	1	4	2.015	1.84	0.1470	-0.2107
	1	6	2.206	1.02	0.1114	-0.1152
	2	3	2.241	0.92	0.1028	-0.0893
	2	5	2.187	1.00	0.1103	-0.0868
	2	8	2.224	0.98	0.1052	-0.0784
	3	4	2.206	1.02	0.1114	-0.1152
	3	7	2.195	0.99	0.1145	-0.1248
	5	6	2.242	0.92	0.1028	-0.0893
P8-3	5	8	2.224	0.98	0.1052	-0.0783
	6	7	2.195	0.99	0.1145	-0.1248
	7	8	2.296	0.92	0.0979	-0.0828
	1	3	2.198	0.96	0.1084	-0.0833
	1	6	2.210	0.95	0.1030	-0.0461
	1	8	2.198	0.96	0.1084	-0.0833
	2	5	2.220	1.01	0.1100	-0.1149
	2	7	2.024	1.82	0.1477	-0.2162
	3	5	2.190	1.00	0.1129	-0.1184
	3	6	2.203	0.98	0.1078	-0.0837
P8-4	4	5	2.207	0.96	0.1120	-0.1222
	4	7	2.220	1.01	0.1100	-0.1149
	4	8	2.190	1.00	0.1129	-0.1184
	6	8	2.203	0.98	0.1078	-0.0837
	1	4	2.226	0.90	0.1046	-0.0770
	1	5	2.392	0.53	0.0760	0.0220
	1	6	2.226	0.90	0.1046	-0.0770
	1	7	2.392	0.53	0.0760	0.0220
	2	3	2.128	1.22	0.1221	-0.1371
	2	5	2.226	0.87	0.1036	-0.0781
P8-5	2	7	2.226	0.87	0.1036	-0.0781
	3	8	2.103	1.24	0.1273	-0.1537
	4	5	2.161	1.02	0.1154	-0.1053
	4	8	2.248	0.88	0.1039	-0.0935
	6	7	2.161	1.02	0.1154	-0.1053
	6	8	2.248	0.88	0.1039	-0.0935
	1	2	2.201	0.98	0.1076	-0.0807
	1	5	2.199	0.95	0.1052	-0.0541
	1	8	2.200	0.98	0.1076	-0.0807
	2	5	2.200	0.98	0.1076	-0.0807

	4	8	2.232	0.98	0.1059	-0.0977
	5	8	2.201	0.98	0.1076	-0.0807
	6	7	2.201	0.98	0.1076	-0.0807
P8-6	1	4	2.770	0.34	0.0433	0.0371
	1	5	2.160	1.05	0.1130	-0.0856
	1	6	2.160	1.05	0.1130	-0.0857
	2	4	2.319	0.81	0.0885	-0.0284
	2	7	2.178	1.04	0.1112	-0.0824
	2	8	2.142	1.02	0.1153	-0.0839
	3	4	2.165	0.94	0.1220	-0.1515
	3	5	2.193	0.88	0.1083	-0.0776
	3	6	2.193	0.88	0.1082	-0.0773
	3	7	2.384	0.60	0.0821	-0.0298
	4	8	2.319	0.81	0.0886	-0.0287
	5	6	2.213	0.98	0.1037	-0.0503
	7	8	2.178	1.04	0.1112	-0.0822
P8-7	1	2	2.205	0.96	0.1079	-0.0931
	1	5	2.082	1.37	0.1327	-0.1723
	1	7	2.402	0.61	0.0716	0.0176
	2	3	2.221	0.97	0.1078	-0.1060
	2	7	2.205	0.96	0.1079	-0.0931
	3	4	2.205	0.96	0.1079	-0.0931
	3	8	2.205	0.96	0.1079	-0.0931
	4	6	2.082	1.37	0.1327	-0.1723
	4	8	2.402	0.61	0.0716	0.0176
	5	8	2.082	1.37	0.1327	-0.1723
	6	7	2.082	1.37	0.1327	-0.1723
P8-8	1	2	2.221	0.99	0.1065	-0.0825
	1	5	2.240	0.97	0.1078	-0.1116
	1	8	2.211	0.99	0.1072	-0.0827
	2	3	2.216	0.98	0.1079	-0.0875
	2	8	2.182	1.00	0.1071	-0.0598
	3	5	2.230	0.99	0.1100	-0.1180
	3	8	2.222	0.95	0.1047	-0.0757
	4	6	1.994	1.86	0.1491	-0.1943
	4	7	2.204	1.01	0.1069	-0.0695
	5	7	2.239	0.95	0.1090	-0.1112
	6	7	2.211	1.01	0.1052	-0.0625
P8-9	1	2	2.186	0.95	0.1067	-0.0730
	1	6	2.191	1.06	0.1104	-0.1067
	1	7	2.186	0.95	0.1067	-0.0730
	2	7	2.217	1.00	0.1073	-0.0842
	2	8	2.258	0.95	0.1016	-0.0867
	3	4	2.186	0.95	0.1067	-0.0730
	3	7	2.258	0.95	0.1016	-0.0867
	3	8	2.217	1.00	0.1073	-0.0842
	4	5	2.191	1.06	0.1104	-0.1067
	4	8	2.186	0.95	0.1067	-0.0730
	5	6	2.005	1.78	0.1484	-0.2158
P8-10	1	6	2.023	1.55	0.1436	-0.1971
	1	7	2.229	0.96	0.1024	-0.0843
	2	4	2.326	0.74	0.0908	-0.0573
	2	5	2.182	1.04	0.1119	-0.0924
	2	7	2.184	1.01	0.1100	-0.0844
	3	4	2.251	0.78	0.0963	-0.0224
	3	5	2.327	0.74	0.0907	-0.0572
	3	6	2.305	0.65	0.0887	-0.0308
	3	8	2.116	1.10	0.1176	-0.0874
	4	6	2.304	0.65	0.0888	-0.0310
	4	8	2.116	1.10	0.1176	-0.0875

	5	7	2.184	1.01	0.1100	-0.0846
P8-11	1	3	1.995	1.86	0.1492	-0.1936
	1	5	2.202	1.01	0.1072	-0.0671
	2	6	2.082	1.43	0.1319	-0.1674
	2	8	2.094	1.42	0.1295	-0.1605
	3	5	2.202	1.01	0.1072	-0.0671
	4	5	2.212	0.92	0.1105	-0.1159
	4	6	2.060	1.30	0.1343	-0.1765
	4	7	2.067	1.25	0.1323	-0.1691
	7	8	2.081	1.43	0.1318	-0.1666
P8-12	1	4	2.294	0.80	0.0976	-0.0749
	1	6	2.096	1.18	0.1249	-0.1220
	1	8	2.456	0.51	0.0706	-0.0025
	2	4	2.234	0.97	0.1085	-0.1087
	2	7	2.208	1.00	0.1078	-0.0889
	2	8	2.231	0.87	0.1048	-0.0743
	3	4	2.218	1.01	0.1117	-0.1173
	3	5	2.294	0.80	0.0976	-0.0748
	3	7	2.234	0.97	0.1085	-0.1087
	5	6	2.095	1.18	0.1250	-0.1223
	5	8	2.458	0.51	0.0705	-0.0022
	7	8	2.231	0.87	0.1048	-0.0743
P8-13	1	2	2.265	1.00	0.1053	-0.1083
	1	4	2.265	1.00	0.1053	-0.1084
	1	8	2.265	1.00	0.1053	-0.1084
	2	3	2.265	1.00	0.1053	-0.1084
	2	5	2.265	1.00	0.1053	-0.1084
	3	4	2.265	1.00	0.1053	-0.1084
	3	6	2.265	1.00	0.1053	-0.1084
	4	7	2.265	1.00	0.1053	-0.1084
	5	6	2.265	1.00	0.1053	-0.1084
	5	8	2.265	1.00	0.1053	-0.1084
	6	7	2.265	1.00	0.1053	-0.1084
	7	8	2.265	1.00	0.1053	-0.1084

Table S6: Calculated molar magnetic susceptibility in cgs ppm units ($10^{-6} \text{ cm}^3 \text{ mol}^{-1}$) at the (M11/def2-TZVP) level of theory, where for benzene (C_6H_6) the experimental value is found to be $-54.4 (10^{-6} \text{ cm}^3 \text{ mol}^{-1})^a$

Structure	Calculated $\chi_M (10^{-6} \text{ cm}^3 \text{ mol}^{-1})$
C6H6	-52.4448
P8-1	-119.9984
P8-2	-121.0013
P8-3	-107.6571
P8-4	-189.8174
P8-5	-136.2405
P8-6	-182.8385
P8-7	-111.5833
P8-8	-109.6991
P8-9	-152.4464
P8-10	-156.8422
P8-11	-112.8774
P8-12	-118.7701
P8-13	-2.0460
C8H8-1	-38.8016
C8H8-2	-51.6034
C8H8-3	-84.0608
C8H8-4	-68.5624
C8H8-5	-76.2359
C8H8-6	-60.5651
C8H8-7	-77.2472
C8H8-8	-74.5895
C8H8-9	-55.8549
C8H8-10	-57.9932
C8H8-11	-80.2488
C8H8-12	-46.6025
C8H8-13	-71.7029
C8H8-14	-88.0765

^aJ. Dauben, J. D. Wilson and J. L. Laity, Diamagnetic Susceptibility Exaltation in Hydrocarbons. *J. Am. Chem. Soc.* 1969, 91, 8, 1991–1998.

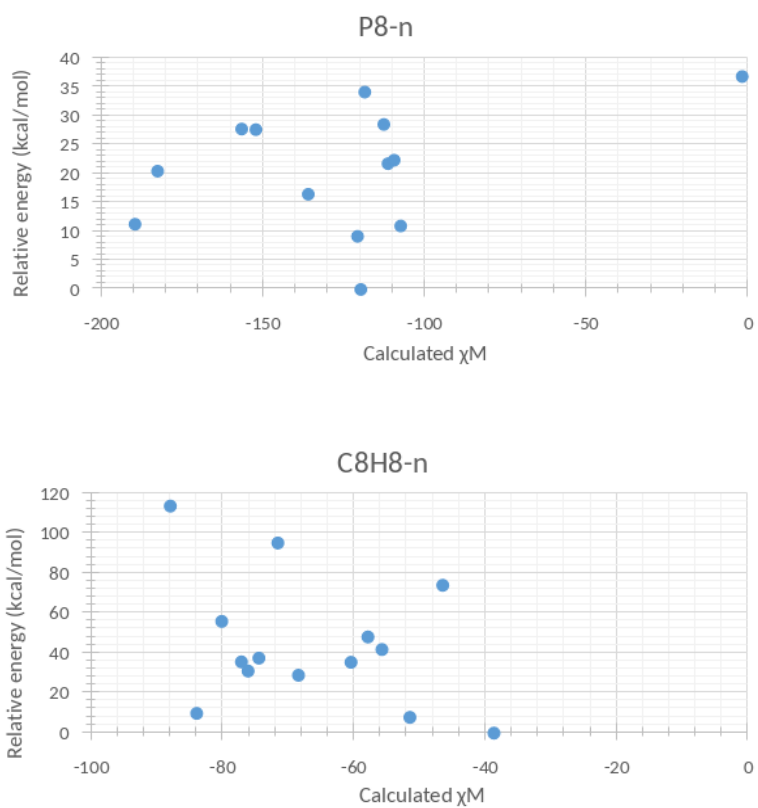


Figure S1. Correlation between the calculated χ_M and relative energy (kcal/mol) for the P_8 and C_8H_8 structures.