

## SUPPLEMENTARY MATERIAL

### Proton Dynamics in a Spark-Plasma Sintered $\text{BaZr}_{0.7}\text{Ce}_{0.2}\text{Y}_{0.1}\text{O}_{3-\delta}$ Proton Conductor investigated by Quasi-elastic neutron scattering

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#### Supplementary Material

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#### 1 Characteristics of the $\text{BaZr}_{0.7}\text{Ce}_{0.2}\text{Y}_{0.1}\text{O}_{3-\delta}$ sample

The  $\text{BaZr}_{0.7}\text{Ce}_{0.2}\text{Y}_{0.1}\text{O}_{3-\delta}$  (BZCY72) sample investigated by QENS in the main article exhibited a high relative density of 97.9 % as determined geometrically from the sample dimensions where a theoretical density of  $6.20 \text{ g/cm}^3$  was used.

Further characterization of the microstructure was carried out by means of an JSM 7500 Field emission SEM. Fig. 1 presents the grain structure of BZCY72 prepared by Spark Plasma Sintering (SPS). The average grain size determined by multiple SEM images is  $222 \pm 98 \text{ nm}$ . The grains are irregular in size and shape indicating abnormal grain growth during the SPS process. The remaining porosity is composed of intergranular pores and spacing between adjacent pores. The grain boundaries appeared to be free of impurities, although the resolution was not sufficient to establish this with high certainty.

XRD measurements confirm a high phase purity of the rhombohedral BZCY72 main phase, fig. 2. The space group is  $R\bar{3}c$  with lattice parameters of  $a = 6.014$  and  $c = 14.704$ . A minor impurity is carbon (PDF 00-001-0640) due to the preparation method containing the sample inside a carbon die. Another impurity at  $2\theta = 28.9^\circ$  matches  $\text{Y}_2\text{O}_3$  (PDF 00-041-1105). The crystallite size was on average  $76 \pm 8 \text{ nm}$  and the calculated B – O bond length from Rietveld refinement was  $2.13 \text{ \AA}$ .

#### 2 TGA measurements

TGA Measurements were carried out by a STA instrument (STA7200RV, Hitachi) for 170-200 mg of powder using a Pt pan. The samples were heated at  $5^\circ\text{C}/\text{min}$  from  $40^\circ\text{C}$  to  $950^\circ\text{C}$  under

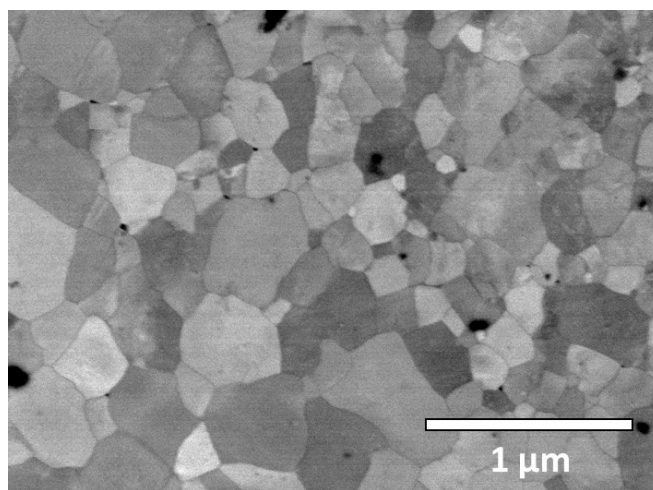


Fig. 1 SEM Image of the polished cross section of the BZCY72 sample prepared by SPS.

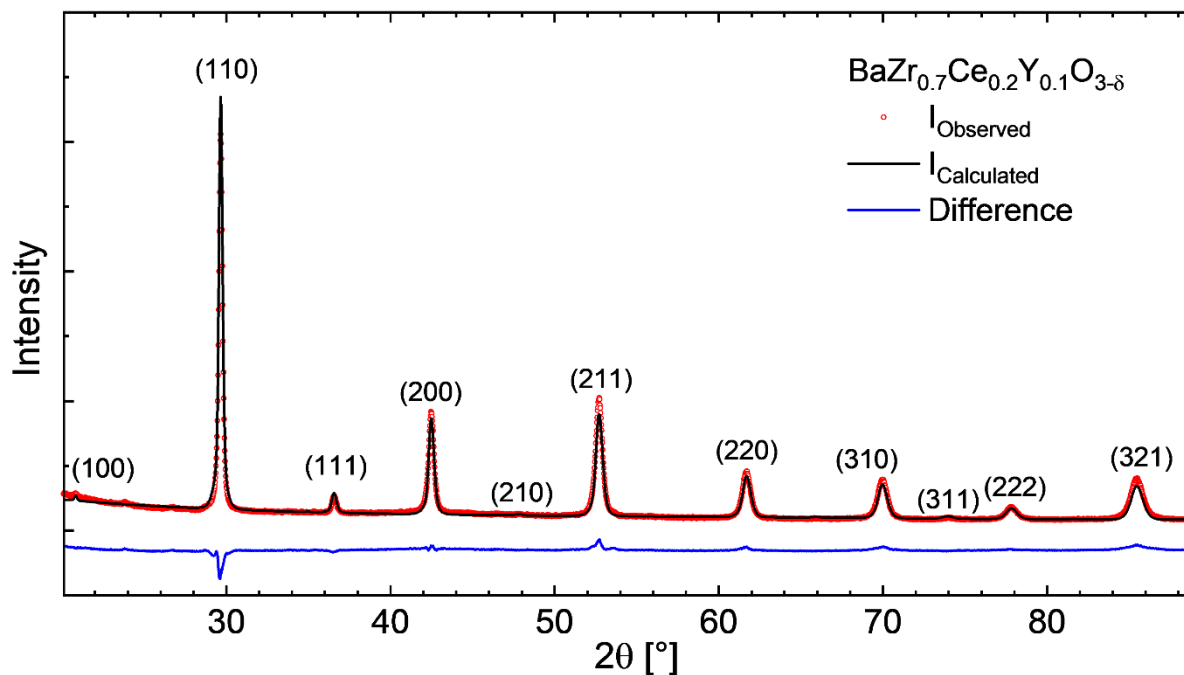
a dry Ar atmosphere with a gas flow of  $100 \text{ ml}/\text{min}$ , while the weight change was recorded simultaneously. After reaching  $950^\circ\text{C}$  the temperature was held for 6 h and then subsequently cooled at  $5^\circ\text{C}/\text{min}$  to  $40^\circ\text{C}$ , which was held again for 20 min. Afterwards the argon was saturated with water vapor ( $p_{\text{H}_2\text{O}} = 19.95 \text{ kPa}$ ) and the increased weight was recorded. The weight change is directly related to the water uptake and therefore the protonic defect concentration. Weight traces and protonic defect concentration are related as follows:

$$[\text{OH}^\bullet] = \frac{2 \Delta m M_{\text{oxide}}}{m_{\text{oxide}} M_{\text{H}_2\text{O}}} \quad (1)$$

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**Fig. 2** XRD pattern of the BZCY72 sample prepared by SPS represented as red dots. The solid black line is the calculated intensity by a Rietveld refinement with the difference between the two intensities as blue solid line. All peaks are labeled with their corresponding miller indices.

where  $M_{oxide}$  and  $M_{H_2O}$  are molecular weights of the oxides and water,  $\Delta m$  and  $m_{oxide}$  are weight change and weight of the specimen, respectively.

For the BZCY72 sample, a weight gain of 0.59 % was recorded between 230 °C and 420 °C, corresponding to a defect concentration  $[OH^\bullet] \approx 0.187$  within this temperature regime, which is in good accordance with the value of 0.2 obtained from Neutron Compton spectroscopy (1).

### 3 Impedance spectroscopy

The impedance data was fitted with the using an equivalent circuit that consists of a resistor  $R$  and a constant phase element or CPE connected in parallel:  $(R_1Q_1)$   $(R_2Q_2)$   $(R_3Q_3)$ , where each parallel circuit represents a specific phenomenon of the inspected system beginning with the bulk at high frequencies in with the resistance  $R_1$ , followed by the grain boundary contribution at intermediate frequencies and the electrode at low frequencies, according to the Boukamp circuit description code (2). The complex impedance of a CPE element and the quasi-equivalent capacity of a RQ element are given by equation 2 and 3, respectively:

$$Z(j, \omega) = \frac{1}{(j\omega)^n Q_0} \quad (2)$$

$$C = R \left( \frac{1}{n} - 1 \right) Q \left( \frac{1}{n} \right) \quad (3)$$

where  $0 \leq n \leq 1$ . The CPE represents a capacitor when  $n = 1$  and a resistor for  $n = 0$ .  $\omega$  is the angular frequency and  $j$

The resistivity  $\rho$  and conductivity  $\sigma$  of the sample and its compartments can be calculated by:

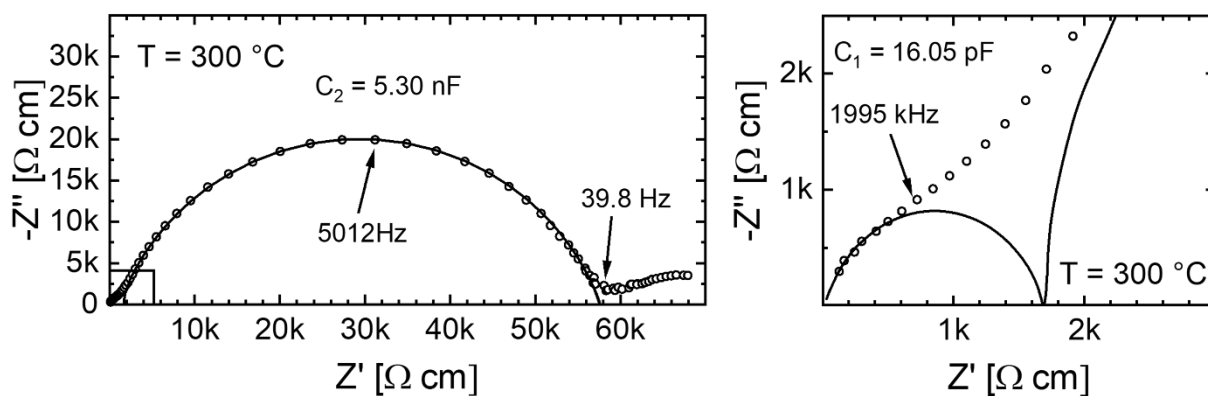
$$\sigma = \frac{1}{\rho} = \frac{L}{RA} \quad (4)$$

taking the samples thickness  $L$  and electrode area  $A$  into account. This is also known as the geometric factor, correcting the data for sample dimensions. For further interpretation the imaginary (capacitive) impedance  $-Z''$  is plotted as a function of the real (resistive) part of the impedance  $Z'$  as a Nyquist plot. Another IS data representation is the Bode plot where  $Z$  is plotted vs the frequency  $f$ . In addition, within complex systems it is often meaningful to calculate the electric modulus  $M^* = M' + jM''$  to give emphasis to elements with small capacitances:

$$M^* = j\omega C_0 Z^* \quad (5)$$

where  $C_0$  is the vacuum capacitance.

Fig. 3 presents the Nyquist plot of the BZCY72 sample investigated in the main article at 300 °C. The sample can be separated into two components as indicated by the equivalent circle fits. The extracted capacities are  $C_1 = 8.2$  pF and  $C_2 = 354$  pF for the bulk and grain boundary, respectively.



**Fig. 3** Complex plane plot (Nyquist plot) of the BZCY72 pellet prepared by SPS at  $T = 300\text{ }^{\circ}\text{C}$ . The capacities are given within the figure. On the right side the high-frequency region is shown to emphasize the bulk contribution. The solid black line represents a fit using individual resistances and constant phase elements in parallel.

#### 4 References

1. Wallis J, Kruth A, Da Silva I, Krzystyniak M. Nuclear dynamics in BaZr<sub>0.7</sub>Ce<sub>0.2</sub>Y<sub>0.1</sub>O<sub>3-δ</sub> proton conductor as observed by neutron diffraction and Compton scattering. *Journal of Physics Communications*. 2020;4(4):045004.
2. Boukamp BA. Electrochemical impedance spectroscopy in solid state ionics: recent advances. *Solid state ionics*. 2004;169(1-4):65-73.