

Absolute Quantum Yield for Understanding the Upconversion and Downshift Properties of Luminescent $\text{PbF}_2:\text{Er}^{3+}, \text{Yb}^{3+}$ Crystals

Eduard Madirov, Dmitry Busko, Ian A. Howard, Bryce S. Richards and Andrey Turshatov

Table S1. Integrated absorption cross-section of the $\text{PbF}_2:\text{Er}^{3+}, \text{Yb}^{3+}$ samples used in the Judd-Ofelt calculations, $\times 10^{-20} \text{ cm}^2$

	Er1.5Yb1.5	Er2Yb2	Er2Yb3	Er2Yb5	Er2Yb7
$^4\text{G}_{11/2}$	5.982	6.628	6.628	6.757	7.825
$^2\text{H}_{9/2}$	0.620	0.877	0.853	0.789	0.988
$^4\text{F}_{7/2}$	2.797	3.860	3.911	3.931	4.782
$^2\text{H}_{11/2}$	6.099	6.860	6.715	6.747	8.450
$^4\text{S}_{3/2}$	0.972	1.649	1.361	1.293	1.727
$^4\text{F}_{9/2}$	5.624	7.443	7.789	7.964	9.657
$^4\text{I}_{13/2}$	34.724	41.620	42.104	44.380	54.139

Table S2. Concentrations of the doping ions based on WDXRF and ions per cm^3 , unit cell parameters of the PbF_2 doped with $\text{Er}^{3+}, \text{Yb}^{3+}$.

Sample name	Er³⁺		Yb³⁺		a, Å
	mol.,%	N, $\times 10^{20} \text{ cm}^{-3}$	mol.,%	N, $\times 10^{20} \text{ cm}^{-3}$	
Er1.5Yb1.5	1.61	3.34	1.436	2.98	5.9301
Er2Yb2	2.106	4.36	2.141	4.44	5.9236
Er2Yb3	2.186	4.53	3.285	6.81	5.9174
Er2Yb5	2.116	4.38	5.142	10.66	5.9078
Er2Yb7.5	2.116	4.38	7.713	15.99	5.8887

Table S3. Predicted radiative lifetimes and branching ratios of some transitions in the Er1.5Yb1.5 sample.

	E1, cm⁻¹	E2, cm⁻¹	ΔE, cm⁻¹	A, s⁻¹	β	τ_{rad}, ms
²H_{9/2} – ²H_{11/2}	24756	19337	5419	18.634	0.0140	0.751
– ⁴F_{9/2}	24756	15455	9301	41.471	0.0311	
– ⁴I_{11/2}	24756	10346	14410	118.013	0.0886	
– ⁴I_{13/2}	24756	6712	18044	542.343	0.407	
– ⁴I_{15/2}	24756	217	24539	611.763	0.459	
²H_{11/2} – ⁴I_{13/2}	19337	6712	12625	41.151	0.0282	0.686
– ⁴I_{15/2}	19337	217	19120	1416.983	0.972	
⁴S_{3/2} – ⁴F_{9/2}	18583	15455	3128	0.3421	3.818E-4	1.116
– ⁴I_{9/2}	18583	12597	5986	30.958	0.0345	
– ⁴I_{11/2}	18583	10346	8237	19.825	0.0221	
– ⁴I_{13/2}	18583	6712	11871	247.769	0.277	
– ⁴I_{15/2}	18583	217	18366	597.118	0.666	
⁴F_{9/2} – ⁴I_{9/2}	15455	12597	2858	0.726	0.00117	1.468
– ⁴I_{11/2}	15455	10346	5109	31.586	0.0464	
– ⁴I_{13/2}	15455	6712	8743	28.874	0.0424	
– ⁴I_{15/2}	15455	217	15238	620.141	0.9102	
⁴I_{9/2} – ⁴I_{11/2}	12597	10346	2251	3.319	0.0399	12.033
– ⁴I_{13/2}	12597	6712	5885	25.395	0.306	
– ⁴I_{15/2}	12597	217	12380	54.392	0.654	
⁴I_{11/2} – ⁴I_{13/2}	10346	6712	3634	22.446	0.259	11.517
– ⁴I_{15/2}	10346	217	10129	64.383	0.741	
⁴I_{13/2} – ⁴I_{15/2}	6712	217	6495	103.025	1	9.706

Table S4. Predicted radiative lifetimes and branching ratios of some transitions in the Er2Yb2 sample.

	E1, cm⁻¹	E2, cm⁻¹	ΔE, cm⁻¹	A, s⁻¹	β	τ_{rad}, ms
²H_{9/2} – ²H_{11/2}	24756	19337	5419	20.613	0.0121	0.588
– ⁴F_{9/2}	24756	15455	9301	45.873	0.0270	
– ⁴I_{11/2}	24756	10346	14410	146.500	0.0862	
– ⁴I_{13/2}	24756	6712	18044	685.112	0.403	
– ⁴I_{15/2}	24756	217	24539	801.826	0.471	
²H_{11/2} – ⁴I_{13/2}	19337	6712	12625	51.242	0.0323	0.629
– ⁴I_{15/2}	19337	217	19120	1537.217	0.968	
⁴S_{3/2} – ⁴F_{9/2}	18583	15455	3128	0.447	3.817E-4	0.853
– ⁴I_{9/2}	18583	12597	5986	40.692	0.0347	
– ⁴I_{11/2}	18583	10346	8237	25.958	0.0221	
– ⁴I_{13/2}	18583	6712	11871	324.008	0.276	
– ⁴I_{15/2}	18583	217	18366	780.852	0.666	
⁴F_{9/2} – ⁴I_{9/2}	15455	12597	2858	0.726	8.072E-4	1.111
– ⁴I_{11/2}	15455	10346	5109	40.562	0.0451	
– ⁴I_{13/2}	15455	6712	8743	37.706	0.0419	
– ⁴I_{15/2}	15455	217	15238	820.850	0.912	
⁴I_{9/2} – ⁴I_{11/2}	12597	10346	2251	3.457	0.0316	9.147
– ⁴I_{13/2}	12597	6712	5885	33.213	0.304	
– ⁴I_{15/2}	12597	217	12380	72.657	0.665	
⁴I_{11/2} – ⁴I_{13/2}	10346	6712	3634	25.155	0.234	9.305
– ⁴I_{15/2}	10346	217	10129	82.314	0.766	
⁴I_{13/2} – ⁴I_{15/2}	6712	217	6495	119.264	1	8.385

Table S5. Predicted radiative lifetimes and branching ratios of some transitions in the Er₂Yb₃ sample.

	E1, cm⁻¹	E2, cm⁻¹	ΔE, cm⁻¹	A, s⁻¹	β	τ_{rad}, ms
²H_{9/2} – ²H_{11/2}	24756	19337	5419	20.971	0.0121	0.561
– ⁴F_{9/2}	24756	15455	9301	46.741	0.0262	
– ⁴I_{11/2}	24756	10346	14410	152.445	0.0854	
– ⁴I_{13/2}	24756	6712	18044	717.234	0.402	
– ⁴I_{15/2}	24756	217	24539	846.532	0.474	
²H_{11/2} – ⁴I_{13/2}	19337	6712	12625	53.226	0.0330	0.621
– ⁴I_{15/2}	19337	217	19120	1558.149	0.967	
⁴S_{3/2} – ⁴F_{9/2}	18583	15455	3128	0.473	3.817E-4	0.807
– ⁴I_{9/2}	18583	12597	5986	42.869	0.0346	
– ⁴I_{11/2}	18583	10346	8237	27.426	0.0221	
– ⁴I_{13/2}	18583	6712	11871	342.655	0.277	
– ⁴I_{15/2}	18583	217	18366	825.792	0.666	
⁴F_{9/2} – ⁴I_{9/2}	15455	12597	2858	0.728	7.720E-4	1.060
– ⁴I_{11/2}	15455	10346	5109	42.759	0.0453	
– ⁴I_{13/2}	15455	6712	8743	39.364	0.0417	
– ⁴I_{15/2}	15455	217	15238	860.269	0.912	
⁴I_{9/2} – ⁴I_{11/2}	12597	10346	2251	3.487	0.0305	8.754
– ⁴I_{13/2}	12597	6712	5885	35.116	0.307	
– ⁴I_{15/2}	12597	217	12380	75.630	0.662	
⁴I_{11/2} – ⁴I_{13/2}	10346	6712	3634	25.785	0.229	8.889
– ⁴I_{15/2}	10346	217	10129	86.719	0.771	
⁴I_{13/2} – ⁴I_{15/2}	6712	217	6495	123.125	1	8.122

Table S6. Predicted radiative lifetimes and branching ratios of some transitions in the Er2Yb5 sample.

	E1, cm⁻¹	E2, cm⁻¹	ΔE, cm⁻¹	A, s⁻¹	β	τ_{rad}, ms
²H_{9/2} – ²H_{11/2}	24756	19337	5419	21.339	0.012	0.562
– ⁴F_{9/2}	24756	15455	9301	46.813	0.0263	
– ⁴I_{11/2}	24756	10346	14410	154.156	0.0872	
– ⁴I_{13/2}	24756	6712	18044	716.779	0.402	
– ⁴I_{15/2}	24756	217	24539	839.599	0.472	
²H_{11/2} – ⁴I_{13/2}	19337	6712	12625	54.359	0.0343	0.617
– ⁴I_{15/2}	19337	217	19120	1567.031	0.966	
⁴S_{3/2} – ⁴F_{9/2}	18583	15455	3128	0.465	3.816E-4	0.820
– ⁴I_{9/2}	18583	12597	5986	42.997	0.0356	
– ⁴I_{11/2}	18583	10346	8237	27.092	0.0221	
– ⁴I_{13/2}	18583	6712	11871	336.800	0.276	
– ⁴I_{15/2}	18583	217	18366	811.681	0.666	
⁴F_{9/2} – ⁴I_{9/2}	15455	12597	2858	0.708	7.303E-4	1.031
– ⁴I_{11/2}	15455	10346	5109	42.022	0.0432	
– ⁴I_{13/2}	15455	6712	8743	40.814	0.0428	
– ⁴I_{15/2}	15455	217	15238	886.471	0.914	
⁴I_{9/2} – ⁴I_{11/2}	12597	10346	2251	3.493	0.0291	8.424
– ⁴I_{13/2}	12597	6712	5885	34.553	0.291	
– ⁴I_{15/2}	12597	217	12380	80.655	0.679	
⁴I_{11/2} – ⁴I_{13/2}	10346	6712	3634	25.712	0.232	9.020
– ⁴I_{15/2}	10346	217	10129	85.155	0.768	
⁴I_{13/2} – ⁴I_{15/2}	6712	217	6495	122.337	1	8.174

Table S7. Predicted radiative lifetimes and branching ratios of some transitions in the Er2Yb7.5 sample.

	E1, cm⁻¹	E2, cm⁻¹	ΔE, cm⁻¹	A, s⁻¹	β	τ_{rad}, ms
²H_{9/2} – ²H_{11/2}	24756	19337	5419	23.065	0.0106	0.445
– ⁴F_{9/2}	24756	15455	9301	59.028	0.0262	
– ⁴I_{11/2}	24756	10346	14410	190.396	0.0855	
– ⁴I_{13/2}	24756	6712	18044	903.994	0.402	
– ⁴I_{15/2}	24756	217	24539	1072.468	0.477	
²H_{11/2} – ⁴I_{13/2}	19337	6712	12625	65.929	0.0327	0.493
– ⁴I_{15/2}	19337	217	19120	1962.310	0.967	
⁴S_{3/2} – ⁴F_{9/2}	18583	15455	3128	0.603	3.819E-4	0.633
– ⁴I_{9/2}	18583	12597	5986	53.822	0.0346	
– ⁴I_{11/2}	18583	10346	8237	34.857	0.022	
– ⁴I_{13/2}	18583	6712	11871	437.221	0.277	
– ⁴I_{15/2}	18583	217	18366	1053.695	0.667	
⁴F_{9/2} – ⁴I_{9/2}	15455	12597	2858	0.943	8.138E-4	0.862
– ⁴I_{11/2}	15455	10346	5109	54.590	0.0471	
– ⁴I_{13/2}	15455	6712	8743	48.078	0.0413	
– ⁴I_{15/2}	15455	217	15238	1055.930	0.910	
⁴I_{9/2} – ⁴I_{11/2}	12597	10346	2251	3.638	0.0264	7.222
– ⁴I_{13/2}	12597	6712	5885	44.770	0.323	
– ⁴I_{15/2}	12597	217	12380	90.052	0.650	
⁴I_{11/2} – ⁴I_{13/2}	10346	6712	3634	29.061	0.207	7.150
– ⁴I_{15/2}	10346	217	10129	110.796	0.792	
⁴I_{13/2} – ⁴I_{15/2}	6712	217	6495	142.934	1	6.996

Table S8. Decay times obtained after fitting the experimental decays in Figures 3b-3d with single-exponential (${}^4I_{13/2}$ - ${}^4I_{15/2}$ and ${}^4F_{9/2}$ - ${}^4I_{15/2}$ transitions) and bi-exponential (${}^4S_{1/2}$ - ${}^4I_{15/2}$ transition) functions.

${}^4I_{13/2}$ - ${}^4I_{15/2}$				
crystal		τ , ms		
Er1.5Yb1.5		11.0±0.5		
Er2Yb2		7.8±0.4		
Er2Yb3		8.2±0.4		
Er2Yb5		8.8±0.4		
Er2Yb7.5		8.9±0.4		

${}^4F_{9/2}$ - ${}^4I_{15/2}$	
crystal	τ , ms
Er1.5Yb1.5	0.44±0.05
Er2Yb2	0.36±0.04
Er2Yb3	0.38±0.04
Er2Yb5	0.36±0.04
Er2Yb7.5	0.37±0.04

${}^4S_{1/2}$ - ${}^4I_{15/2}$				
crystal	τ_1 , ms	A_1	τ_2 , ms	A_2
Er1.5Yb1.5	0.18±0.04	0.37	1.08±0.24	0.58
Er2Yb2	0.08±0.02	0.94	0.94±0.21	0.12
Er2Yb3	0.06±0.01	1.00	0.64±0.14	0.08
Er2Yb5	0.05±0.01	0.96	0.56±0.13	0.05
Er2Yb7.5	0.04±0.01	1.01	0.25±0.06	0.03

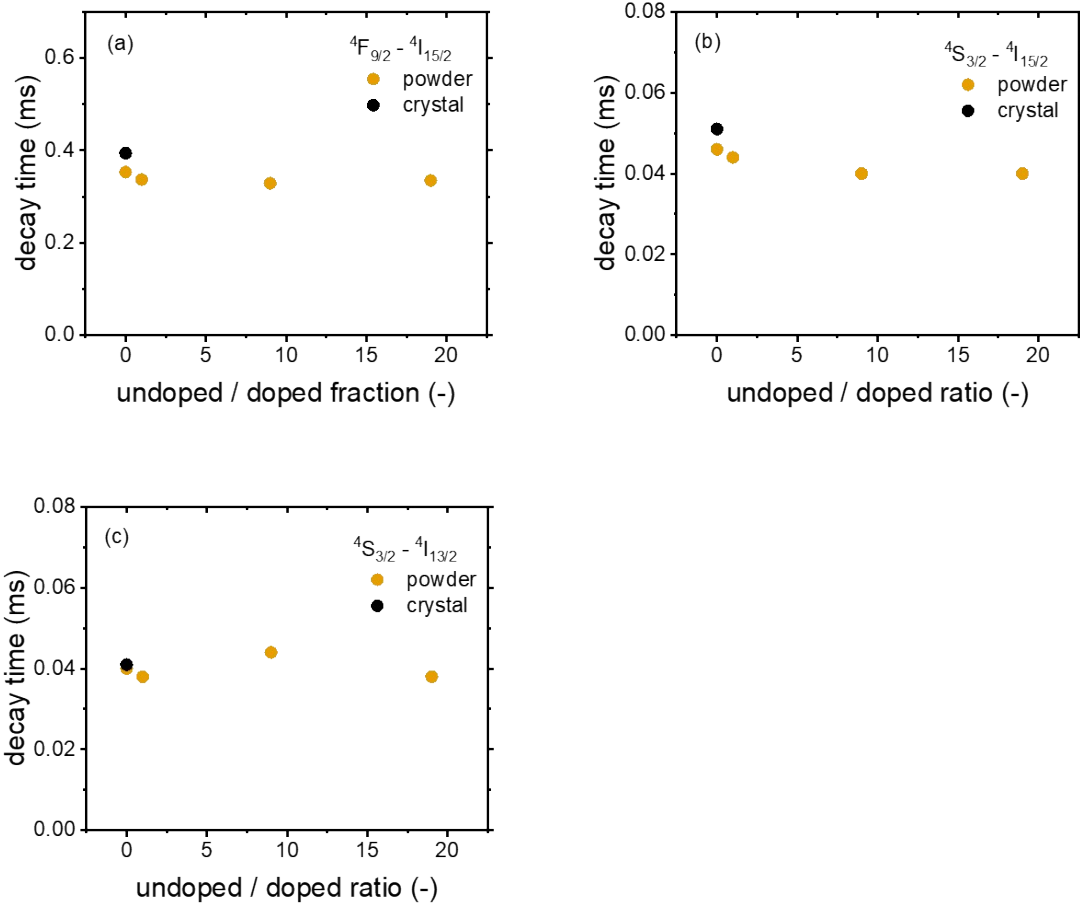


Figure S1 Luminescence decay times of the $\text{Er}^{3+}:{}^4S_{3/2} - {}^4I_{15/2}$, $\text{Er}^{3+}:{}^4S_{3/2} - {}^4I_{13/2}$, $\text{Er}^{3+}:{}^4F_{9/2} - {}^4I_{15/2}$ transitions of the Er_2Yb_5 crystal and diluted powders.

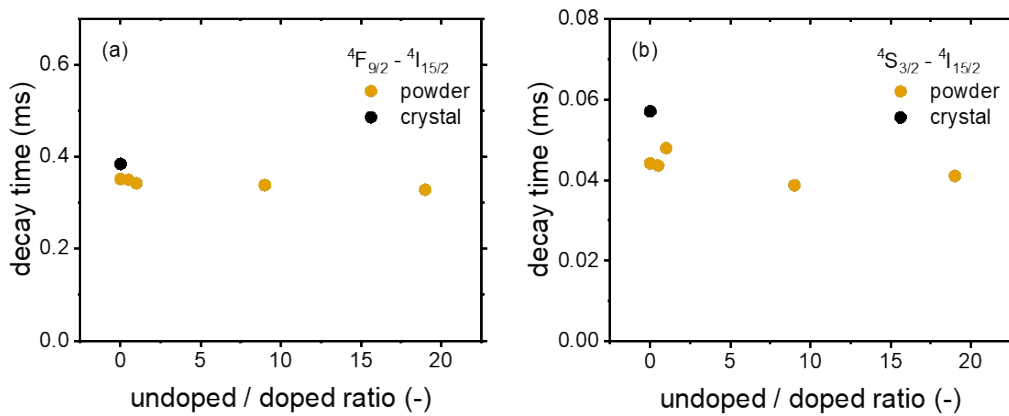


Figure S2. Luminescence decay times of the $\text{Er}^{3+}:{}^4S_{3/2} - {}^4I_{15/2}$ and $\text{Er}^{3+}:{}^4F_{9/2} - {}^4I_{15/2}$ transitions of the Er_2Yb_2 crystal and diluted powders.

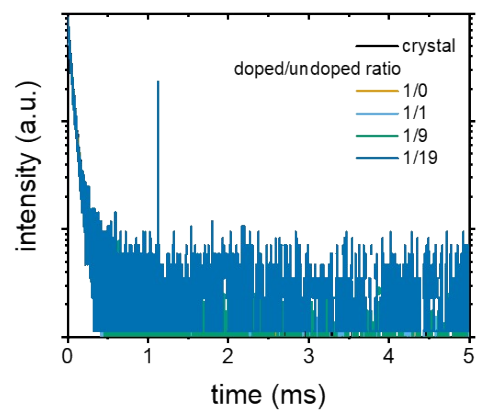


Figure S3. Luminescence decay of the $\text{Er}^{3+}:^4\text{S}_{3/2} - ^4\text{I}_{13/2}$ of the Er_2Yb_5 crystal and diluted powders under 522 nm excitation.

Table S9. Experimentally obtained ϕ_{DS}^* (%) of some transitions in the $\text{PbF}_2:\text{Er}^{3+}$, Yb^{3+} samples upon excitation of the ${}^4\text{S}_{3/2}$, ${}^4\text{F}_{9/2}$, $\text{Er}^{3+}:{}^4\text{I}_{11/2}$ & $\text{Yb}^{3+}:{}^2\text{F}_{7/2}$ and ${}^4\text{I}_{13/2}$ levels as measured in an integrating sphere.

Excitation	Emission	Er1.5Yb1.5	Er2Yb2	Er2Yb3	Er2Yb5	Er2Yb7.5
522 nm 0.1 W/cm²	${}^4\text{S}_{3/2} - {}^4\text{I}_{15/2}$	4.4	2.6	2.9	2.6	1.9
	${}^4\text{S}_{3/2} - {}^4\text{I}_{13/2}$	2	1.2	1.5	1.3	0.9
	${}^4\text{F}_{9/2} - {}^4\text{I}_{15/2}$	7	6.3	5.6	3.5	1.1
	{ $\text{Er}^{3+}:{}^4\text{I}_{11/2}$ & $\text{Yb}^{3+}:{}^2\text{F}_{7/2}$ }	38.2	40	43.9	36.1	30.1
652 nm 0.3 W/cm²	${}^4\text{F}_{9/2} - {}^4\text{I}_{15/2}$	18.3	20.1	23.5	22	16.6
	{ $\text{Er}^{3+}:{}^4\text{I}_{11/2}$ & $\text{Yb}^{3+}:{}^2\text{F}_{7/2}$ }	22.8	22.5	21.3	20.1	12.2
940 nm 0.1 W/cm²	{ $\text{Er}^{3+}:{}^4\text{I}_{11/2}$ & $\text{Yb}^{3+}:{}^2\text{F}_{7/2}$ }	29.6	48.8	57.2	40.5	31.2
	${}^4\text{I}_{13/2} - {}^4\text{I}_{15/2}$	3.5	3.1	3.2	2.1	1.9
1495 nm 0.1 W/cm²	${}^4\text{I}_{13/2} - {}^4\text{I}_{15/2}$	83.2	67.2	61.4	62.4	59.1

The correction of the measured ϕ_{DS} values for reabsorption was performed as follows (by analogy with to C. de Mello Donegá et al¹.): a part of every crystal was ground to powder in a mortar and then the obtained powders were diluted with BaSO_4 in the ration of 9/1 where the first number is the fraction of BaSO_4 and the second one is the fraction of PbF_2 powder. Then spectra of every single crystal and diluted powder were obtained under 378 nm excitation with a spectrofluorometer (FS5, Edinburgh Instruments) in the visible and NIR ranges. The visible emission was normalised to the peak of the ${}^4\text{S}_{3/2} - {}^4\text{I}_{13/2}$ transition at 850 nm. In the case of NIR emission bands, each band was normalised to the long wavelength edge (1585 nm in the case of ${}^4\text{I}_{13/2} - {}^4\text{I}_{15/2}$ emission and 1045 nm in the case of { $\text{Er}^{3+}:{}^4\text{I}_{11/2}$ & $\text{Yb}^{3+}:{}^2\text{F}_{7/2}$ } emission). The corrected ϕ_{DS} values were obtained according to Wilson and Richards² as

$$\phi_{DS} = \frac{\phi_{DS}^*}{1 - a + a * \phi_{DS}}$$

Where $a = 1 - \frac{\int I_{crystal} d\lambda}{\int I_{powder} d\lambda}$, $I_{crystal}$ is the normalized emission intensity of a single crystal sample, I_{powder} is the normalized emission intensity of a 9/1 diluted powder sample. The integration ranges are 500 – 580 nm for the combination of ${}^4\text{S}_{3/2} - {}^4\text{I}_{15/2}$ and ${}^2\text{H}_{11/2} - {}^4\text{I}_{15/2}$ bands, 610 – 705 nm for the ${}^4\text{F}_{9/2} -$

$^4I_{15/2}$ emission, 920 – 1100 nm for the $\{\text{Er}^{3+}:^4I_{11/2} \& \text{Yb}^{3+}:^2F_{7/2}\}$ band and 1430 – 1700 nm for the $^4I_{13/2}$ – $^4I_{15/2}$ emission band.

The spectra that were used for the calculations are presented in **figure S4.1-3**.

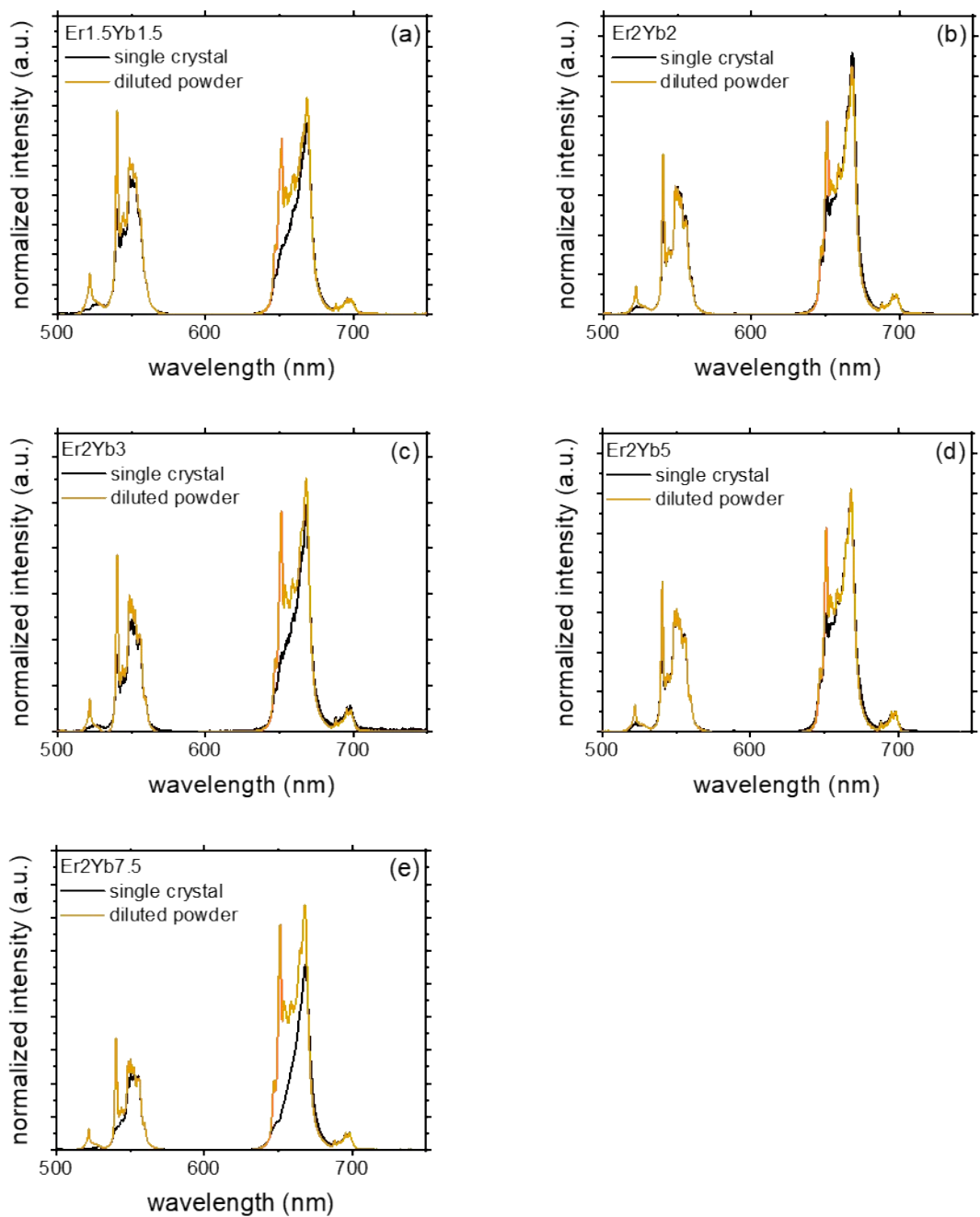


Figure S4.1. Visible range emission spectra of the single crystals and 9/1 diluted powders of the $\text{PbF}_2:\text{Er},\text{Yb}$ samples measured under 378 nm excitation with a spectrofluorometer (FS5, Edinburgh Instruments).

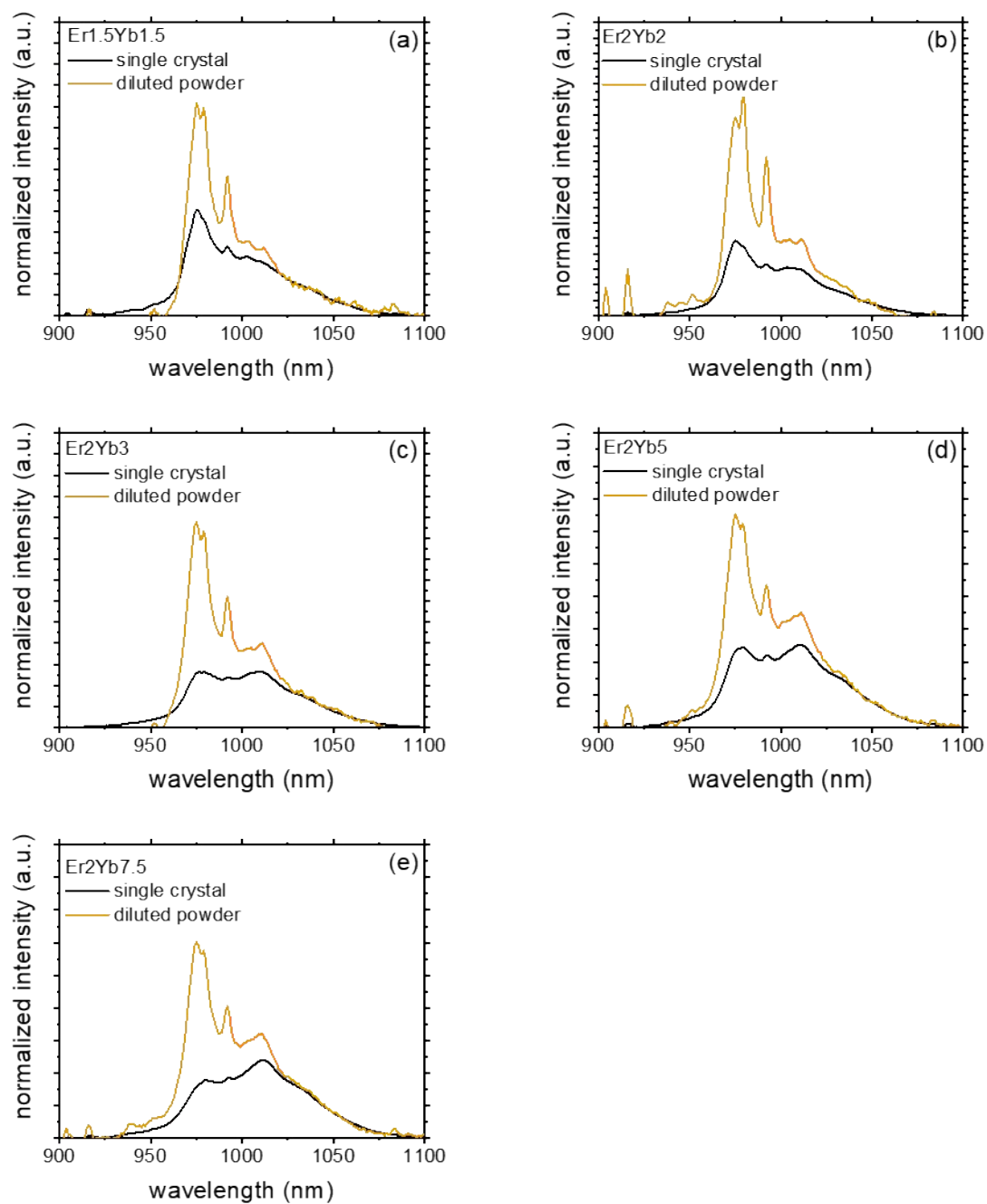


Figure S4.2. NIR range emission spectra of the single crystals and 9/1 diluted powders of the $\text{PbF}_2:\text{Er},\text{Yb}$ samples measured under 378 nm excitation with a spectrofluorometer (FS5, Edinburgh Instruments).

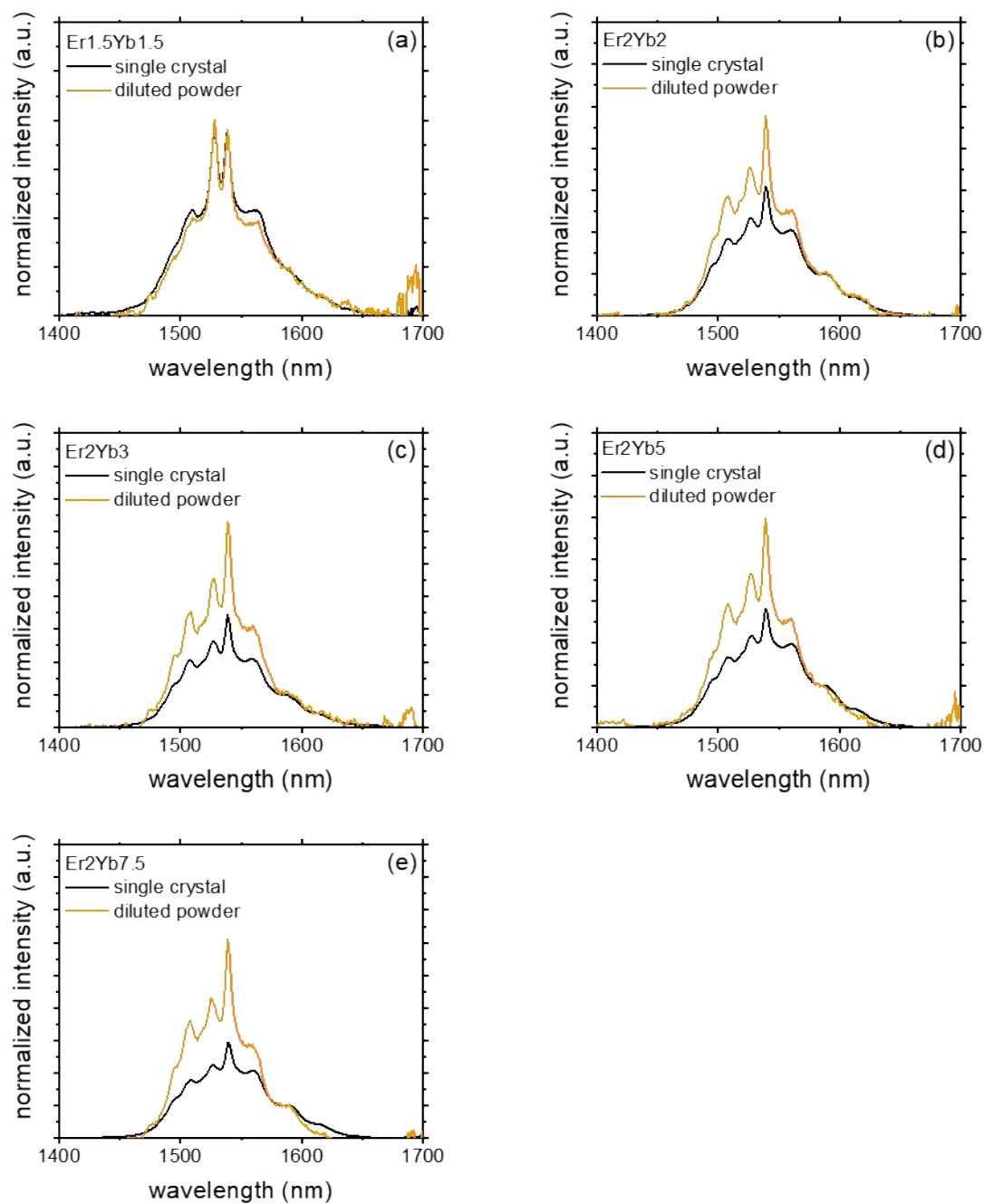


Figure S4.3. NIR range emission spectra of the single crystals and 9/1 diluted powders of the $\text{PbF}_2\text{:Er,Yb}$ samples measured under 378 nm excitation with a spectrofluorometer (FS5, Edinburgh Instruments).

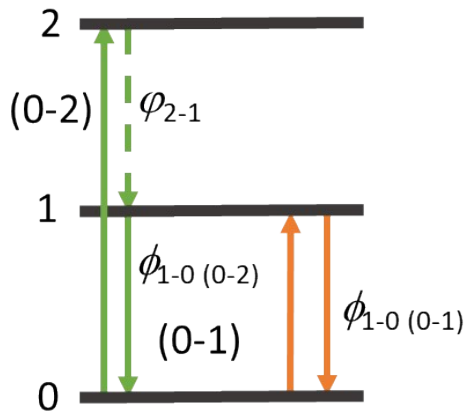


Figure S5. Energy transfer diagrams for the case of DS emission, where the ground state **0** is $\text{Er}^{3+}:^4\text{I}_{15/2}$, excited state **1** is either $\text{Er}^{3+}:^4\text{I}_{13/2}$ or $\text{Er}^{3+}:^4\text{I}_{9/2}$ and excited state **2** is either $\text{Er}^{3+}:^4\text{I}_{11/2}$ or $\text{Er}^{3+}:^4\text{S}_{3/2}$

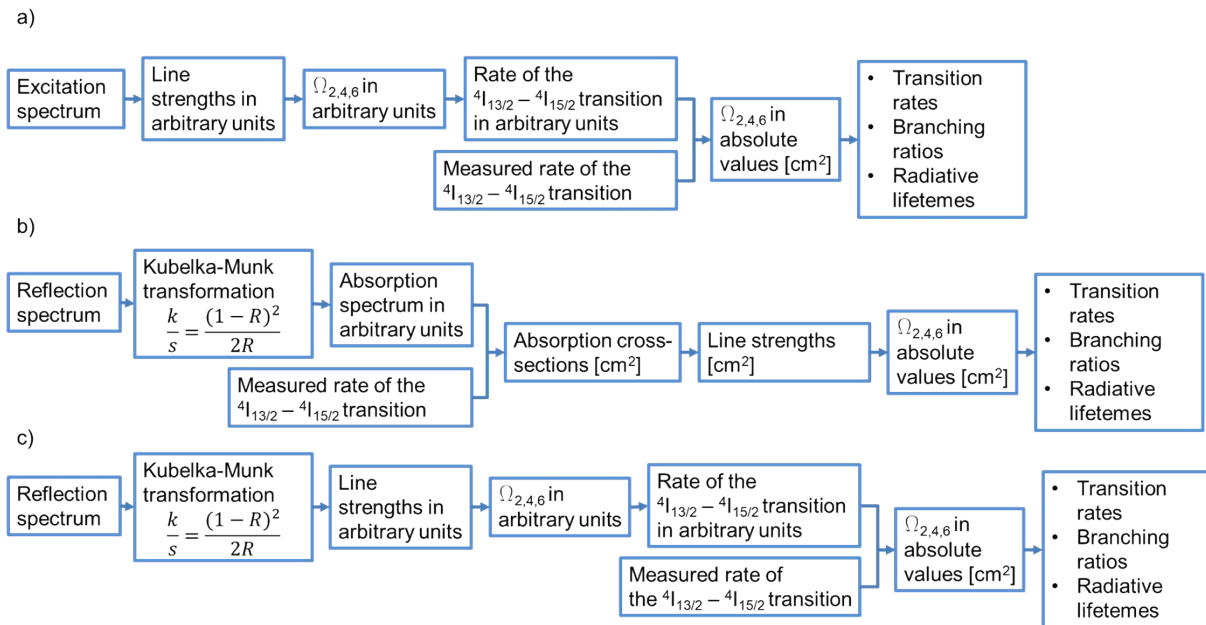


Figure S6. Different algorithms of JO calculation in the case of powder samples a) paper ³; b) paper ⁴; c) papers ^{5,6}

Table S10. The comparison of branching ratios of Er₂Yb₅ powder obtained with different methods.

Emission band	Lifetime, ms			
	Crystal	<i>Method A</i> ³	<i>Method B</i> ⁴	<i>Method C</i> ^{5,6}
⁴ G _{9/2} – ⁴ I _{15/2}	0.42	0.52	0.52	0.42
² H _{11/2} – ⁴ I _{15/2}	0.97	0.97	0.97	0.97
⁴ S _{3/2} – ⁴ I _{15/2}	0.67	0.67	0.67	0.66
⁴ F _{9/2} – ⁴ I _{15/2}	0.91	0.88	0.88	0.93
⁴ I _{9/2} – ⁴ I _{15/2}	0.83	0.24	0.22	0.83
⁴ I _{11/2} – ⁴ I _{15/2}	0.73	0.89	0.78	0.73
⁴ I _{13/2} – ⁴ I _{15/2}	1	1	1	1
Relative RMS (with 4I_{9/2})		0.26	0.68	0.68
Relative RMS (w/o 4I_{9/2})		0.12	0.19	0.11

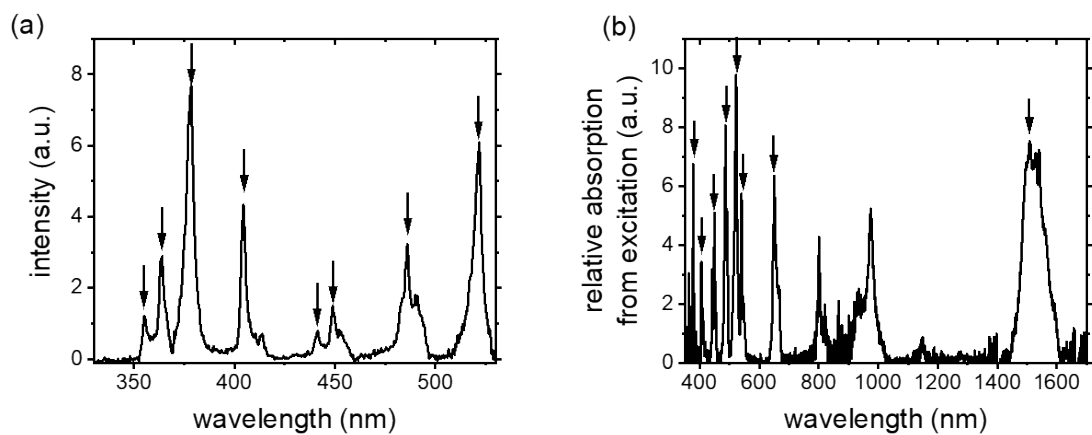


Figure S7. a) the excitation spectrum of the $^4S_{3/2} - ^4I_{15/2}$ transition (detection at 540 nm); b) the reflectance spectrum of the Er_2Yb_2 powder sample.

Table S11. The comparison of Ω_t parameters of Er₂Yb₂ powder obtained with different methods.

	Crystal	Method A ³	Method B ⁴	Method C ^{5,6}
Ω_2	1.34x10 ⁻²⁰	2.73x10 ⁻²⁰	1.60x10 ⁻²⁰	1.72x10 ⁻²¹
Ω_4	4.70x10 ⁻²¹	4.43x10 ⁻²⁰	7.43x10 ⁻²¹	7.96x10 ⁻²¹
Ω_6	1.79x10 ⁻²⁰	2.23x10 ⁻²⁰	2.34x10 ⁻²⁰	2.54x10 ⁻²⁰
Relative RMS		8.50	0.69	0.86

Table S12. The comparison of radiative lifetimes of Er₂Yb₂ powder obtained with different methods.

Emission band	Lifetime, ms			
	Crystal	Method A ³	Method B ⁴	Method C ^{5,6}
${}^4G_{9/2} - {}^4I_{15/2}$	0.59	0.43	0.56	0.52
${}^2H_{11/2} - {}^4I_{15/2}$	0.61	0.35	0.84	0.78
${}^4S_{3/2} - {}^4I_{15/2}$	0.85	0.73	0.69	0.65
${}^4F_{9/2} - {}^4I_{15/2}$	1.14	0.64	1.42	1.32
${}^4I_{9/2} - {}^4I_{15/2}$	9.47	4.93	13.99	12.75
${}^4I_{11/2} - {}^4I_{15/2}$	9.26	8.21	8.83	7.70
${}^4I_{13/2} - {}^4I_{15/2}$	8.39	8.39	12.31	8.39
Relative RMS (with 4I9/2)		0.84	0.83	0.57
Relative RMS (w/o 4I9/2)		0.69	0.68	0.45

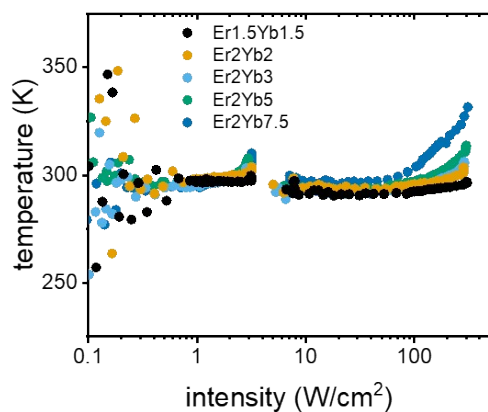


Figure S8. Sample temperature as a function of incident 976 nm intensity.

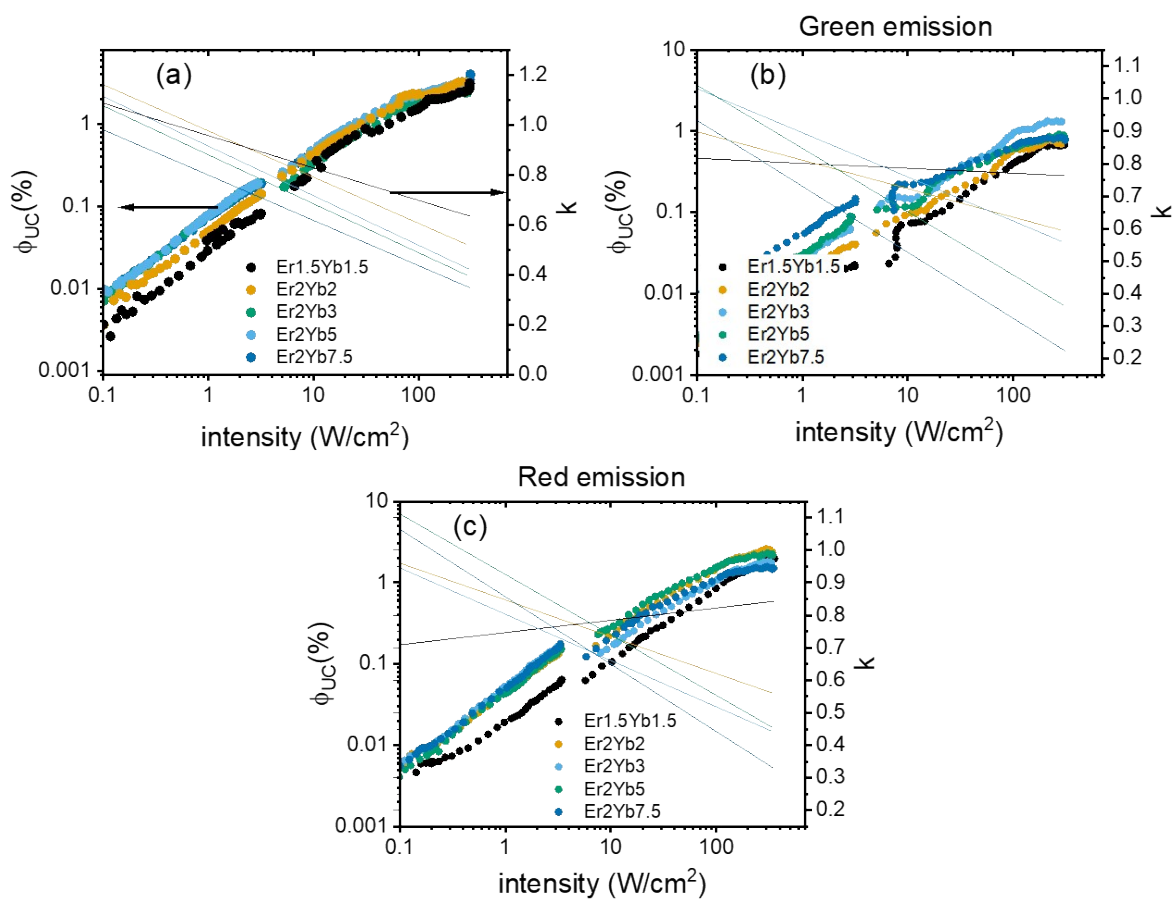


Figure S9. Measured ϕ_{UC} and slopes (k) of the ϕ_{UC} dependence of a) total UC emission in the 400 – 900 nm range, b) emission of the ${}^4S_{3/2} - {}^4I_{15/2}$ transition, c) emission of the ${}^4F_{9/2} - {}^4I_{15/2}$ transition in the intensity range of 0.1 – 350 W/cm^2 .

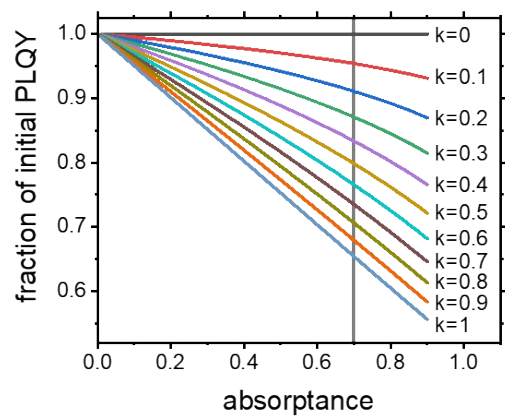


Figure S10. Relative change in ϕ_{UC} of a sample versus total absorbance and slope (k) of the ϕ_{UC} intensity dependence.

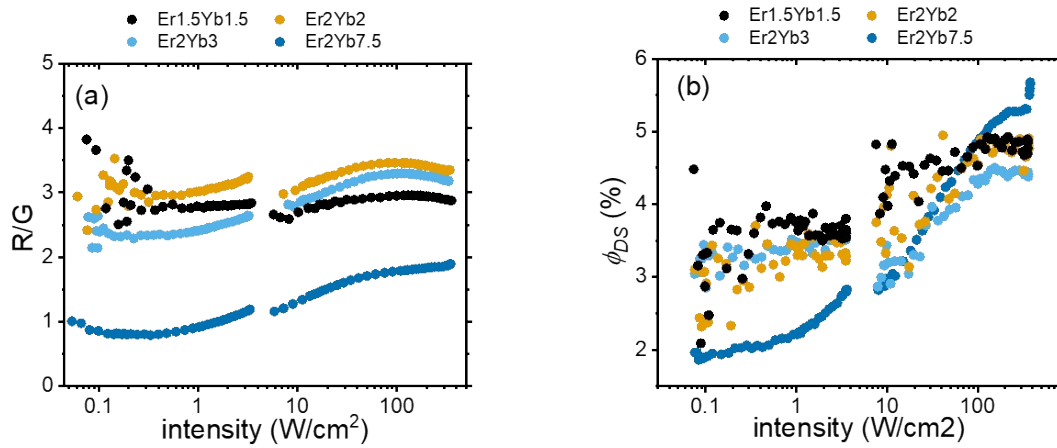


Figure S11. (a) Ratio of the intensities of the ${}^4F_{9/2} - {}^4I_{15/2}$ (Red) transition and the ${}^4S_{3/2} - {}^4I_{15/2}$ (Green) transition as a function of 976 nm excitation intensity in the 0.1 – 350 W/cm²; (b) ϕ_{DS} of the $Er^{3+}:{}^4I_{13/2} - {}^4I_{15/2}$ transition as a function of intensity at 940 nm excitation.

References

1. C. de Mello Donegá, A. Meijerink and G. Blasse, *J. Lumin.*, 1994, **62**, 189-201.
2. L. R. Wilson and B. S. Richards, *Appl. Opt.*, 2009, **48**, 212-220.
3. W. Luo, J. Liao, R. Li and X. Chen, *PCCP*, 2010, **12**, 3276-3282.
4. Y. Zhang, B. Chen, S. Xu, X. Li, J. Zhang, J. Sun, X. Zhang, H. Xia and R. Hua, *PCCP*, 2018, **20**, 15876-15883.
5. E. Cantelar, M. Marin-Dobrincic, T. Jardiel, A. C. Caballero and F. Cussó, *Opt. Mater.*, 2015, **41**, 122-125.
6. A. Egaña, M. Tardío, C. de la Torre-Gamarra, A. Várez, E. Cantelar and J. E. Muñoz Santiuste, *J. Lumin.*, 2018, **202**, 232-238.